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- Число граней в планарном графе
(с учётом бесконечной): R=2-V+E
- \bullet Сумма арифметической прогрессии: $S_n = \frac{n(a_1 + a_n)}{2}$
- Сумма геометрической прогрессии: $S_n = \frac{b_1(q^n-1)}{q-1}$

2 Коды

2.1 Basic setup

```
#include <bits/stdc++.h>
using namespace std;
#define sz(x) (int) ((x).size())
\#define all(x) (x).begin(), (x).end()
#define rall(x) (x).rbegin(), (x).rend()
typedef long long 11;
typedef __int128 int128;
typedef pair<int, int> pii;
typedef pair<11, 11> pll;
const char en = '\n';
const int INF = 1e9 + 7;
const 11 INFLL = 1e18;
mt19937 rnd(chrono::high_resolution_clock::now().time_since_epoch().count()
template<class T>
istream &operator>>(istream &is, vector<T> &a) {
    for (auto &i : a) {
        is >> i;
    return is:
void solve() {
int32_t main() {
#ifdef LOCAL
    freopen("input.txt", "r", stdin);
    ios_base::sync_with_stdio(0);
    cin.tie(0);
#endif
    solve():
    return 0:
```

1 Общее

• Собственное вращение на угол φ с центром вращения в начале координат:

```
x' = x \cos \varphi - y \sin \varphiy' = x \sin \varphi + y \cos \varphi
```

- Расстояние между точками по сфере: $L = R \cdot \arccos(\cos\theta_1 \cdot \cos\theta_2 + \sin\theta_1 \cdot \sin\theta_2 \cdot \cos(\varphi_1 \varphi_2))$ где θ широты (от $-\pi$ до π), φ долготы (от $-\pi$ до π)
- Объем шарового сегмента: $V = \pi h^2 (R \frac{1}{3}h)$, где h высота от вершины сектора до секущей плоскости
- Площадь поверхности шарового сегмента: $S=2\pi Rh,$ где h высота
- Код Грея: $g_n = n \oplus \frac{n}{2}$
- Числа Фибоначчи: $F_0=0, F_1=1, F_n=rac{(rac{1+\sqrt{5}}{2})^n-(rac{1-\sqrt{5}}{2})^n}{\sqrt{5}}$
- Sum-xor property: $a+b=a\oplus b+2(a\&b), a+b=a|b+a\&b, a\oplus b=a|b-a\&b$

2.2 Бесполезное

Санитайзеры:

Прагмы:

```
#pragma GCC optimize("Ofast,no-stack-protector")
#pragma GCC target("sse,sse2,sse3,ssse3,sse4)
#pragma GCC target("popcnt,abm,mmx,avx,avx2,tune=native")
#pragma GCC optimize("unroll-loops")
#pragma GCC optimize("fast-math")
#pragma GCC optimize("section-anchors")
#pragma GCC optimize("profile-values")
#pragma GCC optimize("profile-reorder-functions")
#pragma GCC optimize("tracer")
#pragma GCC optimize("vpt")
#pragma GCC optimize("rename-registers")
#pragma GCC optimize("move-loop-invariants")
#pragma GCC optimize("unswitch-loops")
#pragma GCC optimize("function-sections")
#pragma GCC optimize("data-sections")
#pragma GCC optimize("branch-target-load-optimize")
#pragma GCC optimize("branch-target-load-optimize2")
#pragma GCC optimize("btr-bb-exclusive")
```

Встроенный декартач:

Atomic hashset, hashmap:

Перебор всех подмасок и надмасок:

```
for (int submask = mask;; submask = (submask - 1) & mask) {
    // use submask
    if (submask == 0) break;
}

for (int upmask = mask;; upmask = (upmask + 1) | mask) {
    // use upmask
    if (upmask == maxmask) break;
}
```

2.3 Мосты

2.4 Точки сочленения

```
void dfs(int v, int p = -1) {
    used[v] = true;
    tin[v] = fup[v] = timer++;
   int children = 0;
for (auto to : g[v]) {
        if (to == p) {
            continue;
        if (used[to]) {
            fup[v] = min(fup[v], tin[to]);
        } else {
            dfs(to, v);
fup[v] = min(fup[v], fup[to]);
             if (fup[to] >= tin[v] && p != -1) {
                 IS_CUTPOINT(v);
            }
             ++children;
    if (p == -1 && children > 1) {
        IS_CUTPOINT(v);
    }
```

2.5 DCP (TheEvilBird)

```
struct Query {
    char type;
    int v, u;
    Query(char type) : type(type) {}
Query(char type, int v, int u) : type(type), v(v), u(u) {}
struct DCP {
    int n, k, ans; // n - vertex, k - queries
    vector<int> par, rk;
    vector<pair<pii, int>> hist;
    // 0 - par, 1 - rk, 2 - ans;
    int qL, qR;
    pii edge:
    vector<vector<pii>>> tree;
    vector<Query> qs;
    DCP(int _n, int _k) {
         n = ans = _n;
         par.resize(n);
         rk.resize(n, 1);
         for (int i = 0; i < n; ++i) par[i] = i;
         tree.assign(4 * k, vector<pii>());
    int dsu_get(int v) {
         while (par[v] != v) v = par[v];
         return v;
    void dsu_unite(int a, int b) {
         a = dsu_get(a);
         b = dsu_get(b);
         if (a = b) return;
if (rk[a] > rk[b]) swap(a, b);
hist.emplace_back((pii){0, a}, par[a]);
         hist.emplace_back((pii){2, -1}, ans);
par[a] = b;
         --ans;
         if (rk[a] == rk[b]) {
             hist.emplace_back((pii){1, b}, rk[b]);
             ++rk[b];
         }
    }
    void dsu_unite(pii e) {
         dsu_unite(e.first, e.second);
    void cancel(pair<pii, int> &el) {
         int &type = el.first.first;
         int &id = el.first.second;
         int &val = el.second;
if (type == 0) {
             par[id] = val;
         } else_if_(type == 1) {
             rk[id] = val;
         } else if (type == 2) {
             ans = val;
    }
    void add_edge(int _qL, int _qR, pii e) {// [L, R]
         qL = _qL;

qR = _qR + 1;
         edge = e;
         add_edge_tree(1, 0, k);
    void add_edge_tree(int v, int 1, int r) {
         if (qL \le 1 \&\& r \le qR) {
             tree[v].emplace_back(edge);
             return;
         int m = (1 + r) / 2, vL = 2 * v, vR = vL + 1; if (qL < m) add_edge_tree(vL, 1, m);
         if (m < qR) add_edge_tree(vR, m, r);</pre>
    }
    void go(vector<Query> &_qs) {
         qs = _qs;
         go_tree(1, 0, k);
    void go_tree(int v, int 1, int r) {
         int siz = sz(hist);
         for (auto &e : tree[v]) {
             dsu_unite(e);
```

```
if (1 + 1 == r) {
            if (qs[1].type == '?') {
                 cout << ans << en;</pre>
        } else {
            int m = (1 + r) / 2, vL = 2 * v, vR = vL + 1;
             go_tree(vL, 1, m);
            go_tree(vR, m, r);
        while (sz(hist) > siz) {
             cancel(hist.back());
            hist.pop_back();
void solve() {
   int n, k;
    cin >> n >> k;
    DCP dcp(n, k);
    set<pair<pii, int>> edges;
    vector<Query> qs;
for (int i = 0; i < k; ++i) {</pre>
        char tp;
        cin >> tp;
if (tp == '?') {
            qs.emplace_back(tp);
        } else {
            int v, u;
            cin >> v >> u:
             --v;
            --u;
             if (v > u) swap(v, u);
             qs.emplace_back(tp, v, u);
            if (tp == '+') {
                edges.emplace((pii){v, u}, i);
            } else {
                auto it = edges.lower_bound({(pii){v, u}, 0});
                 dcp.add_edge(it->second, i, it->first);
                 edges.erase(it);
            }
        }
    for (auto &e : edges) {
        dcp.add_edge(e.second, k - 1, e.first);
    if (k) dcp.go(qs);
```

