

ECE 3200
Test 1
Solutions

A) Which of the following elements are used as impurities in n-type silicon?

- a: boron
- b: phosphorus
- c: arsenic
- ☒ d: both b and c
- e: None of the above

*n-type Si requires impurities from group V
 \Rightarrow P and As*

(See text sec. 1.1)

B) The intrinsic carrier concentration of a group IV semiconductor is $2.0 \times 10^9 \text{ cm}^{-3}$ at a certain temperature. If the semiconductor is doped with boron such that the concentration of boron atoms is 10^{12} cm^{-3} , which of the following is closest to the concentration of free electrons in the material?

- a: 10^{12} cm^{-3}
- b: 10^{10} cm^{-3}
- c: 10^8 cm^{-3}
- ☒ d: 10^6 cm^{-3}
- e: 10^4 cm^{-3}

$$N_a = 10^{12} \text{ cm}^{-3} \gg n_i = 2.0 \times 10^9 \text{ cm}^{-3}$$

$$\Rightarrow p_0 \approx N_a$$

$$n_0 = \frac{n_i^2}{p_0} \approx \frac{(2.0 \times 10^9 \text{ cm}^{-3})^2}{10^{12} \text{ cm}^{-3}} \approx 4.0 \times 10^6 \text{ cm}^{-3}$$

C) A sample of silicon at room temperature is doped with phosphorus such that the conductivity of the sample is $2 (\Omega\text{-cm})^{-1}$. The mobility of free electrons is $1350 \text{ cm}^2/\text{V-s}$. Neglecting the effect of holes, which of the following is closest to concentration of phosphorus atoms in the sample?

- a: 10^{12} cm^{-3}
- b: 10^{14} cm^{-3}
- ☒ c: 10^{16} cm^{-3}
- d: 10^{18} cm^{-3}
- e: 10^{20} cm^{-3}

$$\sigma = e\mu_n n + e\mu_p p \xrightarrow{\text{Neglect}} \approx e\mu_n n$$

$$\Rightarrow n \approx \frac{\sigma}{e\mu_n} = \frac{2 (\Omega\text{-cm})^{-1}}{(1.6 \times 10^{-19} \text{ C})(1,350 \frac{\text{cm}^2}{\text{V-s}})}$$

$$\approx 9.26 \times 10^{15} \left(\frac{\text{C}}{\text{s}}\right) \left(\frac{\text{V}}{\text{cm}^2}\right) \text{ cm}^{-3} = 0.926 \times 10^{16} \text{ cm}^{-3}$$

D) The reverse-bias saturation current of a pn junction diode is 10^{-16} A . The diode is reverse biased with a voltage of 700 mV, and its temperature is 300 K. Which of the following is closest to the value of the current flowing through the diode?

- ☒ a: 10^{-16} A
- b: 10^{-13} A
- c: 10^{-10} A
- d: 10^{-7} A
- e: 10^{-4} A

$$I_D = I_s \left[e^{\frac{V_D}{V_T}} - 1 \right] \quad (\text{Note})$$

$$\approx (10^{-16} \text{ A}) \left[e^{\frac{0.7 \text{ V}}{0.026 \text{ V}}} - 1 \right]$$

$$\approx -1.0 \times 10^{-16} \text{ A}$$

- E) A voltage of 5 V is applied across the terminals of a pn junction diode in the reverse-bias direction. If this reverse-bias voltage is then reduced to 1 V, which of the following will happen?
- a: The current through the diode will increase by a factor of approximately five.
 - b: The current through the diode will decrease by a factor of approximately five.
 - c: The diode's junction capacitance will decrease.
 - ☒ d: The diode's junction capacitance will increase.
 - e: None of the above

See sec. 1.2.2

$$C_j = C_{j0} \left(1 + \frac{V_R}{V_{bi}}\right)^{-\frac{1}{2}} \Rightarrow \text{As } V_R \text{ decreases, } C_j \text{ increases.}$$

a, b, and c are false.

- F) The reverse-bias saturation current of a pn junction diode is 2×10^{-12} A. The diode is forward biased with a current of 1.0 mA, and its temperature is 300 K. Which of the following is closest to the value of the voltage across the diode?

