Содержание

	Оби	цее	1
Кодн		<mark>(ы</mark>	
	2.1	Basic setup	1
	2.2	Бесполезное	1
	2.3	Мосты	2
	2.4	Точки сочленения	2
	2.5	DCP (TheEvilBird)	2
	2.6	MaxFlow (TheEvilBird)	3
	2.7	MinCostMaxFlow (TheEvilBird)	3
	2.8	Кун	4
	2.9	HLD (TheEvilBird)	4
	2.10	Dominator tree (TheEvilBird)	5
	2.11	Link-Cut (TheEvilBird)	5
	2.12	Личао (FedShat)	6
		Segment Tree (TheEvilBird)	7
		Segment Tree Down (TheEvilBird)	7
	2.15	Segment Tree Beats (TheEvilBird)	8
	2.16	Persistent Segment Tree (Sweezyk)	9
	2.17	Fenwick (TheEvilBird)	9
	2.18	Sparse table (TheEvilBird)	9
		Treap (Sweezyk)	10
	2.20	Extended GCD (Sweezyk)	10
	2.21	FFT (FedShat)	11
	2.22	KTO (FedShat)	11
		Обратные по простому модулю	12
	2.24	Обратные факториалы	12
	2.25	Γayec	12
	2.26	Быстрая факторизация (FedShat)	12
	2.27	Префикс-функция	13
	2.28	Z-функция	13
	2.29	Суфмас (TheEvilBird)	13
		Суфавтомат (TheEvilBird)	13
	2.31	Axo-Корасик (Sweezyk)	14
	2.32	Манакер	14
		CHT (FedShat)	14
	2.34	Дебаг Туриста	15
	2.35	Геометрия (TheEvilBird)	15

- Число граней в планарном графе
(с учётом бесконечной): R=2-V+E
- Сумма арифметической прогрессии: $S_n = \frac{n(a_1 + a_n)}{2}$
- Сумма геометрической прогрессии: $S_n = \frac{b_1(q^n-1)}{q-1}$

2 Коды

2.1 Basic setup

```
#include <bits/stdc++.h>
using namespace std;
#define sz(x) (int) ((x).size())
\#define all(x) (x).begin(), (x).end()
#define rall(x) (x).rbegin(), (x).rend()
typedef long long 11;
typedef __int128 int128;
typedef pair<int, int> pii;
typedef pair<11, 11> pll;
const char en = '\n';
const int INF = 1e9 + 7;
const 11 INFLL = 1e18;
mt19937 rnd(chrono::high_resolution_clock::now().time_since_epoch().count()
template<class T>
istream &operator>>(istream &is, vector<T> &a) {
    for (auto &i : a) {
        is >> i;
    return is:
void solve() {
int32_t main() {
#ifdef LOCAL
    freopen("input.txt", "r", stdin);
    ios_base::sync_with_stdio(0);
    cin.tie(0);
#endif
    solve():
    return 0:
```

1 Общее

• Собственное вращение на угол φ с центром вращения в начале координат:

```
x' = x \cos \varphi - y \sin \varphiy' = x \sin \varphi + y \cos \varphi
```

- Расстояние между точками по сфере: $L = R \cdot \arccos(\cos\theta_1 \cdot \cos\theta_2 + \sin\theta_1 \cdot \sin\theta_2 \cdot \cos(\varphi_1 \varphi_2))$ где θ широты (от $-\pi$ до π), φ долготы (от $-\pi$ до π)
- Объем шарового сегмента: $V = \pi h^2 (R \frac{1}{3}h)$, где h высота от вершины сектора до секущей плоскости
- Площадь поверхности шарового сегмента: $S=2\pi Rh,$ где h высота
- Код Грея: $g_n = n \oplus \frac{n}{2}$
- Числа Фибоначчи: $F_0=0, F_1=1, F_n=rac{(rac{1+\sqrt{5}}{2})^n-(rac{1-\sqrt{5}}{2})^n}{\sqrt{5}}$
- Sum-xor property: $a+b=a\oplus b+2(a\&b), a+b=a|b+a\&b, a\oplus b=a|b-a\&b$

2.2 Бесполезное

Санитайзеры:

Прагмы:

```
#pragma GCC optimize("Ofast,no-stack-protector")
#pragma GCC target("sse,sse2,sse3,ssse3,sse4)
#pragma GCC target("popcnt,abm,mmx,avx,avx2,tune=native")
#pragma GCC optimize("unroll-loops")
#pragma GCC optimize("fast-math")
#pragma GCC optimize("section-anchors")
#pragma GCC optimize("profile-values")
#pragma GCC optimize("profile-reorder-functions")
#pragma GCC optimize("tracer")
#pragma GCC optimize("vpt")
#pragma GCC optimize("rename-registers")
#pragma GCC optimize("move-loop-invariants")
#pragma GCC optimize("unswitch-loops")
#pragma GCC optimize("function-sections")
#pragma GCC optimize("data-sections")
#pragma GCC optimize("branch-target-load-optimize")
#pragma GCC optimize("branch-target-load-optimize2")
#pragma GCC optimize("btr-bb-exclusive")
```

Встроенный декартач:

Atomic hashset, hashmap:

Перебор всех подмасок и надмасок:

```
for (int submask = mask;; submask = (submask - 1) & mask) {
    // use submask
    if (submask == 0) break;
}
for (int upmask = mask;; upmask = (upmask + 1) | mask) {
    // use upmask
    if (upmask == maxmask) break;
}
```

2.3 Мосты

2.4 Точки сочленения

```
void dfs(int v, int p = -1) {
    used[v] = true;
    tin[v] = fup[v] = timer++;
    int children = 0;
    for (auto to : g[v]) {
        if (to == p) {
             continue;
        if (used[to]) {
            fup[v] = min(fup[v], tin[to]);
        } else {
            dfs(to, v);
fup[v] = min(fup[v], fup[to]);
             if (fup[to] >= tin[v] && p != -1) {
                IS_CUTPOINT(v);
             ++children;
    if (p == -1 &\& children > 1) {
         IS_CUTPOINT(v);
    }
}
```

2.5 DCP (TheEvilBird)

```
struct Query {
    char type;
    int v. u:
    Query(char type) : type(type) {}
    Query(char type, int v, int u) : type(type), v(v), u(u) {}
struct DCP {
    int n, k, ans; // n - vertex, k - queries
    vector<int> par, rk;
    vector<pair<pii, int>> hist;
    // 0 - par, 1 - rk, 2 - ans;
    int qL, qR;
    pii edge;
    vector<vector<pii>>> tree;
    vector<Query> qs;
    DCP(int _n, int _k) {
         n = ans = _n;
par.resize(n);
         rk.resize(n, 1);
         for (int i = 0; i < n; ++i) par[i] = i;
         tree.assign(4 * k, vector<pii>());
    int dsu_get(int v) {
         while (par[v] != v) v = par[v];
         return v;
    void dsu_unite(int a, int b) {
         a = dsu_get(a);
         b = dsu_get(b);
         if (a == b) return;
         if (x=0) results,
if (rk[a] > rk[b]) swap(a, b);
hist.emplace_back((pii){0, a}, par[a]);
hist.emplace_back((pii){2, -1}, ans);
par[a] = b;
          -ans;
         if (rk[a] == rk[b]) {
             hist.emplace_back((pii){1, b}, rk[b]);
             ++rk[b];
         }
    }
    void dsu_unite(pii e) {
         dsu_unite(e.first, e.second);
    void cancel(pair<pii, int> &el) {
         int &type = el.first.first;
         int &id = el.first.second;
         int &val = el.second;
if (type == 0) {
             par[id] = val;
         } else if (type == 1) {
             rk[id] = val;
         } else if (type == 2) {
             ans = val;
         }
    }
    void add_edge(int _qL, int _qR, pii e) {// [L, R]
         qL = _qL;
         qR = _qR + 1;
edge = e;
         add_edge_tree(1, 0, k);
    void add_edge_tree(int v, int 1, int r) {
         if (qL \le 1 \&\& r \le qR) {
             tree[v].emplace_back(edge);
             return;
         int m = (1 + r) / 2, vL = 2 * v, vR = vL + 1;
         if (qL < m) add_edge_tree(vL, 1, m);</pre>
         if (m < qR) add_edge_tree(vR, m, r);</pre>
    void go(vector<Query> &_qs) {
         qs = _qs;
go_tree(1, 0, k);
    void go_tree(int v, int 1, int r) {
         int siz = sz(hist);
for (auto &e : tree[v]) {
             dsu_unite(e);
```

```
if (1 + 1 == r) {
             if (qs[1].type == '?') {
                 cout << ans << en;
             }
        } else {
             int m = (1 + r) / 2, vL = 2 * v, vR = vL + 1;
             go_tree(vL, 1, m);
             go_tree(vR, m, r);
        while (sz(hist) > siz) {
             cancel(hist.back());
             hist.pop_back();
    }
1:
void solve() {
    int n, k;
    cin >> n >> k;
    DCP dcp(n, k);
    set<pair<pii, int>> edges;
    vector<Query> qs;
    for (int i = 0; i < k; ++i) {
        char tp;
        cin >> tp;
if (tp == '?') {
             qs.emplace_back(tp);
        } else {
             int v. u:
             cin >> v >> u;
             --v :
             if (v > u) swap(v, u);
             qs.emplace_back(tp, v, u);
if (tp == '+') {
                 edges.emplace((pii){v, u}, i);
             } else {
                 auto it = edges.lower_bound({(pii){v, u}, 0});
                 dcp.add_edge(it->second, i, it->first);
                 edges.erase(it);
        }
    for (auto &e : edges) {
        dcp.add_edge(e.second, k - 1, e.first);
    if (k) dcp.go(qs);
```

