

1 Chapter 2

1.1 Exercise 2.1

This exercise comes down to verifying that the three conditions are met such that the given collection τ of subsets of X (*open sets*) is indeed a *topology* on X

1.1.1 (a)

$\tau = \{ \{ 1 \} , \{ 1,2 \} , \{ 1,2,3 \} , \emptyset \} = \{ U_1, U_2 , U_3 , U_4 \}$ and $X = \{ 1,2,3 \}$

1. (i) X and \emptyset are elements of τ
2. (ii) τ is indeed closed under finite intersections, gives $\emptyset \in \tau$
3. (iii) τ is indeed closed under arbitrary intersection. $\bigcup_{\alpha \in A} U_{\alpha}$ is in τ