- a: 0.4 V
- ☒ b: 0.5 V
- c: 0.6 V
- d: 0.7 V
- e: 0.8 V

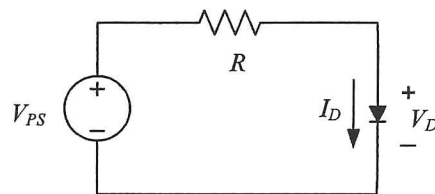
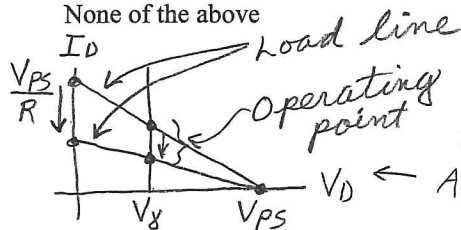
$$I_D = I_S \left[e^{(V_D/V_T)} - 1 \right] \Rightarrow \frac{I_D}{I_S} = e^{(V_D/V_T)} - 1$$

$$\Rightarrow \frac{V_D}{V_T} = \ln\left(\frac{I_D}{I_S} + 1\right) \Rightarrow V_D = V_T \ln\left(\frac{I_D}{I_S} + 1\right)$$

$$\Rightarrow V_D \cong (0.026 \text{ V}) \ln\left(\frac{10^{-3} \text{ A}}{2 \times 10^{-12} \text{ A}} + 1\right) \cong 0.521 \text{ V}$$

- G) The parameters of the diode in the circuit below are $V_\gamma = 0.6$ V and $r_f = 0$. The diode is forward biased. If R increases, which of the following will happen?

- a: The slope of the load line will remain constant.
- ☒ b: I_D will decrease.
- c: V_D will decrease.
- d: All of the above
- e: None of the above

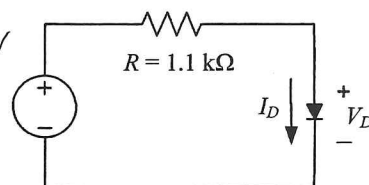


Slope of load line $= -\frac{1}{R}$ (changes)
 As R increases, I_D decreases, and $V_D = V_\gamma$ (constant).

- H) The parameters of the diode in the circuit below are $V_\gamma = 0.6$ V and $r_f = 0$, and $V_{PS} = 10.0$ V. Which of the following is closest to the value of I_D ?

- a: 2 mA
- b: 4 mA
- c: 6 mA
- ☒ d: 8 mA
- e: 10 mA

Note polarity of V_{PS}
 \Rightarrow Forward bias
 $r_f = 0 \Rightarrow V_D = V_\gamma = 0.6 \text{ V}$



$$\Rightarrow I_D = \frac{10 \text{ V} - 0.6 \text{ V}}{1.1 \text{ k}\Omega} \cong 8.545 \text{ mA}$$

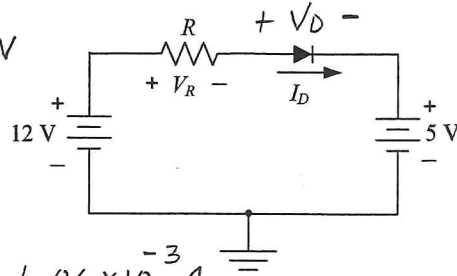
- I) The reverse-bias saturation current of the diode in the circuit below is 10^{-14} A, and the diode's temperature is 300 K. The voltage drop across the resistor V_R is 6.34 V. Which of the following is closest to the value of I_D ?

- a: 0.4 mA
b: 0.7 mA
c: 1.0 mA
d: 1.3 mA
e: 1.6 mA

$$V_D = 12V - 5V - 6.34V = 0.66V$$

$$I_D = I_S \left[e^{\frac{V_D}{V_T}} - 1 \right]$$

$$\Rightarrow I_D = (10^{-14} A) \left[e^{\frac{0.66V}{0.026V}} - 1 \right] \cong 1.06 \times 10^{-3} A$$



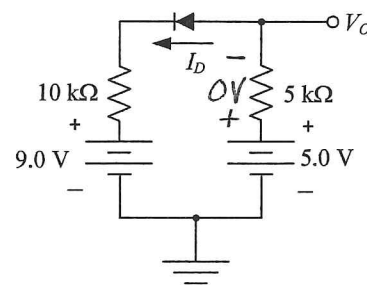
- J) The parameters of the diode in the circuit below are $V_f = 0.7$ V and $r_f = 0$. Which of the following is closest to the value of V_O ?

- a: 9 V
b: 8 V
c: 7 V
d: 6 V
e: 5 V

Note reverse bias

$$\Rightarrow I_D = 0$$

$$\Rightarrow V_O = 5.0V - 0V = 5.0V$$

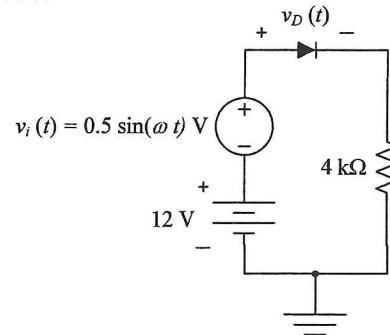


- K) The parameters of the diode in the circuit below are $V_f = 0.7$ V and $r_f = 0$. The diode's temperature is $T = 300$ K. Which of the following is a true statement?