2.6 MaxFlow (TheEvilBird)

```
struct MaxFlow {
     struct Edge {
          11 flow, cap;
          int to, id;
          Edge() {}
          Edge(ll flow, ll cap, int to, int id) : flow(flow), cap(cap), to(to
      ), id(id) {}
    int n;
     vector<vector<Edge>> g;
     vector<int> d, head, used;
     11 max_cap;
     MaxFlow() {}
     MaxFlow(int _n) {
          n = _n;
          g.resize(n);
    }
     void add_edge(int from, int to, ll cap) {
   g[from].emplace_back(0, cap, to, sz(g[to]));
   g[to].emplace_back(0, 0, from, sz(g[from]) - 1);
     bool bfs() {
          d.assign(n, INF);
          d[s] = 0;
          queue<int> q;
          q.push(s);
          while (!q.empty()) {
   int v = q.front();
                q.pop();
               for (auto e : g[v]) {
   if (d[e.to] == INF && e.cap - e.flow >= max_cap) {
      d[e.to] = d[v] + 1;
```

```
q.push(e.to);
            }
        }
        return d[t] != INF:
    11 dfs(int v, 11 cur_flow) {
        if (v == t) {
            return cur_flow;
         for (; head[v] < sz(g[v]); ++head[v]) {</pre>
             auto &e = g[v][head[v]];
             if (e.cap - e.flow >= max_cap && d[v] + 1 == d[e.to]) {
                 11 new_flow = dfs(e.to, min(cur_flow, e.cap - e.flow));
                 if (new_flow) {
                      e.flow += new_flow;
                      g[e.to][e.id].flow -= new_flow;
                      return new_flow;
            }
         return 0:
    }
    11 find_max_flow(int _s, int _t) {
        s = _s;
t = _t;
        11 res = 0;
for (int k = 30; k >= 0; --k) {
            max_cap = (1 << k);
             while (bfs()) {
                 head.assign(n, 0);
                 11 \text{ flow} = 0;
                 do {
                      flow = dfs(s, INFLL);
                      res += flow;
                 } while (flow);
         return res:
    11 dfs_const_flow(int v, 11 cur_flow) {
         used[v] = 1;
         if (v == t) {
             return cur_flow;
         for (auto &e : g[v]) {
            if (!used[e.to] && e.cap - e.flow > 0) {
                 11 new_flow = dfs_const_flow(e.to, min(cur_flow, e.cap - e.
      flow));
                 if (new_flow) {
                      e.flow += new_flow;
                      g[e.to][e.id].flow -= new_flow;
                      return new_flow;
            }
         return 0:
    }
    bool find_const_flow(int _s, int _t, 11 F) {
        s = _s;
t = _t;
        11 \text{ res} = 0, \text{ flow} = 0;
         \max_{z} = F;
             used.assign(n, 0);
             flow = dfs_const_flow(s, INF);
             res += flow;
        } while (flow && res < F);
return res == F;</pre>
    }
    11 get_edge_flow(int v, int id) {
        return g[v][id].flow;
};
```

2.7 MinCostMaxFlow (TheEvilBird)

```
struct MinCostMaxFlow {
    struct Edge {
        ll flow, cap, price;
        int to, id;

        Edge() {}

        Edge() {}

        Edge(ll flow, ll cap, ll price, int to, int id) : flow(flow), cap( cap), price(price), to(to), id(id) {}
    };
```

```
int n;
      int s, t;
      11 ans:
      vector<vector<Edge>> g;
      vector<int> d;
      vector<11> add_f;
      vector<pii> par;
      MinCostMaxFlow() {}
      MinCostMaxFlow(int _n) {
           n = _n;
           g.resize(n);
      void add_edge(int from, int to, ll cap, ll price) {
   g[from].emplace_back(0, cap, price, to, sz(g[to]));
   g[to].emplace_back(0, 0, -price, from, sz(g[from]) - 1);
      11 get_edge_flow(int v, int id) {
           return g[v][id].flow;
      }
      void FB() {
           d.assign(n, INF);
           add_f.assign(n, 0);
           par.assign(n, {-1, -1});
d[s] = 0;
           add_f[0] = INF;
           queue<int> q;
           q.push(s);
           vector<int> used(n, 0);
           used[s] = 1;
           while (!q.empty()) {
   int v = q.front();
                 q.pop();
                 used[v] = 0;
                 for (int i = 0; i < sz(g[v]); ++i) {
                      (int i = 0; i < sz(g(y)); ++i) {
  auto &e = g[v][i];
  if (e.flow < e.cap && d[e.to] > d[v] + e.price) {
    d[e.to] = d[v] + e.price;
    add_f[e.to] = min(add_f[v], e.cap - e.flow);
    par[e.to] = {v, i};
    if (!used[e.to]) {
                                  q.push(e.to);
                                  used[e.to] = 1;
                      }
              }
          }
     }
      void push_flow(ll flow) {
           int cur = t;
           while (cur != s) {
                 int prev = par[cur].first, id = par[cur].second;
                 g[prev][id].flow += flow;
g[cur][g[prev][id].id].flow -= flow;
                 ans += g[prev][id].price * flow;
                 cur = prev;
      11 min_cost_max_flow(int _s, int _t) {
           ans = 0;
s = _s;
           t = _t;
           while (true) {
                 FB();
                 11 flow = add_f[t];
if (flow == 0) {
                      break:
                push_flow(flow);
           return ans;
     }
};
```

2.8 Kyh

```
bool dfs(int v) {
    if (used[v])
        return false;
    used[v] = true;
    for (auto u : g[v]) {
        if (back[u] == -1 || dfs(back[u])) {
            back[u] = v;
            return true;
        }
    }
}
```

```
return false;
}
```

2.9 HLD (TheEvilBird)

```
struct HLD {
     // insert SegTree code
    struct SegTree {};
    int n, T;
    SegTree st;
    vector<vector<int>> tree;
    vector<int> par, siz, tin, tout, head;
    HLD(int n) {
        n = _n;
        tree.resize(n);
        par.resize(n, -1);
         siz.resize(n, 0);
        tin.resize(n);
        tout.resize(n):
        head.resize(n);
        st = SegTree(n);
    }
    void add_edge(int v, int u) {
        tree[v].emplace_back(u);
tree[u].emplace_back(v);
    void build(int v = 0) {
        dfs_siz(v, v);
        T = 0:
        head[v] = v;
        dfs_hld(v, v);
    void dfs_siz(int v, int p) {
        par[v] = p;
siz[v] = 1;
        for (auto &u : tree[v]) {
            if (u != p) {
                 dfs_siz(u, v);
                 siz[v] += siz[u];
        for (int i = 0; i < sz(tree[v]); ++i) {</pre>
             int x = tree[v][0], u = tree[v][i];
             if (x == p \mid \mid siz[u] > siz[x]) {
                 swap(tree[v][0], tree[v][i]);
        }
    }
    void dfs_hld(int v, int p) {
        tin[v] = T++;
        for (auto u : tree[v]) {
            if (u == p) {
                 continue:
             if (u == tree[v][0]) {
                 head[u] = head[v];
             } else {
                 head[u] = u;
             dfs_hld(u, v);
        tout[v] = T;
    }
    void update(int v, int val) {
        st.update_segment(tin[v], tin[v], val);
    bool is_anc(int v, int u) {
    return tin[v] <= tin[u] && tout[u] <= tout[v];</pre>
    void go_up(int &v, int u) {
        while (!is_anc(head[v], u)) {
             ans = max(ans, st.get(tin[head[v]], tin[v]));
             v = par[head[v]];
        }
    }
    11 get(int v, int u) \{// \text{ max on path }
        ans = -INFLL;
        go_up(v, u);
         go_up(u, v);
        if (!is_anc(v, u)) {
             swap(v, u);
```

```
}
ans = max(ans, st.get(tin[v], tin[u]));
return ans;
}
};
```

