



# Take a look.....

WHAT YOU  
WILL LEARN  
IN THIS  
CHAPTER

Use garbage collection as an example

## Fixed input

Capital

One truck

## Variable input

Labor

Workers on the truck

## Output

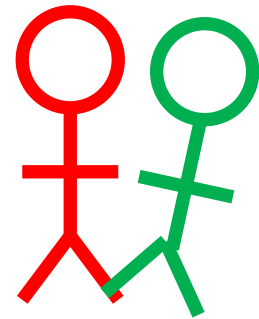
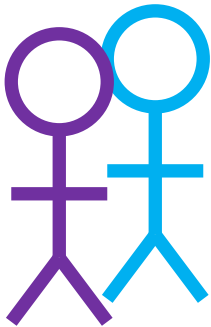
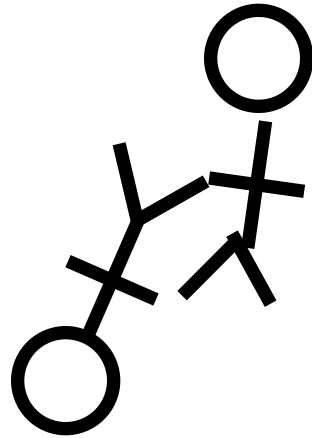
Trash cans picked up





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# PRODUCTION AND COSTS

- › The production function, the relationship between quantity of inputs and quantity of output
- › Production is often subject to diminishing returns to inputs (labor, capital)
- › The various types of costs: fixed cost and variable cost, marginal and average cost curves
- › Technology of production can generate increasing returns to scale



# The Production Function

A **production function** is the relationship between the quantity of inputs a firm uses and the quantity of output it produces.

$$\text{Output} = f \{ \text{inputs} \}$$

A **fixed input** is an input that is fixed in quantity for a period and cannot be varied.

A **variable input** is an input of the firm that can vary at any time.

The **long run** is the period in which all inputs can be varied.

The **short run** is the period in which at least one input is fixed.



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Quantity of labor (hours in surgery)	Quantity of capital (operating rooms)	Total product (number of surgeries)
30	0	0
30	1	15
30	2	25
30	3	32
30	4	35

1. Paul is a surgeon. The information in the table contains information about Paul's production function. It depicts Paul's:

- a) short-run production function.
- b) long-run production function.

2. The fixed input in Paul's production function for surgeries is the quantity of:

- a) labor.
- b) capital.

3. Paul's marginal product of capital from hiring a third operating room is:

- a) 32 surgeries.
- b) 25 surgeries.
- c) 7 surgeries per operating room.
- d) 3 surgeries per operating room.