2.6 MaxFlow (TheEvilBird)

```
struct MaxFlow {
    struct Edge {
         11 flow, cap;
         int to, id;
         Edge(ll flow, ll cap, int to, int id) : flow(flow), cap(cap), to(to
      ), id(id) {}
    vector<vector<Edge>> g;
    vector<int> d, head, used;
    11 max_cap;
    int s, t;
    MaxFlow() {}
    MaxFlow(int _n) {
         n = _n;
         g.resize(n);
    void add_edge(int from, int to, 11 cap) {
         g[from].emplace_back(0, cap, to, sz(g[to]));
         g[to].emplace_back(0, 0, from, sz(g[from]) - 1);
    bool bfs() {
         d.assign(n, INF);
         d[s] = 0;
         queue<int> q;
         a.push(s):
         while (!q.empty()) {
   int v = q.front();
             q.pop();
             for (auto e : g[v]) {
   if (d[e.to] == INF && e.cap - e.flow >= max_cap) {
      d[e.to] = d[v] + 1;
                      q.push(e.to);
```

```
}
         return d[t] != INF;
    }
    11 dfs(int v, 11 cur_flow) {
        if (v == t) {
             return cur_flow;
         for (; head[v] < sz(g[v]); ++head[v]) {
             auto &e = g[v][head[v]];
             if (e.cap - e.flow >= \max_{cap} && d[v] + 1 == d[e.to]) {
                 11 new_flow = dfs(e.to, min(cur_flow, e.cap - e.flow));
                 if (new_flow) {
                     e.flow += new_flow;
g[e.to][e.id].flow -= new_flow;
                     return new_flow;
             }
        }
         return 0;
    }
    11 find_max_flow(int _s, int _t) {
        s = _s;
t = _t;
         11 res = 0;
        for (int k = 30; k >= 0; --k) {
    max_cap = (1 << k);
             while (bfs()) {
                 head.assign(n, 0);
                 11 flow = 0;
                     flow = dfs(s, INFLL);
                     res += flow;
                 } while (flow);
         return res;
    }
    11 dfs_const_flow(int v, 11 cur_flow) {
         used[v] = 1;
         if (v == t) {
             return cur_flow;
         for (auto &e : g[v]) {
             if (!used[e.to] && e.cap - e.flow > 0) {
                 11 new_flow = dfs_const_flow(e.to, min(cur_flow, e.cap - e.
      flow));
                 if (new_flow) {
                      e.flow += new_flow;
                      g[e.to][e.id].flow -= new_flow;
                      return new_flow;
             }
         return 0;
    7
    bool find_const_flow(int _s, int _t, ll F) {
        s = _s;
t = _t;
        11 \text{ res} = 0, \text{ flow} = 0;
         \max_{cap} = F;
         do {
             used.assign(n, 0);
             flow = dfs_const_flow(s, INF);
             res += flow;
         } while (flow && res < F);</pre>
         return res == F;
    11 get_edge_flow(int v, int id) {
         return g[v][id].flow;
};
```

2.7 MinCostMaxFlow (TheEvilBird)

```
struct MinCostMaxFlow {
    struct Edge {
        ll flow, cap, price;
        int to, id;

        Edge() {}

        Edge(1) flow, 11 cap, 11 price, int to, int id) : flow(flow), cap(
        cap), price(price), to(to), id(id) {}
};
```

```
int n;
     int s, t;
     11 ans;
     vector<vector<Edge>> g;
     vector<int> d:
     vector<11> add_f;
     vector<pii> par;
     MinCostMaxFlow() {}
     MinCostMaxFlow(int _n) {
          n = _n;
          g.resize(n);
     void add_edge(int from, int to, ll cap, ll price) {
   g[from].emplace_back(0, cap, price, to, sz(g[to]));
   g[to].emplace_back(0, 0, -price, from, sz(g[from]) - 1);
     11 get_edge_flow(int v, int id) {
          return g[v][id].flow;
     void FB() {
          d.assign(n, INF);
          add_f.assign(n, 0);
          par.assign(n, {-1, -1});
          d[s] = 0;
add_f[0] = INF;
          queue<int> q;
          q.push(s);
          vector<int> used(n, 0);
          used[s] = 1;
          while (!q.empty()) {
   int v = q.front();
               q.pop();
used[v] = 0;
               for (int i = 0; i < sz(g[v]); ++i) {
    auto &e = g[v][i];
                    if (e.flow < e.cap && d[e.to] > d[v] + e.price) {
    d[e.to] = d[v] + e.price;
                        add_f[e.to] = min(add_f[v], e.cap - e.flow);
par[e.to] = {v, i};
                         if (!used[e.to]) {
                             q.push(e.to);
                             used[e.to] = 1;
                        }
                   }
              }
         }
     void push_flow(11 flow) {
          int cur = t:
          while (cur != s) {
               int prev = par[cur].first, id = par[cur].second;
               g[prev][id].flow += flow;
               g[cur][g[prev][id].id].flow -= flow;
               ans += g[prev][id].price * flow;
               cur = prev;
     11 min_cost_max_flow(int _s, int _t) {
          ans = 0;
          s = _s;
t = _t;
          while (true) {
              FB();
               11 flow = add_f[t];
               if (flow == 0) {
                   break:
              push_flow(flow);
          return ans;
    }
};
```

2.8 Кун

```
bool dfs(int v) {
    if (used[v])
        return false;
    used[v] = true;
    for (auto u : g[v]) {
        if (back[u] == -1 || dfs(back[u])) {
            back[u] = v;
            return true;
        }
    }
    return false;
```

}

2.9 HLD (TheEvilBird)

```
struct HLD {
     // insert SegTree code
     struct SegTree {};
     SegTree st;
     vector<vector<int>> tree;
     vector<int> par, siz, tin, tout, head;
    HLD(int _n) {
    n = _n;
         tree.resize(n);
         par.resize(n, -1);
         siz.resize(n, 0);
         tin.resize(n);
         tout.resize(n);
         head.resize(n):
         st = SegTree(n);
     void add_edge(int v, int u) {
         tree[v].emplace_back(u);
         tree[u].emplace_back(v);
     void build(int v = 0) {
         dfs_siz(v, v);
         T = 0:
         head[v] = v:
         dfs_hld(v, v);
     void dfs_siz(int v, int p) {
         par[v] = p;
siz[v] = 1;
         for (auto &u : tree[v]) {
   if (u != p) {
                  dfs_siz(u, v);
                  siz[v] += siz[u];
         for (int i = 0; i < sz(tree[v]); ++i) {
   int x = tree[v][0], u = tree[v][i];
   if (x == p || siz[u] > siz[x]) {
                   swap(tree[v][0], tree[v][i]);
    }
    void dfs_hld(int v, int p) {
         tin[v] = T++;
for (auto u : tree[v]) {
             if (u == p) {
                  continue;
              if (u == tree[v][0]) {
                  head[u] = head[v];
              } else {
                  head[u] = u;
              dfs_hld(u, v);
         tout[v] = T;
     void update(int v, int val) {
         st.update_segment(tin[v], tin[v], val);
    bool is_anc(int v, int u) {
    return tin[v] <= tin[u] && tout[u] <= tout[v];</pre>
     void go up(int &v. int u) {
         while (!is_anc(head[v], u)) {
             ans = max(ans, st.get(tin[head[v]], tin[v]));
              v = par[head[v]];
    }
    11 get(int v, int u) {// max on path
         ans = -INFLL;
         go_up(v, u);
         go_up(u, v);
         if (!is_anc(v, u)) {
              swap(v, u);
```

```
ans = max(ans, st.get(tin[v], tin[u]));
    return ans;
}
```

2.10 Dominator tree (TheEvilBird)

```
struct Edge {
    int from, to, id;
    Edge() = default;
    Edge(int from, int to, int id) : from(from), to(to), id(id) {}
struct DSU {
    int n;
    vector<int> par;
    vector<pii> mn;
    DSU() = default;
    DSU(int n) : n(n) {
         par.resize(n);
         mn.resize(n);
         init();
    void init() {
         for (int i = 0; i < n; ++i) {
             par[i] = i;
              mn[i] = {INF, i};
    }
    int get(int v) {
   if (par[v] == v) {
             return v;
         int p = get(par[v]);
    mn[v] = min(mn[v], mn[par[v]]);
         if (mn[par[v]].first < mn[v].first) {</pre>
              mn[v] = mn[par[v]];
         par[v] = p;
         return p;
    void unite(int a, int b) {
         par[a] = b;
struct DominatorTree {
    int n;
    vector<Edge> edges;
    vector<int> sdom, idom, tin, order, par, used, dp;
     vector<vector<int>>> g, rg, queries;
    DSU dsu_sdom, dsu_idom;
    DominatorTree() = default;
    DominatorTree(int n) : n(n), dsu_sdom(n), dsu_idom(n) {
   sdom.resize(n, INF); // semi-dominator
   idom.resize(n, INF); // immediate dominator
         tin.resize(n, -1);
         par.resize(n);
         used.resize(n, 0);
         dp.resize(n, INF);
         g.resize(n);
         rg.resize(n);
         queries.resize(n);
    }
    void add_edge(int from, int to) {
         edges.emplace_back(from, to, sz(edges));
    void dfs(int v) {
         tin[v] = sz(order);
         order.emplace_back(v);
         for (auto i: g[v]) {
   const auto &e = edges[i];
   if (tin[e.to] == -1) {
                  par[e.to] = v;
                   dfs(e.to);
             }
         }
    void dfs_idom(int v) {
         used[v] = 1;
         for (auto i: g[v]) {
    const auto &e = edges[i];
              if (!used[e.to]) {
                  dfs_idom(e.to);
```

```
for (auto u: queries[v]) {
         dsu_idom.get(u);
         dp[u] = dsu_idom.mn[u].second;
     dsu_idom.mn[v] = {sdom[v], v};
     for (auto i: g[v]) {
         const auto &e = edges[i];
if (par[e.to] == v) {
              dsu_idom.unite(e.to, v);
void build(int s) {
   for (int i = 0; i < sz(edges); ++i) {
      g[edges[i].from].emplace_back(i);</pre>
         rg[edges[i].to].emplace_back(i);
     // reorder vertex
     dfs(s);
     // build sdom
    for (int _ = sz(order) - 1; _ >= 0; --_) {
   int v = order[_];
         if (v == s) {
              continue;
         for (auto i: rg[v]) {
   const auto &e = edges[i];
              if (tin[e.from] == -1) {
              if (tin[e.from] < tin[v]) {</pre>
                   sdom[v] = min(sdom[v], tin[e.from]);
                   int u = dsu_sdom.get(e.from);
                   sdom[v] = min(sdom[v], dsu_sdom.mn[e.from].first);
         dsu_sdom.mn[v] = {sdom[v], v};
         for (auto i: g[v]) {
              const auto &e = edges[i];
              if (v == par[e.to]) {
                   dsu_sdom.unite(e.to, v);
              }
         }
     // build queries for idoms
    for (int i = 0; i < n; ++i) {
   if (i == s || sdom[i] == INF || tin[i] == -1) {
              continue:
         queries[order[sdom[i]]].emplace_back(i);
     dfs_idom(s);
     // build idom
     idom[s] = tin[s];
     for (auto v: order) {
    if (v == s) {
              continue;
         if (v == dp[v]) {
              idom[v] = sdom[v];
              idom[v] = idom[dp[v]];
}
int get_idom(int v) {
     return (idom[v] == INF ? -1 : order[idom[v]]);
```