2.10 Dominator tree (TheEvilBird)

```
struct Edge {
    int from, to, id;
    Edge() = default;
    Edge(int from, int to, int id) : from(from), to(to), id(id) {}
struct DSU {
    int n:
    vector<int> par;
    vector<pii> mn;
    DSU() = default;
    DSU(int n) : n(n) {
        par.resize(n);
        mn.resize(n);
        init();
    }
    void init() {
        for (int i = 0; i < n; ++i) {
             par[i] = i;
             mn[i] = {INF, i};
    }
    int get(int v) {
   if (par[v] == v) {
            return v;
        int p = get(par[v]);
  mm[v] = min(mn[v], mn[par[v]]);
if (mn[par[v]].first < mn[v].first) {</pre>
            mn[v] = mn[par[v]];
        par[v] = p;
        return p;
    }
    void unite(int a, int b) {
        par[a] = b;
};
struct DominatorTree {
    int n:
    vector<Edge> edges;
    vector<int> sdom, idom, tin, order, par, used, dp;
     vector<vector<int>> g, rg, queries;
    DSU dsu_sdom, dsu_idom;
    DominatorTree() = default;
    DominatorTree(int n) : n(n), dsu_sdom(n), dsu_idom(n) {
         sdom.resize(n, INF); // semi-dominator
         idom.resize(n, INF); // immediate dominator
        tin.resize(n, -1);
        par.resize(n);
        used.resize(n, 0);
        dp.resize(n. INF):
         g.resize(n);
         rg.resize(n);
         queries.resize(n);
    }
    void add_edge(int from, int to) {
        edges.emplace_back(from, to, sz(edges));
    void dfs(int v) {
        tin[v] = sz(order);
         order.emplace_back(v);
        for (auto i: g[v]) {
    const auto &e = edges[i];
             if (tin[e.to] == -1) {
                 par[e.to] = v;
                 dfs(e.to);
            }
        }
    void dfs_idom(int v) {
         used[v] = 1;
        for (auto i: g[v]) {
             const auto &e = edges[i];
             if (!used[e.to]) {
```

```
dfs idom(e.to):
         }
     for (auto u: queries[v]) {
         dsu_idom.get(u);
dp[u] = dsu_idom.mn[u].second;
     dsu_idom.mn[v] = {sdom[v], v};
     for (auto i: g[v]) {
         const auto &e = edges[i];
if (par[e.to] == v) {
              dsu_idom.unite(e.to, v);
}
void build(int s) {
    for (int i = 0; i < sz(edges); ++i) {
    g[edges[i].from].emplace_back(i);</pre>
         rg[edges[i].to].emplace_back(i);
     // reorder vertex
     dfs(s):
    for (int _ = sz(order) - 1; _ >= 0; --_) {
    int v = order[_];
         if (v == s) {
              continue;
         for (auto i: rg[v]) {
              const auto &e = edges[i];
              if (tin[e.from] == -1) {
                   continue;
              if (tin[e.from] < tin[v]) {</pre>
                   sdom[v] = min(sdom[v], tin[e.from]);
                   int u = dsu_sdom.get(e.from);
                   sdom[v] = min(sdom[v], dsu_sdom.mn[e.from].first);
         dsu_sdom.mn[v] = {sdom[v], v};
         for (auto i: g[v]) {
              const auto &e = edges[i];
              if (v == par[e.to]) {
                   dsu_sdom.unite(e.to, v);
    // build queries for idoms
for (int i = 0; i < n; ++i) {
   if (i == s || sdom[i] == INF || tin[i] == -1) {</pre>
              continue;
         queries[order[sdom[i]]].emplace_back(i);
     dfs_idom(s);
     // build idom
     idom[s] = tin[s];
     for (auto v: order) {
         if (v == s) {
              continue;
         if (v == dp[v]) {
              idom[v] = sdom[v];
         else {
              idom[v] = idom[dp[v]];
    }
int get_idom(int v) {
     return (idom[v] == INF ? -1 : order[idom[v]]);
```

2.11 Link-Cut (TheEvilBird)

};

```
struct Node {
  Node *ch[2] = {nullptr, nullptr};
  Node *par = nullptr;
  bool rev = false;
  int val, mm;
  int siz = 1;
  Node() {}
  Node(int val) : val(val), mn(val) {}
```

```
typedef Node *pnode;
int get_siz(pnode v) {
     return (v == nullptr ? 0 : v->siz);
int get_min(pnode v) {
     return (v == nullptr ? INF : v->mn);
void update(pnode v) {
     v->siz = 1 + get_siz(v->ch[0]) + get_siz(v->ch[1]);
     v->mn = min(v->val, min(get_min(v->ch[0]), get_min(v->ch[1])));
void push(pnode v) {
     if (v == nullptr || !v->rev) {
    if (v->ch[0] != nullptr) {
    v->ch[0]->rev ^= 1;
     if (v->ch[1] != nullptr) {
         v->ch[1]->rev ^= 1;
     swap(v->ch[0], v->ch[1]);
     v \rightarrow rev = 0;
bool is_root(pnode v) {
   return (v->par == nullptr ||
              (v->par->ch[0] != v && v->par->ch[1] != v));
int child_num(pnode v) {
     return (v->par->ch[1] == v);
void attach(pnode v, pnode p, int num) {
   if (v != nullptr) {
         v \rightarrow par = p;
     if (p != nullptr) {
         p \rightarrow ch[num] = v;
}
void rotate(pnode v) {
     int num = child_num(v);
     pnode p = v->par, vb = v->ch[num ^ 1];
pnode g = (p == nullptr ? nullptr : p->par);
if (g != nullptr) {
         if (!is_root(p)) {
    g->ch[child_num(p)] = v;
     v->par = g;
    attach(p, v, num ^ 1);
attach(vb, p, num);
     update(p);
     update(v);
void splay(pnode v) {
     vector<pnode> st;
pnode cur = v;
     st.emplace_back(cur);
     while (!is_root(cur)) {
         cur = cur->par;
         st.emplace_back(cur);
     for (int i = sz(st) - 1; i \ge 0; --i) {
         push(st[i]);
     while (!is_root(v)) {
         if (!is_root(v->par)) {
              if (child_num(v) == child_num(v->par)) {
                  rotate(v->par);
              } else {
                  rotate(v);
             }
         }
         rotate(v);
    }
void expose(pnode v) {
     splay(v);
     v->ch[1] = nullptr;
     update(v):
     while (v->par != nullptr) {
         splay(v->par);
         attach(v, v->par, 1);
```

update(v->par);

```
splay(v);
    }
}
void make_root(pnode v) {
    expose(v);
    v->rev ^= 1;
void link(pnode v, pnode u) {
   make_root(v);
    make_root(u);
    u \rightarrow par = v;
void cut(pnode v, pnode u) {
    make_root(v);
    make_root(u);
    push(u);
    u->ch[1] = nullptr;
    v->par = nullptr;
bool is_connected(pnode v, pnode u) {
    make_root(v);
    make_root(u);
    if (is_root(v) && u != v) {
        return false;
    } else {
        return true:
int get_min(pnode v, pnode u) {
    make_root(v);
    make root(u):
    return get_min(u);
```

2.12 Личао (FedShat)

```
struct LiChao {// max
    struct Line {
        11 k = 0, b = -INFLL;
        Line() = default;
        Line(11 k, 11 b) : k(k), b(b){}:
        11 operator()(11 x) {
            return k * x + b;
    };
    struct Node {
        Node *1 = nullptr, *r = nullptr;
        Node() = default;
    Node *root = nullptr;
    int n = 1e9 + 1;
    void make_node(Node *&v) {
        if (v == nullptr) {
            v = new Node();
    void add(Node *&v, int 1, int r, Line cur) {
        make_node(v);
int m = (1 + r) / 2;
if (cur(m) > v->cur(m)) {
            swap(cur, v->cur);
        if (1 + 1 == r) {
            return;
        if (cur(1) > v->cur(1)) {
             add(v->1, 1, m, cur);
        } else {
            add(v->r, m, r, cur);
    }
    void add(Line cur) {
        add(root, 0, n, cur);
    11 get(Node *v, int 1, int r, int x) {
        if (v == nullptr) {
            return -INFLL;
```

```
}
    11 ans = v->cur(x);
    if (1 + 1 == r) {
        return ans;
    }
    int m = (1 + r) / 2;
    if (x < m) {
        ans = max(ans, get(v->1, 1, m, x));
    } else {
        ans = max(ans, get(v->r, m, r, x));
    }
    return ans;
}

11 get(int x) {
    return get(root, 0, n, x);
}
```

2.13 Segment Tree (TheEvilBird)

```
struct SegTree {
    static const 11 off = 0;
    struct Node {
         11 val = 0;
         11 push = off;
         Node() {}
         Node(l1 val) : val(val) {}
         Node operator+(const Node &other) const {
             return Node(val + other.val);
         void operator+=(const Node &other) {
             val += other.val;
         void use push(int len = 1) {
             val += push * (11) (1en);
         void update_push(11 pushed) {
            push += pushed;
    int n, qL, qR;
    ll val;
    Node ans:
    vector<Node> tree;
    vector<ll> a;
    SegTree() {}
    SegTree(int _n) {
         n = _n;
         tree.assign(4 * n, 0);
    void update_vertex(int v, int 1, int r) {// [1, r)
   int m = (1 + r) / 2, vL = 2 * v, vR = vL + 1;
         push(vL, 1, m);
         push(vR, m, r);
         tree[v] = tree[vL] + tree[vR];
    void push(int v, int 1, int r) {// [l, r)
   if (tree[v].push == off) return;
         int m = (1 + r) / 2, vL = 2 * v, vR = vL + 1;
         tree[v].use_push(r - 1);
if (1 + 1 != r) {
             tree[vL].update_push(tree[v].push);
             tree[vR].update_push(tree[v].push);
         tree[v].push = off;
    void build(vector<11> &_a) {
         build_tree(1, 0, n);
    void build_tree(int v, int 1, int r) \{// [l, r)
        if (1 + 1 == r) {
    tree[v] = Node(a[1]);
             return;
```

```
int m = (1 + r) / 2, vL = 2 * v, vR = vL + 1;
          build_tree(vL, 1, m);
          build_tree(vR, m, r);
          update_vertex(v, 1, r);
     }
     void update_segment(int _qL, int _qR, 11 _val) {// [_qL, _qR]
          qL = _qL;
qR = _qR + 1;
val = _val;
          update_segment_tree(1, 0, n);
     void update_segment_tree(int v, int 1, int r) \{// [l, r]
          push(v, 1, r);
if (qL <= 1 && r <= qR) {</pre>
               tree[v].update_push(val);
               push(v, 1, r);
               return;
          int m = (1 + r) / 2, vL = 2 * v, vR = vL + 1;
          if (qL < m) update_segment_tree(vL, 1, m);
if (m < qR) update_segment_tree(vR, m, r);</pre>
          update_vertex(v, 1, r);
     11 get(int _qL, int _qR) {// [_qL, _qR]
          qL = _qL;
qR = _qR + 1;
ans = Node();
          get_tree(1, 0, n);
          return ans.val;
     void get_tree(int v, int 1, int r) \{// [l, r)
          push(v, 1, r);
if (qL <= 1 && r <= qR) {</pre>
               ans = ans + tree[v];
          int m = (1 + r) / 2, vL = 2 * v, vR = vL + 1;
if (qL < m) get_tree(vL, 1, m);</pre>
          if (m < qR) get_tree(vR, m, r);</pre>
};
```

