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1 Общее

- Собственное вращение на угол φ с центром вращения в начале координат:

$$x' = x \cos \varphi - y \sin \varphi$$

$$y' = x \sin \varphi + y \cos \varphi$$
- Расстояние между точками по сфере: $L = R \cdot \arccos(\cos \theta_1 \cdot \cos \theta_2 + \sin \theta_1 \cdot \sin \theta_2 \cdot \cos(\varphi_1 - \varphi_2))$ где θ – широты (от $-\pi$ до π), φ – долготы (от $-\pi$ до π)
- Объем шарового сегмента: $V = \pi h^2(R - \frac{1}{3}h)$, где h – высота от вершины сектора до секущей плоскости
- Площадь поверхности шарового сегмента: $S = 2\pi Rh$, где h – высота
- Код Грея: $g_n = n \oplus \frac{n}{2}$
- Числа Фибоначчи: $F_0 = 0, F_1 = 1, F_n = \frac{(\frac{1+\sqrt{5}}{2})^n - (\frac{1-\sqrt{5}}{2})^n}{\sqrt{5}}$
- Sum-xor property: $a + b = a \oplus b + 2(a \& b), a + b = a|b + a \& b, a \oplus b = a|b - a \& b$
- Число граней в планарном графе(с учётом бесконечной):

$$R = 2 - V + E$$

- Сумма арифметической прогрессии: $S_n = \frac{n(a_1 + a_n)}{2}$
- Сумма геометрической прогрессии: $S_n = \frac{b_1(q^n - 1)}{q - 1}$

2 Коды

2.1 Basic setup

```
#include <bits/stdc++.h>

using namespace std;

#define sz(x) (int)((x).size())
#define all(x) (x).begin(), (x).end()
#define rall(x) (x).rbegin(), (x).rend()

using ll = int64_t;
using int128_t = __int128;
using pii = pair<int, int>;
using pll = pair<ll, ll>;

const char en = '\n';
const int INF = 1e9 + 7;
const ll INFL = 1e18;

mt19937 rnd(chrono::high_resolution_clock::now().time_since_epoch().count());

template<class T>
istream &operator>>(istream &is, vector<T> &a) {
    for (auto &i: a) {
        is >> i;
    }
    return is;
}

void solve() {
}

int32_t main() {
#ifdef LOCAL
    freopen("input.txt", "r", stdin);
#else
    ios_base::sync_with_stdio(0); cin.tie(0);
#endif
    solve();
    return 0;
}
```

2.2 Бесполезное

Санитайзеры:

```
set(CMAKE_CXX_FLAGS "${CMAKE_CXX_FLAGS} -Wall -Wshadow -g -fsanitize=
undefined -fsanitize=bounds -fsanitize=address -D_GLIBCXX_DEBUG")

-Wall -Wextra -pedantic -Wformat=2 -Wfloat-equal -Wconversion -Wlogical-op
-Wshift-overflow=2 -Wduplicated-cond -Wcast-qual -Wcast-align -Werror
```

Прагмы:

```
#pragma GCC optimize("Ofast,no-stack-protector")
#pragma GCC target("sse,sse2,sse3,ssse3,sse4")
#pragma GCC target("popcnt,abm,mmx,avx,avx2,tune=native")
#pragma GCC optimize("unroll-loops")
#pragma GCC optimize("fast-math")
#pragma GCC optimize("section-anchors")
#pragma GCC optimize("profile-values")
#pragma GCC optimize("profile-reorder-functions")
#pragma GCC optimize("tracer")
#pragma GCC optimize("vpt")
#pragma GCC optimize("rename-registers")
#pragma GCC optimize("move-loop-invariants")
#pragma GCC optimize("unswitch-loops")
#pragma GCC optimize("function-sections")
#pragma GCC optimize("data-sections")
#pragma GCC optimize("branch-target-load-optimize")
#pragma GCC optimize("branch-target-load-optimize2")
#pragma GCC optimize("btr-bb-exclusive")
```

Встроенный декартач:

```
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;
template<class T>
```

```
using ordered_set = tree<T, null_type, less<T>, rb_tree_tag,
    tree_order_statistics_node_update>;
ordered_set q; q.find_by_order(1); q.order_of_key(2);
```

Atomic hashset, hashmap:

```
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;
gp_hash_table<int, int> table;
-----
const int RANDOM = chrono::high_resolution_clock::now()
    .time_since_epoch().count();

struct chash {
    int operator()(int x) const { return x ^ RANDOM; }
};
gp_hash_table<key, int, chash> table;
-----
typedef cc_hash_table<int, int, hash<int>> ht;
```

Перебор всех подмасок и надмасок:

```
for (int submask = mask; ; submask = (submask - 1) & mask) {
    // use submask
    if (submask == 0) break;
}

for (int upmask = mask; ; upmask = (upmask + 1) | mask) {
    // use upmask
    if (upmask == maxmask) break;
}
```

2.3 Мосты

```
void dfs (int v, int p = -1) {
    used[v] = true;
    tin[v] = fup[v] = timer++;
    for (auto to: g[v]) {
        if (to == p) {
            continue;
        }
        if (used[to]) {
            fup[v] = min(fup[v], tin[to]);
        }
        else {
            dfs(to, v);
            fup[v] = min(fup[v], fup[to]);
            if (fup[to] > tin[v]) {
                IS_BRIDGE(v, to);
            }
        }
    }
}
```

2.4 Точки сочленения

```
void dfs (int v, int p = -1) {
    used[v] = true;
    tin[v] = fup[v] = timer++;
    int children = 0;
    for (auto to: g[v]) {
        if (to == p) {
            continue;
        }
        if (used[to]) {
            fup[v] = min(fup[v], tin[to]);
        }
        else {
            dfs(to, v);
            fup[v] = min(fup[v], fup[to]);
            if (fup[to] >= tin[v] && p != -1) {
                IS_CUTPOINT(v);
            }
            ++children;
        }
    }
    if (p == -1 && children > 1) {
        IS_CUTPOINT(v);
    }
}
```

2.5 DCP (TheEvilBird)

```
struct Query {
    char type;
    int v, u;

    Query(char type) : type(type) {}
    Query(char type, int v, int u) : type(type), v(v), u(u) {}
};
```

```
struct DCP {
    int n, k, ans; // n - vertex, k - queries
    vector<int> par, rk;
    vector<pair<pii, int>> hist;
    // 0 - par, 1 - rk, 2 - ans;

    int qL, qR;
    pii edge;
    vector<vector<pii>> tree;
    vector<Query> qs;
```

```
DCP(int _n, int _k) {
    n = ans = _n;
    par.resize(n);
    rk.resize(n, 1);
    for (int i = 0; i < n; ++i) par[i] = i;
    k = _k;
    tree.assign(4 * k, vector<pii>());
}
```

```
int dsu_get(int v) {
    while (par[v] != v) v = par[v];
    return v;
}
```

```
void dsu_unite(int a, int b) {
    a = dsu_get(a);
    b = dsu_get(b);
    if (a == b) return;
    if (rk[a] > rk[b]) swap(a, b);
    hist.emplace_back((pii){0, a}, par[a]);
    hist.emplace_back((pii){2, -1}, ans);
    par[a] = b;
    --ans;
    if (rk[a] == rk[b]) {
        hist.emplace_back((pii){1, b}, rk[b]);
        ++rk[b];
    }
}
```

```
void dsu_unite(pii e) {
    dsu_unite(e.first, e.second);
}
```

```
void cancel(pair<pii, int> &el) {
    int &type = el.first.first;
    int &id = el.first.second;
    int &val = el.second;
    if (type == 0) {
        par[id] = val;
    }
    else if (type == 1) {
        rk[id] = val;
    }
    else if (type == 2) {
        ans = val;
    }
}
```

```
void add_edge(int _qL, int _qR, pii e) { // [L, R]
    qL = _qL;
    qR = _qR + 1;
    edge = e;
    add_edge_tree(1, 0, k);
}
```

```
void add_edge_tree(int v, int l, int r) {
    if (qL <= l && r <= qR) {
        tree[v].emplace_back(edge);
        return;
    }
    int m = (l + r) / 2, vL = 2 * v, vR = vL + 1;
    if (qL < m) add_edge_tree(vL, l, m);
    if (m < qR) add_edge_tree(vR, m, r);
}
```

```
void go(vector<Query> &_qs) {
    qs = _qs;
    go_tree(1, 0, k);
}
```

```
void go_tree(int v, int l, int r) {
    int siz = sz(hist);
    for (auto &e: tree[v]) {
        dsu_unite(e);
    }
}
```

```

        if (l + 1 == r) {
            if (qs[l].type == '??') {
                cout << ans << en;
            }
        }
        else {
            int m = (l + r) / 2, vL = 2 * v, vR = vL + 1;
            go_tree(vL, l, m);
            go_tree(vR, m, r);
        }
        while (sz(hist) > siz) {
            cancel(hist.back());
            hist.pop_back();
        }
    }
};

void solve() {
    int n, k;
    cin >> n >> k;
    DCP dcp(n, k);
    set<pair<pii, int>> edges;
    vector<Query> qs;
    for (int i = 0; i < k; ++i) {
        char tp;
        cin >> tp;
        if (tp == '??') {
            qs.emplace_back(tp);
        }
        else {
            int v, u;
            cin >> v >> u;
            --v; --u;
            if (v > u) swap(v, u);
            qs.emplace_back(tp, v, u);
            if (tp == '?+') {
                edges.emplace((pii){v, u}, i);
            }
            else {
                auto it = edges.lower_bound((pii){v, u}, 0);
                dcp.add_edge(it->second, i, it->first);
                edges.erase(it);
            }
        }
    }
    for (auto &e: edges) {
        dcp.add_edge(e.second, k - 1, e.first);
    }
    if (k) dcp.go(qs);
}