2.11 Link-Cut (TheEvilBird)

};

```
struct Node {
   Node *ch[2] = {nullptr, nullptr};
   Node *par = nullptr;
   bool rev = false;
   int val, mn;
   int siz = 1;
   Node() {}
   Node(int val) : val(val), mn(val) {}
}.
```

```
typedef Node *pnode;
int get_siz(pnode v) {
    return (v == nullptr ? 0 : v->siz);
int get_min(pnode v) {
    return (v == nullptr ? INF : v->mn);
}
void update(pnode v) {
    v->siz = 1 + get_siz(v->ch[0]) + get_siz(v->ch[1]);
    v->mn = min(v->val, min(get_min(v->ch[0]), get_min(v->ch[1])));
void push(pnode v) {
   if (v == nullptr || !v->rev) {
        return;
    if (v->ch[0] != nullptr) {
        v->ch[0]->rev ^= 1;
    if (v->ch[1] != nullptr) {
        v->ch[1]->rev ^= 1;
    swap(v->ch[0], v->ch[1]);
    v \rightarrow rev = 0;
bool is_root(pnode v) {
    return (v->par == nullptr ||
             (v->par->ch[0] != v && v->par->ch[1] != v));
}
int child_num(pnode v) {
    return (v->par->ch[1] == v);
void attach(pnode v, pnode p, int num) {
    if (v != nullptr) {
        v->par = p;
    if (p != nullptr) {
        p->ch[num] = v;
    }
}
void rotate(pnode v) {
    int num = child_num(v);
pnode p = v->par, vb = v->ch[num ^ 1];
      node g = (p == nullptr ? nullptr : p->par);
    if (g != nullptr) {
        if (!is_root(p)) {
            g->ch[child_num(p)] = v;
    v->par = g;
    attach(p, v, num ^ 1);
    attach(vb, p, num);
    update(p);
    update(v);
void splay(pnode v) {
    vector<pnode> st;
    pnode cur = v:
    st.emplace_back(cur);
    while (!is_root(cur)) {
        cur = cur->par;
        st.emplace_back(cur);
    for (int i = sz(st) - 1; i \ge 0; --i) {
        push(st[i]);
    while (!is_root(v)) {
        if (!is_root(v->par)) {
   if (child_num(v) == child_num(v->par)) {
                 rotate(v->par);
            } else {
                rotate(v);
            }
        }
        rotate(v);
    }
void expose(pnode v) {
    splay(v);
v->ch[1] = nullptr;
    update(v);
    while (v->par != nullptr) {
        splay(v->par);
        attach(v, v->par, 1);
        update(v->par);
        splay(v);
```

```
void make_root(pnode v) {
    expose(v);
    v->rev ^= 1;
void link(pnode v, pnode u) {
    make_root(v);
    make root(u):
    u \rightarrow par = v;
void cut(pnode v, pnode u) {
    make_root(v);
    make_root(u);
    push(u);
    u->ch[1] = nullptr;
    v->par = nullptr;
bool is_connected(pnode v, pnode u) {
    make_root(v);
    make_root(u);
    if (is_root(v) && u != v) {
        return false;
    } else {
        return true;
int get_min(pnode v, pnode u) {
    make_root(v);
    make_root(u);
    return get_min(u);
```

2.12 Личао (FedShat)

```
struct LiChao {// max
    struct Line {
        11 k = 0, b = -INFLL;
         Line() = default;
         Line(11 k, 11 b) : k(k), b(b){};
         11 operator()(11 x) {
             return k * x + b;
        }
    };
    struct Node {
   Node *l = nullptr, *r = nullptr;
         Line cur;
        Node() = default;
    };
    Node *root = nullptr;
    int n = 1e9 + 1;
    void make_node(Node *&v) {
        if (v == nullptr) {
             v = new Node();
    }
    void add(Node *&v, int 1, int r, Line cur) {
         make_node(v);
        int m = (1 + r) / 2;
if (cur(m) > v->cur(m)) {
             swap(cur, v->cur);
         if (1 + 1 == r) {
             return;
         if (cur(1) > v->cur(1)) {
             add(v->1, 1, m, cur);
             add(v->r, m, r, cur);
    }
    void add(Line cur) {
         add(root, 0, n, cur);
    ll get(Node *v, int l, int r, int x) {
   if (v == nullptr) {
             return -INFLL;
```

```
ll ans = v->cur(x);
  if (1 + 1 == r) {
      return ans;
}
  int m = (1 + r) / 2;
  if (x < m) {
      ans = max(ans, get(v->1, 1, m, x));
} else {
      ans = max(ans, get(v->r, m, r, x));
}
  return ans;
}

ll get(int x) {
  return get(root, 0, n, x);
};
};
```

2.13 Segment Tree (TheEvilBird)

```
struct SegTree {
    static const 11 off = 0:
    struct Node {
         11 val = 0;
         11 push = off;
         Node() {}
         Node(ll val) : val(val) {}
         Node operator+(const Node &other) const {
              return Node(val + other.val);
         void operator+=(const Node &other) {
              val += other.val;
         void use_push(int len = 1) {
   val += push * (11) (len);
         void update_push(11 pushed) {
            push += pushed;
         }
    }:
    int n, qL, qR;
    Node ans;
    vector<Node> tree;
    vector<ll> a;
    SegTree() {}
    SegTree(int _n) {
         tree.assign(4 * n, 0);
    void update_vertex(int v, int 1, int r) {// [l, r)}
int m = (1 + r) / 2, vL = 2 * v, vR = vL + 1;
         push(vL, 1, m);
         push(vR, m, r);
         tree[v] = tree[vL] + tree[vR];
    void push(int v, int 1, int r) {// [l, r)
  if (tree[v].push == off) return;
  int m = (1 + r) / 2, vL = 2 * v, vR = vL + 1;
         tree[v].use_push(r - 1);
         if (1 + 1 != r) {
              tree[vL].update_push(tree[v].push);
              tree[vR].update_push(tree[v].push);
         tree[v].push = off:
    void build(vector<11> &_a) {
         build_tree(1, 0, n);
    void build_tree(int v, int 1, int r) \{// [l, r)
         if (1 + 1 == r) {
              tree[v] = Node(a[1]);
             return:
         int m = (1 + r) / 2, vL = 2 * v, vR = vL + 1;
```

```
build_tree(vL, 1, m);
         build_tree(vR, m, r);
         update_vertex(v, 1, r);
    }
     void update_segment(int _qL, int _qR, 11 _val) {// [_qL, _qR]
         qL = _qL;
qR = _qR + 1;
val = _val;
         update_segment_tree(1, 0, n);
     void update_segment_tree(int v, int 1, int r) \{//[l, r)
         push(v, 1, r);
if (qL <= 1 && r <= qR) {</pre>
              tree[v].update_push(val);
              push(v, 1, r);
              return;
         int m = (1 + r) / 2, vL = 2 * v, vR = vL + 1;
         if (qL < m) update_segment_tree(vL, 1, m);</pre>
         if (m < qR) update_segment_tree(vR, m, r);</pre>
         update_vertex(v, 1, r);
     11 get(int _qL, int _qR) {// [_qL, _qR]
         qL = _qL;

qR = _qR + 1;
         ans = Node();
         get_tree(1, 0, n);
         return ans.val;
    void get_tree(int v, int 1, int r) {// [l, r)
         push(v, 1, r);
if (qL <= 1 && r <= qR) {</pre>
              ans = ans + tree[v];
         int m = (1 + r) / 2, vL = 2 * v, vR = vL + 1;
         if (qL < m) get_tree(vL, 1, m);
if (m < qR) get_tree(vR, m, r);</pre>
    }
};
```

2.14 Segment Tree Down (TheEvilBird)

```
struct SegTreeDown {
    struct Node {
        11 val = 0;
        Node() {}
        Node(11 val) : val(val) {}
        Node operator+(const Node &other) const {
           return Node(val + other.val);
        void operator+=(const Node &other) {
            val += other.val:
    vector<Node> tree;
    SegTreeDown(int _n) {
        tree.assign(2 * n, Node());
    void build(vector<11> &a) {
        for (int i = 0; i < n; ++i) {
            tree[i + n] = Node(a[i]);
        for (int i = n - 1; i \ge 1; --i) {
            tree[i] = tree[2 * i] + tree[2 * i + 1];
    void update(int i, ll val) {
        tree[i] = val;
i /= 2;
        while (i != 0) {
            tree[i] = tree[2 * i] + tree[2 * i + 1];
            i /= 2;
   }
    11 get(int 1, int r) {// [l, r)
```

```
1 += n;
        r += n;
        Node ans;
        while (1 \le r) {
            if (1 % 2 == 1) {
                ans += tree[1];
                ++1;
            }
            if (r \% 2 == 0) {
                ans += tree[r];
                --r:
            }
            1 /= 2;
            r /= 2;
        return ans.val;
    }
};
```

