# surface barrier

April 17, 2022

## 1 Surface Barrier

## 1.1 Functions

```
[56]: # %load ../../setup.py
      Packages for plotting and other stuff
      version: 5.0
      author: Riasat
      11 11 11
      # uncomment the below line to use interactive plots
      # %matplotlib widget
      # data loading
      import pandas as pd
      # data maipulation
      import pwlf
      import numpy as np
      from scipy.interpolate import interp1d, UnivariateSpline
      from scipy.signal import find_peaks
      from scipy import optimize
      # plotting tools
      import matplotlib.pyplot as plt
      # extra tweaks
      import warnings
      warnings.filterwarnings("ignore")
      # plot tweaks
      plt.style.use("seaborn-poster")
      pd.options.display.max_columns = None
      pd.options.display.float_format = "{:.5f}".format
      # function for extrapolation
      def extrapolate1d(x, y):
```

```
f = interp1d(x, y, kind="linear", fill_value="extrapolate")
   a = np.arange(0, x[len(x) - 1], 0.001)
   b = f(a)
   return a, b
# function for interpolation
def interpolate1d(x, y):
   f = interp1d(x, y, kind="linear", fill_value="extrapolate")
   a = np.arange(x[0], x[len(x) - 1], 0.001)
   b = f(a)
   return a, b
# function for interpolation
def interpolate2d(x, y):
   f = interp1d(x, y, kind="quadratic", fill_value="extrapolate")
   a = np.arange(x[0], x[len(x) - 1], 0.001)
   b = f(a)
   return a, b
# function for interpolation
def interpolate3d(x, y):
   f = interp1d(x, y, kind="cubic", fill_value="extrapolate")
   a = np.arange(x[0], x[len(x) - 1], 0.001)
   b = f(a)
   return a, b
# funciton for polynomial fitting
def polfit(a, b, c):
   z = np.polyfit(a, b, c)
   f = np.poly1d(z)
   x = np.arange(a[0], a[len(a) - 1], 0.001)
   y = f(x)
   return x, y
# function for picewise linear fit
def picewise_linear_fit(x, y, segments):
   my_pwlf = pwlf.PiecewiseLinFit(x, y) # fit my data
   res = my_pwlf.fit(segments) # fit the data for n line segments
   # slopes = myPWLF.calc_slopes() # calculate slopes
    # predict for the determined points
```

```
xHat = np.linspace(min(x), max(x), num=10000)
   yHat = my_pwlf.predict(xHat)
    # calculate statistics
   # p = myPWLF.p_values(method="non-linear", step_size=1e-4) # p-values
    # se = myPWLF.se # standard errors
   return xHat, yHat
# curve fit
def cur fit(x, y):
   func = lambda t, a, c, d: a * np.log(t + c) + d
   popt, pcov = optimize.curve_fit(func, x, y) # type: ignore
   xx = np.arange(x[0], x[len(x) - 1], 0.001)
   yy = func(xx, *popt)
   return xx, yy
def estimate_coef(x, y):
   # number of observations/points
   n = np.size(x)
   # mean of x and y vector
   m_x = np.sum(x)
   m y = np.sum(y)
   \# calculating cross-deviation and deviation about x
   SS_xy = np.sum(y * x)
   SS_xx = np.sum(x * x)
   deno = n * SS_xx - m_x * m_x
   # calculating regression coefficients
   b = (n * SS_xy - m_x * m_y) / deno
   a = (m_y * SS_xx - m_x * SS_xy) / deno
   return (a, b)
```

