

# EECS3311 Software Design

Why DbC?

Some Examples

Modelling

Hoare Logic

Required Reading:

OOSC2 - whole of chapter 11

See Touch of Class for introductory material on contracts

# Is the contract correct?

Writing PostCondition : Exercise

IS-positive(  $x$ : INTEGER) : BOOLEAN

ensure

$$x > 0$$

# Is the contract correct?

Writing Postcondition: Exercise

a: ARRAY [INTEGER]

change\_at( i: INTEGER ; v: INTEGER )

ensure

across a.lower .. a.upper as j

all

j.item = i implies a[j.item] = v

and

j.item != i implies a[j.item] = (old a.twin)[j.item]

end

```

24 feature -- tests
25   a: ARRAY[INTEGER]
26     attribute
27       Result := <<10, 22>>
28       Result.compare_objects
29   end
30
31   change_at(i: INTEGER; v: INTEGER)
32   do
33     a[i] := v
34     a.force (33, 3)
35   ensure
36   --
37     post0: a.count = old a.count
38     post1: a[i] = v
39     post2:
40       across a.lower |..| a.upper as j all
41         j.item /= i implies a[j.item] = (old a.twin)[j.item]
42   end
43
44   t0: BOOLEAN
45   local
46     a1, a2: like a
47   do
48     comment("t0: test array")
49     a1:= <<10, 22>>; a1.compare_objects
50     a2:= <<11, 22, 33>>; a2.compare_objects
51     Result := a ~ a1
52     check Result end
53     change_at (1, 11)
54     Result := a ~ a2
55     check Result end
56   end

```

```

change_at(i: INTEGER; v: INTEGER)
do
    a[i] := v
    a.force (33, 3) -- BAD
ensure
    post0: a.count = old a.count
    post1: a[i] = v
    post2:
        across a.lower |..| a.upper as j all
            j.item /= i
            implies
                a[j.item] = (old a.twin)[j.item]
    end
end

```

FAILED (1 failed & 0 passed out of 1)		
Case Type	Passed	Total
Violation	0	0
Boolean	0	1
All Cases	0	1
State	Contract Violation	Test Name
Test1	TESTS	
FAILED	Postcondition violated.	t0: test array

# Check violation instead of postcondition violation

The screenshot shows a software interface with a code editor and a status table.

**Code Editor:**

```
Feature tests TESTS change_at < > □ ×
Flat view of feature 'change_at' of class TESTS
change_at (i: INTEGER_32; v: INTEGER_32)
do
    a [i] := v
    a.force (33, 3)
ensure
    post1: a [i] = v
    post2: across
        a.lower ..| a.upper as j
        all
            j.item /= i implies a [j.item] = (old a.twin) [j.item]
        end
end
```

**Status Table:**

In Feature	In Class	From Class	@
item	ARRAY	TESTS	4+1
change_at	TESTS	TESTS	6
t0	TESTS	TESTS	8
fast_item	PREDICATE	FUNCTION	0
item	PREDICATE	FUNCTION	3
run	ES_BOOLEA...	ES_BOOLEA...	3
run_es_test	TESTS	ES_TEST	20
run_es_test	ROOT	ES_SUITE	9
run_espec	ROOT	ES_TESTABLE	2
make	ROOT	ROOT	4

FAILED (1 failed & 0 passed out of 1)		
Case Type	Passed	Total
Violation	0	0
Boolean	0	1
All Cases	0	1
State	Contract Violation	Test Name
Test1	TESTS	
FAILED	Check assertion violated.	t0: test array

# Is contract correct?

Writing Postcondition : Exercise

all-positive-values( a: ARRAY[INTEGER] ): ARRAY[INTEGER]

ENSURE

across Result as x

all

x.item > 0

end

# BIRTHDAY\_BOOK

*model*: FUN[STRING, BIRTHDAY]

-- set of tuples [name, birthday]

*put* (a\_name: STRING; d: BIRTHDAY)

**ensure**

model ~ (**old** model) ↗ [a\_name, d]

-- symbol ↗ used for function override

*remind* (d: BIRTHDAY): ARRAY[STRING]

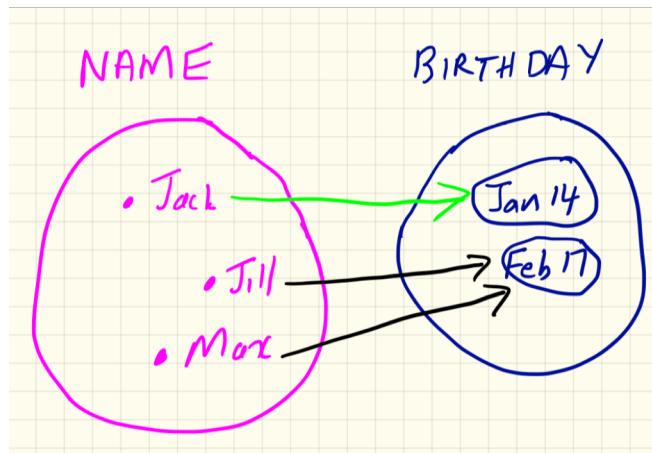
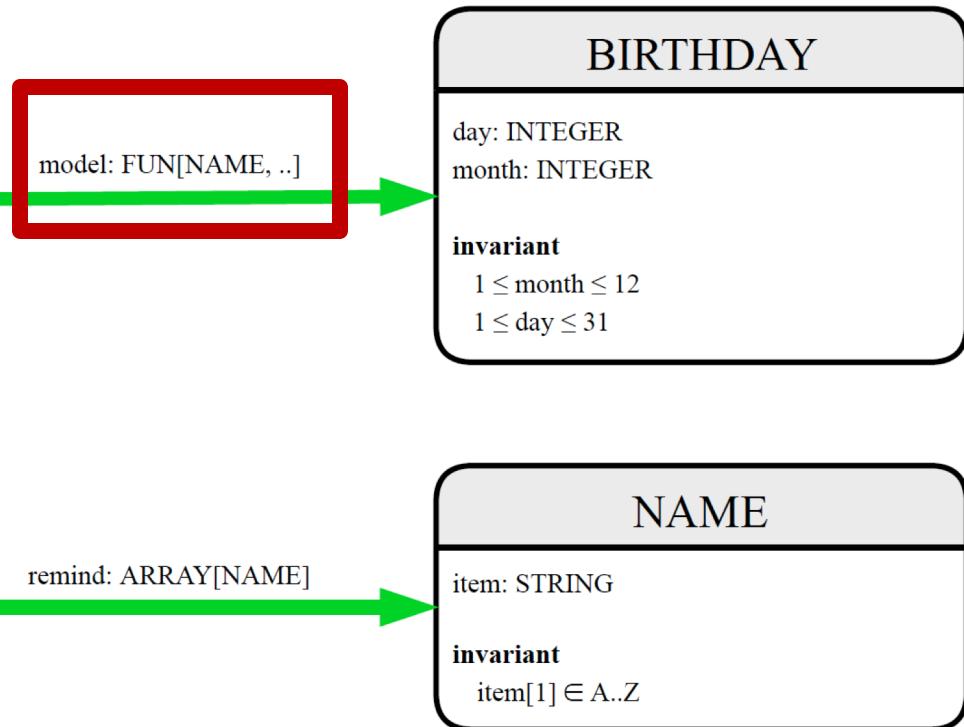
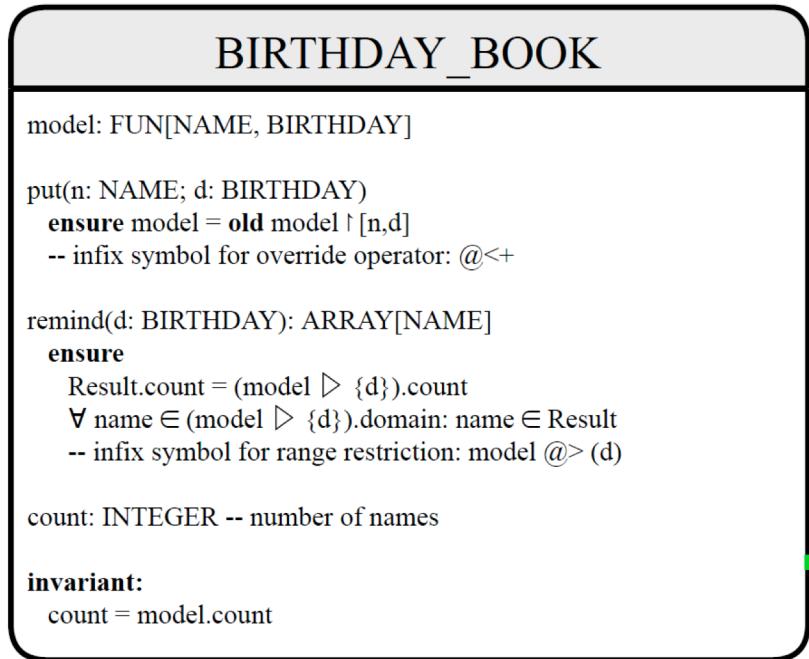
**ensure**