```

2.6 MaxFlow (TheEvilBird)

```

struct MaxFlow {
    struct Edge {
        ll flow, cap;
        int to, id;

        Edge() {}

        Edge(ll flow, ll cap, int to, int id) : flow(flow), cap(cap), to(to), id(id) {}
    };

    int n;
    vector<vector<Edge>> g;
    vector<int> d, head, used;
    ll max_cap;
    int s, t;

    MaxFlow() {}

    MaxFlow(int _n) {
        n = _n;
        g.resize(n);
    }

    void add_edge(int from, int to, ll cap) {
        g[from].emplace_back(0, cap, to, sz(g[to]));
        g[to].emplace_back(0, 0, from, sz(g[from]) - 1);
    }

    bool bfs() {
        d.assign(n, INF);
        d[s] = 0;
        queue<int> q;
        q.push(s);
        while (!q.empty()) {
            int v = q.front();
            q.pop();
            for (auto e: g[v]) {

```

```

                if (d[e.to] == INF && e.cap - e.flow >= max_cap) {
                    d[e.to] = d[v] + 1;
                    q.push(e.to);
                }
            }
        }
        return d[t] != INF;
    }

    ll dfs(int v, ll cur_flow) {
        if (v == t) {
            return cur_flow;
        }
        for (; head[v] < sz(g[v]); ++head[v]) {
            auto &e = g[v][head[v]];
            if (e.cap - e.flow >= max_cap && d[v] + 1 == d[e.to]) {
                ll new_flow = dfs(e.to, min(cur_flow, e.cap - e.flow));
                if (new_flow) {
                    e.flow += new_flow;
                    g[e.to][e.id].flow -= new_flow;
                    return new_flow;
                }
            }
        }
        return 0;
    }

    ll find_max_flow(int _s, int _t) {
        s = _s;
        t = _t;
        ll res = 0;
        for (int k = 30; k >= 0; --k) {
            max_cap = (1 << k);
            while (bfs()) {
                head.assign(n, 0);
                ll flow = 0;
                do {
                    flow = dfs(s, INFL);
                    res += flow;
                } while (flow);
            }
            return res;
        }
    }

    ll dfs_const_flow(int v, ll cur_flow) {
        used[v] = 1;
        if (v == t) {
            return cur_flow;
        }
        for (auto &e: g[v]) {
            if (!used[e.to] && e.cap - e.flow > 0) {
                ll new_flow = dfs_const_flow(e.to, min(cur_flow, e.cap - e.flow));
                if (new_flow) {
                    e.flow += new_flow;
                    g[e.to][e.id].flow -= new_flow;
                    return new_flow;
                }
            }
        }
        return 0;
    }

    bool find_const_flow(int _s, int _t, ll F) {
        s = _s;
        t = _t;
        ll res = 0, flow = 0;
        max_cap = F;
        do {
            used.assign(n, 0);
            flow = dfs_const_flow(s, INF);
            res += flow;
        } while (flow && res < F);
        return res == F;
    }

    ll get_edge_flow(int v, int id) {
        return g[v][id].flow;
    }
};

```

2.7 MinCostMaxFlow (TheEvilBird)

```

struct MinCostMaxFlow {
    struct Edge {
        ll flow, cap, price;
        int to, id;

        Edge() {}

        Edge(ll flow, ll cap, ll price, int to, int id) : flow(flow), cap(cap), price(price), to(to), id(id) {}
    };

```

```

};

int n;
int s, t;
ll ans;
vector<vector<Edge>> g;
vector<int> d;
vector<ll> add_f;
vector<pii> par;

MinCostMaxFlow() {}

MinCostMaxFlow(int _n) {
    n = _n;
    g.resize(n);
}

void add_edge(int from, int to, ll cap, ll price) {
    g[from].emplace_back(0, cap, price, to, sz(g[to]));
    g[to].emplace_back(0, 0, -price, from, sz(g[from]) - 1);
}

ll get_edge_flow(int v, int id) {
    return g[v][id].flow;
}

void FB() {
    d.assign(n, INF);
    add_f.assign(n, 0);
    par.assign(n, {-1, -1});
    d[s] = 0;
    add_f[0] = INF;
    queue<int> q;
    q.push(s);
    vector<int> used(n, 0);
    used[s] = 1;
    while (!q.empty()) {
        int v = q.front();
        q.pop();
        used[v] = 0;
        for (int i = 0; i < sz(g[v]); ++i) {
            auto &e = g[v][i];
            if (e.flow < e.cap && d[e.to] > d[v] + e.price) {
                d[e.to] = d[v] + e.price;
                add_f[e.to] = min(add_f[v], e.cap - e.flow);
                par[e.to] = {v, i};
                if (!used[e.to]) {
                    q.push(e.to);
                    used[e.to] = 1;
                }
            }
        }
    }
}

void push_flow(ll flow) {
    int cur = t;
    while (cur != s) {
        int prev = par[cur].first, id = par[cur].second;
        g[prev][id].flow += flow;
        g[cur][g[prev][id].id].flow -= flow;
        ans += g[prev][id].price * flow;
        cur = prev;
    }
}

ll min_cost_max_flow(int _s, int _t) {
    ans = 0;
    s = _s; t = _t;
    while (true) {
        FB();
        ll flow = add_f[t];
        if (flow == 0) {
            break;
        }
        push_flow(flow);
    }
    return ans;
}
};

```

2.8 Кун

```

bool dfs(int v) {
    if (used[v])
        return false;
    used[v] = true;
    for (auto u: g[v]) {
        if (back[u] == -1 || dfs(back[u])) {
            back[u] = v;
            return true;
        }
    }
}

```

```

    }
    return false;
}

```

2.9 HLD (TheEvilBird)

```

struct HLD {

    // insert SegTree code
    struct SegTree { };

    int n, T;
    SegTree st;
    vector<vector<int>> tree;
    vector<int> par, siz, tin, tout, head;
    ll ans;

    HLD(int _n) {
        n = _n;
        tree.resize(n);
        par.resize(n, -1);
        siz.resize(n, 0);
        tin.resize(n);
        tout.resize(n);
        head.resize(n);
        st = SegTree(n);
    }

    void add_edge(int v, int u) {
        tree[v].emplace_back(u);
        tree[u].emplace_back(v);
    }

    void build(int v = 0) {
        dfs_siz(v, v);
        T = 0;
        head[v] = v;
        dfs_hld(v, v);
    }

    void dfs_siz(int v, int p) {
        par[v] = p;
        siz[v] = 1;
        for (auto &u: tree[v]) {
            if (u != p) {
                dfs_siz(u, v);
                siz[v] += siz[u];
            }
        }
        for (int i = 0; i < sz(tree[v]); ++i) {
            int x = tree[v][0], u = tree[v][i];
            if (x == p || siz[u] > siz[x]) {
                swap(tree[v][0], tree[v][i]);
            }
        }
    }

    void dfs_hld(int v, int p) {
        tin[v] = T++;
        for (auto u: tree[v]) {
            if (u == p) {
                continue;
            }
            if (u == tree[v][0]) {
                head[u] = head[v];
            }
            else {
                head[u] = u;
            }
            dfs_hld(u, v);
        }
        tout[v] = T;
    }

    void update(int v, int val) {
        st.update_segment(tin[v], tin[v], val);
    }

    bool is_anc(int v, int u) {
        return tin[v] <= tin[u] && tout[u] <= tout[v];
    }

    void go_up(int &v, int u) {
        while (!is_anc(head[v], u)) {
            ans = max(ans, st.get(tin[head[v]], tin[v]));
            v = par[head[v]];
        }
    }

    ll get(int v, int u) { // max on path
        ans = -INFL;
        go_up(v, u);
    }
}

```

```

        go_up(u, v);
        if (!is_anc(v, u)) {
            swap(v, u);
        }
        ans = max(ans, st.get(tin[v], tin[u]));
        return ans;
    }
};

```

```

        return ans;
    }

    ll get(int x) {
        return get(root, -n, n, x);
    }
};

