

PHYSICS Tutorial - 7

Q.1. $U_{AB} = \frac{C+C}{1+\frac{C^2}{C^2}} = C$



$U_{BA} = \frac{-C-C}{1+\frac{C^2}{C^2}} = -C$ i.e., velocity of light remained same

Q.2. According to newtonian mechanics, velocity = $0.9C + 0.9C = 1.8C$

According to special theory of relativity $U = \frac{U' + V}{1 + \frac{U'V}{C^2}}$

$U = 0.994C$

Q.3. The amount of work done will be changed in kinetic energy of e^- i.e. $W = K_2 - K_1$, here K_1 & K_2 are the kinetic energies of e^- with velocity v_1 & v_2 respectively.

$$K_1 = m_0 c^2 \left(\left(1 - \frac{v_1^2}{c^2} \right)^{-1/2} - 1 \right), \quad K_2 = m_0 c^2 \left(\left(1 - \frac{v_2^2}{c^2} \right)^{-1/2} - 1 \right)$$

$= 1.278 \times 10^5 \text{ eV}$

$K_2 = 3.423 \times 10^5 \text{ eV}$

$W = K_2 - K_1 = 2.145 \times 10^5 \text{ eV} = 3.434 \times 10^{-14} \text{ J}$

Q.4. Use relativistic formula of momentum.

$$p = mv = \frac{m_0 v}{\sqrt{1 - \frac{v^2}{c^2}}} = \frac{(E_0/c^2) \times 0.6c}{\sqrt{1 - (0.6)^2}} = 0.383 \frac{\text{MeV}}{c}$$

Q.5. $n=2$, $l=0, 1$ for $l=0$, $m_l=0 \rightarrow$ state 2s (one state)
 $l=1$, $m_l=-1, 0, 1 \rightarrow$ 2p (Three state)

since all these 4 states (1+3) have corresponding to $n=2$

So all have same energy i.e. $E_2 = -\frac{13.606}{n^2}$

$E_2 = -3.4015 \text{ eV}$

Q.6. $2^2P_{3/2}$, $L=1$, $2S+1=2 \rightarrow S=1/2$ & $J=3/2$

$$L = \sqrt{l(l+1)} \quad \cancel{\text{or}} \quad L_z = L \cos \theta = m_l \hbar, \quad m_l = -1, 0, +1$$

$$\cos \theta = \frac{m_l}{\sqrt{l(l+1)}} \Rightarrow \theta = 135^\circ, 90^\circ, 45^\circ$$

$$S = \sqrt{s(s+1)} \quad \cancel{\text{or}} \quad S_z = S \cos \theta = m_s \hbar, \quad m_s = -1/2, +1/2$$

$$\cos \theta = \frac{m_s}{\sqrt{s(s+1)}} \Rightarrow \theta = 44.7^\circ, 125.26^\circ$$

$$J = \sqrt{j(j+1)}, \quad J_z = J \cos \theta = m_j \hbar; \quad m_j = m_l + m_s = -3/2, -1/2, 1/2, 3/2$$

$$\cos \theta = \frac{m_j}{\sqrt{j(j+1)}} \Rightarrow \theta = 140.71^\circ, 104.96^\circ, 75^\circ, 39.25^\circ$$

Q.7. $3^2S_{1/2} \Rightarrow n=3, l=0, j=1/2, m_j = \pm 1/2$

$$3^2P_{1/2} \Rightarrow n=3, l=1, j=3/2, m_j = \pm 1/2, \pm 3/2$$

$$n=3, l=1, j=1/2, m_j = \pm 1/2$$

for P state $l=1, j=5/2$ is not possible.

for D state $l=2, j=7/2$ is not possible.