Result.count = (model ▷ {d}).count

∀name ∈ (model ▷ {d}).domain: name ∈ Result

-- symbol ▷ used for range restriction

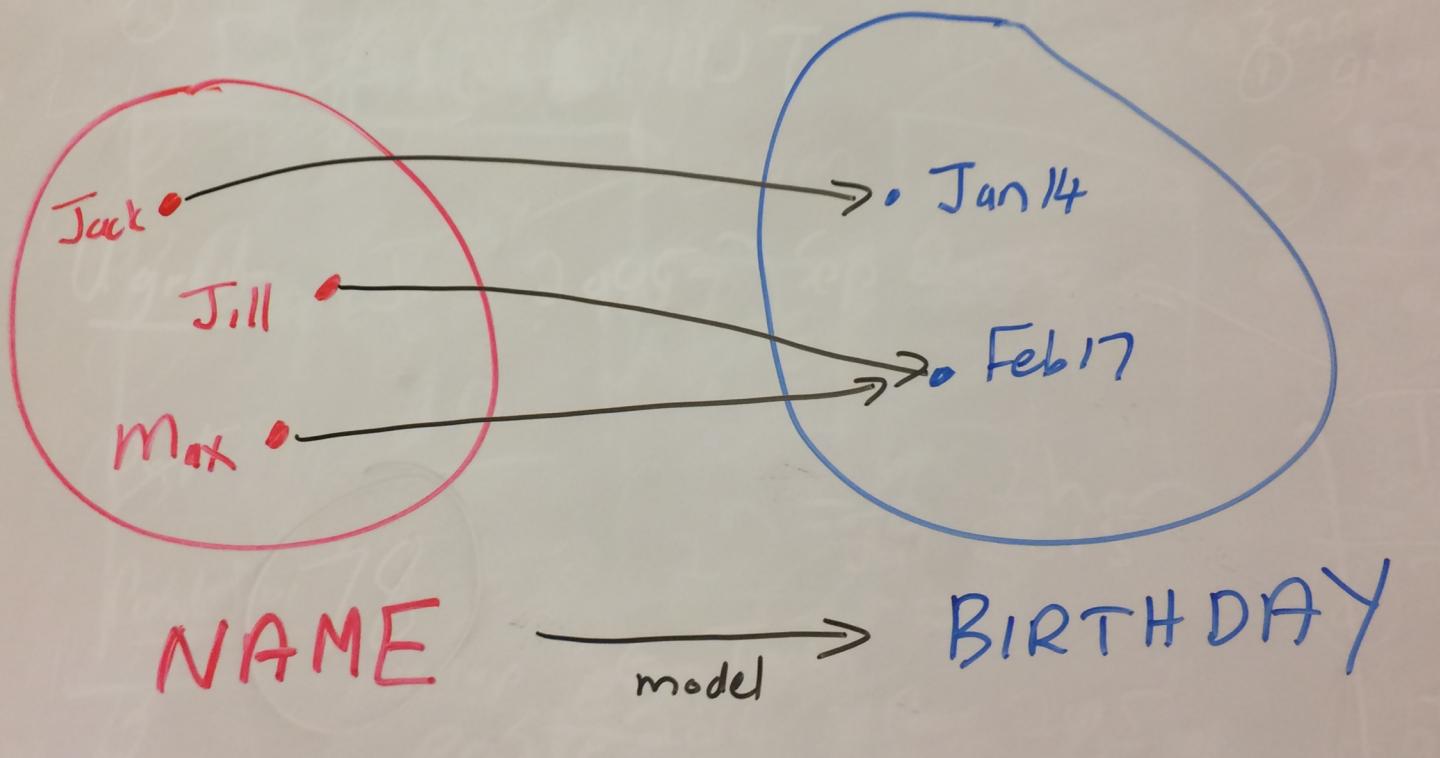
# Design of Birthday Book



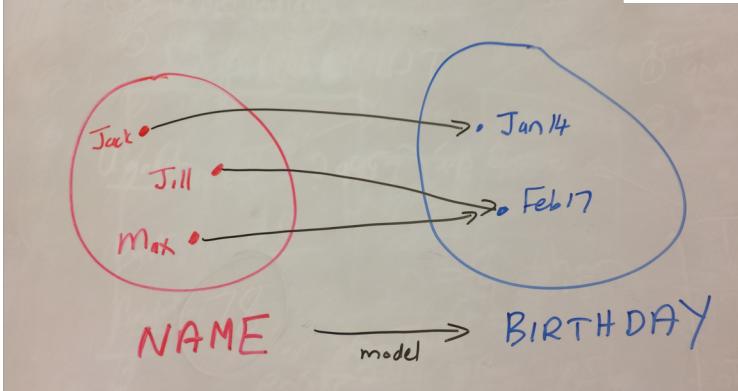
# model: FUN [NAME, BIRTHDAY]

model : FUN [NAME, BIRTHDAY]

model =  $\{ [Jack, Jan14], [Jill, Feb17], [Max, Feb17] \}$



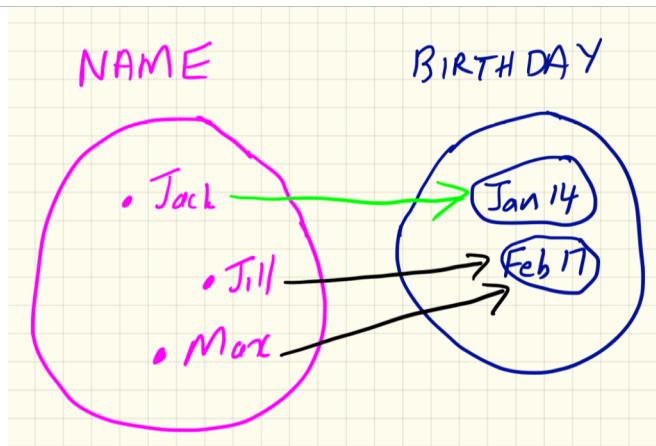
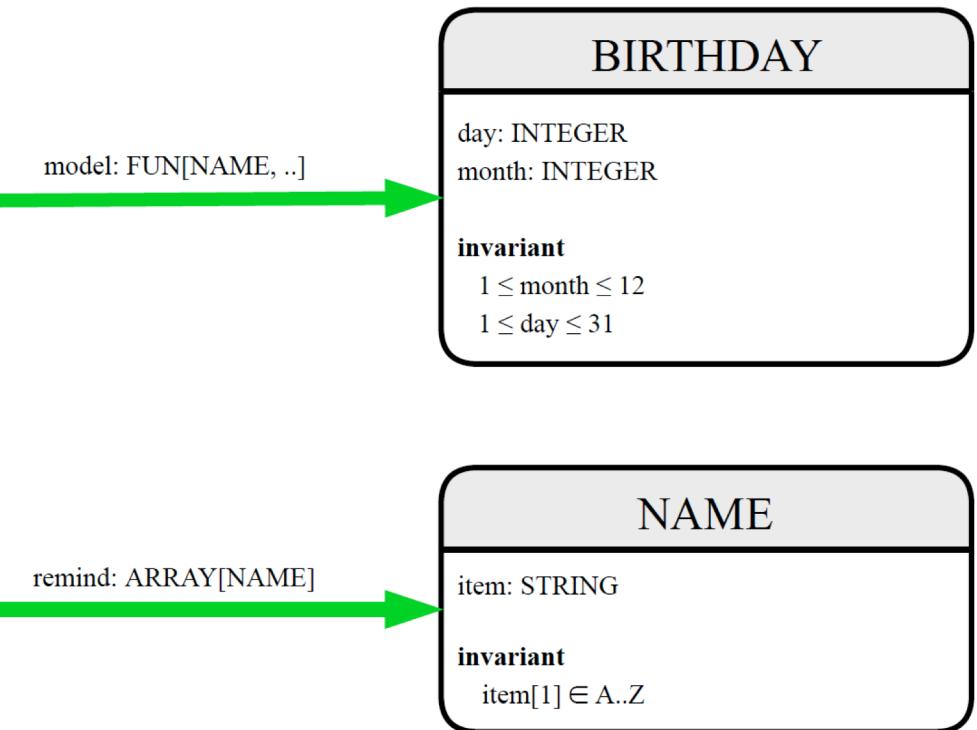
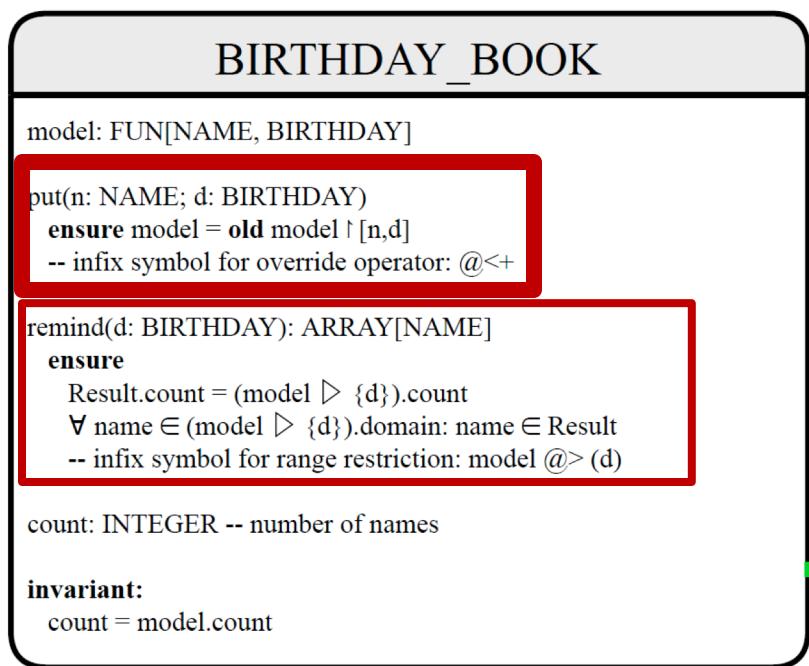
model :  $\text{FUN}[\text{NAME}, \text{BIRTHDAY}]$   
 $\text{model} = \{[\text{Jack}, \text{Jan14}], [\text{Jill}, \text{Feb17}], [\text{Max}, \text{Feb17}]\}$