2.15 Segment Tree Beats (TheEvilBird)

```
struct SegTree {
    struct Node {
        11 max, sec_max;
        int cnt_max;
        11 min, sec_min;
        int cnt_min;
        11 sum:
        11 push_add;
        11 push_eq;
    int n, qL, qR;
    ll val, ans;
    vector<Node> tree;
    vector<11> a;
    SegTree(int _n) {
        n = _n;
        tree.assign(4 * n, {0, -INFLL, 1, 0, INFLL, 1, 0, 0, -1});
    void update_vertex(int v, int 1, int r) {
        int m = (1 + r) / 2, vL = 2 * v, vR = vL + 1;
        tree[v].sum = tree[vL].sum + tree[vR].sum:
        tree[v].max = max(tree[vL].max, tree[vR].max);
        tree[v].sec_max = max(tree[vL].sec_max, tree[vR].sec_max);
        tree[v].cnt_max = 0;
        if (tree[vL].max == tree[v].max) {
            tree[v].cnt_max += tree[vL].cnt_max;
        } else {
            tree[v].sec_max = max(tree[v].sec_max, tree[vL].max);
        if (tree[vR].max == tree[v].max) {
            tree[v].cnt_max += tree[vR].cnt_max;
        } else {
            tree[v].sec_max = max(tree[v].sec_max, tree[vR].max);
        tree[v].min = min(tree[vL].min, tree[vR].min);
        tree[v].sec_min = min(tree[vL].sec_min, tree[vR].sec_min);
        tree[v].cnt_min = 0;
        if (tree[vL].min == tree[v].min) {
    tree[v].cnt_min += tree[vL].cnt_min;
        } else {
            tree[v].sec_min = min(tree[v].sec_min, tree[vL].min);
        if (tree[vR].min == tree[v].min) {
            tree[v].cnt_min += tree[vR].cnt_min;
          else {
            tree[v].sec_min = min(tree[v].sec_min, tree[vR].min);
   }
    void recalc_eq(int v, int 1, int r, 11 cur) {
        tree[v].max = tree[v].min = tree[v].push_eq = cur;
tree[v].sec_max = -INFLL;
        tree[v].sec_min = INFLL;
        tree[v].cnt_max = tree[v].cnt_min = r - 1;
        tree[v].sum = cur * (11) (r - 1);
        tree[v].push_add = 0;
    void recalc_add(int v, int l, int r, ll cur) {
   if (tree[v].min == tree[v].max) {
            recalc_eq(v, 1, r, tree[v].max + cur);
        tree[v].max += cur;
        if (tree[v].sec_max != -INFLL) {
```

```
tree[v].sec_max += cur;
    tree[v].min += cur;
    if (tree[v].sec_min != INFLL) {
         tree[v].sec_min += cur;
    tree[v].sum += (11) (r - 1) * cur;
    tree[v].push_add += cur;
void recalc_min(int v, int l, int r, ll cur) {
   if (tree[v].min >= cur) {
        recalc_eq(v, 1, r, cur);
         return;
    if (tree[v].max <= cur) return;</pre>
    if (tree[v].sec_min == tree[v].max) {
         tree[v].sec_min = cur;
    tree[v].max = cur;
void recalc_max(int v, int 1, int r, 11 cur) {
    if (tree[v].max <= cur) {</pre>
        recalc_eq(v, 1, r, cur);
        return:
    if (tree[v].min >= cur) return;
    if (tree[v].sec_max == tree[v].min) {
    tree[v].sec_max = cur;
    tree[v].sum += (11) (tree[v].max - cur) *
                     (11) (tree[v].cnt_max);
    tree[v].min = cur:
void push(int v, int l, int r) {
   if (1 + 1 == r) return;
    int m = (1 + r) / 2, vL = 2 * v, vR = vL + 1;
    if (tree[v].push_eq != -1) {
         recalc_eq(vL, 1, m, tree[v].push_eq);
         recalc_eq(vR, m, r, tree[v].push_eq);
         tree[v].push_eq = -1;
         return;
    recalc_add(vL, 1, m, tree[v].push_add);
    recalc_add(vR, m, r, tree[v].push_add);
tree[v].push_add = 0;
    recalc_min(vL, 1, m, tree[v].max);
recalc_min(vR, m, r, tree[v].max);
    recalc_max(vL, 1, m, tree[v].min);
    recalc_max(vR, m, r, tree[v].min);
void build(vector<11> &_a) {
    build_tree(1, 0, n);
}
void build_tree(int v, int 1, int r) {
   if (1 + 1 == r) {
        tree[v] = {a[1], -INFLL, 1, a[1],
                     INFLL, 1, a[1], 0, -1};
         return:
    int m = (1 + r) / 2, vL = 2 * v, vR = vL + 1;
    build_tree(vL, 1, m);
build_tree(vR, m, r);
    update_vertex(v, 1, r);
void update_segment_min(int _qL, int _qR, 11 _val) {
    qL = _qL;
qR = _qR + 1;
val = _val;
    update_segment_min_tree(1, 0, n);
void update_segment_min_tree(int v, int 1, int r) {
    if (tree[v].max <= val) return;
    if (qL <= 1 && r <= qR && tree[v].sec_max < val) {</pre>
        recalc_min(v, 1, r, val);
         return:
    push(v, 1, r);
int m = (1 + r) / 2, vL = 2 * v, vR = vL + 1;
    if (qL < m) update_segment_min_tree(vL, 1, m);</pre>
    if (m < qR) update_segment_min_tree(vR, m, r);</pre>
    update_vertex(v, 1, r);
```

```
}
     void update_segment_max(int _qL, int _qR, ll _val) {
           qL = _qL;
qR = _qR + 1;
val = _val;
           update_segment_max_tree(1, 0, n);
     void update_segment_max_tree(int v, int 1, int r) {
   if (tree[v].min >= val) return;
           if (qL <= 1 && r <= qR && tree[v].sec_min > val) {
                recalc_max(v, 1, r, val);
           }
          push(v, 1, r);
int m = (1 + r) / 2, vL = 2 * v, vR = vL + 1;
if (qL < m) update_segment_max_tree(vL, 1, m);
if (m < qR) update_segment_max_tree(vR, m, r);</pre>
           update_vertex(v, 1, r);
     void update_segment_add(int _qL, int _qR, 11 _val) {
           qL = _qL;
qR = _qR + 1;
val = _val;
           update_segment_add_tree(1, 0, n);
     void update_segment_add_tree(int v, int l, int r) { if (qL <= 1 && r <= qR) {
               recalc_add(v, 1, r, val);
          push(v, 1, r);
int m = (1 + r) / 2, vL = 2 * v, vR = vL + 1;
if (qL < m) update_segment_add_tree(vL, 1, m);
if (m < qR) update_segment_add_tree(vR, m, r);</pre>
           update_vertex(v, 1, r);
     11 get(int _qL, int _qR) {
          qL = _qL;
qR = _qR + 1;
           ans = 0;
           get_tree(1, 0, n);
           return ans;
     void get_tree(int v, int l, int r) {
           if (qL <= 1 && r <= qR) {
                ans += tree[v].sum;
                return;
           push(v, 1, r);
int m = (1 + r) / 2, vL = 2 * v, vR = vL + 1;
           if (qL < m) get_tree(vL, 1, m);</pre>
           if (m < qR) get_tree(vR, m, r);</pre>
     void print_all() {
           print_all_tree(1, 0, n);
     void print_all_tree(int v, int l, int r) {
           if (1 + 1 == r) {
                cout << tree[v].sum << en;
                return;
          push(v, 1, r);
int m = (1 + r) / 2, vL = 2 * v, vR = vL + 1;
           print_all_tree(vL, 1, m);
           print_all_tree(vR, m, r);
     }
};
```

2.16 Persistent Segment Tree (Sweezyk)

```
struct Node {
    Node *1, *r;
    int mx;
    Node() {
        mx = -1;
        1 = r = nullptr;
    }
};
const int N = 1e7 + 4e6;
const int LG = 20;
Node *nodes[N];
int ptr;
```

```
Node *new_node() {
     return nodes[ptr++];
 }
 Node *get_left(Node *t) {
     if (t && t->1) return t->1;
     return nullptr;
 Node *get_right(Node *t) {
   if (t && t->r) return t->r;
     return nullptr;
 int get_max(Node *t) {
     if (!t) return 0;
     return t->mx:
 void update(int i, int val, Node *t, Node *old_t, int lx, int rx) {
     if(1x + 1 == rx) {
         t->mx = max(t->mx, val);
         return:
     int m = (1x + rx) / 2;
     if (i < m) {
          t->1 = new_Node();
          if (old_t && old_t->1) {
              t->1->mx = old_t->1->mx;
          t->r = get_right(old_t);
          update(i, val, t->1, get_left(old_t), lx, m);
          t->r = new_Node();
          if (old_t && old_t->r) {
              t \rightarrow r \rightarrow mx = old t \rightarrow r \rightarrow mx:
          t->l = get_left(old_t);
          update(i, val, t->r, get_right(old_t), m, rx);
     t->mx = max(get_max(get_left(t)), get_max(get_right(t)));
 int get(int 1, int r, Node *t, int lx, int rx) {
     if (!t || lx >= r || rx <= 1) return -1;
     if (1x >= 1 &\& rx <= r) return t->mx;
     int m = (lx + rx) / 2;
     return max(get(1, r, t->1, lx, m), get(1, r, t->r, m, rx));
```