```

2.10 Личао (FedShat)

```

struct Lichao { // min
    struct Line {
        ll k, b;

        Line() : k(0), b(INFL) {};

        Line(ll k, ll b) : k(k), b(b) {};

        ll operator()(ll x) {
            return k * x + b;
        }

        bool operator==(Line a) {
            return a.k == k && a.b == b;
        }

        bool operator!=(Line a) {
            return !(a == *this);
        }
    };

    struct Node {
        Node *l = nullptr, *r = nullptr;
        Line cur;

        Node() = default;

        Node *root = nullptr;
        int n = 1e5 + 1;

        void createnode(Node *&v) {
            if (v == nullptr) {
                v = new Node();
            }
        }

        void add(Node *&v, int l, int r, Line cur) {
            createnode(v);
            if (l + 1 == r) {
                if (cur(l) < v->cur(l))
                    v->cur = cur;
                return;
            }
            int m = (l + r) / 2;
            if (v->cur.k == cur.k) {
                v->cur = {cur.k, min(v->cur.b, cur.b)};
                return;
            }
            ll xc = (cur.b - v->cur.b) / (v->cur.k - cur.k);
            auto prev = v->cur;
            if (xc < m) {
                if (v->cur.k < cur.k)
                    add(v->l, l, m, cur);
                else {
                    v->cur = cur;
                    add(v->l, l, m, prev);
                }
            } else {
                if (v->cur.k < cur.k) {
                    v->cur = cur;
                    add(v->r, m, r, prev);
                } else
                    add(v->r, m, r, cur);
            }
        }

        void add(Line cur) {
            add(root, -n, n, cur);
        }

        ll get(Node *v, int l, int r, int x) {
            if (l + 1 == r) {
                return v->cur(x);
            }
            int m = (l + r) / 2;
            ll ans = v->cur(x);
            if (x < m && v->l != nullptr) {
                ans = min(ans, get(v->l, l, m, x));
            } else if (x >= m && v->r != nullptr) {
                ans = min(ans, get(v->r, m, r, x));
            }
        }
    };
};

```

2.11 Segment Tree (TheEvilBird)

```

struct SegTree {

    static const ll off = 0;

    struct Node {
        ll val = 0;
        ll push = off;

        Node() {}

        Node(ll val) : val(val) {}

        Node operator+(const Node &other) const {
            return Node(val + other.val);
        }

        void operator+=(const Node &other) {
            val += other.val;
        }

        void use_push(int len = 1) {
            val += push * (ll)(len);
        }

        void update_push(ll pushed) {
            push += pushed;
        }
    };

    int n, qL, qR;
    ll val;
    Node ans;

    vector<Node> tree;
    vector<ll> a;

    SegTree() {}

    SegTree(int _n) {
        n = _n;
        tree.assign(4 * n, 0);
    }

    void update_vertex(int v, int l, int r) { // [l, r)
        int m = (l + r) / 2, vL = 2 * v, vR = vL + 1;
        push(vL, l, m);
        push(vR, m, r);
        tree[v] = tree[vL] + tree[vR];
    }

    void push(int v, int l, int r) { // [l, r)
        if (tree[v].push == off) return;
        int m = (l + r) / 2, vL = 2 * v, vR = vL + 1;
        tree[v].use_push(r - l);
        if (l + 1 != r) {
            tree[vL].update_push(tree[v].push);
            tree[vR].update_push(tree[v].push);
        }
        tree[v].push = off;
    }

    void build(vector<ll> &a) {
        a = _a;
        build_tree(1, 0, n);
    }

    void build_tree(int v, int l, int r) { // [l, r)
        if (l + 1 == r) {
            tree[v] = Node(a[l]);
            return;
        }
        int m = (l + r) / 2, vL = 2 * v, vR = vL + 1;
        build_tree(vL, l, m);
        build_tree(vR, m, r);
        update_vertex(v, l, r);
    }

    void update_segment(int _qL, int _qR, ll _val) { // [_qL, _qR)
        qL = _qL;
        qR = _qR + 1;
        val = _val;
        update_segment_tree(1, 0, n);
    }
};

```

```

}

void update_segment_tree(int v, int l, int r) { // [l, r)
    push(v, l, r);
    if (ql <= l && r <= qR) {
        tree[v].update_push(val);
        push(v, l, r);
        return;
    }
    int m = (l + r) / 2, vL = 2 * v, vR = vL + 1;
    if (ql < m) update_segment_tree(vL, l, m);
    if (m < qR) update_segment_tree(vR, m, r);
    update_vertex(v, l, r);
}

ll get(int _ql, int _qR) { // [_ql, _qR]
    ql = _ql;
    qR = _qR + 1;
    ans = Node();
    get_tree(1, 0, n);
    return ans.val;
}

void get_tree(int v, int l, int r) { // [l, r)
    push(v, l, r);
    if (ql <= l && r <= qR) {
        ans = ans + tree[v];
        return;
    }
    int m = (l + r) / 2, vL = 2 * v, vR = vL + 1;
    if (ql < m) get_tree(vL, l, m);
    if (m < qR) get_tree(vR, m, r);
}
};

```

2.12 Segment Tree Down (TheEvilBird)

```

struct SegTreeDown {

    struct Node {
        ll val = 0;

        Node() {}
        Node(ll val) : val(val) {}

        Node operator+(const Node &other) const {
            return Node(val + other.val);
        }

        void operator+=(const Node &other) {
            val += other.val;
        }
    };

    int n;
    vector<Node> tree;

    SegTreeDown(int _n) {
        n = _n;
        tree.assign(2 * n, Node());
    }

    void build(vector<ll> &a) {
        for (int i = 0; i < n; ++i) {
            tree[i + n] = Node(a[i]);
        }
        for (int i = n - 1; i >= 1; --i) {
            tree[i] = tree[2 * i] + tree[2 * i + 1];
        }
    }

    void update(int i, ll val) {
        i += n;
        tree[i] = val;
        i /= 2;
        while (i != 0) {
            tree[i] = tree[2 * i] + tree[2 * i + 1];
            i /= 2;
        }
    }

    ll get(int l, int r) { // [l, r)
        --r;
        l += n;
        r += n;
        Node ans;
        while (l <= r) {
            if (l % 2 == 1) {
                ans += tree[l];
                ++l;
            }
            if (r % 2 == 0) {
                ans += tree[r];
            }
        }
    }
};

```

```

        --r;
    }
    l /= 2;
    r /= 2;
}
return ans.val;
}
};

```

2.13 Segment Tree Beats (TheEvilBird)

```

struct SegTree {
    struct Node {
        ll max, sec_max;
        int cnt_max;
        ll min, sec_min;
        int cnt_min;
        ll sum;
        ll push_add;
        ll push_eq;
    };

    int n, ql, qR;
    ll val, ans;

    vector<Node> tree;
    vector<ll> a;

    SegTree(int _n) {
        n = _n;
        tree.assign(4 * n, {0, -INFL, 1, 0, INFL, 1, 0, 0, -1});
    }

    void update_vertex(int v, int l, int r) {
        int m = (l + r) / 2, vL = 2 * v, vR = vL + 1;

        tree[v].sum = tree[vL].sum + tree[vR].sum;

        tree[v].max = max(tree[vL].max, tree[vR].max);
        tree[v].sec_max = max(tree[vL].sec_max, tree[vR].sec_max);
        tree[v].cnt_max = 0;
        if (tree[vL].max == tree[v].max) {
            tree[v].cnt_max += tree[vL].cnt_max;
        }
        else {
            tree[v].sec_max = max(tree[v].sec_max, tree[vL].max);
        }
        if (tree[vR].max == tree[v].max) {
            tree[v].cnt_max += tree[vR].cnt_max;
        }
        else {
            tree[v].sec_max = max(tree[v].sec_max, tree[vR].max);
        }

        tree[v].min = min(tree[vL].min, tree[vR].min);
        tree[v].sec_min = min(tree[vL].sec_min, tree[vR].sec_min);
        tree[v].cnt_min = 0;
        if (tree[vL].min == tree[v].min) {
            tree[v].cnt_min += tree[vL].cnt_min;
        }
        else {
            tree[v].sec_min = min(tree[v].sec_min, tree[vL].min);
        }
        if (tree[vR].min == tree[v].min) {
            tree[v].cnt_min += tree[vR].cnt_min;
        }
        else {
            tree[v].sec_min = min(tree[v].sec_min, tree[vR].min);
        }
    }

    void recalc_eq(int v, int l, int r, ll cur) {
        tree[v].max = tree[v].min = tree[v].push_eq = cur;
        tree[v].sec_max = -INFL;
        tree[v].sec_min = INFL;
        tree[v].cnt_max = tree[v].cnt_min = r - l;
        tree[v].sum = cur * (ll)(r - l);
        tree[v].push_add = 0;
    }

    void recalc_add(int v, int l, int r, ll cur) {
        if (tree[v].min == tree[v].max) {
            recalc_eq(v, l, r, tree[v].max + cur);
            return;
        }
        tree[v].max += cur;
        if (tree[v].sec_max != -INFL) {
            tree[v].sec_max += cur;
        }

        tree[v].min += cur;
        if (tree[v].sec_min != INFL) {
            tree[v].sec_min += cur;
        }
    }
};