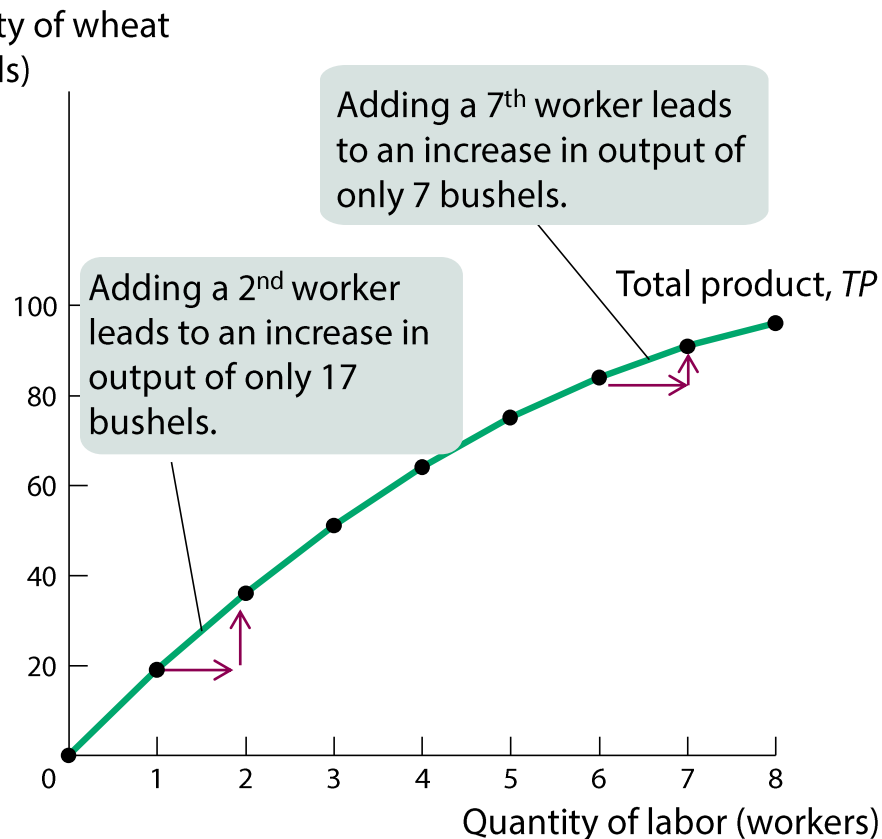
# Marginal Product of Labor

The *marginal product* of an input is the additional quantity of output that is produced by using one more unit of that input.

$$MPL = \frac{\text{Change in quantity of output}}{\text{Change in quantity of labor}} = \frac{\Delta Q}{\Delta L}$$

**MPL**= change in quantity of output generated by one additional unit of labor.

# Production Function and TP Curve



Quantity of labor (worker)	Quantity of wheat (bushels)	MP of labor $MPL = D_Q / D_L$ (bushels per worker)
0	0	
1	19	19
2	36	17
3	51	15
4	64	13
5	75	11
6	84	9
7	91	7
8	96	5

*The relationship between inputs and output is positive, but not constant: **marginal product of labor, MPL, changes along the production function.***

***In other words, MPL is the slope of the TP curve***



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If one worker makes 14 baskets,  
two workers make 34 baskets,  
three workers make 45 baskets, and  
four workers make 50 baskets, *which worker yielded the highest marginal product?*

- a) The first worker
- b) The second worker
- c) The third worker
- d) The fourth worker

Marginal product is the slope of the:

- a) marginal cost curve.
- b) total product curve.
- c) long-run average total cost curve.
- d) total cost curve.

Active  
Learning





# COST Curves

A **fixed cost = FC** is a cost that does **not** depend on the quantity of output produced. **It is the cost of the fixed input.**

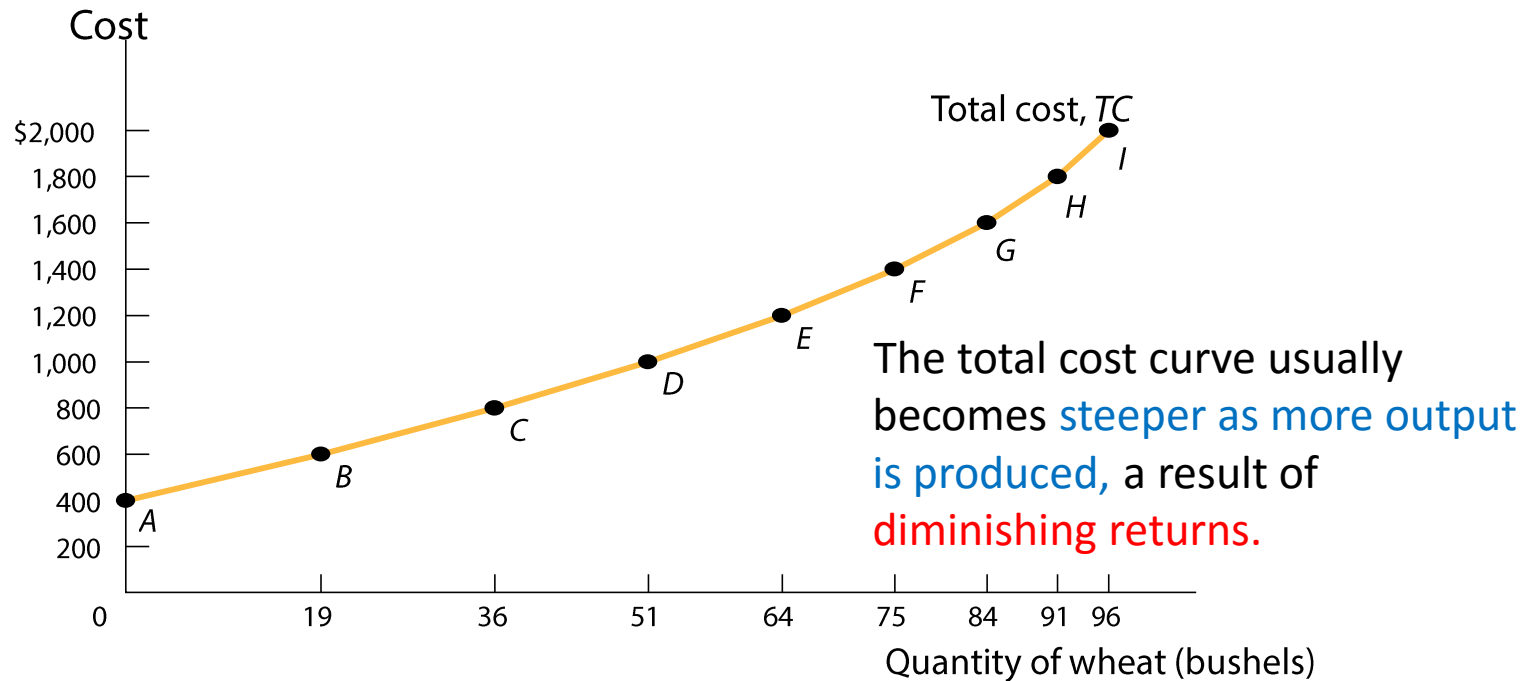
Whether  $Q=0$ , or  $Q=100$ , or  $Q=1000$ , the fixed cost is the same amount.