2.17 Fenwick (TheEvilBird)

```
struct Fenwick {
    int n;
    vector<ll> f:
    Fenwick(int _n) {
        n = _n;
        f.assign(n + 1, 0);
    void update(int x, ll delta) {
        for (int i = x; i <= n; i += i & -i) {
           f[i] += delta;
    11 get_sum(int x) {
        11 s = 0;
        for (int i = x; i > 0; i -= i & -i) {
           s += f[i];
        return s;
    11 get(int L, int R) {// [L, R]
        return get_sum(R) - get_sum(L - 1);
};
```

2.18 Sparse table (TheEvilBird)

```
struct Sparse {
  int n;
  vector<int> lg;
  vector<vector<ll>> table;

Sparse(int _n) {
    n = _n;
}
```

2.19 Treap (Sweezyk)

struct Node {

```
int x, y, size, push, cnt;
Node *1, *r;
    Node(int val) : x(val), y(rng()), size(1), push(0), cnt(0), l(nullptr),
void push(Node *t) {
    if (t == nullptr) return;
    int p = t->push;
    if (p == 0) return;
    if (t->1 != nullptr) {
         t->1->cnt += p;
        t->1->push += p;
    if (t->r != nullptr) {
        t->r->cnt += p;
        t->r->push += p;
    t->push = 0;
int size(Node *t) {
    return (t ? t->size : 0);
void update(Node *t) {
    if (t == nullptr) return;
    t-size = size(t->1) + size(t->r) + 1;
pair<Node *, Node *> split(Node *t, int k) {
    if (t == nullptr) return {nullptr, nullptr};
    if (k == 0) return {nullptr, t};
    push(t);
    if (size(t->1) + 1 \le k) {
        auto [1, r] = split(t->r, k - size(t->l) - 1);
         t->r = 1:
        update(t);
        return {t, r};
    } else {
        auto [1, r] = split(t->1, k);
        update(t);
        return {1, t};
    }
}
Node *merge(Node *t1, Node *tr) {
    if (t1 == nullptr) return tr;
if (tr == nullptr) return tl;
    push(t1);
    push(tr);
    if (t1->y > tr->y) {
        tl->r = merge(tl->r, tr);
        update(t1);
        return t1;
    } else {
        tr->1 = merge(t1, tr->1);
        update(tr);
        return tr;
    }
}
void dfs(Node *t) {
    if (t == nullptr) return;
```

```
dfs(t->1);
    cout << t->x << ' ' ' << t->cnt << '\n';
    dfs(t->r);
}

void solve() {
    int n, m;
    cin >> n >> m;
    Node *root = nullptr;
    for (int i = 1; i <= n; i++) {
        Node *add = new Node(i);
        root = merge(root, add);
}

for (int i = 0; i < m; i++) {
        int l, r;
        cin >> 1 >> r;
        auto [L, R] = split(root, r);
        auto [L1, L2] = split(L, l - 1);
        L2->push = 1;
        L2->cnt += 1;
        root = merge(L2, merge(L1, R));
}

dfs(root);
}
```

2.20 Extended GCD (Sweezyk)

```
template<typename T>
T extgcd(T a, T b, T &x, T &y) {
    if (a == 0) {
        x = 0;
         y = 1;
         return b;
    T p = b / a;
    T g = extgcd(b - p * a, a, y, x);
    x = p * y;
    return g;
{\tt template}{<}{\tt typename} \  \, {\tt T}{>}
bool diophantine(T a, T b, T c, T &x, T &y, T &g) {
   if (a == 0 && b == 0) {
        if (c == 0) {
             x = y = g = 0;
             return true;
        return false:
    if (a == 0) {
         if (c \% b == 0) {
             x = 0;
             y = c / b;
             g = abs(b);
             return true;
         return false;
    if (b == 0) {
        if (c % a == 0) {
    x = c / a;
             y = 0;
             g = abs(a);
             return true;
         return false:
    g = extgcd(a, b, x, y);
if (c % g != 0) {
         return false;
    T dx = c / a;
    c = dx * a;
    T dy = c / b;
    c = dy * b;
    x = dx + (T) ((__int128) x * (c / g) % b);
y = dy + (T) ((__int128) y * (c / g) % a);
    g = abs(g);
    return true;
    //|x|, |y| \le max(|a|, |b|, |c|) [tested]
bool crt(long long k1, long long m1, long long k2, long long m2, long long
     &k, long long &m) {
    k1 %= m1:
    if (k1 < 0) k1 += m1;
    k2 %= m2;
    if (k2 < 0) k2 += m2;
    long long x, y, g;
    if (!diophantine(m1, -m2, k2 - k1, x, y, g)) {
        return false:
    long long dx = m2 / g;
```

```
long long delta = x / dx - (x % dx < 0);
k = m1 * (x - dx * delta) + k1;
m = m1 / g * m2;
assert(0 <= k && k < m);
return true;
}</pre>
```

2.21 FFT (FedShat)

```
constexpr int P = 998244353;
using i64 = long long;
// assume -P \ll x \ll 2P
int norm(int x) {
    if (x < 0) {
       x += P;
    if (x \ge P) {
       x -= P;
    return x;
template<class T>
T power(T a, int b) {
    T res = 1;
    for (; b; b /= 2, a *= a) {
       if (b % 2) {
           res *= a;
    return res;
struct Z {
    int x;
    Z(int x = 0) : x(norm(x)) {}
    int val() const {
        return x;
    Z operator-() const {
        return Z(norm(P - x));
    Z inv() const {
        assert(x != 0);
        return power(*this, P - 2);
    Z &operator*=(const Z &rhs) {
        x = i64(x) * rhs.x % P;
    Z &operator+=(const Z &rhs) {
        x = norm(x + rhs.x);
        return *this:
    Z &operator == (const Z &rhs) {
        x = norm(x - rhs.x);
        return *this;
    Z &operator/=(const Z &rhs) {
        return *this *= rhs.inv();
    friend Z operator*(const Z &lhs, const Z &rhs) {
        Z res = lhs;
res *= rhs;
        return res:
    friend Z operator+(const Z &lhs, const Z &rhs) {
        res += rhs;
        return res;
    friend Z operator-(const Z &lhs, const Z &rhs) {
        Z res = lhs;
    friend Z operator/(const Z &lhs, const Z &rhs) {
        Z res = 1hs:
        res /= rhs;
        return res;
   }
std::vector<int> rev:
std::vector<Z> roots{0, 1};
void dft(std::vector<Z> &a) {
    int n = a.size();
    if (int(rev.size()) != n) {
        int k = __builtin_ctz(n) - 1;
rev.resize(n);
        for (int i = 0; i < n; i++) {
```

```
rev[i] = rev[i >> 1] >> 1 | (i & 1) << k;
     }
     for (int i = 0; i < n; i++) {
   if (rev[i] < i) {</pre>
               std::swap(a[i], a[rev[i]]);
     if (int(roots.size()) < n) {
   int k = __builtin_ctz(roots.size());</pre>
          roots.resize(n);
          while ((1 << k) < n) {
               Z = power(Z(3), (P - 1) >> (k + 1));
for (int i = 1 << (k - 1); i < (1 << k); i++) {
                     roots[2 * i] = roots[i];
roots[2 * i + 1] = roots[i] * e;
          }
     for (int k = 1; k < n; k *= 2) {
   for (int i = 0; i < n; i += 2 * k) {
               for (int j = 0; j < k; j++) {
    Z u = a[i + j];
                     Z v = a[i + j + k] * roots[k + j];
                     a[i + j] = u + v;
                     a[i + j + k] = u - v;
               }
}
void idft(std::vector<Z> &a) {
     int n = a.size();
     std::reverse(a.begin() + 1, a.end());
     dft(a);
     Z inv = (1 - P) / n;
     for (int i = 0; i < n; i++) {
          a[i] *= inv;
```