```

```

    }

    tree[v].sum += (ll)(r - l) * cur;
    tree[v].push_add += cur;
}

void recalc_min(int v, int l, int r, ll cur) {
    if (tree[v].min >= cur) {
        recalc_eq(v, l, r, cur);
        return;
    }
    if (tree[v].max <= cur) return;
    if (tree[v].sec_min == tree[v].max) {
        tree[v].sec_min = cur;
    }
    tree[v].sum -= (ll)(tree[v].max - cur) *
        (ll)(tree[v].cnt_max);
    tree[v].max = cur;
}

void recalc_max(int v, int l, int r, ll cur) {
    if (tree[v].max <= cur) {
        recalc_eq(v, l, r, cur);
        return;
    }
    if (tree[v].min >= cur) return;
    if (tree[v].sec_max == tree[v].min) {
        tree[v].sec_max = cur;
    }
    tree[v].sum += (ll)(tree[v].max - cur) *
        (ll)(tree[v].cnt_max);
    tree[v].min = cur;
}

void push(int v, int l, int r) {
    if (l + 1 == r) return;
    int m = (l + r) / 2, vL = 2 * v, vR = vL + 1;
    if (tree[v].push_eq != -1) {
        recalc_eq(vL, l, m, tree[v].push_eq);
        recalc_eq(vR, m, r, tree[v].push_eq);
        tree[v].push_eq = -1;
        return;
    }

    recalc_add(vL, l, m, tree[v].push_add);
    recalc_add(vR, m, r, tree[v].push_add);
    tree[v].push_add = 0;

    recalc_min(vL, l, m, tree[v].max);
    recalc_min(vR, m, r, tree[v].max);

    recalc_max(vL, l, m, tree[v].min);
    recalc_max(vR, m, r, tree[v].min);
}

void build(vector<ll> &a) {
    a = _a;
    build_tree(1, 0, n);
}

void build_tree(int v, int l, int r) {
    if (l + 1 == r) {
        tree[v] = {a[l], -INFL, 1, a[l],
                    INFL, 1, a[l], 0, -1};
        return;
    }
    int m = (l + r) / 2, vL = 2 * v, vR = vL + 1;
    build_tree(vL, l, m);
    build_tree(vR, m, r);
    update_vertex(v, l, r);
}

void update_segment_min(int _qL, int _qR, ll _val) {
    qL = _qL;
    qR = _qR + 1;
    val = _val;
    update_segment_min_tree(1, 0, n);
}

void update_segment_min_tree(int v, int l, int r) {
    if (tree[v].max <= val) return;
    if (qL <= l && r <= qR && tree[v].sec_max < val) {
        recalc_min(v, l, r, val);
        return;
    }
    push(v, l, r);
    int m = (l + r) / 2, vL = 2 * v, vR = vL + 1;
    if (qL < m) update_segment_min_tree(vL, l, m);
    if (m < qR) update_segment_min_tree(vR, m, r);
    update_vertex(v, l, r);
}

void update_segment_max(int _qL, int _qR, ll _val) {
    qL = _qL;
    qR = _qR + 1;
    val = _val;

```

```

    update_segment_max_tree(1, 0, n);
}

void update_segment_max_tree(int v, int l, int r) {
    if (tree[v].min >= val) return;
    if (qL <= l && r <= qR && tree[v].sec_min > val) {
        recalc_max(v, l, r, val);
        return;
    }
    push(v, l, r);
    int m = (l + r) / 2, vL = 2 * v, vR = vL + 1;
    if (qL < m) update_segment_max_tree(vL, l, m);
    if (m < qR) update_segment_max_tree(vR, m, r);
    update_vertex(v, l, r);
}

void update_segment_add(int _qL, int _qR, ll _val) {
    qL = _qL;
    qR = _qR + 1;
    val = _val;
    update_segment_add_tree(1, 0, n);
}

void update_segment_add_tree(int v, int l, int r) {
    if (qL <= l && r <= qR) {
        recalc_add(v, l, r, val);
        return;
    }
    push(v, l, r);
    int m = (l + r) / 2, vL = 2 * v, vR = vL + 1;
    if (qL < m) update_segment_add_tree(vL, l, m);
    if (m < qR) update_segment_add_tree(vR, m, r);
    update_vertex(v, l, r);
}

ll get(int _qL, int _qR) {
    qL = _qL;
    qR = _qR + 1;
    ans = 0;
    get_tree(1, 0, n);
    return ans;
}

void get_tree(int v, int l, int r) {
    if (qL <= l && r <= qR) {
        ans += tree[v].sum;
        return;
    }
    push(v, l, r);
    int m = (l + r) / 2, vL = 2 * v, vR = vL + 1;
    if (qL < m) get_tree(vL, l, m);
    if (m < qR) get_tree(vR, m, r);
}

void print_all() {
    print_all_tree(1, 0, n);
}

void print_all_tree(int v, int l, int r) {
    if (l + 1 == r) {
        cout << tree[v].sum << endl;
        return;
    }
    push(v, l, r);
    int m = (l + r) / 2, vL = 2 * v, vR = vL + 1;
    print_all_tree(vL, l, m);
    print_all_tree(vR, m, r);
}
};

```

2.14 Persistent Segment Tree (Sweezyk)

```

struct Node {
    Node *l, *r;
    int mx;
    Node() {
        mx = -1;
        l = r = nullptr;
    }
};

const int N = 1e7 + 4e6;
const int LG = 20;

Node* nodes[N];
int ptr;

Node* new_node() {
    return nodes[ptr++];
}

Node* get_left(Node* t) {
    if (t && t->l) return t->l;
}

```

```
    return nullptr;
}

Node* get_right(Node* t) {
    if (t && t->r) return t->r;
    return nullptr;
}

int get_max(Node* t) {
    if (!t) return 0;
    return t->mx;
}

void update(int i, int val, Node* t, Node* old_t, int lx, int rx) {
    if (lx + 1 == rx) {
        t->mx = max(t->mx, val);
        return;
    }
    int m = (lx + rx) / 2;
    if (i < m) {
        t->l = new_Node();
        if (old_t && old_t->l) {
            t->l->mx = old_t->l->mx;
        }
        t->r = get_right(old_t);
        update(i, val, t->l, get_left(old_t), lx, m);
    } else {
        t->r = new_Node();
        if (old_t && old_t->r) {
            t->r->mx = old_t->r->mx;
        }
        t->l = get_left(old_t);
        update(i, val, t->r, get_right(old_t), m, rx);
    }
    t->mx = max(get_max(get_left(t)), get_max(get_right(t)));
};

int get(int l, int r, Node* t, int lx, int rx) {
    if (!t || lx >= r || rx <= l) return -1;
    if (lx >= l && rx <= r) return t->mx;
    int m = (lx + rx) / 2;
    return max(get(l, r, t->l, lx, m), get(l, r, t->r, m, rx));
}
```

2.15 Fenwick (TheEvilBird)

```
struct Fenwick {
    int n;
    vector<ll> f;

    Fenwick(int _n) {
        n = _n;
        f.assign(n + 1, 0);
    }

    void update(int x, ll delta) {
        for (int i = x; i <= n; i += i & -i) {
            f[i] += delta;
        }
    }

    ll get_sum(int x) {
        ll s = 0;
        for (int i = x; i > 0; i -= i & -i) {
            s += f[i];
        }
        return s;
    }

    ll get(int L, int R) { // [L, R]
        return get_sum(R) - get_sum(L - 1);
    }
};
```

2.16 Sparse table (TheEvilBird)

```
struct Sparse {
    int n;
    vector<int> lg;
    vector<vector<ll>> table;

    Sparse(int _n) {
        n = _n;
        lg.resize(n + 1);
        for (int i = 2; i <= n; ++i) {
            lg[i] = lg[i / 2] + 1;
        }
        table.resize(lg[n] + 1, vector<ll> (n));
        for (int i = 0; i < n; ++i) table[0][i] = INF;
    }
};
```

```
    }

    void build() {
        for (int i = 1; i < table.size(); ++i) {
            for (int j = 0; j + (1 << i) <= n; ++j) {
                table[i][j] = min(table[i - 1][j],
                                    table[i - 1][j + (1 << (i - 1))]);
            }
        }

        ll get(int L, int R) { // [L, R]
            int D = R - L + 1, x = lg[D];
            return min(table[x][L], table[x][R - (1 << x) + 1]);
        }
    };
};
```

