

Assignment-2 :-

Q4:- Proofs :-

① Multinomial naive Bayes \rightarrow is a linear classifier

> We know that,

The likelihood of observing x provided class C_k ~~Multinomial naive Bayes classifier~~ is given by

$$P(x|C_k) = \frac{(\sum_i x_i)!}{\prod_i x_i!} \prod_i p_{ki}^{x_i} \quad \text{--- (1)}$$

Where, p_i = Probability that event i occurs

x = A feature vector (x_1, \dots, x_n)

C_k = class k

~~\rightarrow Now, if we express (1) in log-space,~~

~~log~~

\rightarrow Multinomial naive Bayes classifier,

$$P(C_k|x) = P(C_k) \prod_{i=1}^n p_{ki}^{x_i} \quad \text{--- (2)}$$

\rightarrow Expressing (1) in log-space,

$$\log(P(C_k|x)) \propto \log\left(P(C_k) \prod_{i=1}^n p_{ki}^{x_i}\right)$$

$$= \log(P(C_k)) + \sum_{i=1}^n x_i \log p_{ki}$$

$$= |b + w_k^T x| \quad \text{--- (3)}$$

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In ~~(3)~~,

$$b = \log(p(c_k)) \quad \text{and}$$

$$w_{ki} = \log(p_{ki})$$

→ As, we can see, ~~(3)~~ is a linear equation in log-space.

→ Hence, proved

Q-4:-

② Logistic regression \rightarrow linear classifier

\rightarrow We know that decision boundary for logistic regression is sigmoid function given by,

$$\boxed{\frac{1}{1 + e^{-\theta^T x}} = 0.5} \quad \text{--- ①}$$

$$\therefore 1 = 0.5 + 0.5(e^{-\theta^T x})$$

$$\frac{0.5}{0.5} = e^{-\theta^T x}$$

$$\therefore \boxed{e^{-\theta^T x} = 1} \quad \text{--- ②}$$

\rightarrow Taking natural log on both sides of --- ②

$$\ln(e^{-\theta^T x}) = \ln(1)$$

$$\therefore -\theta^T x = 0$$

$$\therefore \theta^T x = 0$$

$$\therefore \boxed{\sum_{i=0}^n \theta_i x_i = 0} \quad \text{--- ③}$$

→ As we ~~have~~ proved, for logistic regression decision boundary translates to linear boundary.

→ Hence, sequised.

Q1: Steps:

1. First get data in dataframes. We need convert labels to numeric values so that we can evaluate after predictions.
2. To perform Linear Discriminant Analysis(LDA), I am using Fisher's LDA method.
3. For fisher's LDA, first we need to calculate within class scatter matrix and between class scatter matrix for both given classes.
4. `get_within_class_scatter_matrix()` and `get_between_class_scatter_matrix()` functions do that.
5. Next, we need to solve standard eigen value problem and get all eigen values and eigen vectors.
6. From eigen value-eigen vector pairs we can see that top 2 values retain maximum variance. Hence, using those top 2 value-vector pairs and translating 4dimensional data to 2 dimensional data.
7. After calculating weights(W), we can perform " $X \text{ dot } W$ ", which will give required predictions