2.22 KTO (FedShat)

```
struct Eq \{// x = a \pmod{m}
    11 a. m:
    Eq(){};
    Eq(11 a, 11 m) : a(a), m(m){};
};
11 binpow(11 a, 11 n, 11 m) {
    if (n == 0) {
        return 1;
    if (n \% 2 == 0) {
        int128_t b = binpow(a, n / 2, m);
return (b * b) % m;
    int128_t x = binpow(a, n - 1, m);
    return (a * x) % m;
11 binpow(11 a, 11 n) {
   if (n == 0) {
        return 1;
    if (n \% 2 == 0) {
        11 b = binpow(a, n / 2);
        return b * b:
    return a * binpow(a, n - 1);
11 phi(11 a) {
    11 d = 2, k = a;
    map<11, int> cnt;
    while (d * d <= a) {
        if (k % d == 0) {
             k /= d;
            ++cnt[d];
        } else {
            ++d:
    if (k != 1) {
        ++cnt[k];
    11 ans = 1;
    for (auto i : cnt) {
        ans *= binpow(i.first, i.second - 1) * (i.first - 1);
```

```
}
return ans;
}

11 gcd(l1 a, l1 b) {
    return std::gcd(abs(a), abs(b));
}

Eq solve(Eq ai, Eq bi) {
    if (ai.m == -1 || bi.m == -1) {
        return {0, -1};
    }
    ll a = ai.m, b = bi.m, c = ai.a - bi.a;
    ll d = ::gcd(a, b);
    a /= d;
    b /= d;
    if (c % d != 0) {
        return {0, -1};
    }
    c /= d;
    ll x = (((int128_t) -c * (int128_t) binpow(a, phi(b) - 1, b)) % b + b)
        % b;
    x = ((int128_t) ai.m * (int128_t) x + ai.a) % lcm(ai.m, bi.m);
    return {x, lcm(ai.m, bi.m)};
}
```

2.23 Обратные по простому модулю

Пусть дан простой модуль m. Для каждого числа из [1, m-1] найти обратное к нему.

```
r[1] = 1;
for (int i = 2; i < m; ++i) {
    r[i] = (m - (m / i) * r[m % i] % m) % m;
}
```

2.24 Обратные факториалы

```
int inv(int a, int m) {
    if (a == 1)
        return 1;
    return (1 - inv(m % a, a) * m) / a + m;
}

{
    f[0] = 1;
    for (int i = 1; i < N; i++) {
        f[i] = i * f[i - 1] % mod;
    }

    r[N - 1] = inv(f[N - 1]) for (int i = N - 1; i >= 1; i--) {
        r[i - 1] = r[i] * i % mod;
    }
}
```

2.25 **Fayce**

```
int gauss(vector<vector<double>> a,
          vector<double> &ans) {
    int n = (int) a.size();
    int m = (int) a[0].size() - 1;
    vector<int> where(m, -1);
    for (int col = 0, row = 0;
          col < m && row < n; ++col) {</pre>
        int sel = row;
        for (int i = row; i < n; ++i)
             if (abs(a[i][col]) > abs(a[sel][col]))
        if (abs(a[sel][col]) < EPS)</pre>
             continue;
        for (int i = col; i <= m; ++i)
             swap(a[sel][i], a[row][i]);
        where[col] = row;
        for (int i = 0; i < n; ++i)
             if (i != row) {
                  double c =
            }
        ++row:
        a[i][col] / a[row][col];
for (int j = col; j <= m; ++j)
a[i][j] -= a[row][j] * c;
    ans.assign(m, 0);
    for (int i = 0; i < m; ++i)
if (where[i] != -1)
             ans[i] =
```

```
a[where[i]][m] / a[where[i]][i];
for (int i = 0; i < n; ++i) {
    double sum = 0;
    for (int j = 0; j < m; ++j)
        sum += ans[j] * a[i][j];
    if (abs(sum - a[i][m]) > EPS)
        return 0;
}
for (int i = 0; i < m; ++i)
    if (where[i] == -1) return INF;
return 1;
}</pre>
```

Бинарный

2.26 Быстрая факторизация (FedShat)

```
11 binpow(11 a, 11 n, 11 mod) {
    if (n == 0) {
        return 1;
    if (n \% 2 == 0) {
        int128_t b = binpow(a, n / 2, mod);
        return (b * b) % mod;
    return (((int128_t) a) * binpow(a, n - 1, mod)) % mod;
constexpr int N = 1e7;
vector<int> pr, lp;
bool prime(ll n) {
    if (n \le N) {
        return binary_search(all(pr), n);
    int iter = 60;
    int s = 0;
    11 d = n - 1;
while (d % 2 == 0) {
        d /= 2;
    auto test = [&](11 a) {
        if (binpow(a, d, n) == 1) {
            return true:
        11 _2r = 1;
        for (int r = 0; r < s; ++r) {
            auto tmp = binpow(binpow(a, d, n), _2r, n);
            if (tmp == n - 1) {
                return true:
            <u>2r</u> *= 2;
        return false;
    for (int _ = 0; _ < iter; ++_) {
        ll a = uniform_int_distribution<ll>(1, n - 1)(rnd);
        if (!test(a)) {
            return false;
    return true;
11 f(11 x, 11 n) {
   return ((int128_t) x * (int128_t) x + (int128_t) 2) % n;
}
11 pollard(11 n) {
    11 a = uniform_int_distribution<11>(0, n - 1)(rnd);
    11 x = a, y = a, d = 1;
```

```
constexpr int iter = 5e4;
    for (int _ = 0; _ < iter; ++_) {
    x = f(f(x, n), n);
         y = f(y, n);
         d = \gcd(abs(x - y), n);
         if (d != 1 && d != n) {
             break;
    if (d == 1 || d == n) {
         pollard(n);
    return d;
vector<11> res;
void factor(ll n) {
    if (n \le N) {
         while (true) {
             if (lp[n] == 0) {
                  break;
             res.push_back(lp[n]);
n /= lp[n];
         return:
    if (prime(n)) {
         res.push_back(n);
         return;
    11 d = pollard(n);
    factor(n / d);
    factor(d);
void solve() {
    cin >> n;
    fin > n,
for (int i = 2; i <= N; ++i) {
   if (lp[i] == 0) {
      lp[i] = i;
   }</pre>
             pr.push_back(i);
         7-
         for (int j = 0; j < (int) pr.size() && pr[j] <= lp[i] && i * pr[j]
      <= N; ++j) {
             lp[i * pr[j]] = pr[j];
    factor(n);
```

2.27 Префикс-функция

2.28 Z-функция

```
vector<int> z_function(string &s) {
    int n = (int) s.length();
    vector<int> z(n);
    for (int i = 1, 1 = 0, r = 0; i < n; ++i) {
        if (i <= r) {
            z[i] = min(r - i + 1, z[i - 1]);
        }
        while (i + z[i] < n && s[z[i]] == s[i + z[i]]) {
            ++z[i];
        }
        if (i + z[i] - 1 > r) {
            1 = i;
            r = i + z[i] - 1;
        }
    }
    return z;
}
```

2.29 Cydmac (TheEvilBird)

```
int mod(int x, int m) {
    if (x < 0) x += m;
     if (x >= m) x -= m;
    return x;
vector<int> sufix_array(string s) {
     int n = sz(s);
    vector<int> arr(n), narr(n), head(n), c(n), nc(n);
for (int i = 0; i < n; ++i) {
    arr[i] = i;</pre>
    sort(all(arr), [&](int x, int y) {
        return s[x] < s[y];
     int cl = 0;
     c[arr[0]] = cl:
    head[0] = 0;
for (int i = 1; i < n; ++i) {</pre>
         if (s[arr[i]] != s[arr[i - 1]]) {
             head[++cl] = i;
         c[arr[i]] = cl;
    for (int k = 1; k < n && cl < n; k *= 2) {
         for (int i = 0; i < n; i++) {
             int j = mod(arr[i] - k, n);
narr[head[c[j]]++] = j;
         c1 = 0;
         head[0] = 0;
         pii prev = {c[narr[0]], c[mod(narr[0] + k, n)]};
         for (int i = 1; i < n; i++) {
   pii cur = {c[narr[i]], c[mod(narr[i] + k, n)]};</pre>
              if (cur != prev) {
    head[++cl] = i;
              nc[narr[i]] = cl;
             prev = cur;
         swap(arr, narr);
         swap(c, nc);
     // returns sufix array without $
     return vector<int>(arr.begin() + 1, arr.end());
vector<int> build_lcp(string &s, vector<int> &suf) {
    int n = sz(s);
     vector<int> lcp(n - 1), order(n);
    for (int i = 0; i < n; ++i) {
    order[suf[i]] = i;
    7
    int 1 = 0;
for (int i = 0; i < n; ++i) {
         int id = order[i];
         if (id + 1 == n) {
             1 = 0;
             continue;
         int j = suf[id + 1];
         if (1) --1;
         while (\max(i + 1, j + 1) < n \&\&
                 s[i + 1] == s[j + 1]) {
         lcp[id] = 1;
    return lcp;
```

2.30 Суфавтомат (TheEvilBird)

```
struct Node {
   int go[26];
   int suf, prev, term, len;

   Node() {
       for (auto &i : go) {
            i = -1;
       }
   len = 0;
       suf = -1;
       prev = -1;
       term = 0;
   }
};
```

```
vector<Node> automat;
int add(int a, int ch) {
    int b = sz(automat);
    automat.emplace_back();
    automat[b].prev = a;
    automat[b].suf = 0;
    automat[b].len = automat[a].len + 1;
    for (; a != -1; a = automat[a].suf) {
    if (automat[a].go[ch] == -1) {
              automat[a].go[ch] = b;
              continue;
         int c = automat[a].go[ch];
         if (automat[c].prev == a) {
   automat[b].suf = c;
              break;
         int d = sz(automat);
         automat.emplace_back();
         automat[d].suf = automat[c].suf;
automat[d].len = automat[a].len + 1;
         automat[c].suf = d;
         automat[b].suf = d;
         automat[d].prev = a;
for (int i = 0; i < 26; ++i) {</pre>
              automat[d].go[i] = automat[c].go[i];
         for (; a != -1 && automat[a].go[ch] == c; a = automat[a].suf) {
             automat[a].go[ch] = d;
         break;
     // returns id of the added vertex
    return b:
```