2.17 Treap (Sweezyk)

```
struct Node {
    int x, y, size, push, cnt;
    Node *l, *r;

    Node(int val) : x(val), y(rng()), size(1), push(0), cnt(0), l(nullptr),
        r(nullptr) {}
};

void push(Node *t) {
    if (t == nullptr) return;
    int p = t->push;
    if (p == 0) return;
    if (t->l != nullptr) {
        t->l->cnt += p;
        t->l->push += p;
    }
    if (t->r != nullptr) {
        t->r->cnt += p;
        t->r->push += p;
    }
    t->push = 0;
}

int size(Node *t) {
    return (t ? t->size : 0);
}

void update(Node *t) {
    if (t == nullptr) return;
    t->size = size(t->l) + size(t->r) + 1;
}

pair<Node *, Node *> split(Node *t, int k) {
    if (t == nullptr) return {nullptr, nullptr};
    if (k == 0) return {nullptr, t};
    push(t);
    if (size(t->l) + 1 <= k) {
        auto [l, r] = split(t->r, k - size(t->l) - 1);
        t->r = l;
        update(t);
        return {t, r};
    } else {
        auto [l, r] = split(t->l, k);
        t->l = r;
        update(t);
        return {l, t};
    }
}

Node *merge(Node *tl, Node *tr) {
    if (tl == nullptr) return tr;
    if (tr == nullptr) return tl;
    push(tl);
    push(tr);
    if (tl->y > tr->y) {
        tl->r = merge(tl->r, tr);
        update(tl);
        return tl;
    } else {
        tr->l = merge(tl, tr->l);
        update(tr);
        return tr;
    }
}

void dfs(Node *t) {
    if (t == nullptr) return;
    push(t);
    dfs(t->l);
    cout << t->x << ' ' << t->cnt << '\n';
    dfs(t->r);
}

void solve() {
```



```
int n, m;
cin >> n >> m;
Node *root = nullptr;
for (int i = 1; i <= n; i++) {
    Node *add = new Node(i);
    root = merge(root, add);
}
for (int i = 0; i < m; i++) {
    int l, r;
    cin >> l >> r;
    auto[L, R] = split(root, r);
    auto[L1, L2] = split(L, l - 1);
    L2->push = 1;
    L2->cnt += 1;
    root = merge(L2, merge(L1, R));
}
dfs(root);
}
```

2.18 Extended GCD (Sweezyk)

```
template<typename T>
T extgcd(T a, T b, T &x, T &y) {
    if (a == 0) {
        x = 0;
        y = 1;
        return b;
    }
    T p = b / a;
    T g = extgcd(b - p * a, a, y, x);
    x -= p * y;
    return g;
}

template<typename T>
bool diophantine(T a, T b, T c, T &x, T &y, T &g) {
    if (a == 0 && b == 0) {
        if (c == 0) {
            x = y = g = 0;
            return true;
        }
        return false;
    }
    if (a == 0) {
        if (c % b == 0) {
            x = 0;
            y = c / b;
            g = abs(b);
            return true;
        }
        return false;
    }
    if (b == 0) {
        if (c % a == 0) {
            x = c / a;
            y = 0;
            g = abs(a);
            return true;
        }
        return false;
    }
    g = extgcd(a, b, x, y);
    if (c % g != 0) {
        return false;
    }
    T dx = c / a;
    c -= dx * a;
    T dy = c / b;
    c -= dy * b;
    x = dx + (T) ((__int128) x * (c / g) % b);
    y = dy + (T) ((__int128) y * (c / g) % a);
    g = abs(g);
    return true;
    // |x|, |y| <= max(|a|, |b|, |c|) [tested]
}

bool crt(long long k1, long long m1, long long k2, long long m2, long long
&k, long long &m) {
    k1 %= m1;
    if (k1 < 0) k1 += m1;
    k2 %= m2;
    if (k2 < 0) k2 += m2;
    long long x, y, g;
    if (!diophantine(m1, -m2, k2 - k1, x, y, g)) {
        return false;
    }
    long long dx = m2 / g;
    long long delta = x / dx - (x % dx < 0);
    k = m1 * (x - dx * delta) + k1;
    m = m1 / g * m2;
    assert(0 <= k && k < m);
    return true;
}
```

2.19 FFT (FedShat)

```
using ll = long long;

constexpr int mod = 998244353, root = 3;

int binpow(int a, int n, int mod) {
    if (n == 0) {
        return 1;
    }
    if (n % 2 == 0) {
        int b = binpow(a, n / 2, mod);
        return (b * 1ll * b) % mod;
    }
    return (a * 1ll * binpow(a, n - 1, mod)) % mod;
}

vector<int> W1, W2;

vector<int> ntt(vector<int> a, bool inv = false) {
    if (a.size() == 1) {
        return a;
    }
    int n = a.size();
    vector<int> a0, a1;
    for (int i = 0; i < n; ++i) {
        if (i % 2 == 0) {
            a0.push_back(a[i]);
        } else {
            a1.push_back(a[i]);
        }
    }
    a0 = ntt(a0, inv);
    a1 = ntt(a1, inv);
    int w = 1, wn = W1[n];
    if (inv) {
        wn = W2[n];
    }
    vector<int> res(n);
    for (int k = 0; k < n / 2; ++k) {
        int t = (w * 1ll * a1[k]) % mod;
        res[k] = (a0[k] + t) % mod;
        res[k + n / 2] = ((a0[k] - t) % mod + mod) % mod;
        w = (w * 1ll * wn) % mod;
    }
    return res;
}

vector<int> ntt_inv(vector<int> a) {
    a = ntt(a, true);
    int n = a.size(), inv = binpow(n, mod - 2, mod);
    for (int i = 0; i < n; ++i) {
        a[i] = (a[i] * 1ll * inv) % mod;
    }
    return a;
}

int main() {
    int n;
    cin >> n;
    n = (1 << n);
    vector<int> a(n), b(n);
    cin >> a >> b;
    n *= 2;
    a.resize(n);
    b.resize(n);
    W1.resize(n + 1);
    W2.resize(n + 1);
    for (int i = 1; i <= n; i *= 2) {
        W1[i] = binpow(root, (mod - 1) / i, mod);
        W2[i] = binpow(W1[i], mod - 2, mod);
    }
    a = ntt(a);
    b = ntt(b);
    for (int i = 0; i < n; ++i) {
        a[i] = (a[i] * 1ll * b[i]) % mod;
    }
    a = ntt_inv(a);
    for (int i: a) {
        cout << i << " ";
    }
}
```

2.20 KTO (FedShat)

```
struct Eq { // x = a (mod m)
    ll a, m;
```

```
Eq() {};  
  
Eq(ll a, ll m) : a(a), m(m) {};  
};  
  
ll binpow(ll a, ll n, ll m) {  
    if (n == 0) {  
        return 1;  
    }  
    if (n % 2 == 0) {  
        int128_t b = binpow(a, n / 2, m);  
        return (b * b) % m;  
    }  
    int128_t x = binpow(a, n - 1, m);  
    return (a * x) % m;  
}  
  
ll binpow(ll a, ll n) {  
    if (n == 0) {  
        return 1;  
    }  
    if (n % 2 == 0) {  
        ll b = binpow(a, n / 2);  
        return b * b;  
    }  
    return a * binpow(a, n - 1);  
}  
  
ll phi(ll a) {  
    ll d = 2, k = a;  
    map<ll, int> cnt;  
    while (d * d <= a) {  
        if (k % d == 0) {  
            k /= d;  
            ++cnt[d];  
        } else {  
            ++d;  
        }  
    }  
    if (k != 1) {  
        ++cnt[k];  
    }  
    ll ans = 1;  
    for (auto i: cnt) {  
        ans *= binpow(i.first, i.second - 1) * (i.first - 1);  
    }  
    return ans;  
}  
  
ll gcd(ll a, ll b) {  
    return std::gcd(abs(a), abs(b));  
}  
  
Eq solve(Eq ai, Eq bi) {  
    if (ai.m == -1 || bi.m == -1) {  
        return {0, -1};  
    }  
    ll a = ai.m, b = bi.m, c = ai.a - bi.a;  
    ll d = ::gcd(a, b);  
    a /= d;  
    b /= d;  
    if (c % d != 0) {  
        return {0, -1};  
    }  
    c /= d;  
    ll x = (((int128_t) -c * (int128_t) binpow(a, phi(b) - 1, b)) % b + b)  
        % b;  
    x = (((int128_t) ai.m * (int128_t) x + ai.a) % lcm(ai.m, bi.m);  
    return {x, lcm(ai.m, bi.m)};  
}
```

2.21 Обратные по простому модулю

Пусть дан простой модуль m . Для каждого числа из $[1, m - 1]$ найти обратное к нему.

```
r[1] = 1;  
for (int i = 2; i < m; ++i) {  
    r[i] = (m - (m / i) * r[m % i] % m) % m;  
}
```

2.22 Обратные факториалы

```
int inv(int a, int m) {  
    if (a == 1)  
        return 1;  
    return (1 - inv(m % a, a) * m) / a + m;  
}
```

```
{  
    f[0] = 1;  
    for (int i = 1; i < N; i++) {  
        f[i] = i * f[i - 1] % mod;  
    }  
  
    r[N - 1] = inv(f[N - 1])  
    for (int i = N - 1; i >= 1; i--) {  
        r[i - 1] = r[i] * i % mod;  
    }  
}
```