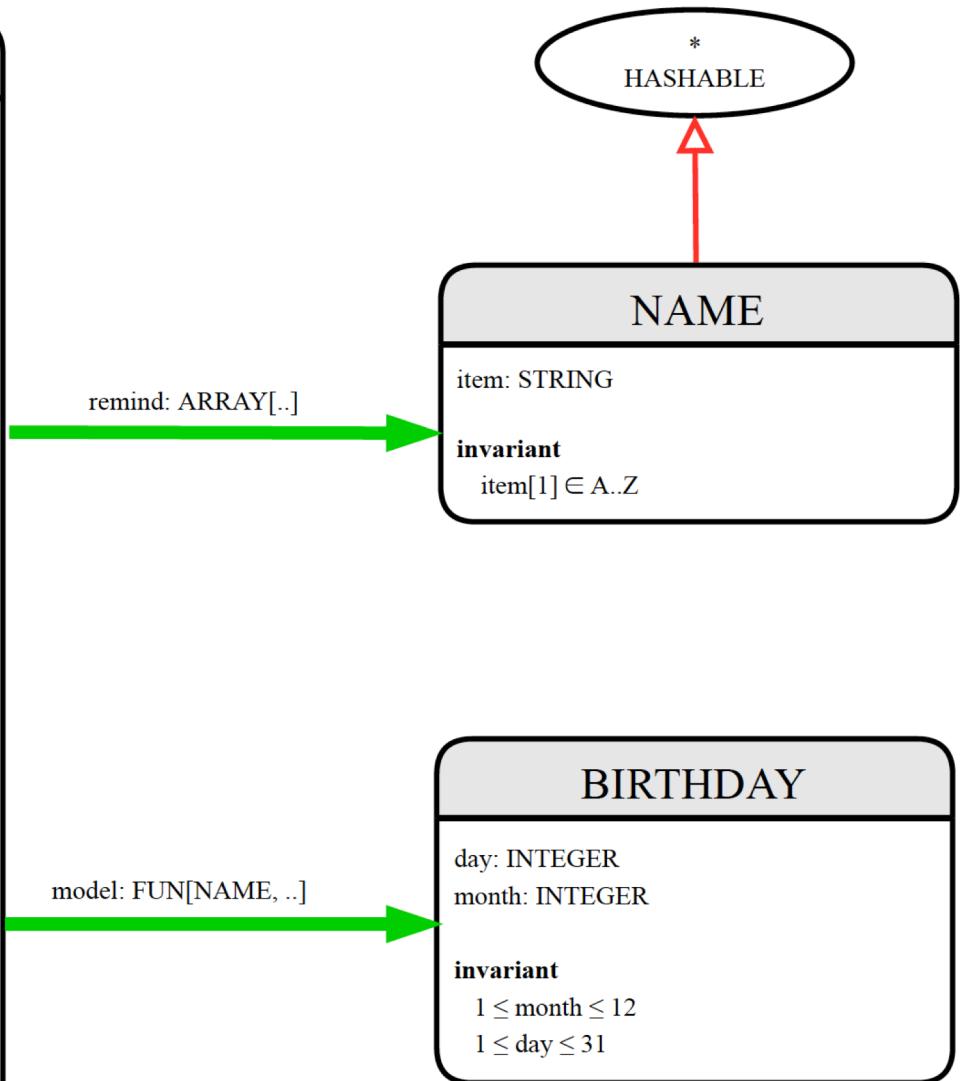
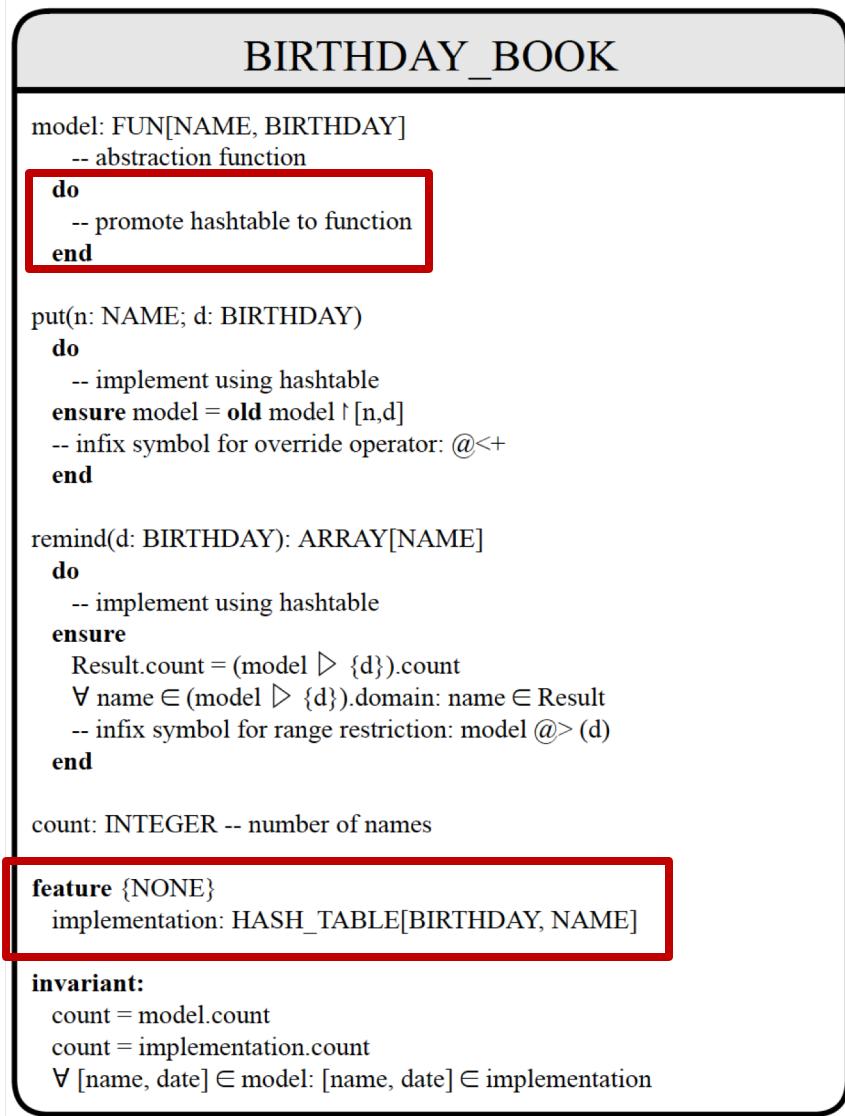
model:  $\text{FUN}[\text{NAME}, \text{BIRTHDAY}]$

- $\text{model} = \{[\text{Jack}, \text{Jan14}], [\text{Jill}, \text{Feb17}], [\text{Max}, \text{Feb17}]\}$
- $\text{model}.\text{domain} = \{\text{Jack}, \text{Jill}, \text{Max}\}$
- $\text{model}.\text{range} = \{\text{Jan14}, \text{Feb17}\}$
- Range restriction:  
 $\text{model} \triangleright \{\text{Feb17}\} = \{[\text{Jill}, \text{Feb17}], [\text{Max}, \text{Feb17}]\}$
- Override operator:  
 $\text{model} \upharpoonright [\text{Pam}, \text{Dec12}] =$   
 $\{[\text{Jack}, \text{Jan14}], [\text{Jill}, \text{Feb17}], [\text{Max}, \text{Feb17}], [\text{Pam}, \text{Dec12}]\}$

# Design of Birthday Book



# Efficient hashtable implementation



```

class interface BIRTHDAY_BOOK feature

    model: FUN [NAME, BIRTHDAY]
        -- model is a function from NAME --> BIRTHDAY
        -- abstraction function

    put (a_name: NAME; d: BIRTHDAY)
        -- add date of birth for `a_name` at date `d`
        -- or override current birthday with new
    ensure
        model_override:
            model ~ (old model @<+ [a_name, d])

    remind (d: BIRTHDAY): ARRAY [NAME]
        -- returns an array of names with birthday `d`
    ensure
        remind_count: Result.count = (model @> (d)).count
        remind_model_range_restriction:
            across
                (model @> (d)).domain as cr
            all
                Result.has (cr.item)
        end
    end

```

# Efficient hash table implementation

```
feature {NONE, ES_TEST} -- implementation

    imp: HASH_TABLE [BIRTHDAY, NAME]
        -- implementation as an efficient hash table

    make
        -- create a birthday book
    do
        create imp.make (10)
    ensure
        model.is_empty
    end

feature -- model

    model: FUN [NAME, BIRTHDAY]
        -- model is a function from NAME --> BIRTHDAY
        -- abstraction function
        -- Abstraction Function from an object's concrete implementation
        -- to the abstract value it represent
    local
        l_name: NAME
        l_date: BIRTHDAY
    do
        create Result.make_empty
        from
            imp.start
        until
            imp.after
        loop
            l_name := imp.key_for_iteration
            l_date := imp [l_name]
            check attached l_date as l_date2 then
                Result.extend ([l_name, l_date2])
            end
            imp.forth
        end
        imp.start
    end
```

# Efficient hash table implementation

```
put (a_name: NAME; d: BIRTHDAY)
    -- add birthday for `a_name' at date `d'
    -- or override current birthday with new
do|
    if not imp.has_key (a_name) then
        imp.extend (d, a_name)
    else
        imp.replace (d, a_name)
    end
ensure
    model_override:
        model ~ (old model @<+ [a_name, d])
end
```

```
feature {NONE, ES_TEST} -- implementation

    imp: HASH_TABLE [BIRTHDAY, NAME]
        -- implementation as an efficient hash table
```

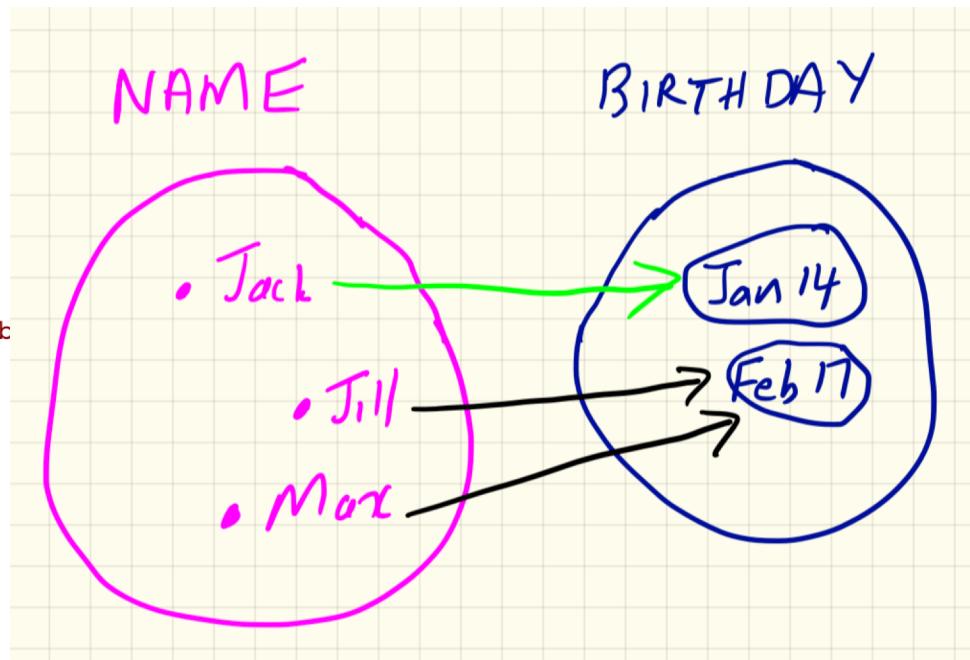
# Efficient hash table implementation

```
remind (d: BIRTHDAY): ARRAY [NAME]
    -- returns an array of names with birthday `d'
local
    l_name: NAME
    l_date: BIRTHDAY
    i: INTEGER
do
    create Result.make_empty
    Result.compare_objects
    from
        imp.start
until
    imp.after
loop
    l_name := imp.key_for_iteration
    l_date := imp [l_name]
    if l_date ~ d then
        Result.force (l_name, i)
        i := i + 1
    end
    imp.forth
end
ensure
    remind_count:
        Result.count = (model @> (d)).count
    remind_model_range_restriction:
        across (model @> (d)).domain as cr all
            Result.has (cr.item)
    end
end
```

```
feature {NONE, ES_TEST} -- implementation
    imp: HASH_TABLE [BIRTHDAY, NAME]
        -- implementation as an efficient hash table
```

# Efficient hash table implementation

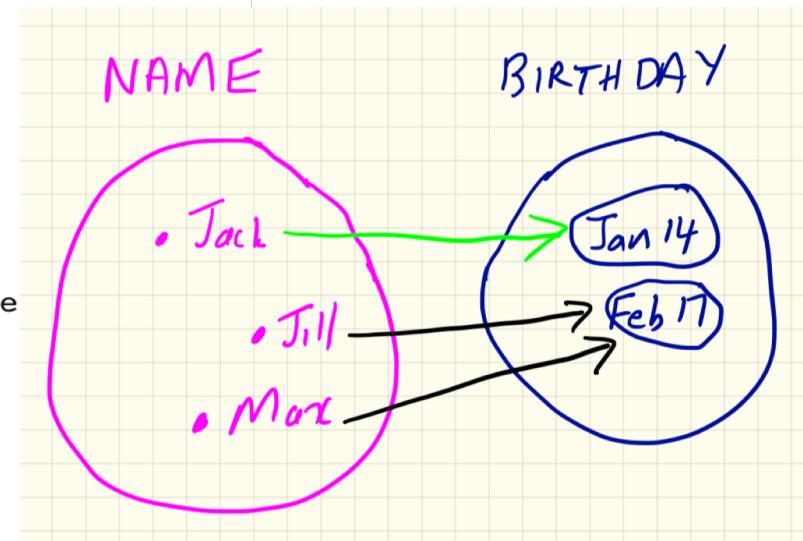
```
remind (d: BIRTHDAY): ARRAY [NAME]
    -- returns an array of names with b
local
    l_name: NAME
    l_date: BIRTHDAY
    i: INTEGER
do
    create Result.make_empty
    Result.compare_objects
    from
        imp.start
until
    imp.after
loop
    l_name := imp.key_for_iteration
    l_date := imp[l_name]
    if l_date ~ d then
        Result.force (l_name, i)
        i := i + 1
    end
    imp.forth
end
ensure
    remind_count:
        Result.count = (model @> (d)).count
    remind_model_range_restriction:
        across (model @> (d)).domain as cr all
            Result.has (cr.item)
        end
end
```



```

t1: BOOLEAN
local
  feb17: BIRTHDAY
  bb: BIRTHDAY_BOOK
  a: ARRAY[NAME]
  l_name: NAME
  l_birthday: BIRTHDAY
  jack,jill,max: NAME
do
  comment("t1: test birthday book")
  create jack.make ("Jack"); create jill.make
  create max.make ("Max")
  create feb17.make (02, 17) -- Feb 17
  create bb.make
  -- add birthdays for Jack and Jill
  bb.put (jack, [14,01]) -- Jan 14
  bb.put (jill, [17,02]) -- Feb 17
  Result := bb.model.count = 2
    and bb.model[jack] ~ [14,01]
    and bb.model[jill] ~ [17,02]
    and bb.out ~ "{ Jack -> (14,1), Jill -> (17,2) }"
check Result end
-- Add birthday for Max
bb.put (max, [17,02])
assert_equal ("Max's birthday", bb.model[max], feb17)
-- Whose birthday is Feb 17th?
a := bb.remind ([17,02])
Result := a.count = 2
  and a.has (max)
  and a.has (jill)
  and not a.has (jack)
check Result end
-- check efficienthash table implementation
across bb.model as cursor loop
  l_name := cursor.item.first
  l_birthday := cursor.item.second
  check
    bb.imp.has (l_name)
    and then bb.imp[l_name] ~ l_birthday
  end
end
end