- a: The voltage $v_D(t)$ includes both DC and AC components.
b: The voltage $v_D(t)$ is constant.
c: The voltage $v_D(t)$ includes no AC component.
d: Both b and c are true.
e: None of the above

See text sec. 1.4

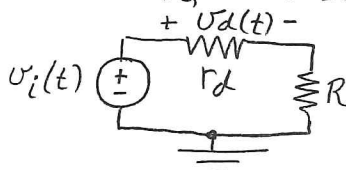
$$v_D(t) = \underset{\substack{\uparrow \\ \text{DC}}}{V_{DQ}} + \underset{\substack{\uparrow \\ \text{AC}}}{v_d(t)}$$



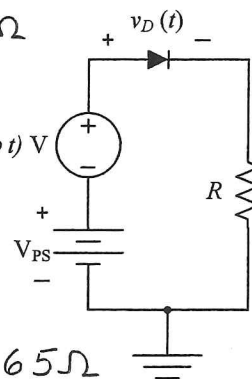
- L) The quiescent current in the circuit below is 3.05 mA. The diode's temperature is $T = 300$ K. Which of the following is closest to the value of R such that the amplitude of the AC component of $v_D(t)$ is 0.95 mV?

- a: 5.0 kΩ
b: 6.0 kΩ
c: 7.0 kΩ
d: 8.0 kΩ
e: 9.0 kΩ

$$r_d = \frac{V_T}{I_{DQ}} \cong \frac{0.026V}{0.00305A} \cong 8.52 \Omega$$



$$v_i(t) = 1.0 \sin(\omega t) V$$



$$0.00095 \sin \omega t V \cong \left(\frac{8.52 \Omega}{8.52 \Omega + R} \right) (1.0 \sin \omega t V)$$

$$\Rightarrow R \cong \left(\frac{1.0}{0.00095} \right) (8.52 \Omega) - 8.52 \Omega \cong 8,965 \Omega$$

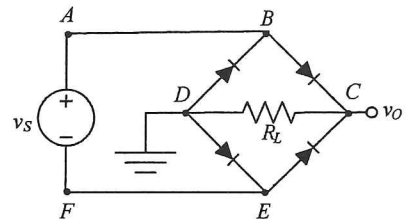
- M) Which of the following materials is used to form the cathode in a Schottky barrier diode?
- a: metal
 - ☒ b: moderately doped n-type semiconductor
 - c: moderately doped p-type semiconductor
 - d: heavily doped n-type semiconductor
 - e: None of the above

See text sec. 1.5.4

- N) Which of the following best describes the typical action of a photodiode?
- ☒ a: Light shining on the diode causes current to flow when the diode is reverse-biased.
 - b: Light shining on the diode causes current to flow when the diode is forward-biased.
 - c: Current flowing through the diode in the reverse-bias direction causes light to be emitted.
 - d: Current flowing through the diode in the forward-bias direction causes light to be emitted.
 - e: None of the above

See text sec. 1.5.2

- O) If a filter capacitor is added to the circuit below, where should it be connected?
- a: between terminals A and B
 - b: between terminals A and D
 - c: between terminals B and E
 - ☒ d: between terminals C and D
 - e: None of the above

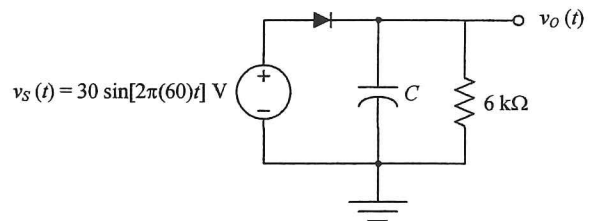


The capacitor is placed in parallel with the load to form an RC lowpass filter.