2.23 Гаусс

```
int gauss(vector<vector<double>>> a,  
          vector<double> &ans) {  
    int n = (int) a.size();  
    int m = (int) a[0].size() - 1;  
    vector<int> where(m, -1);  
    for (int col = 0, row = 0;  
         col < m && row < n; ++col) {  
        int sel = row;  
        for (int i = row; i < n; ++i)  
            if (abs(a[i][col]) > abs(a[sel][col]))  
                sel = i;  
        if (abs(a[sel][col]) < EPS)  
            continue;  
        for (int i = col; i <= m; ++i)  
            swap(a[sel][i], a[row][i]);  
        where[col] = row;  
        for (int i = 0; i < n; ++i)  
            if (i != row) {  
                double c =  
                    a[i][col] / a[row][col];  
                ++row;  
                a[i][col] / a[row][col];  
                for (int j = col; j <= m; ++j)  
                    a[i][j] -= a[row][j] * c;  
            }  
        ans.assign(m, 0);  
        for (int i = 0; i < m; ++i)  
            if (where[i] != -1)  
                ans[i] =  
                    a[where[i]][m] / a[where[i]][i];  
        for (int i = 0; i < n; ++i) {  
            double sum = 0;  
            for (int j = 0; j < m; ++j)  
                sum += ans[j] * a[i][j];  
            if (abs(sum - a[i][m]) > EPS)  
                return 0;  
        }  
        for (int i = 0; i < m; ++i)  
            if (where[i] == -1) return INF;  
        return 1;  
    }  
}
```

Бинарный

```
int gauss(vector<bitset<N>> a, int n, int m,  
          bitset<N> &ans) {  
    vector<int> where(m, -1);  
    for (int col = 0, row = 0; col < m && row < n; ++col) {  
        for (int i = row; i < n; ++i)  
            if (a[i][col]) {  
                swap(a[i], a[row]);  
                break;  
            }  
        if (!a[row][col]) {  
            continue;  
        }  
        where[col] = row;  
        for (int i = 0; i < n; ++i) {  
            if (i != row && a[i][col]) a[i] ^= a[row];  
        }  
        ++row;  
    }  
}
```

2.24 Быстрая факторизация (FedShat)

```
ll binpow(ll a, ll n, ll mod) {  
    if (n == 0) {  
        return 1;  
    }  
    if (n % 2 == 0) {  
        int128_t b = binpow(a, n / 2, mod);  
        return (b * b) % mod;  
    }  
    return (((int128_t) a) * binpow(a, n - 1, mod)) % mod;
```

```
}

constexpr int N = 1e7;
vector<int> pr, lp;

bool prime(ll n) {
    if (n <= N) {
        return binary_search(all(pr), n);
    }
    int iter = 60;
    int s = 0;
    ll d = n - 1;
    while (d % 2 == 0) {
        d /= 2;
        ++s;
    }
    auto test = [&](ll a) {
        if (binpow(a, d, n) == 1) {
            return true;
        }
        ll _2r = 1;
        for (int r = 0; r < s; ++r) {
            auto tmp = binpow(binpow(a, d, n), _2r, n);
            if (tmp == n - 1) {
                return true;
            }
            _2r *= 2;
        }
        return false;
    };
    for (int _ = 0; _ < iter; ++_) {
        ll a = uniform_int_distribution<ll>(1, n - 1)(rnd);
        if (!test(a)) {
            return false;
        }
    }
    return true;
}

ll f(ll x, ll n) {
    return ((int128_t) x * (int128_t) x + (int128_t) 2) % n;
}

ll pollard(ll n) {
    ll a = uniform_int_distribution<ll>(0, n - 1)(rnd);
    ll x = a, y = a, d = 1;
    constexpr int iter = 5e4;
    for (int _ = 0; _ < iter; ++_) {
        x = f(x, n);
        y = f(y, n);
        d = gcd(abs(x - y), n);
        if (d != 1 && d != n) {
            break;
        }
    }
    if (d == 1 || d == n) {
        pollard(n);
    }
    return d;
}

vector<ll> res;

void factor(ll n) {
    if (n <= N) {
        while (true) {
            if (lp[n] == 0) {
                break;
            }
            res.push_back(lp[n]);
            n /= lp[n];
        }
        return;
    }
    if (prime(n)) {
        res.push_back(n);
        return;
    }
    ll d = pollard(n);
    factor(n / d);
    factor(d);
}

void solve() {
    ll n;
    cin >> n;
    lp.resize(N + 1);
    for (int i = 2; i <= N; ++i) {
        if (lp[i] == 0) {
            lp[i] = i;
            pr.push_back(i);
        }
        for (int j = 0; j < (int) pr.size() && pr[j] <= lp[i] && i * pr[j]
<= N; ++j) {
            lp[i * pr[j]] = pr[j];
        }
    }
}
```

```
    }
    factor(n);
}
```

2.25 Префикс-функция

```
vector<int> prefix_function (string &s) {
    int n = (int)s.length();
    vector<int> pi(n);
    for (int i = 1; i < n; ++i) {
        int j = pi[i - 1];
        while (j > 0 && s[i] != s[j])
            j = pi[j - 1];
        if (s[i] == s[j]) {
            ++j;
        }
        pi[i] = j;
    }
    return pi;
}
```

2.26 Z-функция

```
vector<int> z_function(string &s) {
    int n = (int)s.length();
    vector<int> z(n);
    for (int i = 1, l = 0, r = 0; i < n; ++i) {
        if (i <= r) {
            z[i] = min(r - i + 1, z[i - l]);
        }
        while (i + z[i] < n && s[z[i]] == s[i + z[i]]) {
            ++z[i];
        }
        if (i + z[i] - 1 > r) {
            l = i;
            r = i + z[i] - 1;
        }
    }
    return z;
}
```

2.27 Суфмас (TheEvilBird)

```
int mod(int x, int m) {
    if (x < 0) x += m;
    if (x >= m) x -= m;
    return x;
}

vector<int> suffix_array(string s) {
    s += '$';
    int n = sz(s);
    vector<int> arr(n), narr(n), head(n), c(n), nc(n);
    for (int i = 0; i < n; ++i) {
        arr[i] = i;
    }
    sort(all(arr), [&](int x, int y) {
        return s[x] < s[y];
    });
    int cl = 0;
    c[arr[0]] = cl;
    head[0] = 0;
    for (int i = 1; i < n; ++i) {
        if (s[arr[i]] != s[arr[i - 1]]) {
            head[++cl] = i;
        }
        c[arr[i]] = cl;
    }
    for (int k = 1; k < n && cl < n; k *= 2) {
        for (int i = 0; i < n; i++) {
            int j = mod(arr[i] - k, n);
            narr[head[c[j]]++] = j;
        }
        cl = 0;
        head[0] = 0;
        pii prev = {c[narr[0]], c[mod(narr[0] + k, n)]};
        for (int i = 1; i < n; i++) {
            pii cur = {c[narr[i]], c[mod(narr[i] + k, n)]};
            if (cur != prev) {
                head[++cl] = i;
            }
            nc[narr[i]] = cl;
            prev = cur;
        }
        swap(arr, narr);
        swap(c, nc);
    }
}
```

```

    }
    // returns suffix array without $
    return vector<int> (arr.begin() + 1, arr.end());
}

vector<int> build_lcp(string &s, vector<int> &suf) {
    int n = sz(s);
    vector<int> lcp(n - 1, order(n));
    for (int i = 0; i < n; ++i) {
        order[suf[i]] = i;
    }
    int l = 0;
    for (int i = 0; i < n; ++i) {
        int id = order[i];
        if (id + 1 == n) {
            l = 0;
            continue;
        }
        int j = suf[id + 1];
        if (l) --l;
        while (max(i + l, j + l) < n &&
            s[i + l] == s[j + l]) {
            ++l;
        }
        lcp[id] = l;
    }
    return lcp;
}

```

2.28 Суфавтомат (TheEvilBird)

```

struct Node {
    int go[26];
    int suf, prev, term, len;

    Node() {
        for (auto &i: go) {
            i = -1;
        }
        len = 0;
        suf = -1;
        prev = -1;
        term = 0;
    }
};

vector<Node> automat;

int add(int a, int ch) {
    int b = sz(automat);
    automat.emplace_back();
    automat[b].prev = a;
    automat[b].suf = 0;
    automat[b].len = automat[a].len + 1;
    for (; a != -1; a = automat[a].suf) {
        if (automat[a].go[ch] == -1) {
            automat[a].go[ch] = b;
            continue;
        }
        int c = automat[a].go[ch];
        if (automat[c].prev == a) {
            automat[b].suf = c;
            break;
        }
    }
    int d = sz(automat);
    automat.emplace_back();
    automat[d].suf = automat[c].suf;
    automat[d].len = automat[a].len + 1;
    automat[c].suf = d;
    automat[b].suf = d;
    automat[d].prev = a;
    for (int i = 0; i < 26; ++i) {
        automat[d].go[i] = automat[c].go[i];
    }
    for (; a != -1 && automat[a].go[ch] == c; a = automat[a].suf) {
        automat[a].go[ch] = d;
    }
    break;
}
// returns id of the added vertex
return b;
}

```

2.29 Ахо-Корасик (Sweezyk)

```

struct Node {
    int par;
    int par_c;
    int go[26];
}