```



```

class BIRTHDAY inherit
    ANY
        redefine
            out
        end
create
    make, make_from_tuple
convert
    make_from_tuple ({TUPLE [INTEGER, INTEGER]})

feature {NONE} -- Initialization

    make (a_month: INTEGER; a_day: INTEGER)
        -- Initialization for `Current'.
        do
            month := a_month
            day := a_day
        end

    make_from_tuple (t: TUPLE [day: INTEGER; month: INTEGER])
        require
            t.count = 2
            attached {INTEGER} t.day
            attached {INTEGER} t.month
        do
            make (t.month, t.day)
        end

feature
    day: INTEGER
    month: INTEGER

```

# You'd rather discover the bug...

## Fault could send Jaguars into reverse

By GRAHAM TIBBETTS

JAGUAR has recalled thousands of cars after discovering a gearbox fault that could send them into reverse at high speed.

The problem, traced to computer software, could cause drivers to lose control, safety experts said. But in most cases it would wreck the gearbox and engine.

The company has recalled 68,000 vehicles, including 14,000 in Britain.

The ranges affected are the top-of-the-range XJ model, which costs from £65,000, the S-Type, which costs up to £47,000, and the £59,000 XK coupe. Those at risk were all built before June 2003.

The recall, which is expected to cost the company millions of pounds, follows

four cases of the gearboxes selecting reverse.

The Premiership footballers Michael Owen and Alan Shearer were believed to have been among those contacted, along with Gabby Logan, the television sports presenter.

A Jaguar spokesman said yesterday that if oil pressure in the transmission system reached a very low point a warning light would come on.

"In this condition it is possible that reverse could be selected by mistake," he said.

"There have been four instances of this problem, including one in the UK, but there were no crashes and no one was hurt."

The company said the repair work, involving the reprogramming of the transmission control module, would take about one hour.

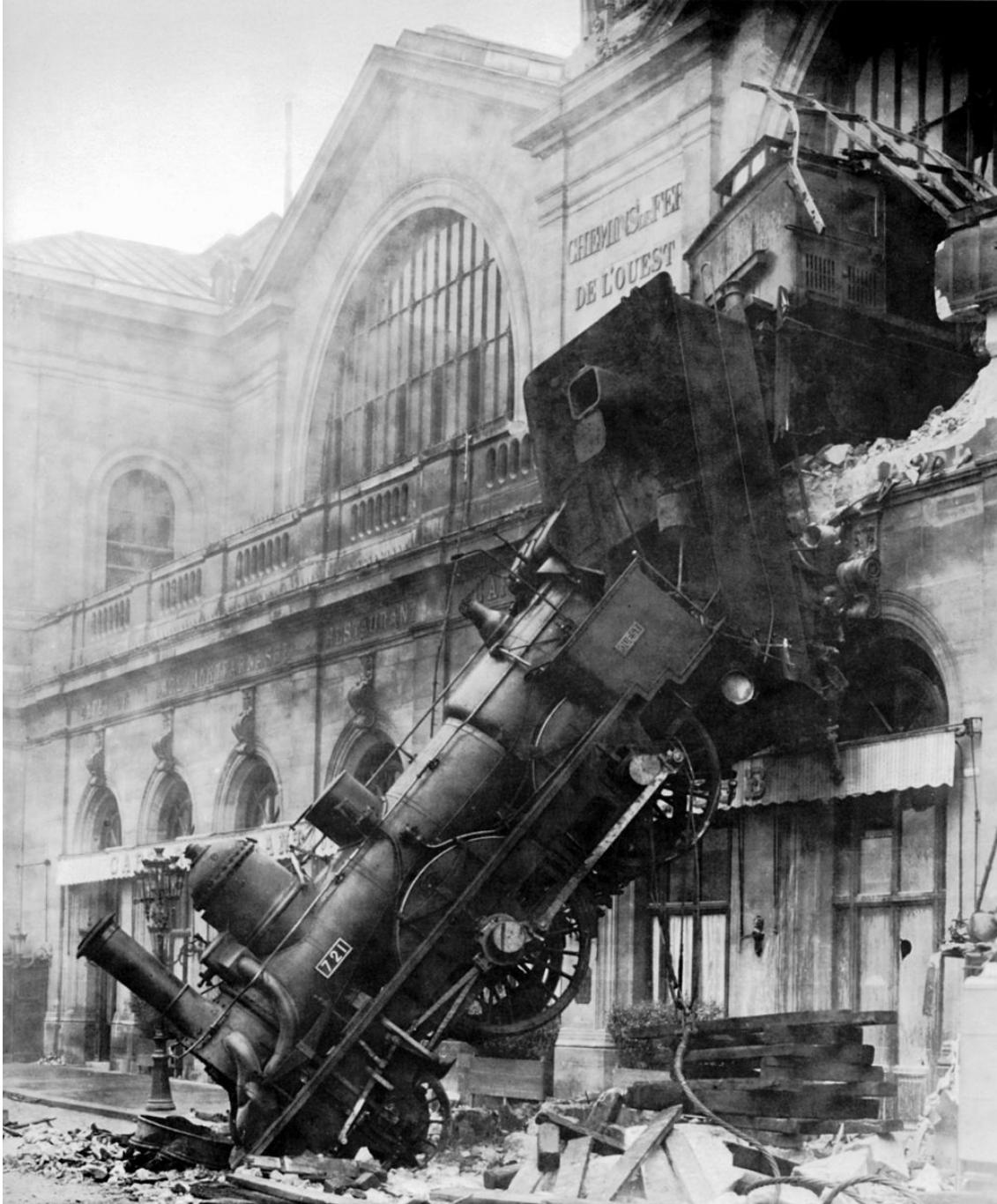


... before your users discover, on your behalf, that in fact:

WHEN Oil Pressure Low  
AND *unspecified conditions*  
THEN Reverse Gear Engages  
Automatically on the Highway  
AND 68,000 formerly loyal customers  
spend a day visiting their garage

# Some recent software disasters

- Bay Area Rapid Transit new extension two years behind due to errors
- Uber and Tesla self-driving car crashes
- Court software is so awful it's getting people wrongly arrested
- FAA Requiring Airlines to Reboot Dreamliners Every Three Weeks
- Software Error crashes Mars Lander
- Stanford Mall robot runs over small child
- Nanaimo doctors say electronic health record system unsafe, should be shut down
- Google to cloud customers: Sorry, but here's how two bugs knocked us out worldwide
- A bug in fMRI software could invalidate 15 years of brain research
- Volvo recalls 59,000 cars over software fault
- Patch Linux now, Google, Red Hat warn, over critical glibc bug
- Billion-dollar mistake: How inferior IT killed Target Canada
- Centrelink blames computer glitch for wrongly billing 73,000 customers



## Investigating the use of analysis contracts to improve the testability of object-oriented code

L. C. Briand\*,†, Y. Labiche and H. Sun



**Contracting -- order of magnitude improvement in empirical tests**

Another important result shown to be very strong and of high practical significance is that diagnosability, as we measure it, improves nearly an order of magnitude between mutant programs without contract assertions and those with contract assertions, regardless of the level of precision. This suggests significant savings during debugging, as faults will be much easier to locate if contracts are being instrumented and checked during execution.

In conclusion, our overall results suggest that instrumented contracts have a strong potential in terms of decreasing the cost of testing. Furthermore, they do not need to be defined and instrumented at a high level of precision to be useful. Those results are the outcome of a carefully planned and designed study and can be replicated on other system examples, using well-defined procedures and a commercial tool. Replication is essential in order to confirm the results we obtained here.

**Contracting -- strong decrease in cost of testing**

\*They cannot be detected by instrumentation, but can be detected by exception tracking, which provides information regarding where the exception was raised.

# Unix string concatenation

Let's use Linux string concatenation (strcat) to concatenate a string to itself, e.g.

```
# include <stdio.h> /* For printf() */
# include <string.h> /* For strcat() */
int main (void)
{
    char s[11] = "hello";
    strcat(s,s);
    printf("%s\n",s);
    return 0; //program exits successfully
}
```

/\* What happens?  
Hopefully:  
"hellohello"  
\*/

# Prism Linux

red% more append.c

```
# include <stdio.h> /* For printf() */
# include <string.h> /* For strcat() */
int main (void)
{
    char s[11] = "hello";
    strcat(s,s);
    printf("%s\n",s);
    return 0;
}
```

red% gcc append.c

red% ./a.out

Segmentation fault (core dumped) - centos6

red%

```
mac% ls  
append.c  
mac% more append.c
```

## On my Mac/Mojave

```
# include <stdio.h> /* For printf() */  
# include <string.h> /* For strcat() */  
  
int main (void)  
{  
  
    char s[11] =  
"hello";  strcat(s,s); printf("%s\n",s);  
  
    return 0; //program exits successfully  
}
```

```
mac% gcc append.c  
mac% ls
```

```
a.out      append.c
```

```
mac% ./a.out
```

```
Abort trap: 6
```

# Prism Linux

man strcat

STRCAT(3)

Linux Programmer's Manual

NAME

strcat, strncat - concatenate two strings

SYNOPSIS

```
#include <string.h>
char *strcat(char *dest, const char *src);
char *strncat(char *dest, const char *src, size_t n);
```

DESCRIPTION

The strcat() function appends the src string to the dest string overwriting the '\0' character at the end of dest, and then adds a terminating '\0' character. The strings may not overlap, and the dest string must have enough space for the result.

# Testing the informal documentation

## ➤ Testing string concatenation on several platforms yields

- different results depending on the platform:
- crashes due to segmentation error (Solaris 5.6).
- crashes due to uncaught signal (macos Abort trap: 6).
- crashes due to arithmetic error (!?).
- hangs in an infinite loop.
- success (yields “hellohello”).