2.14 Segment Tree Down (TheEvilBird)

```
struct SegTreeDown {
    struct Node {
        11 val = 0;
        Node() {}
        Node(11 val) : val(val) {}
        Node operator+(const Node &other) const {
             return Node(val + other.val);
        void operator+=(const Node &other) {
            val += other.val;
    };
    int n:
    vector<Node> tree:
    SegTreeDown(int _n) {
        tree.assign(2 * n, Node());
    void build(vector<11> &a) {
        for (int i = 0; i < n; ++i) {
            tree[i + n] = Node(a[i]);
        for (int i = n - 1; i >= 1; --i) {
    tree[i] = tree[2 * i] + tree[2 * i + 1];
    void update(int i, ll val) {
        i += n;
tree[i] = val;
        i /= 2;
        while (i != 0) {
            tree[i] = tree[2 * i] + tree[2 * i + 1];
             i /= 2;
    }
    11 get(int 1, int r) {// [l, r)
```

```
--r;

1 += n;

r += n;

Node ans;

while (1 <= r) {

    if (1 % 2 == 1) {

        ans += tree[1];

        ++1;

    }

    if (r % 2 == 0) {

        ans += tree[r];

        --r;

    }

    1 /= 2;

    r /= 2;

}

return ans.val;

}
```

2.15 Segment Tree Beats (The Evil Bird)

```
struct SegTree {
    struct Node {
        11 max, sec_max;
        int cnt_max;
        11 min, sec_min;
        int cnt_min;
        11 sum:
        11 push_add;
        ll push_eq;
    int n, qL, qR;
    ll val, ans;
    vector<Node> tree;
    vector<11> a;
    SegTree(int _n) {
        tree.assign(4 * n, {0, -INFLL, 1, 0, INFLL, 1, 0, 0, -1});
    void update_vertex(int v, int 1, int r) {
   int m = (1 + r) / 2, vL = 2 * v, vR = vL + 1;
        tree[v].sum = tree[vL].sum + tree[vR].sum;
        tree[v].max = max(tree[vL].max, tree[vR].max);
        tree[v].sec_max = max(tree[vL].sec_max, tree[vR].sec_max);
        tree[v].cnt_max = 0;
        if (tree[vL].max == tree[v].max) {
            tree[v].cnt_max += tree[vL].cnt_max;
        } else {
            tree[v].sec_max = max(tree[v].sec_max, tree[vL].max);
        if (tree[vR].max == tree[v].max) {
            tree[v].cnt_max += tree[vR].cnt_max;
        } else {
            tree[v].sec_max = max(tree[v].sec_max, tree[vR].max);
        tree[v].min = min(tree[vL].min, tree[vR].min);
        tree[v].sec_min = min(tree[vL].sec_min, tree[vR].sec_min);
        tree[v].cnt_min = 0;
        if (tree[vL].min == tree[v].min) {
            tree[v].cnt_min += tree[vL].cnt_min;
            tree[v].sec_min = min(tree[v].sec_min, tree[vL].min);
        if (tree[vR].min == tree[v].min) {
            tree[v].cnt_min += tree[vR].cnt_min;
          else {
            tree[v].sec_min = min(tree[v].sec_min, tree[vR].min);
    void recalc_eq(int v, int 1, int r, 11 cur) {
   tree[v].max = tree[v].min = tree[v].push_eq = cur;
        tree[v].sec_max = -INFLL;
        tree[v].sec_min = INFLL;
        tree[v].cnt_max = tree[v].cnt_min = r - 1;
tree[v].sum = cur * (11) (r - 1);
        tree[v].push_add = 0;
    void recalc_add(int v, int 1, int r, 11 cur) {
        if (tree[v].min == tree[v].max) {
            recalc_eq(v, 1, r, tree[v].max + cur);
            return:
        tree[v].max += cur;
```

```
if (tree[v].sec_max != -INFLL) {
         tree[v].sec_max += cur;
    tree[v].min += cur;
    if (tree[v].sec_min != INFLL) {
         tree[v].sec_min += cur;
    tree[v].sum += (11) (r - 1) * cur;
tree[v].push_add += cur;
void recalc_min(int v, int 1, int r, 11 cur) {
    if (tree[v].min >= cur) {
        recalc_eq(v, 1, r, cur);
        return:
    if (tree[v].max <= cur) return;</pre>
    if (tree[v].sec_min == tree[v].max) {
         tree[v].sec_min = cur;
    tree[v].sum -= (11) (tree[v].max - cur) *
                    (11) (tree[v].cnt_max);
    tree[v].max = cur;
void recalc_max(int v, int 1, int r, 11 cur) {
    if (tree[v].max <= cur) {</pre>
        recalc_eq(v, 1, r, cur);
        return;
    if (tree[v].min >= cur) return;
    if (tree[v].sec_max == tree[v].min) {
         tree[v].sec_max = cur;
    tree[v].sum += (11) (tree[v].max - cur) *
                    (11) (tree[v].cnt_max);
    tree[v].min = cur;
}
void push(int v, int 1, int r) {
    if (1 + 1 == r) return;
int m = (1 + r) / 2, vL = 2 * v, vR = vL + 1;
    if (tree[v].push_eq != -1) {
        recalc_eq(vL, 1, m, tree[v].push_eq);
         recalc_eq(vR, m, r, tree[v].push_eq);
         tree[v].push_eq = -1;
        return:
    recalc_add(vL, 1, m, tree[v].push_add);
    recalc_add(vR, m, r, tree[v].push_add);
tree[v].push_add = 0;
    recalc_min(vL, 1, m, tree[v].max);
    recalc_min(vR, m, r, tree[v].max);
    recalc_max(vL, 1, m, tree[v].min);
    recalc_max(vR, m, r, tree[v].min);
void build(vector<11> &_a) {
    build_tree(1, 0, n);
void build_tree(int v, int 1, int r) {
    if (1 + 1 == r) {
        tree[v] = {a[1], -INFLL, 1, a[1],
                    INFLL, 1, a[1], 0, -1};
        return;
    int m = (1 + r) / 2, vL = 2 * v, vR = vL + 1;
    build_tree(vL, 1, m);
    build_tree(vR, m, r);
    update_vertex(v, 1, r);
void update_segment_min(int _qL, int _qR, ll _val) {
    qL = _qL;
qR = _qR + 1;
val = _val;
    update_segment_min_tree(1, 0, n);
void update_segment_min_tree(int v, int 1, int r) {
    if (tree[v].max <= val) return;</pre>
    if (qL <= 1 && r <= qR && tree[v].sec_max < val) {</pre>
         recalc_min(v, 1, r, val);
        return;
    push(v, 1, r);
int m = (1 + r) / 2, vL = 2 * v, vR = vL + 1;
    if (qL < m) update_segment_min_tree(vL, 1, m);</pre>
    if (m < qR) update_segment_min_tree(vR, m, r);</pre>
```

```
update_vertex(v, 1, r);
}
void update_segment_max(int _qL, int _qR, 11 _val) {
    qL = _qL;
qR = _qR + 1;
val = _val;
    update_segment_max_tree(1, 0, n);
void update_segment_max_tree(int v, int 1, int r) {
    if (tree[v].min >= val) return;
    if (qL <= 1 && r <= qR && tree[v].sec_min > val) {
         recalc_max(v, 1, r, val);
         return;
    push(v, 1, r);
int m = (1 + r) / 2, vL = 2 * v, vR = vL + 1;
    if (qL < m) update_segment_max_tree(vL, 1, m);</pre>
    if (m < qR) update_segment_max_tree(vR, m, r);</pre>
    update_vertex(v, 1, r);
void update_segment_add(int _qL, int _qR, 11 _val) {
    qL = _qL;

qR = _qR + 1;
     val = _val;
    update_segment_add_tree(1, 0, n);
void update_segment_add_tree(int v, int 1, int r) {
    if (qL <= 1 && r <= qR) {
         recalc_add(v, 1, r, val);
         return;
    push(v, 1, r);
int m = (1 + r) / 2, vL = 2 * v, vR = vL + 1;
    if (qL < m) update_segment_add_tree(vL, 1, m);</pre>
    if (m < qR) update_segment_add_tree(vR, m, r);</pre>
    update_vertex(v, 1, r);
11 get(int _qL, int _qR) {
    qL = _qL;
qR = _qR + 1;
     ans = 0;
    get_tree(1, 0, n);
    return ans;
void get_tree(int v, int 1, int r) {
   if (qL <= 1 && r <= qR) {
      ans += tree[v].sum;
}</pre>
         return:
     int m = (1 + r) / 2, vL = 2 * v, vR = vL + 1;
    if (qL < m) get_tree(vL, 1, m);
if (m < qR) get_tree(vR, m, r);</pre>
void print_all() {
    print_all_tree(1, 0, n);
void print_all_tree(int v, int 1, int r) {
    if (1 + 1 == r) {
         cout << tree[v].sum << en;</pre>
         return;
    push(v, 1, r);
int m = (1 + r) / 2, vL = 2 * v, vR = vL + 1;
    print_all_tree(vL, 1, m);
    print_all_tree(vR, m, r);
```