2.31 Axo-Корасик (Sweezyk)

```
struct Node {
    int par;
    int par_c:
    int go[26];
    int term;
    int link:
    int super;
    int cnt:
const int N = 1e6 + 5;
int ptr = 1;
Node trie[N]:
void add(string s) {
    int cur = 1;
    for (auto &q : s) {
        int c = q - 'a';
        if (trie[cur].go[c]) {
            cur = trie[cur].go[c];
        } else {
           ++ptr;
            trie[cur].go[c] = ptr;
            trie[ptr].par = cur;
            trie[ptr].par_c = c;
            cur = ptr;
       }
    trie[cur].cnt++;
void build() {
    queue<int> q;
    q.push(1);
    while (!q.empty()) {
        int v = q.front();
        q.pop();
        if (v != 1) {
            if (trie[v].par == 1) {
                trie[v].link = trie[v].super = 1;
                trie[v].link = trie[trie[trie[v].par].link].go[trie[v].
                trie[v].super = (trie[trie[v].link].cnt ? trie[v].link :
     trie[trie[v].link].super);
           }
        trie[v].cnt += trie[trie[v].link].cnt;
        for (int c = 0; c < 26; c++) {
           if (trie[v].go[c]) {
                q.push(trie[v].go[c]);
            } else {
               if (v == 1) {
```

2.32 Манакер

```
vector<int> d1(n);
int l = 0, r = -1;
for (int i = 0; i < n; ++i) {
    int k = (i > r ? 1 : min(d1[1 + r - i], r - i + 1));
    while (i + k < n && i - k >= 0 && s[i + k] == s[i - k]) {
        ++k;
    }
    d1[i] = k;
    if (i + k - 1 > r) {
        1 = i - k + 1;
        r = i + k - 1;
    }
}
vector<int> d2(n);
l = 0;
r = -1;
for (int i = 0; i < n; ++i) {
    int k = (i > r ? 0 : min(d2[1 + r - i + 1], r - i + 1));
    while (i + k < n && i - k - 1 >= 0 && s[i + k] == s[i - k - 1]) {
        ++k;
    }
    d2[i] = k;
    if (i + k - 1 > r) {
        1 = i - k;
        r = i + k - 1;
    }
}
```

2.33 CHT (FedShat)

```
struct Line {
    11 k = 0, b = -INFLL;
    Line() = default;
    Line(11 k, 11 b) : k(k), b(b){};
    ld operator()(ld x) {
        return k * x + b;
};
bool operator<(Line a, Line b) {
    return a.k < b.k || (a.k == b.k && a.b > b.b);
bool operator<(pair<Line, ld> a, pair<Line, ld> b) {
   return a.second < b.second;
}
struct CHT {
    vector<pair<Line, ld>> convex;
        while (!convex.empty() && a(convex.back().second) > convex.back().
      first(convex.back().second)) {
            convex.pop_back();
        if (!convex.empty()) {
            xn = (a.b - convex.back().first.b + 0.0) / (convex.back().first
      .k - a.k);
        convex.push back({a, xn}):
    CHT(vector<Line> lines) {
        sort(all(lines));
        for (int i = 0; i < (int) lines.size();) {</pre>
             int j = i;
             while (j < (int) lines.size() && lines[i].k == lines[j].k) {
             add(lines[i]);
             i = j;
```

```
ld get(ld x) {
   auto it = upper_bound(all(convex), pair(Line(), x)) - convex.begin
   return convex[it - 1].first(x):
```

```
#ifdef LOCAL
#define debug(...) cerr << "[" << #__VA_ARGS__ << "]:", debug_out(
     __VA_ARGS__)
#else
#define debug(...) 42
#endif
```

2.34Дебаг Туриста

```
template<typename A, typename B>
string to_string(pair<A, B> p);
template<typename A, typename B, typename C>
string to_string(tuple<A, B, C> p);
template<typename A, typename B, typename C, typename D>
string to_string(tuple<A, B, C, D> p);
string to_string(const string &s) {
    return '"' + s + '"';
string to_string(const char *s) {
    return to_string((string) s);
string to_string(bool b) {
    return (b ? "true" : "false");
string to_string(vector<bool> v) {
    bool first = true;
string res = "{";
    for (int i = 0; i < static_cast<int>(v.size()); i++) {
   if (!first) {
            res += ", ";
         first = false;
        res += to_string(v[i]);
    res += "}";
    return res;
template<size_t N>
string to_string(bitset<N> v) {
    string res = "";
    for (size_t i = 0; i < N; i++) {
        res += static_cast<char>('0' + v[i]);
    }
    return res;
template<typename A>
string to_string(A v) {
    bool first = true;
string res = "{";
    for (const auto &x : v) {
        if (!first) {
            res += ", ";
         first = false;
         res += to_string(x);
    res += "}":
    return res:
template<typename A, typename B>
string to_string(pair<A, B> p) {
   return "(" + to_string(p.first) + ", " + to_string(p.second) + ")";
template<typename A, typename B, typename C>
string to_string(tuple<A, B, C> p)
    return "(" + to_string(get<0>(p)) + ", " + to_string(get<1>(p)) + ", "
      + to_string(get<2>(p)) + ")";
template<typename A, typename B, typename C, typename D>
string to_string(tuple<A, B, C, D> p) {
   return "(" + to_string(get<0>(p)) + ", " + to_string(get<1>(p)) + ", "
      + to_string(get<2>(p)) + ", " + to_string(get<3>(p)) + ")";
void debug_out() { cerr << endl; }</pre>
template<typename Head, typename... Tail>
void debug_out(Head H, Tail... T) {
   cerr << " " << to_string(H);</pre>
    debug_out(T...);
```

