

Huffman Coding

↳ lossless algorithm
data compression

string \rightarrow "a a b c d a g" \rightarrow 7×2 bytes or
 $7 \times 2 \times 8 = \underline{112 \text{ bits}}$
size of file

2 Hashmaps \approx

encoder

char	string
a	
b	
c	
d	

decoder

string	char
	a
	b
	c
	d

steps :

① pass the main string that we wanna compress
(data, aka feeder)

a is used 60 times

② make a frequency map \rightarrow

a	60
b	30
c	8
d	2

- ③ For every key in a frequency map, create a node and insert that node in a min heap/priority queue.

Node data : char data; int cost + frequency
 \downarrow \downarrow
 a 60

It will also have node left and right

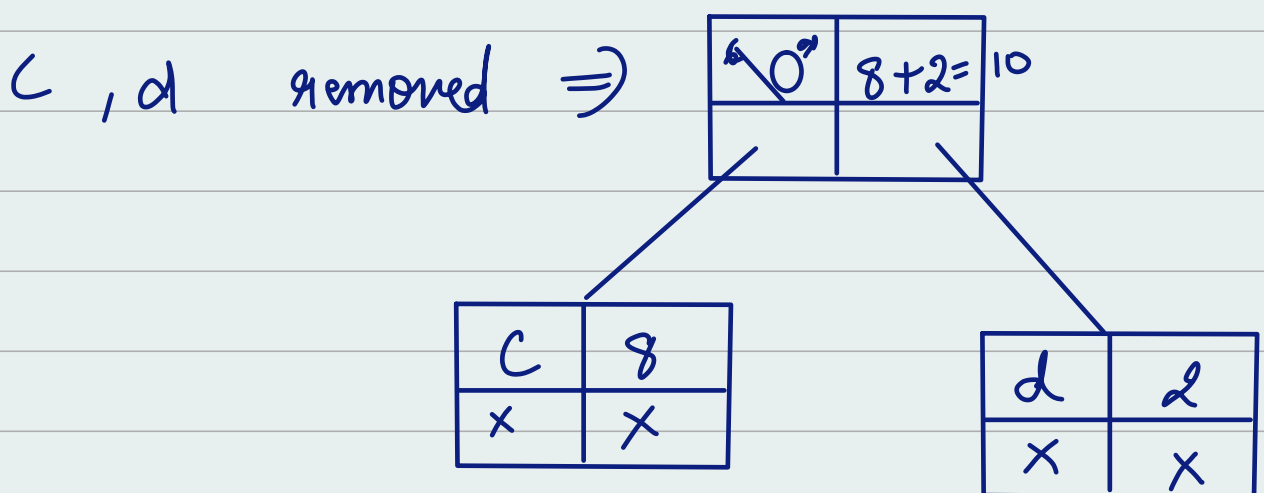
a	60
X	X

b	30
X	X

c	8
X	X

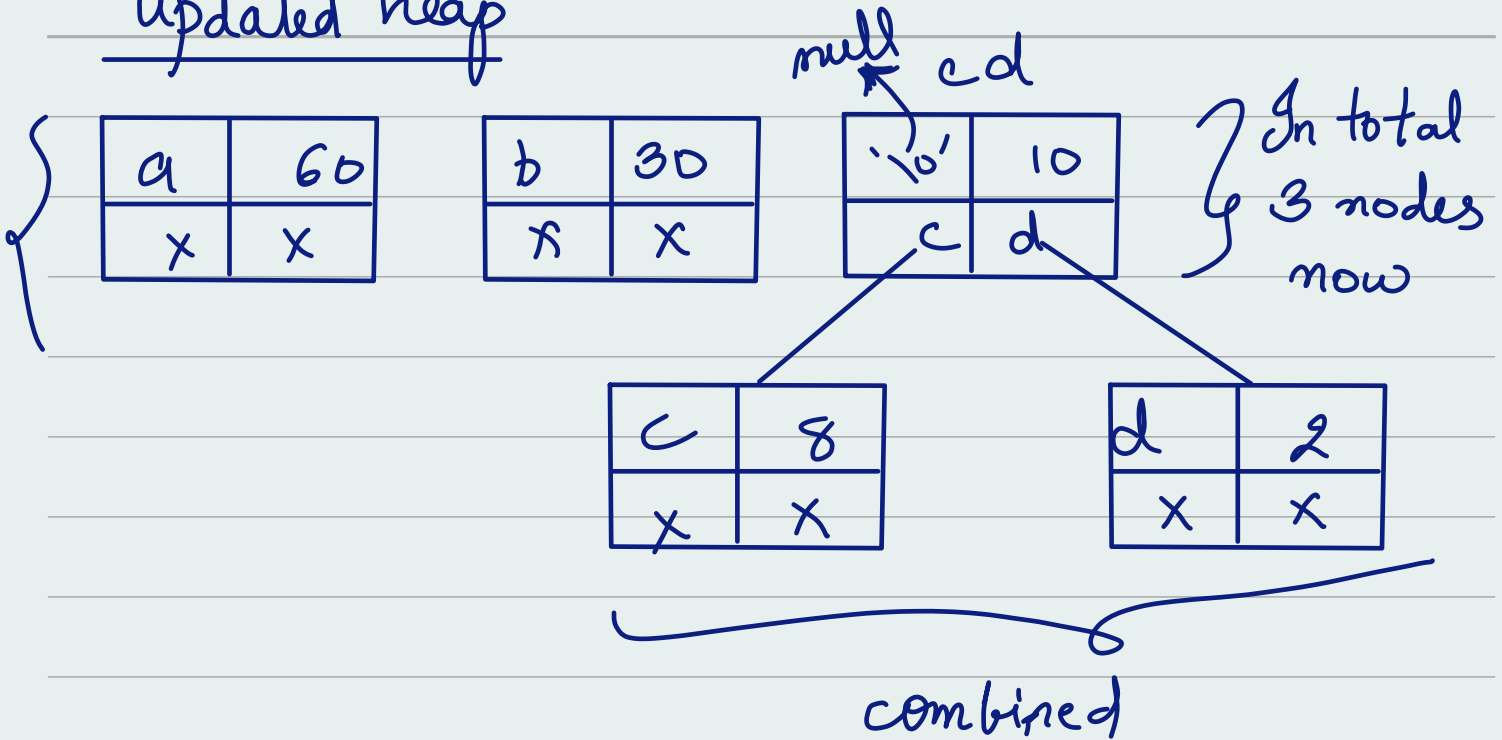
d	2
X	X

- ④ Remove 2 elements from heap & combine
 (c & d will be removed because it's min heap).

