

Some Applications of Phase-Field Approaches to Fracture (Need to somehow mention variational frameworks and nonlinearity)

by

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Dissertation submitted in partial fulfillment of the requirements for the degree of
Doctor of Philosophy in the Department of Mechanical Engineering and Materials
Science
in the Graduate School of Duke University
2021

ABSTRACT

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Abstract

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I am thankful for the many people.

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Introduction placeholder.

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Code availability

Appendix B

On the phase-field irreversibility constraint

Appendix C

The flooding algorithm for counting fragments

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Biography

About myself.