2.35Геометрия (TheEvilBird)

```
const long double PI = 3.1415926535897932384626433832795;
const long double EPS = 1e-7;
 * Rotate relative to the origin, a - rotation angle:
 * new_x = x \cos(a) - y \sin(a)
* new_y = x \sin(a) + y \cos(a)
 * new_x = x cos(a) + y sin(a)
 * new_y = x sin(a) - y cos(a)
 * rad = degree * PI / 180
   degree = rad * 180 / PI
struct Point {
    11 x = 0, y = 0;
     // int id = -1:
     Point() : x(0), y(0) {}
     Point(11 _x, 11 _y) : x(_x), y(_y) {}
    bool operator==(const Point other) const {
    return x == other.x && y == other.y;
     void operator*=(11 k) {
         y *= k;
    }
}:
istream &operator>>(istream &is, Point &point) {
     is >> point.x >> point.y;
    return is;
ostream & operator << (ostream & os, const Point & point) {
    os << point.x << ' ' << point.y;
     return os;
}
struct Vec {
    11 x, y;
     Vec() : x(0), y(0) {}
    Vec(11 _x, 11 _y) : x(_x), y(_y) {}
Vec(Point a) : x(a.x), y(a.y) {}
     Vec(Point a, Point b) : x(b.x - a.x), y(b.y - a.y) {}
    ld len() const {
         return sqrtl(x * x + y * y);
    11 len_sq() const {
         return (x * x + y * y);
     Vec operator*(11 k) const {
         return \{x * k, y * k\};
     void operator*=(11 k) {
     Vec operator+(const Vec other) const {
         return {x + other.x, y + other.y};
    Vec operator-(const Vec other) const {
         return {x - other.x, y - other.y};
    bool operator==(const Vec other) const {
         return x == other.x && y == other.y;
    bool operator!=(const Vec other) const {
         return !(*this == other);
```

```
11 operator*(const Vec other) const {// dot product
         return x * other.x + y * other.y;
    }
    11 operator%(const Vec other) const {// cross product
         return x * other.y - y * other.x;
     7
};
istream &operator>>(istream &is, Vec &vec) {
     is >> vec.x >> vec.y;
     return is;
ostream &operator<<(ostream &os, const Vec &vec) {</pre>
     os << vec.x << ' ' << vec.y;
     return os;
typedef vector<Point> Polygon;
typedef vector<Vec> vPolygon;
bool cmp_vectors(Vec a, Vec b) {
    if ((a.y < 0 || (a.y == 0 && a.x < 0)) && (b.y > 0 || (b.y == 0 && b.x > 0))) {
         return true:
     if ((b.y < 0 \mid | (b.y == 0 \&\& b.x < 0)) \&\& (a.y > 0 \mid | (a.y == 0 \&\& a.x > 0))) {
         return false;
     return (a % b > 0 || (a % b == 0 && a.len_sq() < b.len_sq()));
int get_sign(ld kek) {
     if (kek > 0) return 1;
     if (kek < 0) return -1;
     return 0;
Polygon build_convex_hull(Polygon &a) {
     int n = sz(a);
     for (int i = 1; i < n; ++i) {
         if ((a[i].y < a[0].y) \mid | (a[i].y == a[0].y && a[i].x < a[0].x))
      swap(a[0], a[i]);
     sort(a.begin() + 1, a.end(), [&](Point A, Point B) {
   Vec oa(a[0], A), ob(a[0], B);
   if ((oa % ob) == 0) return oa.len_sq() < ob.len_sq();</pre>
         return (oa % ob) > 0;
     Polygon hull = {a[0]};
    for (int i = 1; i < n; ++i) {
   while (sz(hull) >= 2) {
              Vec ab(hull[sz(hull) - 2], hull[sz(hull) - 1]), bp(hull[sz(hull
      ) - 1], a[i]);
             if ((ab % bp) <= 0) {
                  hull.pop_back();
              } else {
                  break;
             }
         hull.emplace_back(a[i]);
     7
     return hull;
11 area_of_polygon(Polygon &poly) {
    11 res = 0;
int n = sz(poly);
     for (int i = 2; i < n; ++i) {
    Vec ab(poly[0], poly[i - 1]), ac(poly[0], poly[i]);</pre>
         res += (ab % ac):
     // don't forget to divide the result by 2!
     return res;
ld perimeter_of_polygon(Polygon &poly) {
     ld res = 0;
     int n = sz(poly);
     for (int i = 0; i < n; ++i) {
         Vec v(poly[i], poly[(i + 1 == n ? 0 : i + 1)]);
         res += v.len();
     return res;
11 diameter_of_polygon(Polygon &poly) {
    int n = sz(poly), x = 1;
ll ans = 0;
     for (int i = 0; i < n; ++i) {
         int j = (i + 1) \% n;
         while (true) {
```

```
Vec ac(poly[i], poly[x]), ab(poly[i], poly[j]), cd(poly[x],
      poly[(x + 1) % n]);
             ans = max(ans, ac.len_sq());
             if ((ab % cd) <= 0) {
                 break:
             x %= n;
    // don't forget to extract root!
    return ans;
ld angle(const Vec &a, const Vec &b) {
    return fabsl(atan2(a \% b, a * b) / PI * 180);
}
ld angle_rad(const Vec &a, const Vec &b) {
    return (atan2(a % b, a * b));
}
ld angle rad(const Point &a) {
    return atan2(a.y, a.x);
ld from_point_to_line(const Point &p, const Point &a, const Point &b) {
    Vec ba(b, a), ap(a, p);
return fabs((ba % ap) / ba.len());
ld from_point_to_ray(const Point &p, const Point &a, const Point &b) {
    Vec ba(b, a), ap(a, p), ab(a, b);
if ((ab * ap) < 0) {
        return ap.len();
    } else {
        return fabs((ba % ap) / ba.len());
ld from_point_to_segment(const Point &p, const Point &a, const Point &b) {
    Vec ab(a, b), ap(a, p), bp(b, p), ba(b, a); if ((ab * ap) < 0) {
        return fabsl(ap.len());
    } else if ((ab * bp) > 0) {
        return fabsl(bp.len());
    } else {
         return fabsl((ba % ap) / ba.len());
bool point_on_line(const Point &p, const Point &a, const Point &b) {
    Vec ab(a, b), ap(b, p);
    return (ab % ap) == 0;
bool point_on_ray(const Point &p, const Point &a, const Point &b) {
    Vec ab(a, b), ap(a, p);
return ((ab % ap) == 0 && (ab * ap) > 0 || (a == p));
bool point_on_segment(const Point &p, const Point &a, const Point &b) {
    Vec ap(a, p), bp(b, p), ab(a, b);
return ((ap * bp) <= 0 && (ap % ab) == 0);
7
bool point_in_angle(const Point &p, const Point &a, const Point &o, const
Point &b) {
    Vec oa(o, a), ob(o, b), op(o, p);
    if ((oa % ob) < 0) swap(oa, ob);
    return ((oa % op) >= 0 && (ob % op) <= 0);
}
bool segment intersection(const Point &a. const Point &b. const Point &c.
      const Point &d) {
    Vec ab(a, b), cd(c, d), ac(a, c), ad(a, d), cb(c, b), ca(c, a);
    if (get_sign((ab % ac)) * get_sign((ab % ad)) <= 0 && get_sign((cd % ca )) * get_sign((cd % cb)) <= 0) {
        11 \times 1 = \max(\min(a.x, b.x), \min(c.x, d.x)), \times 2 = \min(\max(a.x, b.x),
      max(c.x, d.x));
        11 y1 = max(min(a.y, b.y), min(c.y, d.y)), y2 = min(max(a.y, b.y),
      max(c.y, d.y));
        return (x1 <= x2 && y1 <= y2);
    return false:
bool rays_intersection(const Point &a, const Point &b, const Point &c,
      const Point &d) {
    Vec ab(a, b), cd(c, d);
    11 k = 1e6;
    ab *= k:
    cd *= k;
    Point nb(ab.x + a.x, ab.y + a.y), nd(cd.x + c.x, cd.y + c.y);
    return segment_intersection(a, nb, c, nd);
```

```
bool lines_intersection(const Point &a, const Point &b, const Point &c,
      const Point &d) {
    Vec ab(a, b), cd(c, d);
return ((ab % cd) != 0);
int point_in_polygon(const Point &p, const Polygon &poly) {
     // 0 - outside, 1 - inside, 2 - border;
     int n = sz(poly);
     if (point_in_angle(p, poly[n - 1], poly[0], poly[1])) {
         int 1 = 1, r = n - 1;
         while (r - 1 > 1) {
              int md = (1 + r) / 2;
              if (point_in_angle(p, poly[md], poly[0], poly[1])) {
                  r = md;
              } else {
                  1 = md;
              }
         if (point_in_angle(p, poly[r], poly[0], poly[1]) &&
              point_in_angle(p, poly[0], poly[1], poly[r]) &&
point_in_angle(p, poly[1], poly[r], poly[0])) {
              if (point_on_segment(p, poly[1], poly[r]) ||
    point_on_segment(p, poly[(1 ? 1 - 1 : n - 1)], poly[1]) ||
                  point_on_segment(p, poly[r], poly[(r + 1 == n ? 0 : r + 1)
      1)) {
                  return 2;
              } else {
                  return 1:
         } else {
             return 0;
         1
     } else {
         return 0;
int point_in_nonconvex_polygon(const Point &p, const Polygon &poly) {
     // 0 - outside, 1 - inside, 2 - border;
int n = sz(poly);
     for (int i = 0; i < n; ++i) {
         if (point_on_segment(p, poly[i], poly[(i + 1) % n])) {
              return 2;
         }
    ld s = 0.0;
for (int i = 0; i < n; ++i) {</pre>
          Vec pa(p, poly[i]), pb(p, poly[(i + 1 == n ? 0 : i + 1)]);
         s += angle_rad(pa, pb);
     if (s \ge PI \mid \mid s \le -PI) {
         return 1;
     } else {
         return 0;
     }
}
Polygon minkowski_sum(Polygon &a, Polygon &b) {
     // a[0], b[0]: y - max, y1 = y2 => x - max. Against clockwise
     int n = sz(a), m = sz(b);
     assert(n >= 3 \&\& m >= 3);
     Point high_a = a[0], high_b = b[0];
     vPolygon va(n), vb(m);
     for (int i = 0; i < n; ++i) {
         va[i] = Vec(a[i], a[(i + 1) % n]);
     for (int i = 0; i < m; ++i) {
         vb[i] = Vec(b[i], b[(i + 1) % m]);
           sort(all(va), cmp_vectors);
sort(all(vb), cmp_vectors);
     vPolvgon vc:
     merge(all(va), all(vb), back_inserter(vc), cmp_vectors);
     Point high_c(high_a.x + high_b.x, high_a.y + high_b.y);
     Polygon c(sz(vc) + 1);
    c[0] = high_c;
for (int i = 0; i < sz(c) - 1; ++i) {
    c[i + 1] = Point(c[i].x + vc[i].x, c[i].y + vc[i].y);</pre>
     return c:
}
ld from_polygon_to_polygon(Polygon a, Polygon b) {
    for (auto &i : b) {
         i *= -1;
     for (int i = 1; i < sz(b); ++i) {
         if ((b[i].y > b[pos].y) ||
    (b[i].y == b[pos].y && b[i].x > b[pos].x)) {
              pos = i;
     rotate(b.begin(), b.begin() + pos, b.end());
```

```
Polygon c = minkowski_sum(a, b);
    int n = sz(c);
    Point p(0, 0);
    1d ans = 1e20;
    for (int i = 0; i < n - 1; ++i) {
        ans = min(ans, from_point_to_segment(p, c[i], c[i + 1]));
    return ans;
11 diameter_of_polygon_minkowski(Polygon &a) {
    Polygon ra = a;
    for (auto &i : ra) {
    }
    int pos = 0;
for (int i = 1; i < sz(a); ++i) {
        if ((a[i].y > a[pos].y) ||
             (a[i].y == a[pos].y && a[i].x > a[pos].x)) {
        }
    }
    rotate(a.begin(), a.begin() + pos, a.end());
    pos = 0;
    for (int i = 1; i < sz(a); ++i) {
        if ((ra[i].y > ra[pos].y) ||
(ra[i].y == ra[pos].y && ra[i].x > ra[pos].x)) {
        }
    rotate(ra.begin(), ra.begin() + pos, ra.end());
    Polygon c = minkowski_sum(a, ra);
    int n = sz(c);
    11 ans = 0;
    for (int i = 0; i < n; ++i) {
        ans = max(ans, Vec(c[i]).len_sq());
    // don't forget to extract root!
```