A **variable cost = VC** is a cost that depends on the quantity of output produced. **It is the cost of the variable input.**

The **total cost** of producing a given quantity of output is the sum of the fixed cost and the variable cost of producing that quantity of output.

$$TC = FC + VC$$

# Total Cost Curve



Point on graph	Quantity of labor (INPUT)	Quantity of wheat (OUTPUT)	Variable cost (VC)	Fixed Cost (FC)	Total cost ( $TC = FC + VC$ )
A	0	0	\$0	\$400	<b>\$400</b>
B	1	19	200	400	<b>600</b>
C	2	36	400	400	<b>800</b>
D	3	51	600	400	<b>1,000</b>
E	4	64	800	400	<b>1,200</b>
F	5	75	1,000	400	<b>1,400</b>
G	6	84	1,200	400	<b>1,600</b>
H	7	91	1,400	400	<b>1,800</b>
I	8	96	1,600	400	<b>2,000</b>

# Various Costs of Selena's Gourmet Salsas

Quantity of salsa Q (cases)	Fixed cost FC	Variable cost VC	Total cost TC = FC + VC	Marginal cost of case MC = $\Delta TC / \Delta Q$
0	\$108	\$0	\$108	(also check the change in VC)
1	108	12	120	\$12
2	108	48	156	36
3	108	108	216	60
4	108	192	300	84
5	108	300	408	108
6	108	432	540	132
7	108	588	696	156
8	108	768	876	180
9	108	972	1,080	204
10	108	1,200	1,308	228



# Let's try this: MPL and MC

Magnificent Blooms is a florist specializing in floral arrangements. Its fixed cost (space and equipment) is \$100 per day. Each worker is paid \$50 per day. The table below shows the production function.

a. Calculate the marginal product of each worker (MPL). What principle explains why the MPL (marginal product of labor) declines as the number of workers employed increases?

b. Calculate the marginal cost (MC). What principle explains why the MC increases as the number of arrangements increases?

Qty (labor)	Qty of floral arrangements	MPL	MC
0	0		
1	5		
2	9		
3	12		
4	14		
5	15		

# Average Cost

**Average total cost** (often referred to simply as **average cost**) = total cost divided by quantity of output produced.

$$ATC = \frac{TC}{Q} = \frac{\text{Total cost}}{Q \text{ of output}}$$

**Average fixed cost** = the fixed cost per unit of output.

$$AFC = \frac{FC}{Q} = \frac{\text{Fixed cost}}{Q \text{ of output}}$$

**Average variable cost** = the variable cost per unit of output.

$$AVC = \frac{VC}{Q} = \frac{\text{Variable cost}}{Q \text{ of output}}$$



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**Average fixed cost** =  $TFC/Q$ .

