Day 21 Observers (implementation, design, and analysis)

AE353 Spring 2022 Bret1

example (control of platform angle, no gravity)

$$\begin{array}{c}
\dot{x} = Ax + Bu \\
\dot{y} = Cx
\end{array}$$

$$\begin{array}{c}
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$$\begin{array}{c}
\dot{x} = A\hat{x} + Bu - L \cdot (\hat{x} - y)
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 $\dot{y} = Cx$
 $\dot{x} = A\hat{x} + Bu - L(C\hat{x} - y)$

$$RUN \longrightarrow \left\{ \begin{array}{l} u(t) = -K \hat{\chi}(t) \\ \hat{\chi}(t+\Delta t) \approx (\hat{\chi}(t) + \Delta t) \left(A \hat{\chi}(t) + B u(t) - L \left(C \hat{\chi}(t) - y(t) \right) \right) \end{array} \right.$$

WHEN DOES IT WORK?

$$x_{err} = \hat{x} - \hat{x}$$

$$(A - LC)^{T} = A^{T} - (LC)^{T}$$
$$= A^{T} - C^{T}L^{T}$$

$$\dot{x} = A \times + B u$$

$$u = -U \times U$$

$$\dot{x} = (A - B \times U) \times U$$

xerr = (A-LC) xerr

















WHEN IS OBSERVER DESIGN POSSIBLE?

X = (A-BK) x controllable when

[B AB AB ... A" B]

is full rank

is the last

xerr = (A-LC) xerr obse

observable when

[CT ATCT (AT)2CT -- (AT)"CT]

is full rank

Xerr = (A-LC) Xerr

= Ax+ Bu-L(Cx-y)