```

```

    int term;
    int link;
    int super;
    int cnt;
};

const int N = 1e6 + 5;
int ptr = 1;
Node trie[N];

void add(string s) {
    int cur = 1;
    for (auto &q : s) {
        int c = q - 'a';
        if (trie[cur].go[c]) {
            cur = trie[cur].go[c];
        } else {
            ++ptr;
            trie[cur].go[c] = ptr;
            trie[ptr].par = cur;
            trie[ptr].par_c = c;
            cur = ptr;
        }
    }
    trie[cur].cnt++;
}

void build() {
    queue<int> q;
    q.push(1);
    while (!q.empty()) {
        int v = q.front();
        q.pop();
        if (v != 1) {
            if (trie[v].par == 1) {
                trie[v].link = trie[v].super = 1;
            } else {
                trie[v].link = trie[trie[v].par].link.go[trie[v].par_c];
                trie[v].super = (trie[trie[v].link].cnt ? trie[v].link : trie[trie[v].link].super);
            }
        }
        trie[v].cnt += trie[trie[v].link].cnt;
        for (int c = 0; c < 26; c++) {
            if (trie[v].go[c]) {
                q.push(trie[v].go[c]);
            } else {
                if (v == 1) {
                    trie[v].go[c] = 1;
                } else {
                    trie[v].go[c] = trie[trie[v].link].go[c];
                }
            }
        }
    }
}

trie[1].link = trie[1].super = trie[1].par = 1;
build();

```

2.30 Манакер

```

vector<int> d1(n);
int l = 0, r = -1;
for (int i = 0; i < n; ++i) {
    int k = (i > r ? 1 : min (d1[l + r - i], r - i + 1));
    while (i + k < n && i - k >= 0 && s[i + k] == s[i - k]) {
        ++k;
    }
    d1[i] = k;
    if (i + k - 1 > r) {
        l = i - k + 1; r = i + k - 1;
    }
}

vector<int> d2(n);
l = 0; r = -1;
for (int i = 0; i < n; ++i) {
    int k = (i > r ? 0 : min (d2[l + r - i + 1], r - i + 1));
    while (i + k < n && i - k - 1 >= 0 && s[i + k] == s[i - k - 1]) {
        ++k;
    }
    d2[i] = k;
    if (i + k - 1 > r) {
        l = i - k; r = i + k - 1;
    }
}
}

```

2.31 CHT (FedShat)

```

struct Line {
    ll k = 0, b = -INFL;
    Line() = default;
    Line(ll k, ll b) : k(k), b(b){};

    ld operator()(ld x) {
        return k * x + b;
    }
};

bool operator<(Line a, Line b) {
    return a.k < b.k || (a.k == b.k && a.b > b.b);
}

bool operator<(pair<Line, ld> a, pair<Line, ld> b) {
    return a.second < b.second;
}

struct CHT {
    vector<pair<Line, ld>> convex;

    void add(Line a) {
        while (!convex.empty() && a(convex.back().second) > convex.back().
            first(convex.back().second)) {
            convex.pop_back();
        }
        ld xn = -INFL;
        if (!convex.empty()) {
            xn = (a.b - convex.back().first.b + 0.0) / (convex.back().first
                .k - a.k);
        }
        convex.push_back({a, xn});
    }

    CHT(vector<Line> lines) {
        sort(all(lines));
        for (int i = 0; i < (int) lines.size(); i) {
            int j = i;
            while (j < (int) lines.size() && lines[i].k == lines[j].k) {
                ++j;
            }
            add(lines[i]);
            i = j;
        }
    }

    ld get(ld x) {
        auto it = upper_bound(all(convex), pair<Line(), x) - convex.begin
            ();
        return convex[it - 1].first(x);
    }
};

```

```

string res = "";
for (size_t i = 0; i < N; i++) {
    res += static_cast<char>('0' + v[i]);
}
return res;
}

template <typename A>
string to_string(A v) {
    bool first = true;
    string res = "{";
    for (const auto &x : v) {
        if (!first) {
            res += ", ";
        }
        first = false;
        res += to_string(x);
    }
    res += "}";
    return res;
}

template <typename A, typename B>
string to_string(pair<A, B> p) {
    return "(" + to_string(p.first) + ", " + to_string(p.second) + ")";
}

template <typename A, typename B, typename C>
string to_string(tuple<A, B, C> p) {
    return "(" + to_string(get<0>(p)) + ", " + to_string(get<1>(p)) + ", " +
        to_string(get<2>(p)) + ")";
}

template <typename A, typename B, typename C, typename D>
string to_string(tuple<A, B, C, D> p) {
    return "(" + to_string(get<0>(p)) + ", " + to_string(get<1>(p)) + ", " +
        to_string(get<2>(p)) + ", " + to_string(get<3>(p)) + ")";
}

void debug_out() { cerr << endl; }

template <typename Head, typename... Tail>
void debug_out(Head H, Tail... T) {
    cerr << " " << to_string(H);
    debug_out(T...);
}

#ifdef LOCAL
#define debug(...) cerr << "[" << __VA_ARGS__ << "]:", debug_out(
    __VA_ARGS__)
#else
#define debug(...) 42
#endif

```

2.32 Дебаг Туриста

```

template <typename A, typename B>
string to_string(pair<A, B> p);

template <typename A, typename B, typename C>
string to_string(tuple<A, B, C> p);

template <typename A, typename B, typename C, typename D>
string to_string(tuple<A, B, C, D> p);

string to_string(const string& s) {
    return '"' + s + '"';
}

string to_string(const char* s) {
    return to_string((string) s);
}

string to_string(bool b) {
    return (b ? "true" : "false");
}

string to_string(vector<bool> v) {
    bool first = true;
    string res = "{";
    for (int i = 0; i < static_cast<int>(v.size()); i++) {
        if (!first) {
            res += ", ";
        }
        first = false;
        res += to_string(v[i]);
    }
    res += "}";
    return res;
}

template <size_t N>
string to_string(bitset<N> v) {

```

2.33 Геометрия (TheEvilBird)

```

const long double PI = 3.1415926535897932384626433832795;

/*
 * Rotate relative to the origin, a - rotation angle:
 * new_x = x cos(a) - y sin(a)
 * new_y = x sin(a) + y cos(a)
 *
 * new_x = x cos(a) + y sin(a)
 * new_y = x sin(a) - y cos(a)
 *
 *
 * rad = degree * PI / 180
 * degree = rad * 180 / PI
 */

struct Point {
    ll x = 0, y = 0;
    // int id = -1;

    Point() : x(0), y(0) {}
    Point(ll _x, ll _y) : x(_x), y(_y) {}

    bool operator==(const Point other) const {
        return x == other.x && y == other.y;
    }

    void operator*=(ll k) {
        x *= k;
        y *= k;
    }
};

istream &operator>>(istream &is, Point &point) {
    is >> point.x >> point.y;
    return is;
}

```

```
ostream &operator<<(ostream &os, const Point &point) {
    os << point.x << ' ' << point.y;
    return os;
}

struct Vec {
    ll x, y;

    Vec() : x(0), y(0) {}
    Vec(ll _x, ll _y) : x(_x), y(_y) {}
    Vec(Point a) : x(a.x), y(a.y) {}
    Vec(Point a, Point b) : x(b.x - a.x), y(b.y - a.y) {}

    ld len() const {
        return sqrtl(x * x + y * y);
    }

    ll len_sq() const {
        return (x * x + y * y);
    }

    Vec operator *(ll k) const {
        return {x * k, y * k};
    }

    void operator *=(ll k) {
        x *= k;
        y *= k;
    }

    Vec operator +(const Vec other) const {
        return {x + other.x, y + other.y};
    }

    Vec operator -(const Vec other) const {
        return {x - other.x, y - other.y};
    }

    bool operator ==(const Vec other) const {
        return x == other.x && y == other.y;
    }

    bool operator !=(const Vec other) const {
        return !(*this == other);
    }

    ll operator *(const Vec other) const { // dot product
        return x * other.x + y * other.y;
    }

    ll operator %(const Vec other) const { // cross product
        return x * other.y - y * other.x;
    }
};

istream &operator>>(istream &is, Vec &vec) {
    is >> vec.x >> vec.y;
    return is;
}

ostream &operator<<(ostream &os, const Vec &vec) {
    os << vec.x << ' ' << vec.y;
    return os;
}

typedef vector<Point> Polygon;
typedef vector<Vec> vPolygon;

bool cmp_vectors(Vec a, Vec b) {
    if ((a.y < 0 || (a.y == 0 && a.x < 0)) &&
        (b.y > 0 || (b.y == 0 && b.x > 0))) {
        return true;
    }
    if ((b.y < 0 || (b.y == 0 && b.x < 0)) &&
        (a.y > 0 || (a.y == 0 && a.x > 0))) {
        return false;
    }
    return (a % b > 0 || (a % b == 0 && a.len_sq() < b.len_sq()));
}

int get_sign(ld kek) {
    if (kek > 0) return 1;
    if (kek < 0) return -1;
    return 0;
}

Polygon build_convex_hull(Polygon &a) {
    int n = sz(a);
    for (int i = 1; i < n; ++i) {
        if ((a[i].y < a[0].y) || (a[i].y == a[0].y && a[i].x < a[0].x))
            swap(a[0], a[i]);
    }
    sort(a.begin() + 1, a.end(), [&](Point A, Point B) {
        Vec oa(a[0], A), ob(a[0], B);
        if ((oa % ob) == 0) return oa.len_sq() < ob.len_sq();
        return (oa % ob) > 0;
    });