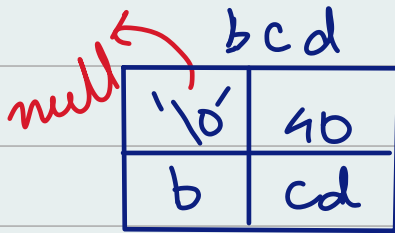


This can also be d & c (interchanged)
 is fine

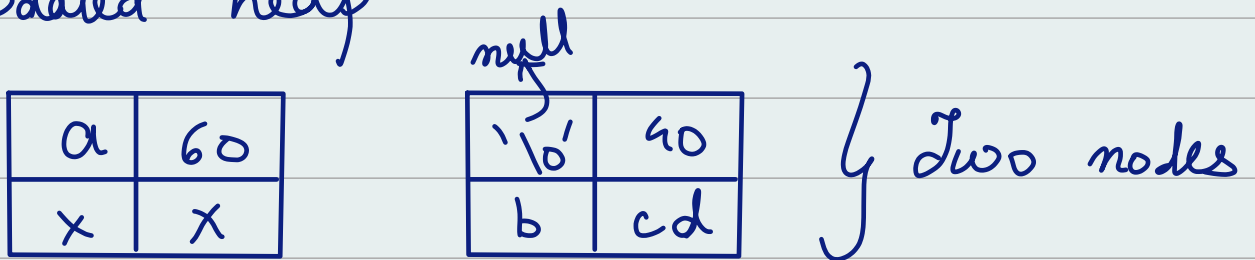
updated heap



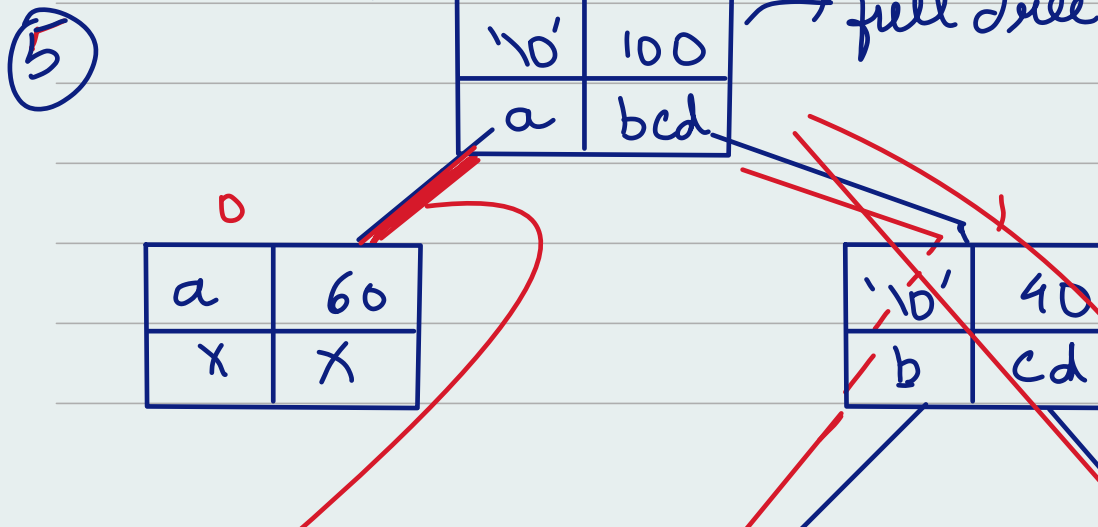
c d & b removed



updated heap



Now combined! a bcd



~~| | |
|---|----|
| b | 30 |
| x | x |~~
~~| | |
|----|----|
| 10 | 10 |
| c | d |~~
~~| | |
|---|---|
| c | 8 |
| x | x |~~
~~| | |
|---|---|
| d | 2 |
| x | x |~~

all the left will be zero and the right will be 1

encoder

decoder

⑥

a	0
b	10
c	110
d	111

Here no value is prefix of another value
 $a \rightarrow 0$ If a started from 0 no other element started from zero,

0	a
10	b
110	c
111	d

similarly b started with 10 no other element

started with 10 everyone is unique because of the tree structure

⑦ How to encode & decode?

string = a b b c c d a
 = 112 bits ($7 \times 2 \times 8$)

a b b c c d a

↓

0 10 10 110 110 111 0 → 15 bits

instead of 112 bits

→ Now converting back to original message
 → Does 0 exist; yes → a (In the encoder)
 → Does 1 exist, no Does 10 exist yes → b
 → again 10 → b similarly 11 → Slot existing
 110 → yes → c 110 → yes → c

011 → no 111 → yes → d
 0 → yes → a

a b b c c d a

Space complexity → $O(N)$

Time Complexity = $2 * (n-1)$ times

(Here every element is inserted or removed ^{so twice} but not the ^{very} first element that is why $(n-1)$)

$\approx O[n \log(n)]$ → Jc in heap for insertion or deletion

→ Code ~