# Contracts for strings

**append** (s: STRING)

-- append copy of 's' at end of Current.

**require**

*argument\_not\_void:*

s /= Void

*argument\_must\_be\_different:*

s /= Current

**external**

-- C code goes here

**ensure**

*new\_count:*

count = old count + old s.count

*argument\_appended:* -- try your skill ?

*old\_prefix\_unchanged:* -- try your skill ?

**end**

```
class EIFFEL_WITH_C
feature
    max3 (x, y, z: REAL_64): REAL_64
        external
            "[
                C use "eiffel_with_c.h"
            ]"
        alias "maxThree"
end
```

```
double maxThree(double x, double y, double z) {
    if (x>=y)
    {
        if(x>=z)
            return x;
        else
            return z;
    }
    else
    {
        if(y>=z)
            return y;
        else
            return z;
    }
}
```

# C++ Core Guidelines: A Short Detour to Contracts in C++20

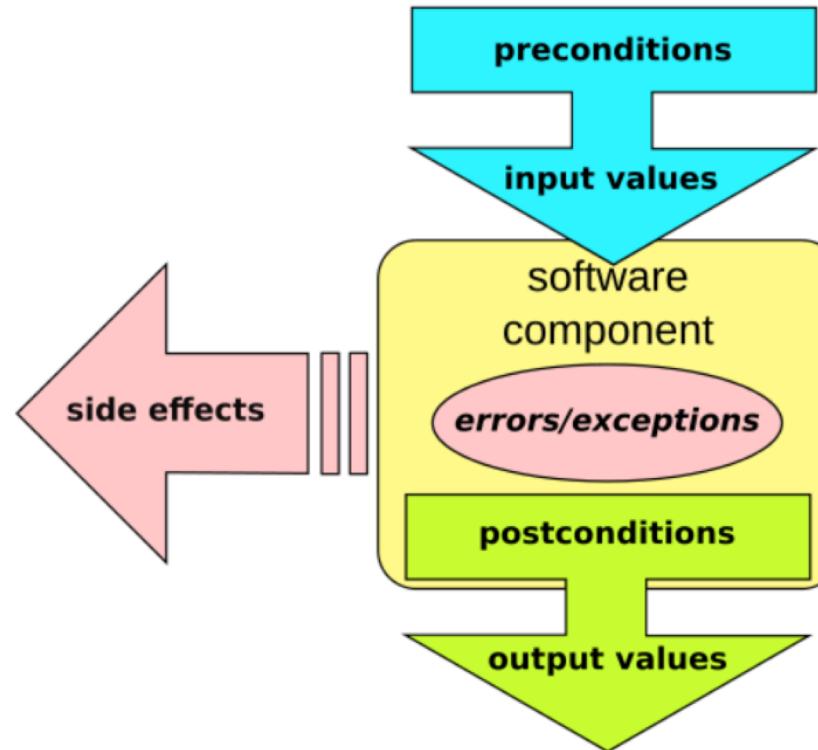
20 July 2018

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My original plan was it to write in this post about the next rules to error handling. But I changed my plan to write about the future: contracts in C++20.



# Ariane-5



- On June 4, 1996, the maiden flight of the European Ariane 5 launcher crashed about 40 seconds after takeoff.
- Media reports indicated that the amount lost was half a billion dollars -- uninsured.

# Ariane-5 investigation

- The CNES (French National Center for Space Studies) and the European Space Agency immediately appointed an international inquiry board, made of respected experts from major European countries, who produced their report in hardly more than a month
- Its conclusion: the explosion was the result of a software error -- possibly the costliest in history up to that point (at least in dollar terms, since earlier cases have caused loss of life).

## Ariane-5 investigation (2)

- The exception was due to a floating-point error in the Inertial Reference System
- a conversion from a 64-bit integer to a 16-bit signed integer, which should only have been applied to a number less than  $2^{15}$ , was erroneously applied to a greater number, representing the "horizontal bias" of the flight.
- There was no explicit exception handler to catch the exception, so it followed the usual fate of uncaught exceptions and crashed the entire software, hence the on-board computers, hence the mission.

## Ariane-5 investigation (3)

- The Inertial Reference subsystem in the Ariane-5 was re-used from the Ariane-4 where the documented constraint was calculated to hold.
- That constraint never made it into the software code!

**convert (horizontal\_bias: INTEGER): INTEGER**

**require**

**horizontal\_bias <= Maximum\_bias**

-- from Ariane-4

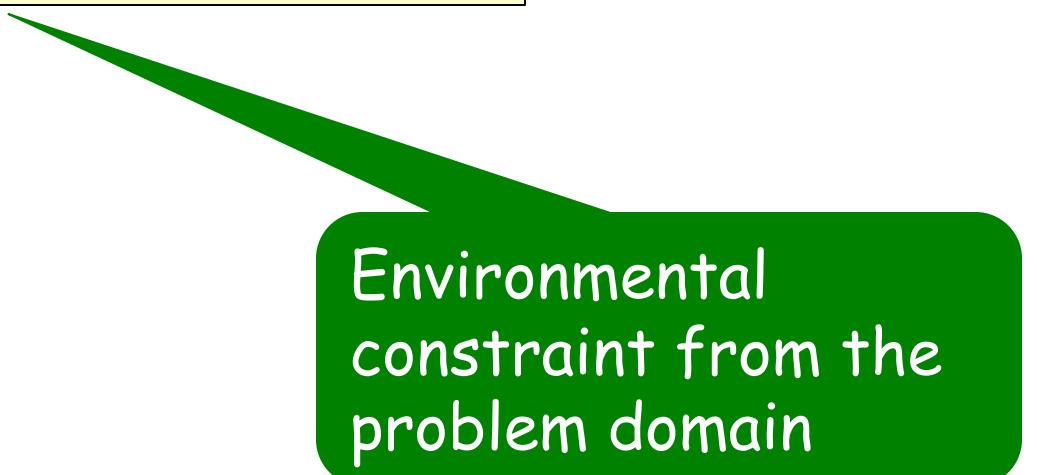
**do**

...

**ensure**

...

**end**



Environmental  
constraint from the  
problem domain

# How would the precondition have helped?

- Contracts are a prime component of the software and its documentation ("contract view" is produced automatically by tools).
- In an environment such as that of Ariane where there is much emphasis on thorough validation of everything, the contracts would be the QA team's primary focus of attention.

- Any team worth its salt would have checked systematically that every call satisfies the precondition.

# Hoare Logic

The meaning of a program statement  $S$  is described by a triple

$$\{ P \} \quad S \quad \{ Q \}$$

where  $P$  is called the **precondition**

$Q$  is called the **postcondition**

## Informal meaning

“when program  $S$  is started in a state satisfying  $P$ , all executions of  $S$  terminate in a state satisfying  $Q$ ”

# Hoare Logic

{ P }

S

{ Q }

{ ? }

}  $x := x - 1$  { ( $x + y < 0$ ) and ( $y = \text{old } y$ ) and ( $x = \text{old } x - 1$ )}

{ ? }

}  $x := x^*x$  {  $x^4 = 10$ }

# Hoare Logic

{ P }

S

{ Q }

{  $x + y < 1$  }  $x := x - 1$  { ( $x+y < 0$ ) and ( $y = \text{old } y$ ) and ( $x = \text{old } x - 1$ ) }

{ ? }  $x := x^*x$  {  $x^4 = 10$  }

{ P }  $\xrightarrow{S}$  { Q }

Weakest precondition  
calculation of precondition from postcondition

$\text{wp}(\text{"}x := \text{exp}\text{"}, Q) \triangleq Q[x := \text{exp}]$

In postcondition Q,

- replace (old x) by constant  $x_{-1}$
- replace (old y) by constant  $y_{-1}$
- {  $x=x_{-1} \wedge y=y_{-1} \wedge \dots ?$  }  $\xrightarrow{S}$  { Q }

# Hoare Logic -- replace (old x) by $x_{-1}$

{  $P$  }

$S$

{  $Q$  }

$\{x=x_{-1} \wedge y=y_{-1} \wedge ?\} \quad x := x*x \quad \{Q: x+y < 0 \wedge (y=y_{-1}) \wedge (x=x_{-1}-1)\}$

