

Physics - 2 (ISB11PH11)

Tutorial - 7

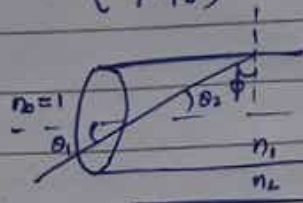
Q.1. For TIR $\mu_1(\text{core}) > \mu_2(\text{cladding})$, $\theta_c = \sin^{-1}\left(\frac{n_2}{n_1}\right)$

Q.2. (a) $n_1 = 1.48$, $n_2 = 1.44$

$$\theta_c = \sin^{-1}\left(\frac{n_2}{n_1}\right) = \sin^{-1}\left(\frac{1.44}{1.48}\right) \approx 76.65^\circ$$

(b) $\phi > \phi_c$

$$\begin{aligned}\theta_2 &= 90 - \theta_c \\ &= 90 - 76.65 \\ &= 13.35^\circ\end{aligned}$$



$\theta_2 < 13.35^\circ$ Angle of propagation.

(c) for θ_1 either $n_2 \sin \theta_1 = n_1 \sin \theta$

$$\sin \theta_1 = n_1 \sin \theta$$

$$\theta_1 < 1.48 \sin(13.35^\circ)$$

$$\theta_1 < 20^\circ$$

$$NA = \sin \theta_1 = \sqrt{n_1^2 - n_2^2} = \sqrt{2.1904 - 2.0730}$$

$$\theta_1 \approx 20^\circ$$

so Acceptance Angle $< 20^\circ$
 or
 Incidence Angle.

(d) yes.

Q.3. $n_1 = 1.5$, fraction diff $\Delta = 0.005$

$$\Delta = \frac{n_1 - n_2}{n_1} \Rightarrow n_2 = 1.4925$$

$$NA = \sqrt{n_1^2 - n_2^2} = \sqrt{2.25 - (1.49)^2} \approx 0.15$$

$$NA = \sin i \rightarrow i = \sin^{-1}(0.15) = 8.64^\circ$$

$$Q.4. \quad V = \frac{\pi d \times NA}{\lambda} = \frac{\pi d \sqrt{n_1^2 - n_2^2}}{\lambda} = \frac{3.14 \times 50 \times 10^{-6} \sqrt{(1.54)^2 - (1.5)^2}}{1500 \times 10^{-9}}$$

$$= 36.4$$

$$\text{no. of modes} = \frac{V^2}{2} = 662$$

$$Q.5. \quad NA = \sqrt{n_1^2 - n_2^2} = 0.348$$

$$\text{Acceptance Angle } i = \sin^{-1}(NA) = 20.4^\circ$$

$$\text{for steepest angle } \phi = \phi_c = \sin^{-1}\left(\frac{n_2}{n_1}\right) = \sin^{-1}(0.974) = 76.9^\circ$$

$$x = d \tan \phi_c = 50 \times 10^{-6} \tan(76.9) = 215.07 \mu\text{m}$$

$$\text{No. of reflection per meter } N = \frac{1}{215.07 \times 10^{-6}} \approx 4650 \text{ reflection}$$

$$Q.6. \quad V = \frac{\pi d \sqrt{n_1^2 - n_2^2}}{\lambda}$$

$$V = 2.405 \text{ for single mode}$$

$$\lambda = \frac{\pi d NA}{V} \rightarrow \frac{\lambda_1}{\lambda_2} = \frac{d_1}{d_2}$$

% change in core diameter

$$\frac{d_1 - d_2}{d_1} = \frac{\lambda_1 - \lambda_2}{\lambda_1} \times 100 = \frac{1.2 - 0.63}{1.2} \times 100 \approx 47.5\%$$

$$Q.7. \quad \text{loss/km in dB} = \frac{10}{L} \log_{10} \frac{P_{out}}{P_{in}}$$

$$= -10 \log_{10} \left(\frac{25}{100} \right) \cdot \frac{1}{0.5}$$

$$= 20(2 - 1.39) \approx 12.042 \text{ dB/km}$$