#### 1.2 Data

```
[57]: file_name = "data_surface.xlsx"
    res_name = ["Am-241", "Pu-239", "Cm-244"]
    # calibration data
    data_cesium_calib = pd.read_excel(file_name, sheet_name="calibration")
    peak_channel = data_cesium_calib["calib_channel"]
    known_energy = data_cesium_calib["calib_energy"]

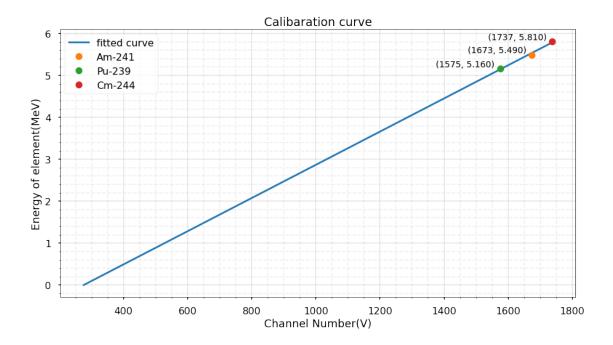
    data_am = pd.read_excel(file_name, sheet_name='thick')
    left_air = data_am['left_air']
    right_air = data_am['right_air']
    left_vacc = data_am['left_vacc']
```

```
right_vacc = data_am['right_vacc']
vaccum_peak = data_am['vaccum_peak']
air_peak = data_am['air_peak']
thickness = data_am['thickness']
print(data_cesium_calib)
```

```
calib_channel calib_energy
0 1673 5.49000
1 1575 5.16000
2 1737 5.81000
```

#### 1.3 Calibration

```
[58]: # extrapolated points
     peak_channel_fit, known_energy_fit = polfit(peak_channel, known_energy, 1)
     cal_chan_ext, cal_eng_ext = extrapolate1d(peak_channel_fit, known_energy_fit)
     ckt = [item for item in cal_eng_ext if item >= 0]
     plt.style.use("seaborn-poster")
     plt.figure(figsize=(15, 8))
     plt.title(f"Calibaration curve")
     plt.xlabel("Channel Number(V)")
     plt.ylabel("Energy of element(MeV)")
     plt.plot(cal_chan_ext[275635:], ckt, "-", label="fitted curve")
     for i in range(len(res name)):
         plt.plot(peak_channel[i], known_energy[i], "o", label=res_name[i])
         plt.annotate(f"({peak_channel[i]}, {known_energy[i]:.3f})",
      plt.legend(loc="upper left")
     plt.grid(alpha=0.3, which="major")
     plt.minorticks on()
     plt.grid(alpha=0.2, which="minor", ls="--")
     plt.show()
```



## 1.4 FWHM

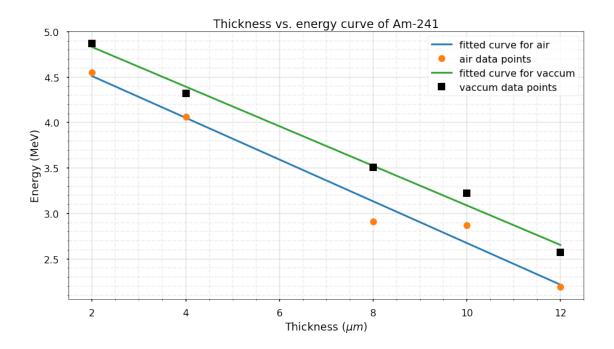
```
[59]: # air energy from calibration curve
    peak_energy_air = np.interp(air_peak, cal_chan_ext, cal_eng_ext)
    peak_energy_vaccum = np.interp(vaccum_peak, cal_chan_ext, cal_eng_ext)

data_am['energy air'] = peak_energy_air
    data_am['energy vaccum'] = peak_energy_vaccum

# print(data_am)
```

