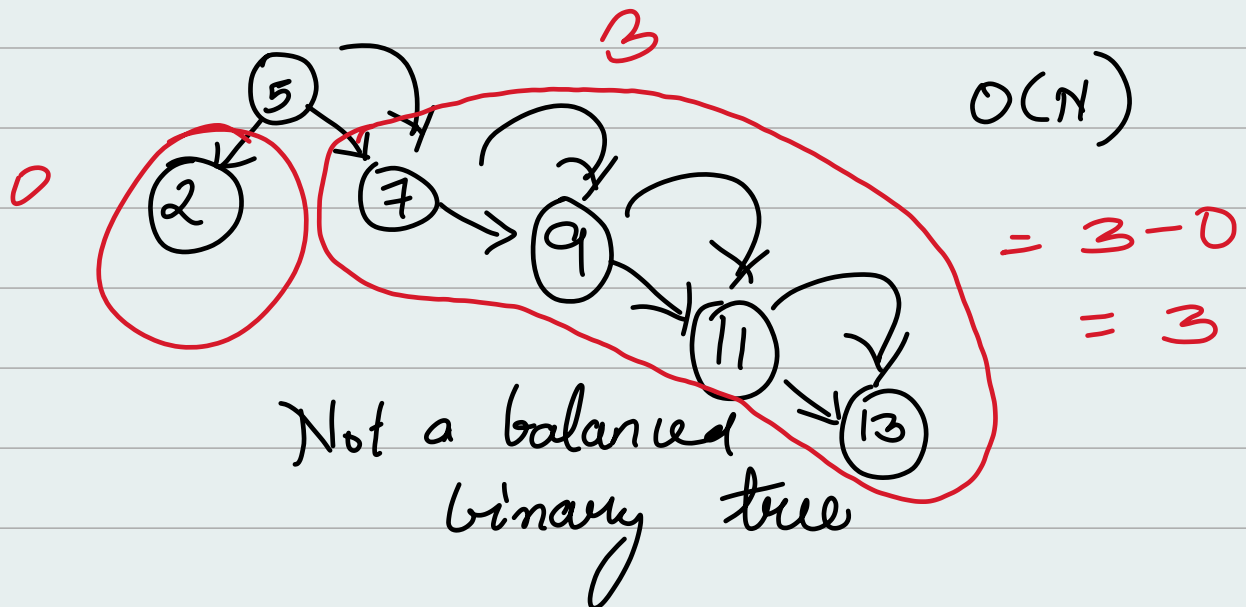


# AVL Trees ~

\* Not confusing

\* A lot of moving parts  $\rightarrow$  very simple.

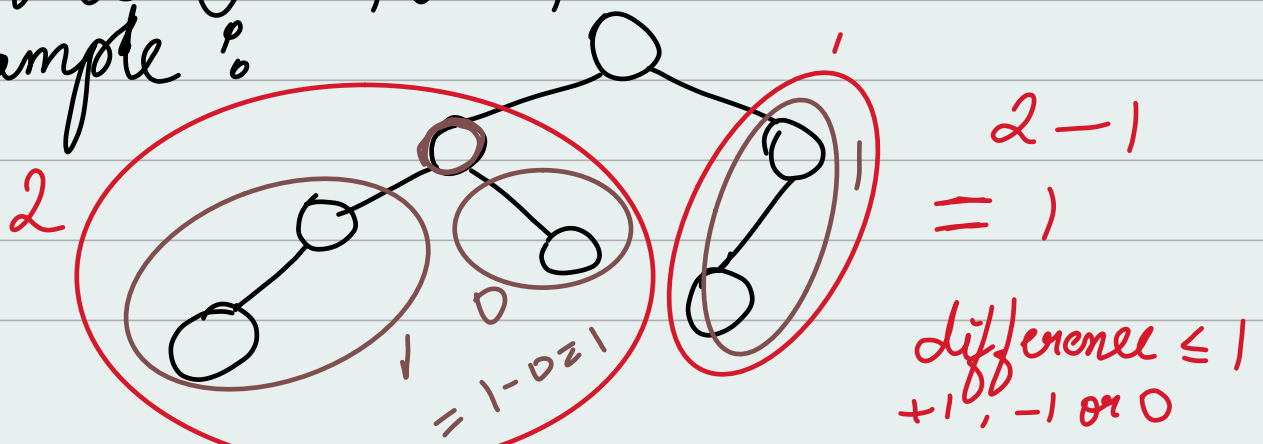
$\rightarrow$  For every single node in binary tree must be  $+1$ ,  $-1$ , or  $0$ .