- P) The cut-in voltage of the diode in the circuit shown below is 0 V. Which of the following is closest to the minimum acceptable value of C if the output's ripple voltage must not exceed 2 mV?
- a: 20 mF
 - b: 30 mF
 - ☒ c: 40 mF
 - d: 50 mF
 - e: 60 mF

$$V_r = \frac{V_M}{fRC}$$

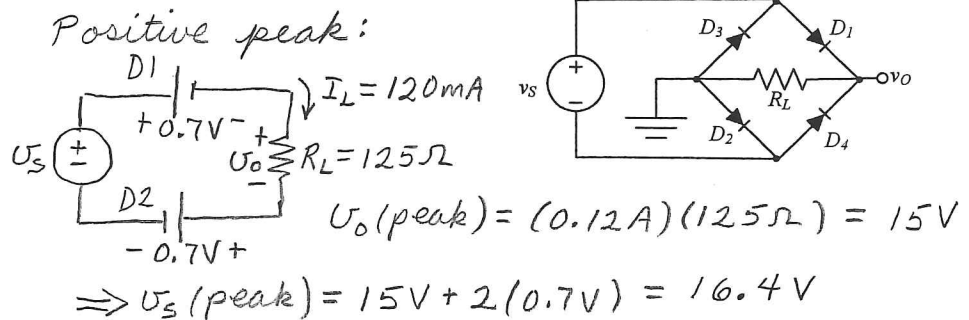
$$\Rightarrow C = \frac{V_M}{fR V_r}$$



$$\Rightarrow C_{min} = \frac{30 \text{ V}}{(60 \text{ Hz})(6 \times 10^3 \Omega)(2 \times 10^{-3} \text{ V})} \approx 41.7 \times 10^{-3} \text{ F}$$

- Q) The parameters of the diodes in the circuit below are $V_f = 0.7 \text{ V}$ and $r_f = 0$, $R_L = 125 \Omega$, and v_S is a 60-Hz sine wave. If the peak current through R_L is 120 mA, which of the following is closest to the peak amplitude of v_S ?

- a: 15.0 V
b: 15.5 V
c: 16.0 V
d: 16.5 V
e: 17.0 V



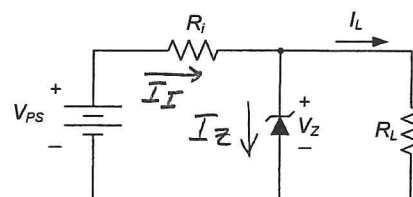
- R) Which of the following functions is typically performed by a Zener diode in a traditional DC power supply?

- a: Half-wave rectification
b: Full-wave rectification
c: Voltage regulation
d: Filtering
e: None of the above

See text sec. 2.2

- S) In the circuit shown below, $R_i = 10 \Omega$, V_{PS} varies between 30 V and 40 V, $V_Z = 15 \text{ V}$, and R_L varies between 5Ω and 9Ω . Which of the following is closest to the maximum diode current?

- a: 0.8 A
b: 0.9 A
c: 1.0 A
d: 1.1 A
e: 1.2 A
- $I_Z = I_Z(\text{max})$
when $V_{PS} = V_{PS}(\text{max})$
and $I_L = I_L(\text{min})$
 $\Rightarrow R_L = R_L(\text{max})$

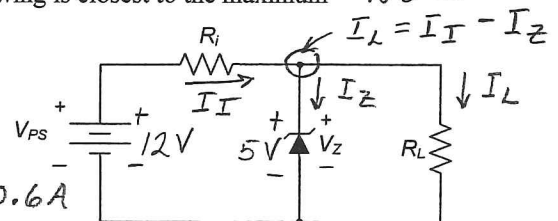


$$\Rightarrow I_I = \frac{40 \text{ V} - 15 \text{ V}}{10 \Omega} = 2.5 \text{ A}, \quad I_L = \frac{15 \text{ V}}{9 \Omega} \approx 1.67 \text{ A}$$

$$\Rightarrow I_Z = I_I - I_L \approx 2.5 \text{ A} - 1.67 \text{ A} \approx 0.83 \text{ A}$$

- T) In the circuit shown below, $R_i = 10 \Omega$, $V_Z = 5 \text{ V}$, and $V_{PS} = 12 \text{ V}$. The current through the diode must be between 100 mA and 400 mA. Which of the following is closest to the maximum permissible value of R_L ?

- a: 22 Ω
b: 17 Ω
c: 12 Ω
d: 7 Ω
e: 2 Ω
- $I_I = \frac{12 \text{ V} - 5 \text{ V}}{10 \Omega} = 0.7 \text{ A}$
 $\Rightarrow I_L(\text{max}) = 0.7 \text{ A} - 0.1 \text{ A} = 0.6 \text{ A}$
 $I_L(\text{min}) = 0.7 \text{ A} - 0.4 \text{ A} = 0.3 \text{ A}$



$$\Rightarrow R_L(\text{max}) = \frac{5 \text{ V}}{0.3 \text{ A}} \approx 16.7 \Omega$$