

Physics-2 (15B11PH211)Tutorial -10

Q.1. $a = 3.61 \text{ \AA}$

$$\frac{1}{\rho} = \sigma = \frac{ne^2\tau}{m} \rightarrow \tau = 2.37 \times 10^{-8} \text{ sec}$$

$m \rightarrow \text{in gram}$

$$a^3 = 4$$

$$n \text{ m}^3 = \frac{4}{a^3} \rightarrow n = \frac{4}{(3.61)^3} = 8.5 \times 10^{28}$$

$$V_d = \frac{eE\tau}{m} = 0.416 \text{ m/s}$$

Q.2. $f(\epsilon) = \frac{1}{e^{\frac{(\epsilon - \epsilon_F)}{kT}} + 1}$

probability of occupancy of ϵ $\epsilon - \epsilon_F = k_B T$

$$= \frac{1}{e^{kT/kT} + 1} = \frac{1}{e+1} \approx 0.268$$

Q.3. $\frac{1}{20} = \frac{1}{e^{\frac{0.1 \text{ eV}}{kT}} + 1}$

$$20 = e^{\frac{0.1 \text{ eV}}{kT}} + 1$$

$$2.94 = \frac{0.1 \times 1.6 \times 10^{-19}}{kT} = \frac{1.6 \times 10^{-20}}{T \times 1.38 \times 10^{-23}}$$

$$T = 394 \text{ K}$$

Q.4. $k_B T_F = E_F = \frac{h^2}{2m} \times \left(\frac{3}{8\pi} \frac{N}{V} \right)^{2/3}$

$$\rho = \frac{M}{V} = \frac{N \times m}{V}$$

$1 \text{ Kg} = \frac{N \times m}{27}$

$$n = 1 \text{ kg} = \frac{N_A \times 10^3}{27} \times 9 \quad \left(\frac{\text{atom} \times \text{kg}}{\text{kg} \times \text{m}^3} \right)$$

$$n = \frac{N}{V} = 18.07 \times 10^{28} / \text{m}^3 \rightarrow E_F = \frac{h^2}{2m} \times \left(\frac{3}{8\pi} \times 18.07 \times 10^{28} \right)^{2/3}$$

$$T_F = \frac{E_F}{k_B} = \frac{18.88 \times 10^{-19}}{1.38 \times 10^{-23}} = 13.68 \times 10^4 \text{ K} = 18.88 \times 10^{-19} \text{ J}$$

Q.5. $E_n = \frac{n^2 \pi^2 \hbar^2}{2m l^2}$

$$E_n = \frac{(n_x^2 + n_y^2 + n_z^2) \pi^2 \hbar^2}{8m l^2} \quad (\text{in 3D})$$

Given: $E_n = \frac{38 \pi^2 \hbar^2}{8 m l^2}$

$n_x \quad n_y \quad n_z \quad (\text{for } 38)$

6 1 1

1 6 1

1 1 6

5 3 2

5 2 3

3 5 2

2 5 3

2 3 5

3 2 5

9 fold degeneracy.

Q.6. (a) Assumption :-

- * valence e^- are treated as though they constitute an ideal Gas
- * Valence e^- are move freely in the volume of the solid.
- * the Attraction force b/w e^- & cation ions & Repulsion b/w e^- are insignificant

Merits :-

- * It explain the specific heat of free e^- .
- * It explain the temp. dependence of resistivity or Conductivity in metal.
- * It explain the dependence of ρ on e^- concentration.
- * ferromagnetism is also explain by him.

Demerit :-

- * It does not explain why are some metals & other non-metal.
- * It does not explain the conductivity of conductor, semiconductor & insulator.
- * It does not explain the e^- does not move under constant potential.

$$(b) \quad \vec{J} = neV_d = \frac{Teen}{m} \vec{E}$$

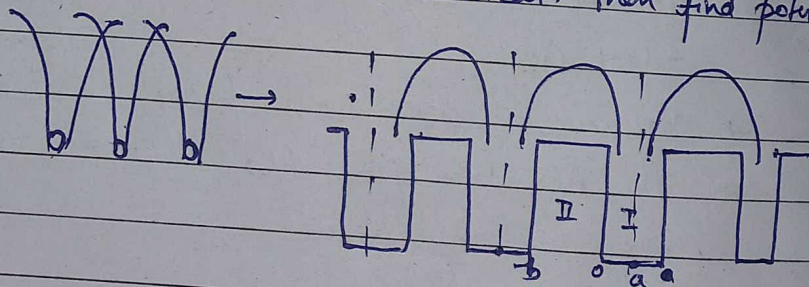
we've know ; $\vec{J} = \sigma \vec{E}$

$$\therefore \sigma = \frac{Teen}{m}$$

$$\sigma = \frac{ne^2 \tau}{m^*} = \frac{ne^2}{m^*} \frac{\lambda}{v_F}$$

(c) Bloch Theorem : ^{free} e^- move in periodic field provided by the lattice.

~~Q7~~ KP model : It is difficult to find ^{potential is} potential because ^{variable} so we assume it linear. then find potential



Q7.

$$\frac{P \sin \alpha a}{\alpha a} + \cos \alpha a = \cos k a = 1$$

$$\frac{P}{\alpha a} = \frac{1 - \cos \alpha a}{\sin \alpha a}$$

$$\frac{P}{\alpha a} = \frac{1 - (1 - \frac{\alpha^2 a^2}{2!} + \dots)}{(\alpha a - \frac{(\alpha a)^3}{3!} + \dots)} = \frac{\alpha^2 a^2}{2 \alpha a}$$

$$P = \frac{\alpha^2 a^2}{2} = \frac{2mE}{\hbar^2} \times \frac{a^2}{2} \rightarrow E = \frac{\hbar^2 P}{ma^2}$$