**Average variable cost** =  $TVC/Q$ .

**Average total cost** =  $TC/Q$ .

**Example:** Assume fixed cost, FC, is 100 and fill in the following table.

<b><i>Q</i></b>	<b><i>TVC</i></b>	<b><i>TC</i></b>	<b><i>AFC</i></b>	<b><i>AVC</i></b>	<b><i>ATC</i></b>
0	0				
1	30				
2	46				
3	80				



# Average Costs for Selena's Gourmet Salsas

Quantity of salsa $Q$ (cases)	Total cost $TC$	Average total cost of case $ATC = TC/Q$	Average fixed cost of case $AFC = FC/Q$	Average variable cost of case $AVC = VC/Q$
1	\$120	\$120.00	\$108.00	\$12.00
2	156	78.00	54.00	24.00
3	216	72.00	36.00	36.00
4	300	75.00	27.00	48.00
5	408	81.60	21.60	60.00
6	540	90.00	18.00	72.00
7	696	99.43	15.43	84.00
8	876	109.50	13.50	96.00
9	1,080	120.00	12.00	108.00
10	1,308	130.80	10.80	120.00

# Some “Effects”

## Opposing effects on ATC :

- 1) *The spreading effect*: The larger the output, the more output over which **fixed cost is spread**, leading to **lower** average fixed cost.
- 2) *The diminishing returns effect*: The larger the output, the **more variable input required to produce additional units**, which leads to **higher** average variable cost.

### *Additionally:*

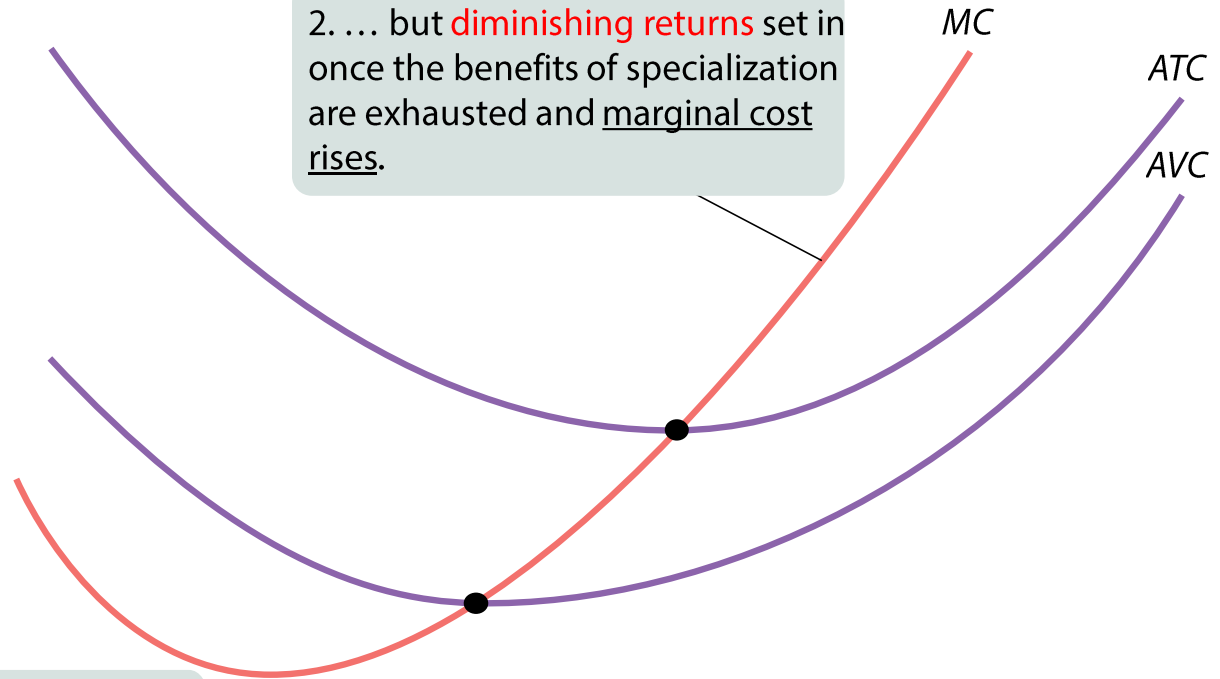
*Specialization effect on MC*: As the firms learn to specialize and experience learning curve, output, the **additional cost to produce one more unit** will be/might be lower, leading to lower **Marginal cost**.