2.16 Persistent Segment Tree (Sweezyk)

```
struct Node {
    Node *1, *r;
    int mx;
    Node() {
        mx = -1;
        1 = r = nullptr;
    }
};
const int N = 1e7 + 4e6;
const int LG = 20;
Node *nodes[N];
int ptr;
```

```
Node *new_node() {
    return nodes[ptr++];
}
Node *get_left(Node *t) {
    if (t && t->1) return t->1;
    return nullptr;
}
Node *get_right(Node *t) {
    if (t && t->r) return t->r;
    return nullptr;
int get_max(Node *t) {
    if (!t) return 0;
    return t->mx;
void update(int i, int val, Node *t, Node *old_t, int lx, int rx) {
    if (lx + 1 == rx) {
    t->mx = max(t->mx, val);
        return;
    int m = (lx + rx) / 2;
    if (i < m) {
        t->1 = new_Node();
        if (old_t && old_t->1) {
            t - > 1 - > mx = old t - > 1 - > mx:
        t->r = get_right(old_t);
        update(i, val, t->1, get_left(old_t), lx, m);
    } else {
        t->r = new_Node();
        if (old_t && old_t->r) {
            t->r->mx = old_t->r->mx;
        t->l = get_left(old_t);
        update(i, val, t->r, get_right(old_t), m, rx);
    t->mx = max(get_max(get_left(t)), get_max(get_right(t)));
};
int get(int 1, int r, Node *t, int lx, int rx) {
    if (!t || lx >= r || rx <= 1) return -1;
    if (1x >= 1 \&\& rx <= r) return t->mx;
    int m = (lx + rx) / 2;
    return max(get(1, r, t->1, lx, m), get(1, r, t->r, m, rx));
```

2.17 Fenwick (TheEvilBird)

```
struct Fenwick {
    int n:
    vector<11> f;
    Fenwick(int _n) {
        f.assign(n + 1, 0);
    void update(int x, ll delta) {
        for (int i = x; i <= n; i += i & -i) {
           f[i] += delta;
    }
    11 get_sum(int x) {
        11 s = 0;
        for (int i = x; i > 0; i -= i & -i) {
            s += f[i];
        return s:
    11 get(int L, int R) {// [L, R]
        return get_sum(R) - get_sum(L - 1);
};
```

2.18 Sparse table (TheEvilBird)

```
struct Sparse {
  int n;
  vector<int> lg;
  vector<vector<ll>> table;
  Sparse(int _n) {
```

2.19 Treap (Sweezyk)

struct Node {

```
int x, y, size, push, cnt;
Node *1, *r;
    Node(int val) : x(val), y(rng()), size(1), push(0), cnt(0), 1(nullptr),
};
void push(Node *t) {
    if (t == nullptr) return;
    int p = t->push;
    if (p == 0) return;
    if (t->1 != nullptr) {
        t->1->cnt += p;
        t->1->push += p;
    if (t->r != nullptr) {
        t->r->cnt += p;
        t->r->push += p;
    t->push = 0;
}
int size(Node *t) {
    return (t ? t->size : 0);
}
void update(Node *t) {
    if (t == nullptr) return;
    t->size = size(t->1) + size(t->r) + 1;
pair<Node *, Node *> split(Node *t, int k) {
    if (t == nullptr) return {nullptr, nullptr};
    if (k == 0) return {nullptr, t};
    push(t);
     if (size(t->1) + 1 <= k) {
        auto [1, r] = split(t->r, k - size(t->l) - 1);
        t->r = 1:
        update(t);
        return {t, r};
    } else {
        auto [1, r] = split(t->1, k);
         t->1 = r;
        update(t);
        return {1, t};
    }
Node *merge(Node *tl, Node *tr) {
    if (t1 == nullptr) return tr;
if (tr == nullptr) return tl;
    push(t1);
    push(tr):
    if (tl->y > tr->y) {
         tl->r = merge(tl->r, tr);
        update(t1);
        return t1;
    } else {
        tr->l = merge(tl, tr->l);
        update(tr);
        return tr;
    }
}
void dfs(Node *t) {
    if (t == nullptr) return;
```

```
push(t);
    dfs(t->1);
    cout << t->x << ' ' ' << t->cnt << '\n';
    dfs(t->r);
}

void solve() {
    int n, m;
    cin >> n >> m;
    Node *root = nullptr;
    for (int i = 1; i <= n; i++) {
        Node *add = new Node(i);
        root = merge(root, add);
    }
    for (int i = 0; i < m; i++) {
        int l, r;
        cin >> l >> r;
        auto [L, R] = split(root, r);
        auto [L1, L2] = split(L, l - 1);
        L2->push = 1;
        L2->cnt += 1;
        root = merge(L2, merge(L1, R));
    }
    dfs(root);
}
```

2.20 Extended GCD (Sweezyk)

```
template<typename T>
T extgcd(T a, T b, T &x, T &y) {
    if (a == 0) {
        x = 0;
         y = 1;
         return b;
    T p = b / a;
    T g = \text{extgcd}(b - p * a, a, y, x);
    x = p * \bar{y};
    return g;
template<tvpename T>
bool diophantine(T a, T b, T c, T &x, T &y, T &g) {
    if (a == 0 && b == 0) {
         if (c == 0) {
    x = y = g = 0;
             return true;
         return false;
    if (a == 0) {
         if (c \% b == 0) {
             x = 0;

y = c / b;
             g = abs(b);
             return true;
         return false;
    if (b == 0) {
         if (c % a == 0) {
    x = c / a;
             y = 0;
             g = abs(a);
              return true;
         }
         return false:
       = extgcd(a, b, x, y);
    if (c % g != 0) {
         return false;
    T dx = c / a;
    c = dx * a;
    T dy = c / b;
    x = dx + (T) ((__int128) x * (c / g) % b);
y = dy + (T) ((__int128) y * (c / g) % a);
    g = abs(g);
    return true:
    // |x|, |y| \le max(|a|, |b|, |c|) [tested]
bool crt(long long k1, long long m1, long long k2, long long m2, long long
     &k, long long &m) {
    k1 %= m1;
if (k1 < 0) k1 += m1;
    k2 %= m2;
    if (k2 < 0) k2 += m2;
    long long x, y, g;
if (!diophantine(m1, -m2, k2 - k1, x, y, g)) {
         return false;
```

```
long long dx = m2 / g;
long long delta = x / dx - (x % dx < 0);
k = m1 * (x - dx * delta) + k1;
m = m1 / g * m2;
assert(0 <= k && k < m);
return true;
}
```

2.21 FFT (FedShat)

```
constexpr int P = 998244353;
using i64 = long long;
// assume -P \ll x \ll 2P
int norm(int x) {
   if (x < 0) {
    x += P;
    if (x \ge P) {
       x -= P;
   }
    return x;
template<class T>
T power(T a, int b) {
    T res = 1;
    for (; b; b /= 2, a *= a) {
   if (b % 2) {
           res *= a;
   }
    return res;
struct Z {
    Z(int x = 0) : x(norm(x)) {}
    int val() const {
       return x;
    Z operator-() const {
        return Z(norm(P - x));
    Z inv() const {
        assert(x != 0);
        return power(*this, P - 2);
    Z &operator*=(const Z &rhs) {
        x = i64(x) * rhs.x % P;
        return *this;
    Z &operator+=(const Z &rhs) {
        x = norm(x + rhs.x):
        return *this;
    Z &operator == (const Z &rhs) {
        x = norm(x - rhs.x);
        return *this:
    Z &operator/=(const Z &rhs) {
        return *this *= rhs.inv();
    friend Z operator*(const Z &lhs, const Z &rhs) {
        Z res = lhs;
        res *= rhs;
        return res:
    friend Z operator+(const Z &lhs, const Z &rhs) {
        Z res = lhs;
        res += rhs;
        return res:
    friend Z operator-(const Z &lhs, const Z &rhs) {
        Z res = lhs;
        res -= rhs;
        return res;
    friend Z operator/(const Z &lhs, const Z &rhs) {
        Z res = lhs;
        res /= rhs;
        return res;
   }
std::vector<int> rev:
std::vector<Z> roots{0, 1};
void dft(std::vector<Z> &a) {
    int n = a.size();
    if (int(rev.size()) != n) {
        int k = __builtin_ctz(n) - 1;
rev.resize(n);
```

```
for (int i = 0; i < n; i++) {
               rev[i] = rev[i >> 1] >> 1 | (i & 1) << k;
     }
     for (int i = 0; i < n; i++) {
   if (rev[i] < i) {</pre>
               std::swap(a[i], a[rev[i]]);
     if (int(roots.size()) < n) {</pre>
          int k = __builtin_ctz(roots.size());
          roots.resize(n);
           while ((1 << k) < n) {
               }
     for (int k = 1; k < n; k *= 2) {
  for (int i = 0; i < n; i += 2 * k) {
    for (int j = 0; j < k; j++) {
        Z u = a[i + j];
        Z v = a[i + j + k] * roots[k + j];
    }
}</pre>
                     a[i + j] = u + v;

a[i + j + k] = u - v;
    }
}
void idft(std::vector<Z> &a) {
     int n = a.size();
     std::reverse(a.begin() + 1, a.end());
     dft(a);
     Z inv = (1 - P) / n;
     for (int i = 0; i < n; i++) {
    a[i] *= inv;
}
```

