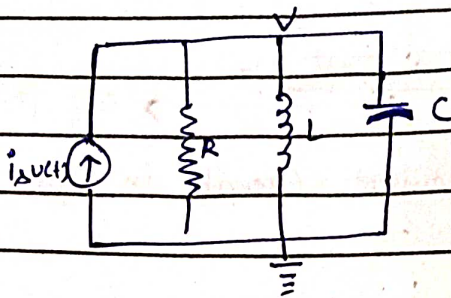


ES-2 (Take Away -2)

Q.1.



$$i_s = 8e^{-2t} \text{ A}$$

$$R = 6 \Omega$$

$$L = 7 \text{ H}$$

$$C = 1/42 \text{ F}$$

$$i + \frac{V}{R} + C \frac{dV}{dt} = i_s \quad \text{--- (1)}$$

$$V = L \frac{di}{dt} \quad \text{--- (2)}$$

$$\frac{dV}{dt} = L \frac{d^2i}{dt^2} \quad \text{--- (3)}$$

from (1), (2), (3) :

$$i + \frac{L}{R} \frac{di}{dt} + CL \frac{d^2i}{dt^2} = i_s \quad \text{--- (4)}$$

$$\frac{d^2i}{dt^2} + \frac{1}{RC} \frac{di}{dt} + \frac{1}{LC} i = \frac{i_s}{LC} \quad \text{--- (5)}$$

$$\cancel{\frac{d^2i}{dt^2}} + \cancel{\frac{1}{RC}}$$

from (4) & (5) we get :

$$\frac{d^2i}{dt^2} + 7 \frac{di}{dt} + 6i = 48e^{-2t} \quad \text{--- (6)}$$

$$i_f = Be^{-2t} \quad \text{--- (7)}$$

from (6) & (7) :

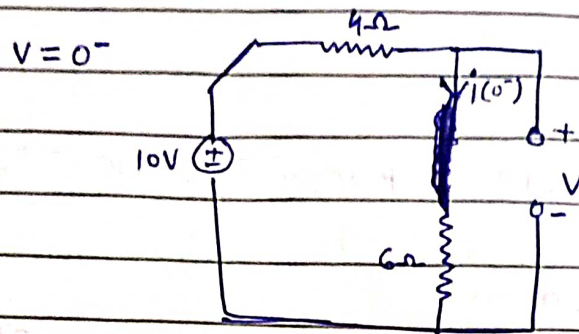
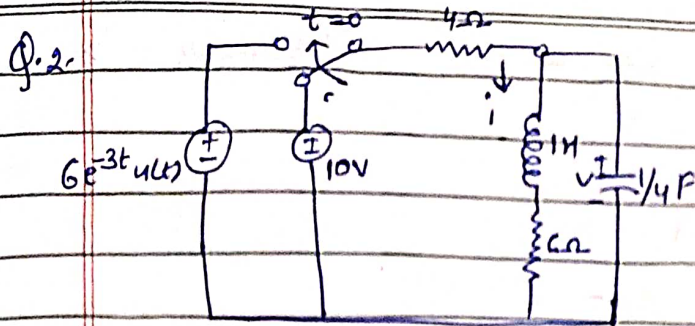
$$48e^{-2t} + 7(-2Be^{-2t}) + 6Be^{-2t} = 48e^{-2t}$$

$$(4 - 14 + 6) Be^{-2t} = 48e^{-2t}$$

$$\therefore B = -12$$

$$i_f = -12e^{-2t} \text{ A}$$

✓



$$V(0^-) = 6V$$

$$i(0^-) = \frac{10}{10} = 1A$$

After switch is thrown,

$$-V + \frac{di}{dt} + 6i = 0$$

$$\frac{V - V_s}{4} + i + \frac{1}{4} \frac{dV}{dt} = 0$$

$$\left(\frac{di}{dt} + 6i \right) - V = 0$$

$$i + \left(\frac{V}{4} + \frac{1}{4} \frac{dV}{dt} \right) = \frac{V_s}{4}$$

$$(s+6)i - V = 0 \quad \text{--- ①}$$

$$i + \frac{V}{4} + \frac{1}{4} sV = \frac{V_s}{4} \quad \text{--- ②}$$

from ① & ② -

$$((s+6)(s+1)+4)V = (s+6)V_s$$

$$(s^2 + 7s + 10)V = (s+6)V_s$$

$$\frac{d^2v}{dt^2} + 7\frac{dv}{dt} + 10v = \frac{dv_s}{dt} + 6v_s$$

CF :

$$(\lambda^2 + 7\lambda + 10) = 0$$

$$\lambda_1 = -2, \lambda_2 = -5$$

$$v_h = A_1 e^{-2t} + B_1 e^{-5t}$$

$$v_f = B e^{-3t}$$

v_s in diff. eq. :

$$9B e^{-3t} - 21B e^{-3t} + 10B e^{-3t} = -18e^{-3t} + 36e^{-3t}$$

$$B = -9$$

$$v_f = -9e^{-3t}$$

$$v = v_h + v_f = A_1 e^{-2t} + A_2 e^{-5t} - 9e^{-3t}$$

$$\therefore v(0) = 6$$

$$6 = A_1 + A_2 - 9$$

$$A_1 + A_2 = 15$$

$$\therefore i(0) = 1A$$

$$\frac{dv(0)}{dt} = ? \text{ at } t=0$$

$$\frac{dv}{dt} = -4i - v + v_s$$

$$\text{At } t=0,$$

$$\frac{dv(0)}{dt} = -4i(0) - v(0) + v_s(0) = -4 - 6 + 6 = -4$$

$$\frac{dv}{dt} = -2A_1 e^{-2t} - 5A_2 e^{-5t} + 27e^{-3t}$$

$$\text{At } t=0,$$

$$\frac{dv(0)}{dt} = -2A_1 - 5A_2 + 27 = -4$$

$$2A_1 + 5A_2 = 31$$

$$A_1 = \frac{44}{3}, A_2 = \frac{1}{3}$$

$$v = \frac{44}{3} e^{-2t} + \frac{1}{3} e^{-5t} - 9e^{-3t}$$