# More Realistic Cost Curves

Cost of unit

2. ... but **diminishing returns** set in once the benefits of specialization are exhausted and marginal cost rises.

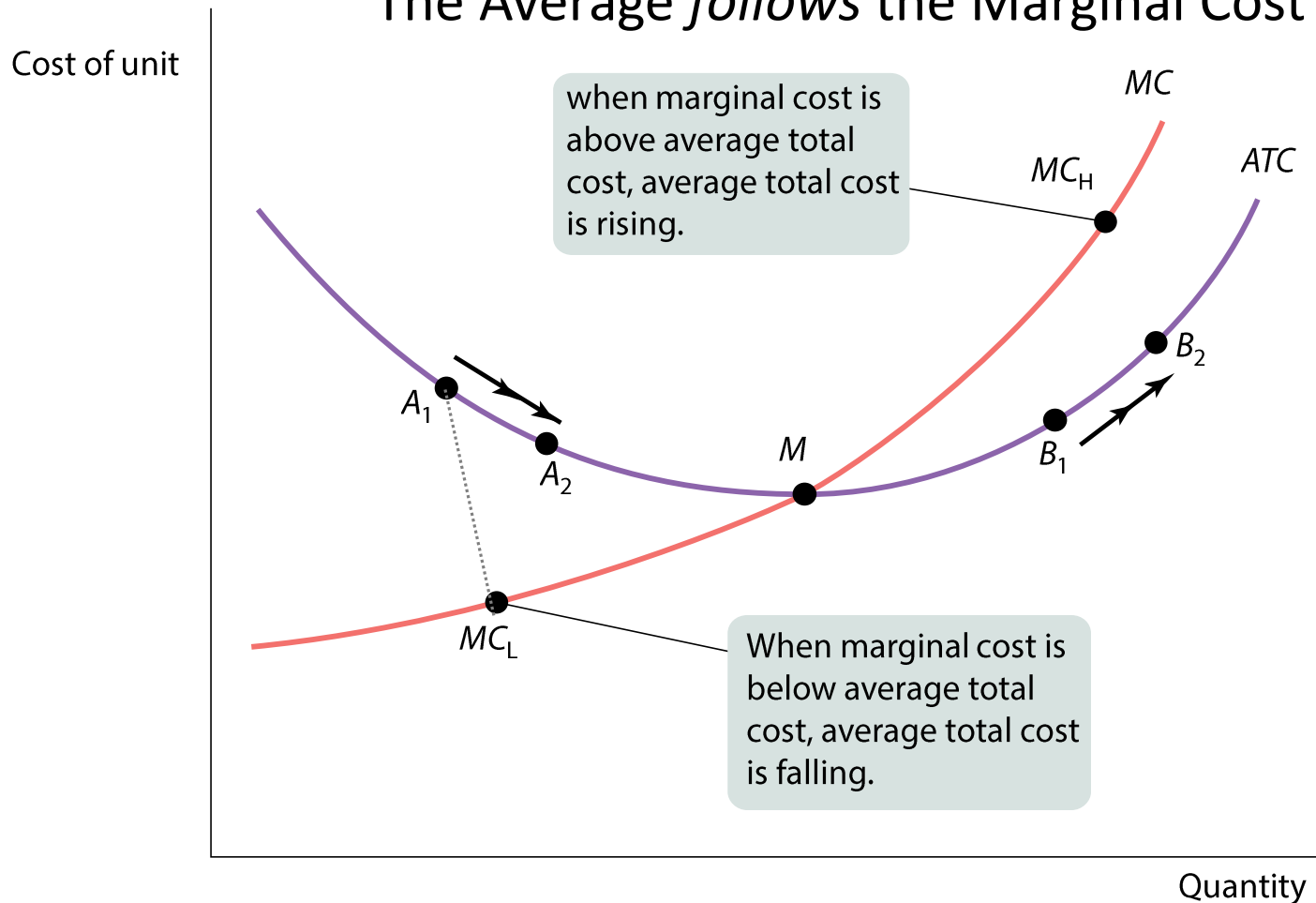
1. Increasing **specialization** leads to lower marginal cost...(downward sloping)