2.22 KTO (FedShat)

```
struct Eq \{// x = a \pmod{m}
    11 a. m:
    Eq(11 a, 11 m) : a(a), m(m){};
11 binpow(ll a, ll n, ll m) {
    if (n == 0) {
       return 1;
    if (n \% 2 == 0) {
        int128_t b = binpow(a, n / 2, m);
return (b * b) % m;
    int128_t x = binpow(a, n - 1, m);
    return (a * x) % m;
11 binpow(11 a, 11 n) {
   if (n == 0) {
    if (n % 2 == 0) {
    11 b = binpow(a, n / 2);
        return b * b;
    return a * binpow(a, n - 1);
11 phi(11 a) {
    11 d = 2, k = a;
    map<11, int> cnt;
    while (d * d <= a) {
        if (k \% d == 0) {
             k /= d;
             ++cnt[d];
        } else {
             ++d:
    if (k != 1) {
        ++cnt[k];
    11 ans = 1;
    for (auto i : cnt) {
```

```
ans *= binpow(i.first, i.second - 1) * (i.first - 1);
    }
    return ans;
}
11 gcd(11 a, 11 b) {
    return std::gcd(abs(a), abs(b));
Eq solve(Eq ai, Eq bi) {
   if (ai.m == -1 || bi.m == -1) {
        return {0, -1};
    11 a = ai.m, b = bi.m, c = ai.a - bi.a;
    11 d = ::gcd(a, b);
    a /= d;
    b /= d;
    if (c % d != 0) {
        return {0, -1};
    c /= d;
    11 x = (((int128_t) -c * (int128_t) binpow(a, phi(b) - 1, b)) % b + b)
    x = ((int128_t) ai.m * (int128_t) x + ai.a) % lcm(ai.m, bi.m);
    return {x, lcm(ai.m, bi.m)};
```

2.23 Обратные по простому модулю

Пусть дан простой модуль m. Для каждого числа из [1, m-1] найти обратное к нему.

```
r[1] = 1;
for (int i = 2; i < m; ++i) {
    r[i] = (m - (m / i) * r[m % i] % m) % m;
}</pre>
```

2.24 Обратные факториалы

```
int inv(int a, int m) {
    if (a == 1)
        return 1;
    return (1 - inv(m % a, a) * m) / a + m;
}

{
    f[0] = 1;
    for (int i = 1; i < N; i++) {
        f[i] = i * f[i - 1] % mod;
    }

    r[N - 1] = inv(f[N - 1]) for (int i = N - 1; i >= 1; i--) {
        r[i - 1] = r[i] * i % mod;
    }
}
```

2.25 Γaycc

```
int gauss(vector<vector<double>> a,
          vector<double> &ans) {
    int n = (int) a.size();
    int m = (int) a[0].size() - 1;
    vector<int> where(m, -1);
    for (int col = 0, row = 0;
          col < m && row < n; ++col) {</pre>
        int sel = row;
        for (int i = row; i < n; ++i)
             if (abs(a[i][col]) > abs(a[sel][col]))
        if (abs(a[sel][col]) < EPS)
             continue;
        for (int i = col; i \le m; ++i)
             swap(a[sel][i], a[row][i]);
        where [col] = row;
for (int i = 0; i < n; ++i)
            if (i != row) {
                 double c =
            }
        a[i][col] / a[row][col];
for (int j = col; j <= m; ++j)
             a[i][j] -= a[row][j] * c;
    ans.assign(m, 0);
for (int i = 0; i < m; ++i)</pre>
         if (where[i] != -1)
```

Бинарный

2.26 Быстрая факторизация (FedShat)

```
ll binpow(ll a, ll n, ll mod) {
    if (n == 0) {
        return 1:
    if (n \% 2 == 0) {
         int128_t b = binpow(a, n / 2, mod);
         return (b * b) % mod;
    return (((int128_t) a) * binpow(a, n - 1, mod)) % mod;
constexpr int N = 1e7;
vector<int> pr, lp;
bool prime(ll n) {
    if (n <= N) {
        return binary_search(all(pr), n);
    int iter = 60;
    int s = 0;
    11 d = n - 1;
    while (d % 2 == 0) {
        d /= 2;
    auto test = [&](11 a) {
        if (binpow(a, d, n) == 1) {
            return true;
         11 _2r = 1;
         for (int r = 0; r < s; ++r) {
            auto tmp = binpow(binpow(a, d, n), _2r, n);
if (tmp == n - 1) {
                 return true;
             <u>2r</u> *= 2;
         return false;
    }:
    for (int _ = 0; _ < iter; ++_) {
    ll a = uniform_int_distribution<ll>(1, n - 1)(rnd);
         if (!test(a)) {
            return false;
        }
    }
    return true:
}
11 f(11 x, 11 n) {
    return ((int128_t) x * (int128_t) x + (int128_t) 2) % n;
}
11 pollard(ll n) {
    11 a = uniform_int_distribution<11>(0, n - 1)(rnd);
```

```
11 x = a, y = a, d = 1;
    constexpr int iter = 5e4;
    for (int _ = 0; _ < iter; ++_) {
    x = f(f(x, n), n);
        y = f(y, n);
d = gcd(abs(x - y), n);
         if (d != 1 && d != n) {
             break;
    if (d == 1 || d == n) {
        pollard(n);
    return d;
vector<ll> res:
void factor(ll n) {
    if (n \le N) {
         while (true) {
             if (lp[n] == 0) {
                  break;
             res.push_back(lp[n]);
             n /= lp[n];
        }
         return;
    if (prime(n)) {
         res.push_back(n);
         return;
    11 d = pollard(n);
    factor(n / d);
    factor(d);
void solve() {
    cin >> n:
    lp.resize(N + 1);
    for (int i = 2; i <= N; ++i) {
    if (lp[i] == 0) {
        lp[i] = i;
             pr.push_back(i);
         for (int j = 0; j < (int) pr.size() && pr[j] <= lp[i] && i * pr[j]
      <= N; ++j) {
             lp[i * pr[j]] = pr[j];
    factor(n);
```

2.27 Префикс-функция

2.28 Z-функция

```
return z; }
```

2.29 Суфмас (TheEvilBird)

```
int mod(int x, int m) {
    if (x < 0) x += m;
     if (x >= m) x -= m;
    return x;
vector<int> sufix_array(string s) {
     int n = sz(s);
    vector<int> arr(n), narr(n), head(n), c(n), nc(n);
for (int i = 0; i < n; ++i) {</pre>
         arr[i] = i;
    sort(all(arr), [&](int x, int y) {
        return s[x] < s[y];
    int cl = 0;
c[arr[0]] = cl;
    head[0] = 0;
for (int i = 1; i < n; ++i) {
         if (s[arr[i]] != s[arr[i - 1]]) {
             head[++cl] = i;
         c[arr[i]] = cl;
    for (int k = 1; k < n && cl < n; k *= 2) {
         for (int i = 0; i < n; i++) {
   int j = mod(arr[i] - k, n);
              narr[head[c[j]]++] = j;
         c1 = 0:
         head[0] = 0;
         pii prev = {c[narr[0]], c[mod(narr[0] + k, n)]};
for (int i = 1; i < n; i++) {</pre>
             pii cur = {c[narr[i]], c[mod(narr[i] + k, n)]};
if (cur != prev) {
                  head[++cl] = i;
             nc[narr[i]] = cl;
             prev = cur;
         swap(c, nc);
     // returns sufix array without $
    return vector<int>(arr.begin() + 1, arr.end());
vector<int> build_lcp(string &s, vector<int> &suf) {
     int n = sz(s);
     vector<int> lcp(n - 1), order(n);
     for (int i = 0; i < n; ++i) {
         order[suf[i]] = i;
    int 1 = 0;
for (int i = 0; i < n; ++i) {
         int id = order[i];
         if (id + 1 == n) {
             1 = 0;
             continue;
         int j = suf[id + 1];
if (1) --1;
         while (\max(i + 1, j + 1) < n \&\&
                 s[i + 1] == s[j + 1]) {
              ++1;
         lcp[id] = 1;
    return lcp;
```

