

Physics - 2 (ISB/PH211)

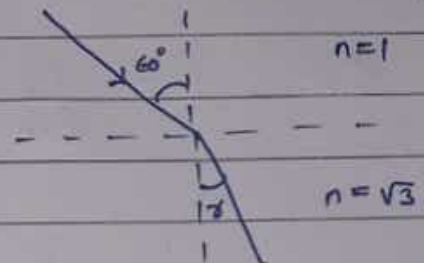
Tutorial - 6

Q.1. $n = \sqrt{3}$, $i = 60^\circ$

$$1 \times \sin 60 = \sqrt{3} \sin r$$

$$\frac{\sqrt{3}}{2} = \sqrt{3} \sin r$$

$$r = 30^\circ$$



$$r_{11} = \left(\frac{E_{OR}}{E_{OI}} \right)_{11} = \frac{n_1 \cos \theta_2 - n_2 \cos \theta_1}{n_1 \cos \theta_2 + n_2 \cos \theta_1} = \frac{\sqrt{3}/2 - \sqrt{3} \times 1/2}{\sqrt{3}/2 + \sqrt{3} \times 1/2} = 0$$

$$t_{11} = \left(\frac{E_{OT}}{E_{OI}} \right)_{11} = \frac{2n_1 \cos \theta_1}{n_1 \cos \theta_2 + n_2 \cos \theta_1} = \frac{2 \times 1 \times 1/2}{\sqrt{3}} = \frac{1}{\sqrt{3}} = 0.57$$

$$R = 0, \quad T = 1$$

Q.2. (i) Spontaneous emission :

is the process by which a quantum system such as an atom, molecule, nanocrystal or nucleus in an excited state undergoes a transition high energy to a state with a lower energy and emits quanta of energy.

(ii) Stimulated emission :

is the process by which an atomic electron from an excited state when interacts with EM wave of a certain frequency (ν), drops to a lower energy level and emits the energy with same frequency. In this process, the incident photon ($h\nu$) is not absorbed and the process is called Stimulated emission.

(iii) meta-stable state : is particular excited state of an atom, nucleus etc that has a longer lifetime than the ordinary excited state and that generally has a shorter lifetime.

(iv) Population inversion : describes that more atoms are in an excited state than in ground state, which is achieved by optical pumping. Such condition is called population inversion.

(v) optical pumping : is a process in which light is used to raise electrons from lower energy level in an atom or molecule to higher one.

$$Q.3. \quad P = \frac{E}{t \cdot A} = \frac{4 \times 10^{-3}}{10^{-9} \times 3.14 \times (1.5 \times 10^{-5})^2} = \frac{4 \times 10^{-3}}{3.14 \times 2.25 \times 10^{-19}} \\ = 5.7 \times 10^{15} \text{ watt/m}^2$$

$$Q.4. \quad n = 2.8 \times 10^9, \quad \lambda = 700 \text{ nm}$$

$$E = \frac{nhc}{\lambda} = \frac{2.8 \times 10^9 \times 6.6 \times 10^{-34} \times 3 \times 10^8}{700 \times 10^{-9}} \\ = 0.0792 \times 10^{-8} \text{ J}$$

$$Q.5. \quad \frac{N_2}{N_1} = \exp\left(-\frac{E_2 - E_1}{k_B T}\right) = \exp\left(-\frac{hc}{\lambda k_B T}\right)$$

$$\left. \frac{N_2}{N_1} \right|_{T=300\text{K}} = \exp\left(-\frac{6.6 \times 10^{-34} \times 3 \times 10^8}{700 \times 10^{-9} \times 1.38 \times 10^{-23} \times 300}\right) \\ = \exp\left(-\frac{19.8 \times 10^{-26}}{289800 \times 10^{-32}}\right) = \exp(-68.3 \times 10^{-6}) \\ = e^{-68.3}$$

$$\left. \frac{N_2}{N_1} \right|_{T=500\text{K}} = e^{-41.1}$$

$$Q.6. \quad \frac{B_{21}}{A_{21}} = \frac{\lambda^3}{8\pi h} \quad \therefore A_{21} = \frac{1}{\tau} = 10^6 \text{ --- (1)}$$

$$B_{21} = \frac{10^6 \times (600 \times 10^{-9})^3}{8 \times 3.14 \times 6.64 \times 10^{-34}} = 1.305 \times 10^{19}$$

Q.7. $P_0 = 10^2 \text{ W}$

$\eta = 1\%$

$\frac{P_0}{P_i} = \frac{1}{100} \quad \therefore P_i = P_0 \times 100 = 10^4 \text{ watt}$

Energy for 1 atom = $20 \text{ eV} = 20 \times 1.6 \times 10^{-19}$

$N = \frac{1}{20 \times 1.6 \times 10^{-19}} \text{ /s}$

$= 3.12 \times 10^{17} \text{ atoms/sec.}$