$\text{wp}(“x := x-1”, Q)$

= < replace by wp defn.>

$Q [x := x-1]$

= <replace  $Q$  by its defn>

$(x+y < 0 \wedge (y = y_{-1}) \wedge (x = x_{-1} - 1)) [x := x-1]$

= < do the substitution for  $x$ >

$(x-1)+y < 0 \wedge (y = y_{-1}) \wedge ((x-1) = x_{-1} - 1)$

= < arithmetic and Leibniz>

$(x+y < 1) \wedge (y = y_{-1}) \wedge (x = x_{-1})$

# Hoare Logic -- replace (old x) by $x_1$

{ P }

{ $x = x_1 \wedge ?$ }

S

$x := x * x$

{ Q }

{Q:  $x^4 = 10$ }

`wp("x := x*x1", Q)`

= < replace by wp defn.>

$Q [x := x * x]$

= <replace Q by its defn>

$(x^4 = 10) [x := x*x1]$

= < do the substitution for x>

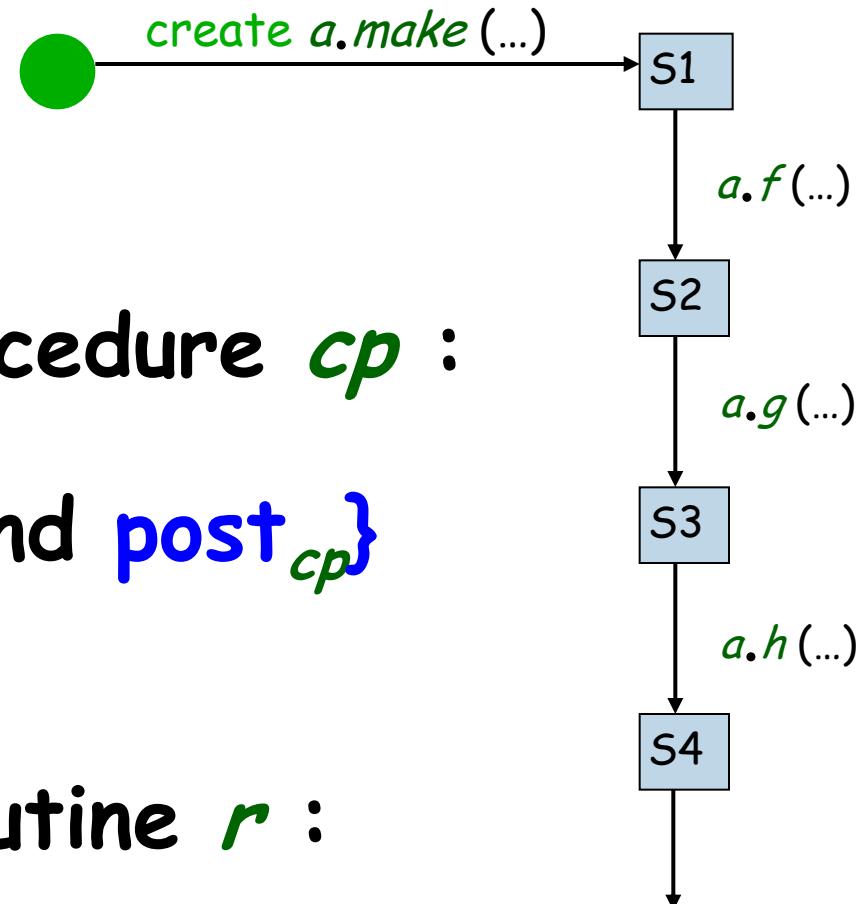
$(x * x)^4 = 10$

= < arithmetic and Leibniz>

$x^8 = 10$

Week	Date	Labs	Weights	Required Readings
1	Thu 03 Jan	Lab0		OOSC2 Chapters 7 and 8 (Classes vs. Objects, Reference vs. Value Types)
2	Mon 07 Jan	Lab1	3%	OOSC2 Chapter 11.1-11.9 (Specifications, Design by Contract)
3	Mon 14 Jan	Lab1		OOSC2 Chapter 6 (Abstract Data Types)
4	Mon 21 Jan	Lab2	3%	OOSC2 Chapter 10 (Genericity)
5	Mon 28 Jan	Lab3	4%	OOSC2 Chapter 14 (Inheritance)
6	Mon 04 Feb	Lab4	5%	OOSC2 Chapter 15 (Multiple Inheritamce)
7	Mon 11 Feb	Lab4		OOSC2 Chapter 11.10 -11.15 (DbC, ADTs and loop variants/inv)
<b>Mon 18 Feb</b>			<b>OOSC2 Chapter 21 (Undo/redo Design pattern)</b>	
8	Mon 25 Feb	Labtest 1	10%	OOSC2 Chapter 12 (Broken contract, exceptions)
9	Mon 04 Mar	Project		OOSC2 Chapter 17 (Class as a merge of Typing/Modularity)
10	Mon 11 Mar	Labtest 2	10%	OOSC2 Chapters 20, 23.1, 23.4, 23.8 (Design of Classes)
11	Mon 18 Mar	Lab 5	5%	OOSC2 Chapters 1-3 (Software Quality/Modularity)
12	Mon 25 Mar	Project	15%	OOSC2 chapter 18 (Global constants)
13	Mon 01 April			OOSC2 Chapter 26 (A Sense of Style)
5-20, April		Exam	45%	See also <i>Touch of Class</i>

# The correctness of a class



For every creation procedure  $cp$  :

$\{\text{pre}_{cp}\} \text{ do}_{cp} \{\text{INV and post}_{cp}\}$

For every exported routine  $r$  :

$\{\text{INV and pre}_r\} \text{ do}_r \{\text{INV and post}_r\}$

- Any team worth its salt would have checked systematically that every call satisfies the precondition, i.e.
- {INV & Pre} sri.convert(horizontal\_bias) {INV & post}

```
{horizontal_bias <= Maximum_bias}  
sri.convert(horizontal_bias)  
{INV & post}
```

- Any team worth its salt would have checked systematically that every call satisfies the precondition, i.e.
- {INV & Pre} sri.convert(horizontal\_bias) {INV & post}

```
{horizontal_bias <= Maximum_bias}  
sri.convert(horizontal_bias)  
{INV & post}
```

- Do the above check either via calculation or run-time assertion checking
- That would have immediately revealed that the Ariane 5 calling software did not meet the expectation of the Ariane 4 routines that it called.

- The Inquiry Board made a number of recommendations with respect to improving the software process of the European Space Agency. Many are justified; some may be overkill; some may be very expensive to put in place.
- There is a more simple lesson to be learned from this unfortunate event:
- **REUSE WITHOUT A CONTRACT IS SHEER FOLLY**



If they stop explosions ...  
Contracts are cool!



# a\_other.pair is a qualified call

```
note
    description: "Two members make a team"
class
    MEMBER
feature
    team_mate: detachable like Current

    pair (a_other: like Current)
        do
            team_mate := a_other
            a_other.pair (Current) -- problematic!
        end
invariant
    team_mate.team_mate = Current -- problematic?
end
```

```

team_mate: detachable MEMBER

pair(other: like Current)
  do
    team_mate ::= other
  end

```

```

t0: BOOLEAN
local
  m1, m2: MEMBER
do
  comment ("t0: test symmetry pairing team mates")
  create m1
  create m2
  m1.pair (m2)
  Result := m1.team_mate = m2 and m2.team_mate = m1
  check
    Result
  end
end

```

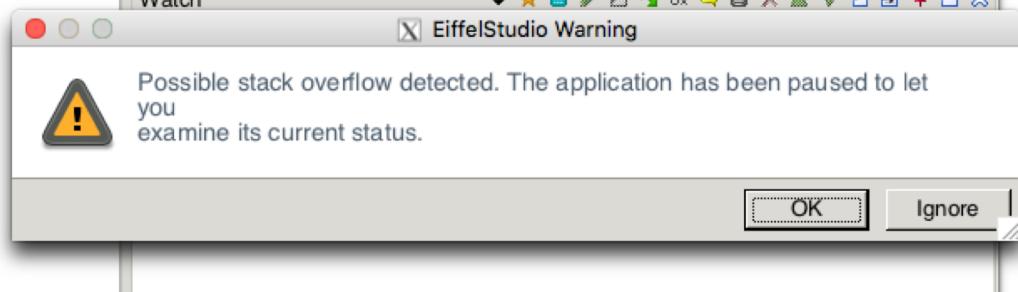
Call Stack

Status = Implicit exception pending

CHECK\_VIOLATION raised

In Feature	In Class	From Class	@
► t0	* TESTS	TESTS	6
► fast_item	PREDICATE	FUNCTION	0
► item	PREDICATE	FUNCTION	5
► run	☒ ES_BOOLEA...	ES_BOOLEA...	3
► run_es_test	☒ TESTS	ES_TEST	20
► run_es_test	ROOT	ES_SUITE	9
► run_espec	☒ ROOT	ES_TESTABLE	2
► make	ROOT	ROOT	4

```
team_mate: detachable MEMBER  
  
pair(other: like Current)  
  do  
    team_mate := other  
    other.pair (Current)  
  end
```



```

class MEMBER
feature
    team_mate: detachable MEMBER

    pair(other: like Current)
        do
            team_mate := other
--            other.pair (Current) -- stack overflow
            other.imp_pair (Current)
        end

feature{MEMBER}
    imp_pair(other: like Current)
        do
            team_mate := other
        end

invariant
    spouse_of_spouse:
        attached team_mate as mate
        and then attached mate.team_mate
        implies
        mate.team_mate = Current
end

```

# Complementarity of Tests and Contracts

Specification tests  
vs  
Unit Tests

# Square root test - precision?

epsilon: REAL = .001

test\_square\_root\_of\_ten: BOOLEAN

local

m: MATH

d: REAL

do

create m

d := 10 - (m.sqrt (10) \* m.sqrt (10))

Result := d.abs <= epsilon

end

$$|\sqrt{10} * \sqrt{10} - 10| \leq .001$$

# Tests vs. Contracts

## ➤ Test

Result :=

$$(m.\text{sqrt}(10) * m.\text{sqrt}(10) - 10).\text{abs} \leq m.\text{epsilon}$$

## ➤ Contract

$$(\text{Result} * \text{Result} - x).\text{abs} \leq \text{epsilon}$$

- The contract is a more general specification of the correct behaviour than the test
- The unit test can be used to exercise and verify the contract.  
i.e. the test “amplifies the contract”

**epsilon**: REAL

**sqrt** (x:REAL): REAL

-- return square root of `x'

**require**

**non\_zero**:  $x \geq 0$

**local**

guess: REAL

**do**

**from**

guess := 1

**until**

$(\text{guess}^* \text{guess} - x).abs \leq \text{epsilon}$

**loop**

guess := .5\*(guess + x/guess)

**end**

Result := guess

**ensure**

**result\_accurate**:  $(\text{Result} * \text{Result} - x).abs \leq \text{epsilon}$

**epsilon\_unchanged**: epsilon = old epsilon

**end**

# Unit Test

```
t0: BOOLEAN
local
    s: SQUARE_ROOT
    sqrt10: REAL_64
do
    comment("t0: Unit Test for sqrt")
    create s.make
    sqrt10 := s.sqrt (10)
    Result := sqrt10 - 3.1623 <= s.epsilon
end
```

# Specification Test

```
t1: BOOLEAN
  local
    s: SQUARE_ROOT
    x: REAL_64
    r: RANDOM
    low, hi: REAL_64
  do
    comment("t0: Specification Test for sqrt")
    create r.make
    -- range of random numbers
    low := 0.01; hi := 20000.00
    create s.make
    across 1 | .. | 100000 as i loop
      x := r.real_item
      x := x * ( hi - low )
      r.forth
      Result := (x - s.sqrt (x)*s.sqrt (x)).abs
              <= s.epsilon
      check Result end
    end
  end
```

# Specification Tests

- Once you start thinking **specifications** (contracts) you can write specification tests in any language with a unit testing framework



# Loop Variants and Invariants

from

init statements

invariant

assertions for invariant

until

exit condition

loop

body statements

variant

integer expression

end

- always non negative
- body decreases value on every iteration

```

sum: INTEGER
sum_of(a: ARRAY[INTEGER])
    -- calculate the sum of all elements in array a
    local i: INTEGER;
    do
        from
            i := a.lower; sum := 0
        invariant
            a.lower <= i
            i <= a.upper + 1
        until
            i > a.upper
        loop
            sum := sum + a [i]
            i := i + 1
        variant
            a.upper + 1 - i
    end
end

```

Guarantees  
loop  
termination

```

max_of_array(t: ARRAY[INTEGER]):INTEGER
    -- maximum value of array `t'
    require
        not t.is_empty
    local
        i: INTEGER
    do
        from
            i := t.lower
            Result := t[t.lower]
    invariant
        t.lower <= i and i <= t.upper
        across t.lower |..| i as cr all
            Result >= t[cr.item]
        end
    until
        i = t.upper
    loop
        i := i + 1
        Result := Result.max (t[i])
--      if i = 4 then Result := 16 end -- coding error|
        variant
            t.upper - i
        end
    ensure
        across t.lower |..| t.upper as cr all
            Result >= t[cr.item]
        end
    end

```

```

max_of_array(t: ARRAY[INTEGER]
             -- maximum value of array t
             t1: BOOLEAN)
require
    not t.is_max
local
    i: INTEGER
do
    from
        i := 1
    Result := 0
invariant
    t.lower <= i and i <= t.upper
    across t.lower |..| i as cr all
        Result >= t[cr.item]
    end
until
    i = t.upper
loop
    i := i + 1
    Result := Result.max (t[i])
    if i = 4 then Result := 16 end -- coding error
variant
    t.upper - i
end
ensure
    across t.lower |..| t.upper as cr all
        Result >= t[cr.item]
    end
end

```

t1: BOOLEAN  
**local**  
 a: ARRAY[INTEGER]  
 am: MAX\_ARRAY  
**do**  
 comment("test\_max\_of\_array")  
**create** am  
 a := <<191, 32, 423, 16>>  
**Result** := am.max\_of\_array (a) = 423  
**end**