2.30 Суфавтомат (TheEvilBird)

```
struct Node {
    int go[26];
    int suf, prev, term, len;

Node() {
       for (auto &i : go) {
          i = -1;
       }
       len = 0;
       suf = -1;
    }
}
```

```
term = 0;
    }
1:
vector<Node> automat;
int add(int a, int ch) {
    int b = sz(automat);
    automat.emplace_back();
automat[b].prev = a;
    automat[b].suf = 0;
    automat[b].len = automat[a].len + 1;
     for (; a != -1; a = automat[a].suf) {
        if (automat[a].go[ch] == -1) {
             automat[a].go[ch] = b;
             continue:
         int c = automat[a].go[ch];
        if (automat[c].prev == a) {
             automat[b].suf = c;
             break:
        int d = sz(automat);
        automat.emplace_back();
         automat[d].suf = automat[c].suf;
        automat[d].len = automat[a].len + 1;
        automat[c].suf = d;
        automat[b].suf = d:
        automat[d].prev = a;
for (int i = 0; i < 26; ++i) {
            automat[d].go[i] = automat[c].go[i];
        for (; a != -1 \&\& automat[a].go[ch] == c; a = automat[a].suf) {
             automat[a].go[ch] = d;
        break;
     // returns id of the added vertex
    return b;
```

2.31 Axo-Корасик (Sweezyk)

```
struct Node {
    int par;
    int par_c;
    int go[26];
    int term;
    int super;
    int cnt;
const int N = 1e6 + 5;
int ptr = 1;
Node trie[N];
void add(string s) {
   int cur = 1;
    for (auto &q : s) {
        int c = q - 'a';
        if (trie[cur].go[c]) {
            cur = trie[cur].go[c];
        } else {
            ++ptr;
            trie[cur].go[c] = ptr;
            trie[ptr].par = cur;
            trie[ptr].par_c = c;
            cur = ptr;
       }
    trie[cur].cnt++;
void build() {
    queue<int> q;
    q.push(1);
    while (!q.empty()) {
        int v = q.front();
        q.pop();
        if (v != 1) {
            if (trie[v].par == 1) {
                trie[v].link = trie[v].super = 1;
            } else {
                trie[v].link = trie[trie[trie[v].par].link].go[trie[v].
     par_c];
                trie[v].super = (trie[trie[v].link].cnt ? trie[v].link :
     trie[trie[v].link].super);
          }
        trie[v].cnt += trie[trie[v].link].cnt;
        for (int c = 0; c < 26; c++) {
```

2.32 Манакер

```
vector<int> d1(n);
int 1 = 0, r = -1;
for (int i = 0; i < n; ++i) {
    int k = (i > r ? 1 : min(d1[l + r - i], r - i + 1));
     while (i + k < n \&\& i - k >= 0 \&\& s[i + k] == s[i - k]) {
         ++k:
     d1[i] = k;
     if (i + k - 1 > r) {
         1 = i - k + 1;
         r = i + k - 1;
vector<int> d2(n);
1 = 0;
r = -1;
for (int i = 0; i < n; ++i) { int k = (i > r ? 0 : min(d2[1 + r - i + 1], r - i + 1));
     while (i + k < n & i - k - 1) = 0 & k & s[i + k] == s[i - k - 1]) {
         ++k;
     d2[i] = k;
     if (i + k - 1 > r) {
         1 = i - k;
r = i + k - 1;
```

2.33 CHT (FedShat)

```
struct Line {
    11 k = 0, b = -INFLL;
    Line() = default;
    Line(11 k, 11 b) : k(k), b(b){};
    ld operator()(ld x) {
        return k * x + b;
    }
};
bool operator<(Line a, Line b) {</pre>
   return a.k < b.k || (a.k == b.k && a.b > b.b);
bool operator<(pair<Line, ld> a, pair<Line, ld> b) {
   return a.second < b.second;
}
struct {\tt CHT} {
    vector<pair<Line, ld>> convex;
    void add(Line a) {
        while (!convex.empty() && a(convex.back().second) > convex.back().
      first(convex.back().second)) {
            convex.pop_back();
        1d \times n = -INFLL:
        if (!convex.empty()) {
    xn = (a.b - convex.back().first.b + 0.0) / (convex.back().first
        convex.push_back({a, xn});
    CHT(vector<Line> lines) {
        sort(all(lines));
        for (int i = 0; i < (int) lines.size();) {
             int j = i;
             while (j < (int) lines.size() && lines[i].k == lines[j].k) {</pre>
                 ++j;
```

```
add(lines[i]);
        i = j;
    7-
}
    auto it = upper_bound(all(convex), pair(Line(), x)) - convex.begin
    return convex[it - 1].first(x);
```

```
void debug_out(Head H, Tail... T) {
    cerr << " " << to_string(H);
debug_out(T...);</pre>
}
#define debug(...) cerr << "[" << #__VA_ARGS__ << "]:", debug_out(
      __VA_ARGS__)
#define debug(...) 42
#endif
```

Дебаг Туриста 2.34

```
template<typename A, typename B>
string to_string(pair<A, B> p);
template<typename A, typename B, typename C>
string to_string(tuple<A, B, C> p);
template<typename A, typename B, typename C, typename D>
string to_string(tuple<A, B, C, D> p);
string to_string(const string &s) {
    return '"' + s + '"
string to_string(const char *s) {
    return to_string((string) s);
string to_string(bool b) {
    return (b ? "true" : "false");
string to_string(vector<bool> v) {
    bool first = true;
string res = "{";
    for (int i = 0; i < static_cast<int>(v.size()); i++) {
        if (!first) {
             res += ", ";
         first = false;
        res += to_string(v[i]);
    res += "}";
    return res;
template<size_t N>
string to_string(bitset<N> v) {
    string res = "";
    for (size_t i = 0; i < N; i++) {
        res += static_cast<char>('0' + v[i]);
    return res;
template<typename A>
string to_string(A v) {
    bool first = true;
string res = "{";
    for (const auto &x : v) {
        if (!first) {
             res += ", ";
        first = false:
        res += to_string(x);
    return res;
template<typename A, typename B>
string to_string(pair<A, B> p) {
    return "(" + to_string(p.first) + ", " + to_string(p.second) + ")";
template<typename A, typename B, typename C>
string to_string(tuple<A, B, C> p) {
    return "(" + to_string(get<0>(p)) + ", " + to_string(get<1>(p)) + ", "
      + to_string(get<2>(p)) + ")";
template<typename A, typename B, typename C, typename D>
string to_string(tuple<A, B, C, D> p) {
return "(" + to_string(get<0>(p)) + ", " + to_string(get<1>(p)) + ", "
      + to_string(get<2>(p)) + ", " + to_string(get<3>(p)) + ")";
void debug_out() { cerr << endl; }</pre>
template<typename Head, typename... Tail>
```

Геометрия (TheEvilBird) 2.35

```
const long double PI = 3.1415926535897932384626433832795;
const long double EPS = 1e-7;
 * Rotate relative to the origin, a - rotation angle:
* new_x = x \cos(a) - y \sin(a)
* new_y = x \sin(a) + y \cos(a)
* new_x = x cos(a) + y sin(a)
* new_y = x sin(a) - y cos(a)
 * rad = degree * PI / 180
* degree = rad * 180 / PI
struct Point {
    11 x = 0, y = 0;
     // int id = -1;
    Point() : x(0), y(0) {}
Point(11 _x, 11 _y) : x(_x), y(_y) {}
     bool operator==(const Point other) const {
         return x == other.x && y == other.y;
    void operator*=(11 k) {
         y *= k;
};
istream &operator>>(istream &is, Point &point) {
    is >> point.x >> point.y;
ostream &operator<<(ostream &os, const Point &point) {</pre>
    os << point.x << ' ' << point.y;
    return os;
struct Vec {
    11 x, y;
    Vec() : x(0), y(0) {}
Vec(11 _x, 11 _y) : x(_x), y(_y) {}
Vec(Point a) : x(a.x), y(a.y) {}
     Vec(Point a, Point b) : x(b.x - a.x), y(b.y - a.y) {}
    ld len() const {
         return sqrtl(x * x + y * y);
     11 len_sq() const {
        return (x * x + y * y);
     Vec operator*(11 k) const {
         return \{x * k, y * k\};
    void operator*=(11 k) {
    Vec operator+(const Vec other) const {
         return {x + other.x, y + other.y};
    Vec operator-(const Vec other) const {
         return {x - other.x, y - other.y};
    bool operator == (const Vec other) const {
         return x == other.x && y == other.y;
```

```
bool operator!=(const Vec other) const {
         return !(*this == other);
    }
    11 operator*(const Vec other) const {// dot product
         return x * other.x + y * other.y;
    ll operator%(const Vec other) const \{//\ cross\ product\ 
         return x * other.y - y * other.x;
    }
};
istream &operator>>(istream &is, Vec &vec) {
    is >> vec.x >> vec.y;
    return is:
ostream &operator<<(ostream &os, const Vec &vec) {</pre>
    os << vec.x << ' ' << vec.y;
    return os;
typedef vector<Point> Polygon;
typedef vector<Vec> vPolygon;
bool cmp_vectors(Vec a, Vec b) {
    if ((a.y < 0 | | (a.y == 0 \&\& a.x < 0)) \&\& (b.y > 0 | | (b.y == 0 \&\& b.x > 0))) {
         return true;
    if ((b.y < 0 || (b.y == 0 && b.x < 0)) && (a.y > 0 || (a.y == 0 && a.x > 0))) {
         return false;
    return (a % b > 0 || (a % b == 0 && a.len_sq() < b.len_sq()));
int get_sign(ld kek) {
    if (kek > 0) return 1;
if (kek < 0) return -1;</pre>
    return 0;
Polygon build_convex_hull(Polygon &a) {
    int n = sz(a);
    for (int i = 1; i < n; ++i) {
   if ((a[i].y < a[0].y) || (a[i].y == a[0].y && a[i].x < a[0].x))
      swap(a[0], a[i]);
    sort(a.begin() + 1, a.end(), [&](Point A, Point B) {
         Vec oa(a[0], A), ob(a[0], B);
if ((oa % ob) == 0) return oa.len_sq() < ob.len_sq();</pre>
         return (oa % ob) > 0;
     Polygon hull = {a[0]};
    for (int i = 1; i < n; ++i) {
         while (sz(hull) >= 2) {
             Vec ab(hull[sz(hull) - 2], hull[sz(hull) - 1]), bp(hull[sz(hull
      ) - 1], a[i]);
             if ((ab % bp) <= 0) {
                  hull.pop_back();
             } else {
                  break:
             }
         hull.emplace_back(a[i]);
    return hull;
11 area_of_polygon(Polygon &poly) {
    11 \text{ res} = 0:
    int n = sz(poly);
for (int i = 2; i < n; ++i) {
         Vec ab(poly[0], poly[i - 1]), ac(poly[0], poly[i]);
         res += (ab % ac);
    // don't forget to divide the result by 2!
    return res;
ld perimeter_of_polygon(Polygon &poly) {
    1d res = 0:
    int n = sz(poly);
for (int i = 0; i < n; ++i) {
         Vec v(poly[i], poly[(i + 1 == n ? 0 : i + 1)]);
         res += v.len();
    7
    return res;
11 diameter_of_polygon(Polygon &poly) {
    int n = sz(poly), x = 1;
```