## 1.5 Thickness vs. energy

```
# predicted response vector
      ye_pred_air = be_air[0] + be_air[1] * xe
      ye_pred_vac = be_vac[0] + be_vac[1] * xe
     Estimated coefficients (Air):
      a = 4.970
      b = -0.230
     Estimated coefficients (Vaccum):
      a = 5.266
      b = -0.218
[64]: | # thickness_fitted_air, peak_energy_air_fitted = polfit(thickness,
       \rightarrow peak_energy_air, 1)
      \# thickness_fitted_vaccum , peak_energy_vaccum_fitted = polfit(thickness, \sqcup
       ⇒peak_energy_vaccum, 1)
      plt.style.use("seaborn-poster")
      plt.figure(figsize=(15, 8))
      plt.title(f"Thickness vs. energy curve of Am-241")
      plt.xlabel(r"Thickness ($\mu m$)")
      plt.ylabel("Energy (MeV)")
      plt.plot(xe, ye_pred_air, "-", label="fitted curve for air")
      plt.plot(thickness, peak_energy_air, "o", label='air data points')
      plt.plot(xe, ye_pred_vac, "-", label="fitted curve for vaccum")
      plt.plot(thickness, peak_energy_vaccum, "ks", label='vaccum data points')
      plt.legend(loc="upper right")
      plt.grid(alpha=0.3, which="major")
      plt.minorticks_on()
      plt.grid(alpha=0.2, which="minor", ls="--")
      plt.show()
```



## 1.6 Thickness vs. FWHM

```
[62]: left_air_energy = np.interp(left_air, cal_chan_ext, cal_eng_ext)
    right_air_energy = np.interp(right_air, cal_chan_ext, cal_eng_ext)
    fwhm_air_mev = abs(left_air_energy - right_air_energy)

left_vaccum_energy = np.interp(left_vacc, cal_chan_ext, cal_eng_ext)
    right_vaccum_energy = np.interp(right_vacc, cal_chan_ext, cal_eng_ext)
    fwhm_vaccum_mev = abs(left_vaccum_energy - right_vaccum_energy)

data_am['fwhm_air_mev'] = fwhm_air_mev
    data_am['fwhm_vaccum_mev'] = fwhm_vaccum_mev
    print(data_am)
```

	thickness	vaccum_peak	air_peak	left_vacc	right_vacc	left_air	\
0	2	1506	1425	1345	1568	1326	
1	4	1367	1303	1206	1446	1138	
2	8	1162	1011	862	1255	798	
3	10	1090	1001	779	1177	724	
4	12	925	829	575	1024	537	
	right_air	energy air	energy vacc	um fwhm_a	ir_mev fwhm	_vaccum_me	v
0	1491	4.54981	4.870	45 0	.65316	0.8827	'5
1	1372	4.06687	4.320	22 0	.92630	0.9500	)5
2	1094	2.91098	3.508	72 1	.17173	1.5557	1
3	1093	2.87139	3.223	70 1	.46070	1.5755	0

4 925 2.19052 2.57054 1.53591 1.77739

```
[65]: # observations
      x = thickness
      y_air = fwhm_air_mev
      y_vac = fwhm_vaccum_mev
      # estimating coefficients
      b_air = estimate_coef(x, y_air)
      b_vac = estimate_coef(x, y_vac)
      print(
          f"Estimated coefficients (Air): n = \{b_air[0]:.3f\} \setminus b = \{b_air[1]:.3f\}_{\sqcup}
          \nEstimated coefficients (Vaccum): \n a = \{b_vac[0]:.3f\} \n b = \{b_vac[1]:.
      )
      # predicted response vector
      y_pred_air = b_air[0] + b_air[1] * x
      y_pred_vac = b_vac[0] + b_vac[1] * x
      plt.style.use("seaborn-poster")
      plt.figure(figsize=(15, 8))
      plt.title(f"Thickness vs. FWHM curve of Am-241")
      plt.xlabel(r"Thickness ($\mu$m)")
      plt.ylabel("FWHM (MeV)")
      plt.plot(x, y_pred_air, "-", label="fitted curve for air")
      plt.plot(thickness, fwhm_air_mev, "o", label="air data points")
      plt.plot(x, y_pred_vac, "-", label="fitted curve for vaccum")
      plt.plot(thickness, fwhm_vaccum_mev, "ks", label="vaccum_data_points")
      plt.legend(loc="upper left")
      plt.grid(alpha=0.3, which="major")
      plt.minorticks_on()
      plt.grid(alpha=0.2, which="minor", ls="--")
      plt.show()
     Estimated coefficients (Air):
      a = 0.518
      b = 0.088
     Estimated coefficients (Vaccum):
      a = 0.662
      b = 0.095
```