Feature

Flat view of feature `max\_of\_array` of class MAX\_ARRAY

```

model  MAX_ARRAY  max_of_array < > □ ×
do
  from
    i := t.lower
    Result := t [t.lower]
  invariant
    t.lower <= i and i <= t.upper
    across
      t.lower |..| i as cr
    all
      Result >= t [cr.item]
    end
  variant
    t.upper - i
  until
    i = t.upper
  loop
    i := i + 1
    Result := Result.max (t [i])
    if i = 4 then
      Result := 16
    end
  end
end

```

LOOP\_INVARIANT\_VIOLATION raised

In Feature	In Class	From Class	@
max_of_array	MAX_ARRAY	MAX_ARRAY	8
t1	TESTS	TESTS	4
fast_item	PREDICATE	FUNCTION	0
item	PREDICATE	FUNCTION	5
run	ES_BOOLEA...	ES_BOOLEA...	3
run_es_test	TESTS	ES_TEST	22
run_es_test	ROOT	ES_SUITE	9
run_espec	ROOT	ES_TESTABLE	2
make	ROOT	ROOT	4

Call Stack | AutoTest | Favorites

Feature

model MAX\_ARRAY max\_of\_array

Flat view of feature `max\_of\_array' of class MAX\_ARRAY

```

max_of_array (t: ARRAY [INTEGER_32]): INTEGER_32
    -- maximum value of array `t'
    require
        not t.is_empty
    local
        i: INTEGER_32
    do
        from
            i := t.lower
            Result := t [t.lower]
        invariant
            t.lower <= i and i <= t.upper
        across
            t.lower |...| i as cr
        all
            Result >= t [cr.item]
        end
    variant
        t.upper - i
    until
        i = t.upper
    loop
        i := i
        Result := Result.max (t [i])
    
```

Status — implicit exception pending  
VARIANT\_VIOLATION raised

In Feature	In Class	From Class	@
► max_of_array	MAX_ARRAY	MAX_ARRAY	9
► t1	TESTS	TESTS	4
► fast_item	PREDICATE	FUNCTION	0
► item	PREDICATE	FUNCTION	5
► run	ES_BOOLEA...	ES_BOOLEA...	3
► run_es_test	TESTS	ES_TEST	22
► run_es_test	ROOT	ES_SUITE	9
► run_espec	ROOT	ES_TESTABLE	2
► make	ROOT	ROOT	4

Call Stack AutoTest Favorites

Watch

Expression	Value	Type
t[cr.item]	Error occurred (double...)	
...		

# Abstract Data Types

*This opened my mind, I started to grasp what it means to use the tool known as algebra. I'll be damned if anyone had ever told me before: over and again Mr. Dupuy [the mathematics teacher] was making pompous sentences on the subject, but not once would he say this simple word: it is a **division of labor**, which like any division of labor produces miracles, and allows the mind to concentrate all of its forces on just one side of objects, on just one of their qualities.*

Stendhal, *The Life of Henry Brulard*, 1836.

$$\cos^2(a - b) + \sin^2(a + b - 2 \times b)$$

- $STACK [G]$

## FUNCTIONS

- $put: STACK [G] \times G \rightarrow STACK [G]$
- $remove: STACK [G] \nrightarrow STACK [G]$
- $item: STACK [G] \nrightarrow G$
- $empty: STACK [G] \rightarrow BOOLEAN$
- $new: STACK [G]$

## AXIOMS

For any  $x: G, s: STACK [G]$

A1 •  $item (put (s, x)) = x$

A2 •  $remove (put (s, x)) = s$

A3 •  $empty (new)$

A4 • **not**  $empty (put (s, x))$

## PRECONDITIONS

- $remove (s: STACK [G])$  **require** **not**  $empty (s)$
- $item (s: STACK [G])$  **require** **not**  $empty (s)$

# Use Axioms to calculate

*item (remove (put (remove (put (put (remove (put (put (put (new, x1), x2), x3)), item (remove (put (put (new, x4), x5)))), x6)), x7)))*

= x4

- STACK [G]

## FUNCTIONS

- *put*: STACK [G] × G → STACK [G]
- *remove*: STACK [G] ↳ STACK [G]
- *item*: STACK [G] ↳ G
- *empty*: STACK [G] → BOOLEAN
- *new*: STACK [G]

## AXIOMS

For any  $x: G$ ,  $s: \text{STACK}[G]$

A1 •  $\text{item}(\text{put}(s, x)) = x$

A2 •  $\text{remove}(\text{put}(s, x)) = s$

A3 •  $\text{empty}(\text{new})$

A4 •  $\text{not empty}(\text{put}(s, x))$

## PRECONDITIONS

- *remove* ( $s: \text{STACK}[G]$ ) require  $\text{not empty}(s)$
- *item* ( $s: \text{STACK}[G]$ ) require  $\text{not empty}(s)$

# Abstract State Machine

```
class ABSTRACT_STACK [G -> attached ANY] inherit
  ANY
    redefine is_equal end
create
  make
feature {NONE}
  make
    do
      create model.make_empty
    end
```

```
feature -- model
  model: SEQ [G]
```

## Immutable Queries

```
feature -- Queries
  is_equal (other: like Current): BOOLEAN
    do
      Result := model ~ other.model
    end

  count: INTEGER
    -- number of items in stack
    do
      Result := model.count
    ensure
      Result = model.count
    end
```

```

top: G
    -- top of stack
require
    not model.is_empty
do
    Result := model[1]
ensure
    Result ~ model.first
end

```

**feature** -- model  
 model: SEQ [G]

**feature** -- Commands

```

push (x: G)
    -- push `x' on to the stack

```

```

do
    model.prepend (x)

```

```

ensure
    pushed_otherwise_unchanged:
        model ~ ((old model.deep_twin) |<- x)

```

```

end

```

pop

-- pop top of stack

```

require
    not model.is_empty

```

```

do
    model.remove (1)

```

```

ensure
    model ~ old model.deep_twin.tail

```

```

end

```

**end**

```

top: G
    -- top of stack
require
    not model.is_empty
do
    Result := model[1]
ensure
    Result ~ model.first
end

```

**feature -- model**  
**model:** SEQ [G]

**feature -- Commands**

```

push (x: G)
    -- push `x' on to the stack

```

```

do
    model.prepend (x)

```

```

ensure
    pushed_otherwise_unchanged:
        model ~ ((old model.deep_twin) |<- x)

```

```

end

```

Command  
prepend

```

pop
    -- pop top of stack

```

```

require
    not model.is_empty

```

```

do
    model.remove (1)

```

```

ensure
    model ~ old model.deep_twin.tail

```

```

end

```

Immutable Query  
prepended

# ADT vs. ASM

- $STACK [G]$

## FUNCTIONS

- $put: STACK [G] \times G \rightarrow STACK [G]$
- $remove: STACK [G] \nrightarrow STACK [G]$
- $item: STACK [G] \nrightarrow G$
- $empty: STACK [G] \rightarrow BOOLEAN$
- $new: STACK [G]$

## AXIOMS

For any  $x: G, s: STACK [G]$

$$A1 \bullet item(put(s, x)) = x$$

$$A2 \bullet remove(put(s, x)) = s$$

$$A3 \bullet empty(new)$$

$$A4 \bullet \text{not } empty(put(s, x))$$

## PRECONDITIONS

- $remove(s: STACK [G])$  require  $\text{not } empty(s)$
- $item(s: STACK [G])$  require  $\text{not } empty(s)$

```
top: G
    -- top of stack
require
    not model.is_empty
do
    Result := model[1]
ensure
    Result ~ model.first
end

feature -- Commands
push (x: G)
    -- push `x' on to the stack
do
    model.prepend (x)
ensure
    pushed_othewise_unchanged:
        model ~ ((old model.deep_twin) |<- x)
end

pop
    -- pop top of stack
require
    not model.is_empty
do
    model.remove (1)
ensure
    model ~ old model.deep_twin.tail
end

end
```

# For Descendants (inheritance = reuse)

```
note
    description: "[
        Infinite stack API,
        fully contracted using Mathmodels SEQ[G]
    ]"

class ABSTRACT_STACK [G -> attached ANY] inherit
    ANY
        redefine is_equal end
create
    make
feature {NONE}
    make
        do
            create imp.make_empty
        end

imp: SEQ[G]

feature -- model

model: SEQ [G]
    do
        Result := imp|
    end
```

```
class
  MY_STACK [ G -> attached ANY ]
inherit
ANY
  undefine is_equal end
```

```
ABSTRACT_STACK [ G ]
  redefine
    count,
    make,
    model,
    top,
    push,
    pop
  end

create
make
```

```
feature {NONE} -- creation
  implementation: LINKED_LIST [ G ]
  -- implementation of stack as array

feature -- model
  model: SEQ [ G ]
  -- abstraction function
  do
    create Result.make_empty
    from
      implementation.start
    until
      implementation.after
    loop
      Result.append (implementation.item)
      implementation.forth
    end
  end
```

```
feature {NONE} -- creation

    implementation: LINKED_LIST [G]
        -- implementation of stack as array
```

```
feature -- model

    model: SEQ [G]
        -- abstraction function
    do
        create Result.make_empty
        from
            implementation.start
        until
            implementation.after
        loop
            Result.append (implementation.item)
            implementation.forth
        end
    end
```

```
invariant

    same_count:
        model.count = implementation.count
    equality: across 1 |..| count as i all
        model [i.item] ~ implementation [i.item] end
    -- top of stack is model[1] and implementation[1])
end
```

```
pop
  -- pop top of stack
require -- from ABSTRACT_STACK
  not model.is_empty
do
  implementation.start
  implementation.remove
ensure -- from ABSTRACT_STACK
  model ~ old model.deep_twin.tail
end
```

```
push (x: G)
  -- push x on to the stack
do
  implementation.put_front (x)
ensure -- from ABSTRACT_STACK
  pushed_othewise_unchanged:
    model ~ ((old model.deep_twin) |<- x)
end
```

# Readings

- OOSC2 Chapter 11
- For introductory material, see Touch of Class  
(available online via Steacie)
  - ↳ For loop variants and invariants see Chapter 7.5

# What's wrong with `break`

| | Subject: AT& T Bug

| | Date: Fri Jan 19 12: 18: 33 1990

| |

| | This is the bug that caused the AT& T breakdown the other day:

| | In the switching software (written in C),

| |       there was a long do . . . while construct,

| |           which contained a switch statement,

| |           which contained an if clause,

| |           which contained a break,

| |           which was intended for the if clause,

| |           but instead broke from the switch.

- A missing “**break**” statement brought down the entire long-distance telephone network in the North Eastern US, resulting in millions of dollars of damage!

# Breaks/Go-Tos

- 1970, Edsger Dijkstra: don't use control structures other than one-entry/one-exit blocks ("structured programming").
- With one-entry/one-exit, you can read/reason about the code sequentially
  - ↳ You don't have to turn yourself into a computer and apply operational reasoning: "if when executing this instruction I'm coming from here it will satisfy this property, but if I am coming from there it will satisfy that other property, so in both cases ... it will be true that ... maybe ... wait a minute... etc." Humans are not computers!