11 ans = 0;

```
for (int i = 0; i < n; ++i) {
         int j = (i + 1) \% n;
         while (true) {
              Vec ac(poly[i], poly[x]), ab(poly[i], poly[j]), cd(poly[x],
      poly[(x + 1) % n]);
              ans = max(ans, ac.len_sq());
              if ((ab % cd) <= 0) {
                   break;
              x++;
              x %= n:
     // don't forget to extract root!
    return ans;
}
ld angle(const Vec &a, const Vec &b) {
    return fabsl(atan2(a % b, a * b) / PI * 180);
}
ld angle_rad(const Vec &a, const Vec &b) {
    return (atan2(a % b, a * b));
}
ld angle_rad(const Point &a) {
    return atan2(a.y, a.x);
7
ld from_point_to_line(const Point &p, const Point &a, const Point &b) {
     Vec ba(b, a), ap(a, p);
    return fabs((ba % ap) / ba.len());
ld from_point_to_ray(const Point &p, const Point &a, const Point &b) {
    Vec ba(b, a), ap(a, p), ab(a, b);
if ((ab * ap) < 0) {</pre>
         return ap.len();
         return fabs((ba % ap) / ba.len());
ld from_point_to_segment(const Point &p, const Point &a, const Point &b) {
     Vec ab(a, b), ap(a, p), bp(b, p), ba(b, a); if ((ab * ap) < 0) {
         return fabsl(ap.len());
    } else if ((ab * bp) > 0) {
    return fabsl(bp.len());
         return fabsl((ba % ap) / ba.len());
}
bool point_on_line(const Point &p, const Point &a, const Point &b) {
    Vec ab(a, b), ap(b, p);
return (ab % ap) == 0;
bool point_on_ray(const Point &p, const Point &a, const Point &b) {
    Vec ab(a, b), ap(a, p);
return ((ab % ap) == 0 && (ab * ap) > 0 || (a == p));
bool point_on_segment(const Point &p, const Point &a, const Point &b) {
    Vec ap(a, p), bp(b, p), ab(a, b);
return ((ap * bp) <= 0 && (ap % ab) == 0);
bool point_in_angle(const Point &p, const Point &a, const Point &o, const
      Point &b) {
    Vec oa(o, a), ob(o, b), op(o, p);
if ((oa % ob) < 0) swap(oa, ob);</pre>
    return ((oa % op) >= 0 && (ob % op) <= 0);
bool segment_intersection(const Point &a, const Point &b, const Point &c,
      const Point &d) {
    Vec ab(a, b), cd(c, d), ac(a, c), ad(a, d), cb(c, b), ca(c, a); if (get_sign((ab % ac)) * get_sign((ab % ad)) <= 0 && get_sign((cd % ca)) * get_sign((cd % cb)) <= 0) {
         11 \times 1 = \max(\min(a.x, b.x), \min(c.x, d.x)), \times 2 = \min(\max(a.x, b.x),
      max(c.x, d.x));
         11 y1 = max(min(a.y, b.y), min(c.y, d.y)), y2 = min(max(a.y, b.y),
      max(c.y, d.y));
return (x1 <= x2 && y1 <= y2);</pre>
    return false;
bool rays_intersection(const Point &a, const Point &b, const Point &c,
      const Point &d) {
     Vec ab(a, b), cd(c, d):
    11 k = 1e6;
     ab *= k;
     cd *= k;
```

```
Point nb(ab.x + a.x, ab.y + a.y), nd(cd.x + c.x, cd.y + c.y);
          return segment_intersection(a, nb, c, nd);
}
bool lines intersection(const Point &a. const Point &b. const Point &c.
            const Point &d) {
          Vec ab(a, b), cd(c, d);
return ((ab % cd) != 0);
int point_in_polygon(const Point &p, const Polygon &poly) {
   // 0 - outside, 1 - inside, 2 - border;
          int n = sz(poly);
          if (point_in_angle(p, poly[n - 1], poly[0], poly[1])) {
                  int 1 = 1, r = n - 1;
while (r - 1 > 1) {
                            int md = (1 + r) / 2;
                            if (point_in_angle(p, poly[md], poly[0], poly[1])) {
                            } else {
                                   1 = md;
                            }
                  if (point_in_angle(p, poly[r], poly[0], poly[1]) && point_in_angle(p, poly[0], poly[1], poly[r]) && point_in_angle(p, poly[1], poly[r], poly[0])) {
                            product | p
            ])) {
                                    return 2;
                            } else {
                                    return 1;
                           7
                  } else {
                           return 0:
          } else {
                 return 0;
         }
}
int point_in_nonconvex_polygon(const Point &p, const Polygon &poly) {
          // 0 - outside, 1 - inside, 2 - border;
          int n = sz(poly);
          for (int i = 0; i < n; ++i) {
                  if (point_on_segment(p, poly[i], poly[(i + 1) % n])) {
                            return 2:
          ld s = 0.0;
          for (int i = 0; i < n; ++i) {
                  Vec pa(p, poly[i]), pb(p, poly[(i + 1 == n ? 0 : i + 1)]);
                  s += angle_rad(pa, pb);
          if (s >= PI || s <= -PI) {
                  return 1;
          } else {
                  return 0;
         7
}
Polygon minkowski_sum(Polygon &a, Polygon &b) {
          // a[0], b[0]: y - max, y1 = y2 => x - max. Against clockwise int n = sz(a), m = sz(b);
          assert(n >= 3 \&\& m >= 3);
          Point high_a = a[0], high_b = b[0];
          vPolygon va(n), vb(m);
          for (int i = 0; i < n; ++i) {
                  va[i] = Vec(a[i], a[(i + 1) % n]);
          for (int i = 0; i < m; ++i) {
   vb[i] = Vec(b[i], b[(i + 1) % m]);</pre>
          //
                       sort(all(va), cmp_vectors);
                       sort(all(vb), cmp_vectors);
          vPolygon vc;
          merge(all(va), all(vb), back_inserter(vc), cmp_vectors);
         Point high_c(high_a.x + high_b.x, high_a.y + high_b.y);
Polygon c(sz(vc) + 1);
          c[0] = high_c;
for (int i = 0; i < sz(c) - 1; ++i) {
                  c[i + 1] = Point(c[i].x + vc[i].x, c[i].y + vc[i].y);
          return c;
ld from_polygon_to_polygon(Polygon a, Polygon b) {
         for (auto &i : b) {
                  i *= -1:
          int pos = 0;
          for (int i = 1; i < sz(b); ++i) {
    if ((b[i].y > b[pos].y) ||
                            (b[i].y == b[pos].y \&\& b[i].x > b[pos].x)) {
```

```
}
    rotate(b.begin(), b.begin() + pos, b.end());
    Polygon c = minkowski_sum(a, b);
    int n = sz(c);
    Point p(0, 0);
    ld ans = 1e20;
    for (int i = 0; i < n - 1; ++i) {
        ans = min(ans, from_point_to_segment(p, c[i], c[i + 1]));
    return ans:
11 diameter_of_polygon_minkowski(Polygon &a) {
    Polygon ra = a;
    for (auto &i : ra) {
        i *= -1:
    int pos = 0;
    for (int i = 1; i < sz(a); ++i) {
        if ((a[i].y > a[pos].y) | |
            (a[i].y == a[pos].y && a[i].x > a[pos].x)) {
            pos = i:
    rotate(a.begin(), a.begin() + pos, a.end());
    pos = 0;
    for (int i = 1; i < sz(a); ++i) {
        if ((ra[i].y > ra[pos].y) ||
          (ra[i].y == ra[pos].y && ra[i].x > ra[pos].x)) {
            pos = i;
    }
    rotate(ra.begin(), ra.begin() + pos, ra.end());
    Polygon c = minkowski_sum(a, ra);
    int n = sz(c):
    11 ans = 0;
    for (int i = 0; i < n; ++i) {
        ans = max(ans, Vec(c[i]).len_sq());
    // don't forget to extract root!
    return ans;
```