Quantity

# The Relationship Between the ATC and MC Curves

The Average *follows* the Marginal Cost curve



Think in terms of your GPA (as your “average”)

# Margin and Average Relationship (MC and ATC): Class GPA



**Think of this example:**

**Class GPA**

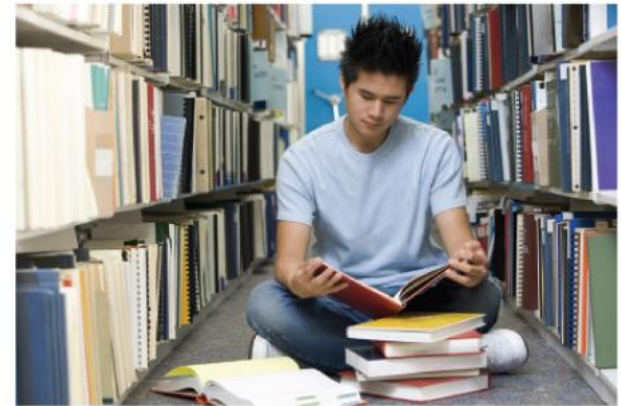
**Suppose the class average grade on the economics exam is 85%**

**Smarty McGenius joins the class, gets 100% on the exam**

**The class average rises**

**Lazy NoStudyson joins the class, gets 34% on the exam**

**The class average falls**



# MC and ATC: Sports Statistics



**Suppose LeBron James has a scoring *average* of 30 points per game**

**If he has a game in which he scores 45 points**

**His average increases**

**If he has a game in which he scores 12 points**

**His average decreases**

**Once again:**

**The average follows the margin**





# Putting the Four Cost Curves Together

Note that:

1. MC is upward sloping because of diminishing returns. (but downward sloping because of specialization)
2. AVC is also upward sloping but flatter than the MC curve.
3. Average fixed cost, AFC is downward sloping because of the spreading effect.
4. MC curve intersects the ATC curve from below, crossing it at its lowest point (the “minimum-cost” output).

# Long Run Costs



## Economies of scale

**ATC *falls*** when production expands

eg: Larger firm more efficient than a smaller firm

## Diseconomies of scale

**ATC *rises*** when production expands

eg: Very large firm has to deal with additional management, coordination, logistical expenses