```

```
});
Polygon hull = {a[0]};
for (int i = 1; i < n; ++i) {
    while (sz(hull) >= 2) {
        Vec ab(hull[sz(hull) - 2], hull[sz(hull) - 1]), bp(hull[sz(hull) - 1], a[i]);
        if ((ab % bp) <= 0) {
            hull.pop_back();
        }
        else {
            break;
        }
    }
    hull.emplace_back(a[i]);
}
return hull;
}

ll area_of_polygon(Polygon &poly) {
    ll res = 0;
    int n = sz(poly);
    for (int i = 2; i < n; ++i) {
        Vec ab(poly[0], poly[i - 1]), ac(poly[0], poly[i]);
        res += (ab % ac);
    }
    // don't forget to divide the result by 2!
    return res;
}

ld perimeter_of_polygon(Polygon &poly) {
    ld res = 0;
    int n = sz(poly);
    for (int i = 0; i < n; ++i) {
        Vec v(poly[i], poly[(i + 1 == n ? 0 : i + 1)]);
        res += v.len();
    }
    return res;
}

ll diameter_of_polygon(Polygon &poly) {
    int n = sz(poly), x = 1;
    ll ans = 0;
    for (int i = 0; i < n; ++i) {
        int j = (i + 1) % n;
        while (true) {
            Vec ac(poly[i], poly[x]), ab(poly[i], poly[j]), cd(poly[x], poly[(x + 1) % n]);
            ans = max(ans, ac.len_sq());
            if ((ab % cd) <= 0) {
                break;
            }
            x++;
            x %= n;
        }
    }
    // don't forget to extract root!
    return ans;
}

ld angle(const Vec &a, const Vec &b) {
    return fabsl(atan2(a % b, a * b) / PI * 180);
}

ld angle_rad(const Vec &a, const Vec &b) {
    return (atan2(a % b, a * b));
}

ld angle_rad(const Point &a) {
    return atan2(a.y, a.x);
}

ld from_point_to_line(const Point &p, const Point &a, const Point &b) {
    Vec ba(b, a), ap(a, p);
    return fabsl((ba % ap) / ba.len());
}

ld from_point_to_ray(const Point &p, const Point &a, const Point &b) {
    Vec ba(b, a), ap(a, p), ab(a, b);
    if ((ab * ap) < 0) {
        return ap.len();
    }
    else {
        return fabsl((ba % ap) / ba.len());
    }
}

ld from_point_to_segment(const Point &p, const Point &a, const Point &b) {
    Vec ab(a, b), ap(a, p), bp(b, p), ba(b, a);
    if ((ab * ap) < 0) {
        return fabsl(ap.len());
    }
    else if ((ab * bp) > 0) {
        return fabsl(bp.len());
    }
    else {
        return fabsl((ba % ap) / ba.len());
    }
}

```

```

    }
}

bool point_on_line(const Point &p, const Point &a, const Point &b) {
    Vec ab(a, b), ap(b, p);
    return (ab % ap) == 0;
}

bool point_on_ray(const Point &p, const Point &a, const Point &b) {
    Vec ab(a, b), ap(a, p);
    return ((ab % ap) == 0 && (ab * ap) > 0 || (a == p));
}

bool point_on_segment(const Point &p, const Point &a, const Point &b) {
    Vec ap(a, p), bp(b, p), ab(a, b);
    return ((ap * bp) <= 0 && (ap % ab) == 0);
}

bool point_in_angle(const Point &p, const Point &a, const Point &o, const
    Point &b) {
    Vec oa(o, a), ob(o, b), op(o, p);
    if ((oa % ob) < 0) swap(oa, ob);
    return ((oa % op) >= 0 && (ob % op) <= 0);
}

bool segment_intersection(const Point &a, const Point &b, const Point &c,
    const Point &d) {
    Vec ab(a, b), cd(c, d), ac(a, c), ad(a, d), cb(c, b), ca(c, a);
    if (get_sign((ab % ac)) * get_sign((ab % ad)) <= 0 && get_sign((cd % ca))
        * get_sign((cd % cb)) <= 0) {
        ll x1 = max(min(a.x, b.x), min(c.x, d.x)), x2 = min(max(a.x, b.x),
            max(c.x, d.x));
        ll y1 = max(min(a.y, b.y), min(c.y, d.y)), y2 = min(max(a.y, b.y),
            max(c.y, d.y));
        return (x1 <= x2 && y1 <= y2);
    }
    return false;
}

bool rays_intersection(const Point &a, const Point &b, const Point &c,
    const Point &d) {
    Vec ab(a, b), cd(c, d);
    ll k = 1e6;
    ab *= k;
    cd *= k;
    Point nb(ab.x + a.x, ab.y + a.y), nd(cd.x + c.x, cd.y + c.y);
    return segment_intersection(a, nb, c, nd);
}

bool lines_intersection(const Point &a, const Point &b, const Point &c,
    const Point &d) {
    Vec ab(a, b), cd(c, d);
    return ((ab % cd) != 0);
}

int point_in_polygon(const Point &p, const Polygon &poly) {
    // 0 - outside, 1 - inside, 2 - border;
    int n = sz(poly);
    if (point_in_angle(p, poly[n - 1], poly[0], poly[1])) {
        int l = 1, r = n - 1;
        while (r - l > 1) {
            int md = (l + r) / 2;
            if (point_in_angle(p, poly[md], poly[0], poly[l])) {
                r = md;
            }
            else {
                l = md;
            }
        }
        if (point_in_angle(p, poly[r], poly[0], poly[l]) &&
            point_in_angle(p, poly[0], poly[l], poly[r]) &&
            point_in_angle(p, poly[l], poly[r], poly[0])) {
            if (point_on_segment(p, poly[l], poly[r]) ||
                point_on_segment(p, poly[(l ? 1 - 1 : n - 1)], poly[l]) ||
                point_on_segment(p, poly[r], poly[(r + 1 == n ? 0 : r + 1)
            ])) {
                return 2;
            }
            else {
                return 1;
            }
        }
        else {
            return 0;
        }
    }
    else {
        return 0;
    }
}

Polygon minkowski_sum(Polygon &a, Polygon &b) {
    // a[0], b[0]: y - max, y1 = y2 => x - max
    int n = sz(a), m = sz(b);
    assert(n >= 3 && m >= 3);
    Point high_a = a[0], high_b = b[0];

```

```

    vPolygon va(n), vb(m);
    for (int i = 0; i < n; ++i) {
        va[i] = Vec(a[i], a[(i + 1) % n]);
    }
    for (int i = 0; i < m; ++i) {
        vb[i] = Vec(b[i], b[(i + 1) % m]);
    }
    sort(all(va), cmp_vectors);
    sort(all(vb), cmp_vectors);
    vPolygon vc;
    merge(all(va), all(vb), back_inserter(vc), cmp_vectors);
    Point high_c(high_a.x + high_b.x, high_a.y + high_b.y);
    Polygon c(sz(vc) + 1);
    c[0] = high_c;
    for (int i = 0; i < sz(c) - 1; ++i) {
        c[i + 1] = Point(c[i].x + vc[i].x, c[i].y + vc[i].y);
    }
    return c;
}

ld from_polygon_to_polygon(Polygon a, Polygon b) {
    for (auto &i: b) {
        i *= -1;
    }
    int pos = 0;
    for (int i = 1; i < sz(b); ++i) {
        if ((b[i].y > b[pos].y) ||
            (b[i].y == b[pos].y && b[i].x > b[pos].x)) {
            pos = i;
        }
    }
    rotate(b.begin(), b.begin() + pos, b.end());
    Polygon c = minkowski_sum(a, b);
    int n = sz(c);
    Point p(0, 0);
    ld ans = 1e20;
    for (int i = 0; i < n - 1; ++i) {
        ans = min(ans, from_point_to_segment(p, c[i], c[i + 1]));
    }
    return ans;
}

ll diameter_of_polygon_minkowski(Polygon &a) {
    Polygon ra = a;
    for (auto &i: ra) {
        i *= -1;
    }
    int pos = 0;
    for (int i = 1; i < sz(a); ++i) {
        if ((a[i].y > a[pos].y) ||
            (a[i].y == a[pos].y && a[i].x > a[pos].x)) {
            pos = i;
        }
    }
    rotate(a.begin(), a.begin() + pos, a.end());
    pos = 0;
    for (int i = 1; i < sz(a); ++i) {
        if ((ra[i].y > ra[pos].y) ||
            (ra[i].y == ra[pos].y && ra[i].x > ra[pos].x)) {
            pos = i;
        }
    }
    rotate(ra.begin(), ra.begin() + pos, ra.end());
    Polygon c = minkowski_sum(a, ra);
    int n = sz(c);
    ll ans = 0;
    for (int i = 0; i < n; ++i) {
        ans = max(ans, Vec(c[i]).len_sq());
    }
    // don't forget to extract root!
    return ans;
}

```