## Numerical Exercise #1

Caspar Gutsche

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## 1 Question #1

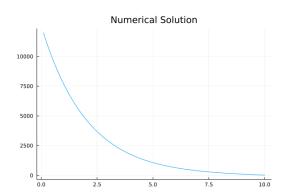


Figure 1: Analytical Solution for the neutron flux as a function of depth.

Flux values at the following locations (4 significant digits):

Flux value at  $x_0$ : 13.5896  $cm^{-2}s^{-1}$ 

Flux value at  $0^{+}$ :12276.897875372839  $cm^{-2}s^{-1}$ 

## 2 Question #2

The differential Equation is given as

$$D\frac{d^2}{dx^2}\Phi - \Sigma_a \Phi = 0 \tag{1}$$

Right hand side

$$\frac{1}{dx^2}(D\phi_{n-1} - (D + dxBC_n + \Sigma_a dx^2)\phi_n) = 0$$

Left hand side:

$$\frac{1}{dx^{2}}(-(D + \Sigma_{a}dx^{2})\phi_{1} + D\phi_{2}) = -\frac{S}{2dx}$$

Middle:

$$\frac{D}{dx^2}(\Phi_{i-1} - 2\Phi_i + \Phi_{i+1}) - \Sigma_a \Phi_i = 0$$

Associated coefficients of the matrix A (4 significant digits), for a mesh size of  $0.1 \mathrm{cm}$ : at the source:

$$A_{1.1} = -8.31187 \tag{2}$$

$$A_{1,2} = 8.29187 \tag{3}$$

$$A_{2,1} = -8.29187 \tag{4}$$

at teh right hand side:

$$A_{n,n} = 12.1536 \tag{5}$$

$$A_{n-1,n} = -8.29187 \tag{6}$$

$$A_{n,n-1} = -8.29187 (7)$$

## 3 Question #3

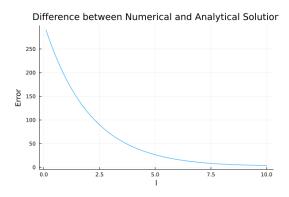


Figure 2: Distance between the solutions at each mesh point for a mesh size of 0.1 cm.

Flux values from the numerical solver at the following locations (4 significant digits): Flux value at  $0^+ = 11979.0980cm^{-2}s^{-1}$ : Flux value at  $x_0 = 17.732cm^{-2}s^{-1}$ :

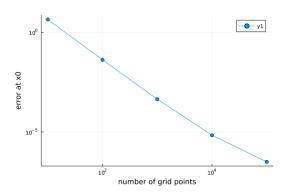


Figure 3: Evolution with mesh size of the absolute error of  $\Phi(x_0)$ .

In figure 3 you can see the sum of the errors and in 4 you can see the maximum deviation from the reference solution.

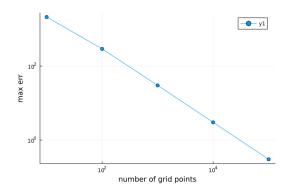


Figure 4: Evolution with mesh size of the absolute error of  $\Phi(x_0)$ .