## Constant returns to scale

**ATC *doesn't change*** when production expands

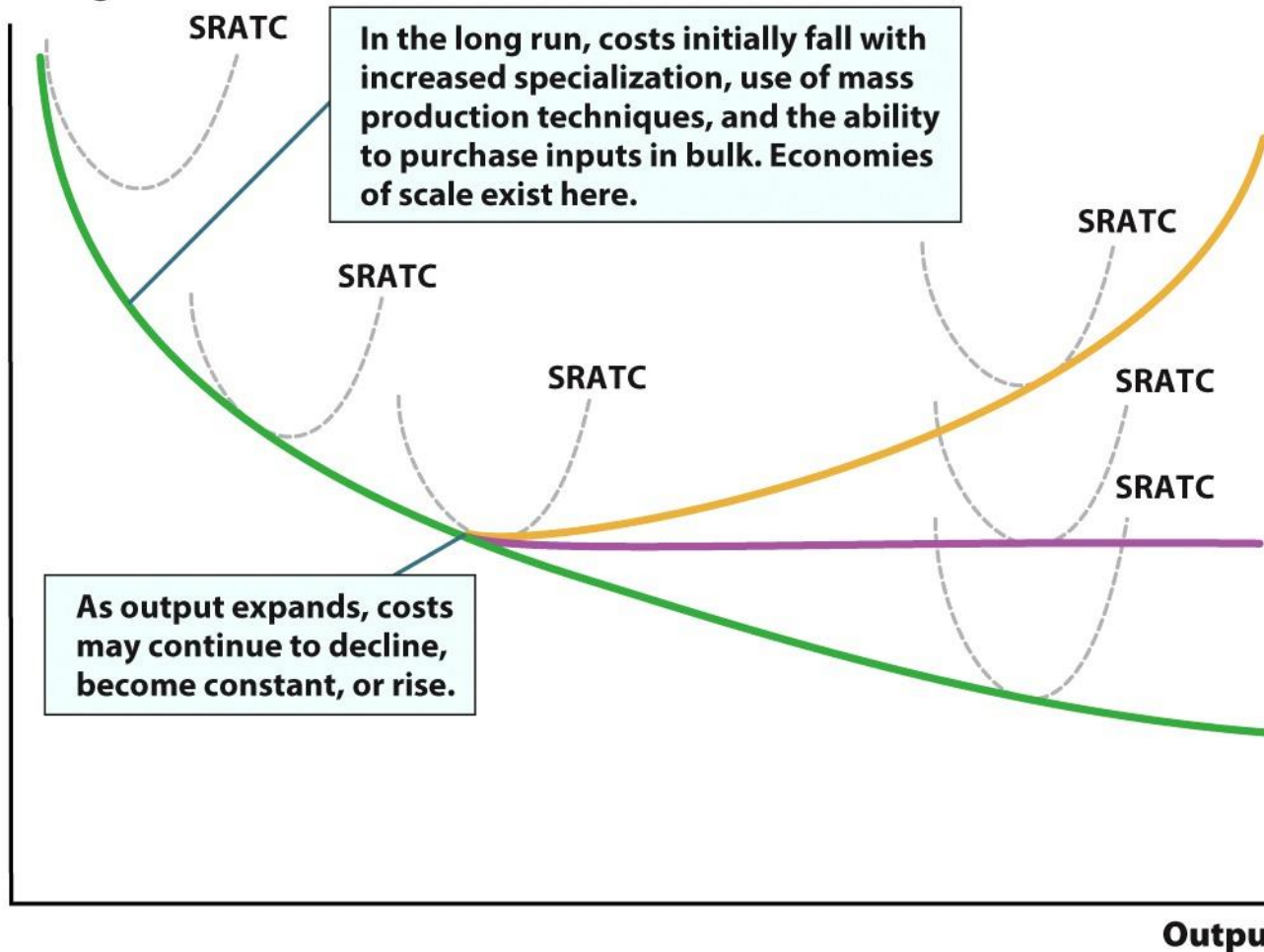
eg: Olive Garden builds another restaurant. Requires same K and L as previous restaurants. Output similar.

# Costs in the Long Run



## Costs in the Long Run

Average  
Total Cost



LRATC: diseconomies of scale



LRATC: constant returns to scale



LRATC: economies of scale

# SR and LR Cost Comparison

**The short run cost curve and the long run cost curve are both U-shaped. However, they are U-shaped for different reasons!**

## **SR-AC**

**U-shaped because of diminishing marginal product  
MPL falls, MC rises, and ATC follows MC**

## **LR-AC**

**U-shaped because of economies and diseconomies of scale  
Smaller firms can lower costs by growing, but if they get too big (and inefficient), costs can grow**



# In-Class Exercise:

## 1. Evaluate each statement.

If a statement is true, explain why.

If it is false, identify the mistake and try to correct it.

- a. A decreasing marginal product tells us that marginal cost must be rising.
- b. An increase in fixed cost increases the minimum-cost output.
- c. An increase in fixed cost increases marginal cost
- d. When marginal cost is above ATC, ATC must be falling.
- e. When marginal cost is rising, ATC and AVC must be rising too.



# Let's try this:

You have the information below about a firm's costs. Complete the missing data. Then find the minimum value of ATC and AVC, and the minimum-cost output.

Qty	TC	MC	FC	VC	AFC	AVC	ATC
0	20	-					
1		20					
2		10					
3		16					
4		20					
5		24					