# Breaks/Go-Tos

## ➤ Understanding a loop:

↳ **loop invariant**: property ensured by initialization and maintained by every iteration. Combined with the loop exit condition it allows the program reader to check, through a simple inspection of the loop text, that the loop is doing its job.

↳ **loop variant**: reason about termination by telling us which decreasing quantity guarantees that the loop will terminate.

# Structured Programming

- The key point is to be able to reason about a program statically, i.e. by associating properties with its text as given, rather than operationally, i.e. by trying to mimic its execution within your head.
- Computers are there to execute programs; humans can't really do it effectively for any non-trivial examples.
- The one-entry, one-exit structure helps us do something at which we are much better: static reasoning based on the simple rules of logic.

# Use Check Statements as well

- To know if all the strings in `my_list` have lengths greater than three characters, we could code:

`my_list: LIST[STRING]`

`check`

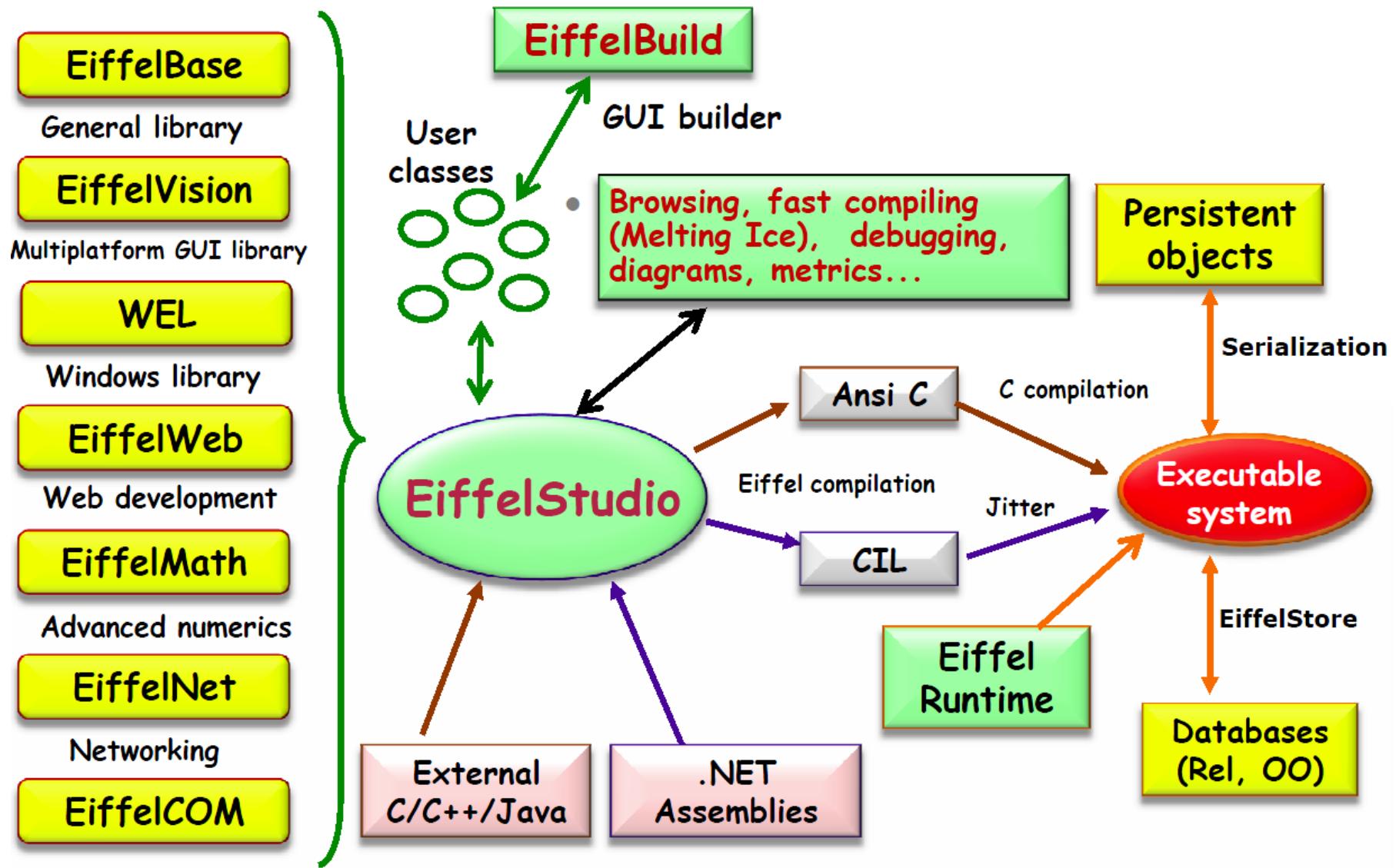
`across my_list as ic all ic.item.count > 3 end`

`end`

- Class `LIST` inherits from `ITERABLE`

>From: Thomas Beale (Chief Technology Officer, Ocean Informatics)  
>Date: Monday, May 04, 2009  
>To: eiffel software@yahoogroups.com

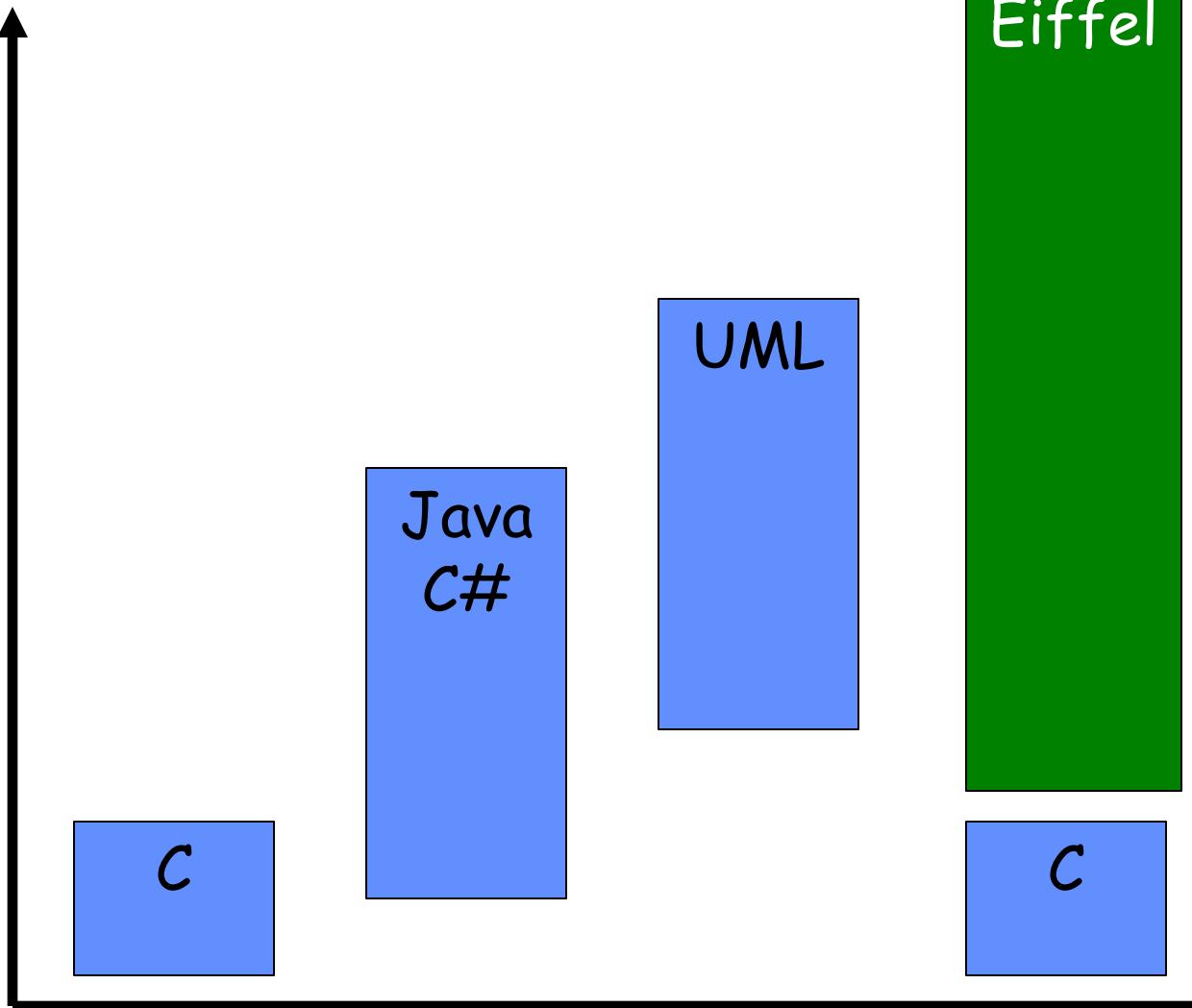
- I had also meant to say that another strength of Eiffel is that its semantics are very close to the theoretically ideal OO meta-model, so you don't have to continually perform workarounds when formalizing any design concept - all the basics are there - nested generics (that work; by contrast, see the horror that is UML generics);
  - ↳ multiple inheritance (that works, no need for 'aspect-oriented programming');
  - ↳ agents (a real source of power when performing recursive processing and event-handling), DbC and other features (let's not forget basics like covariant redefinition, uniform reference etc).
  - ↳ There are some things I would really like, that we do have to work around: the ability to distinguish between an association reference to another object and an aggregation reference (i.e. uses vs. part-of), and to mark which attributes should be persistable. But just try doing any clear design thinking in Java, and you soon see the difference.
- In the old days, 'design' was a largely non-computational exercise, sometimes using UML or other graphical tools to help understand things;
- today (and for at least 10 years) it has been possible to do serious 'design' using less documentary effort, and more formal tools.
- For me, this is in fact why I can't leave Eiffel - it is a killer design lab. Our little application built for openEHR (ADL workbench, a kind of compiler tool) is what enabled me to do the design of the 'archetype' language ADL (now an ISO standard 13606-2). While the design is not perfect, it is pretty coherent, and the defects are details rather than theoretical problems.



# Design Notation

- Abstraction
- Information hiding
- Seamlessness
- Reversibility
- Design by Contract
- Open-Closed principle
- Single choice principle
- Single model principle
- Uniform access principle
- Command-query separation principle
- Option-operand separation principle
- Style matters

## Abstract Expressive Power



**Modelling = a mental representation of a future system that**

- includes constraints from a possibly hostile Environment
- describes the Design Decisions/Patterns
- we can reason about the model and predict its behaviour
- The correctness of the program can be checked against the model
- it is included as part of the program text
- Single Model Principle

# Take home lesson from EECS3311

## ➤ The 3311-Ostroff Rule

↳ Always work one level of abstraction higher than where you started

BIRTHDAY\_BOOK

```
model: FUN[STRING, BIRTHDAY]
-- set of tuples [name, birthday]

put (a_name: STRING; d: BIRTHDAY)
ensure
    model ~ (old model) ▷ [a_name, d]
    -- symbol ▷ used for function override

remind (d: BIRTHDAY): ARRAY[STRING]
ensure
    Result.count = (model ▷ {d}).count
    ∀name ∈ (model ▷ {d}).domain: name ∈ Result
    -- symbol ▷ used for range restriction
```