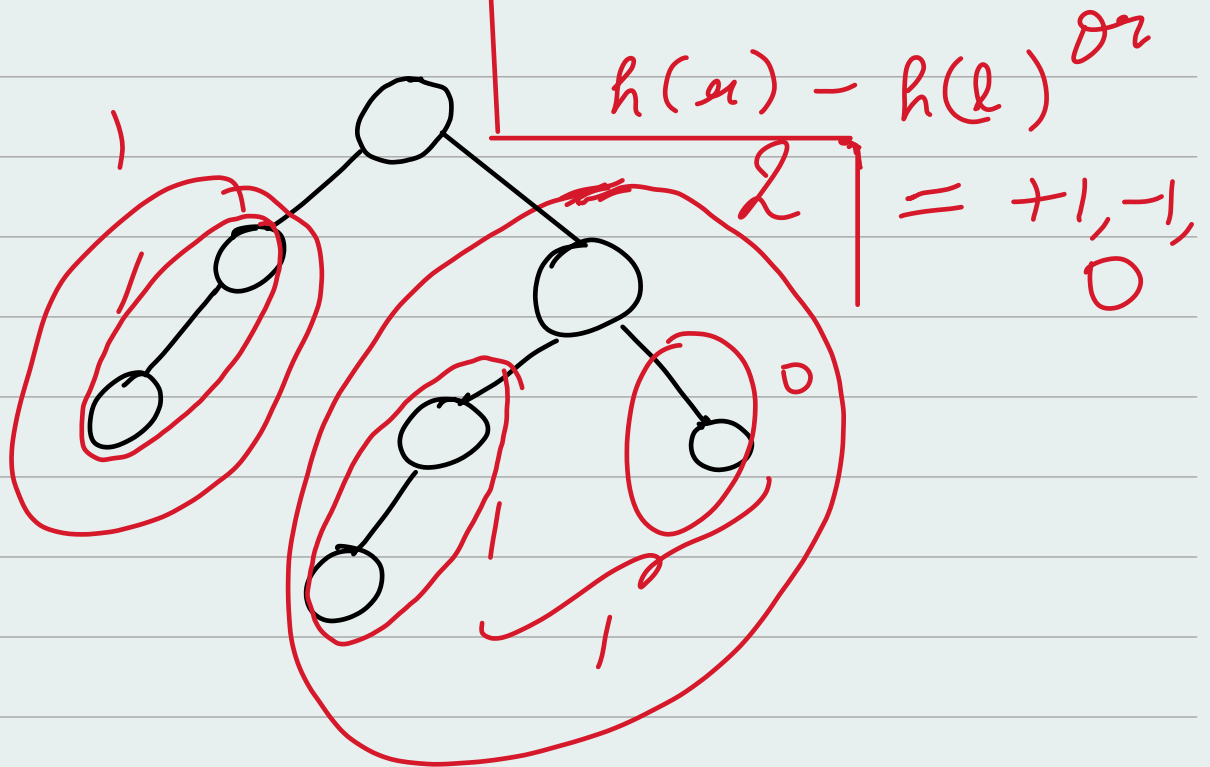
$\rightarrow$  Balanced binary tree

For every single node in binary tree must be  $+1$ ,  $-1$ , or  $0$ .

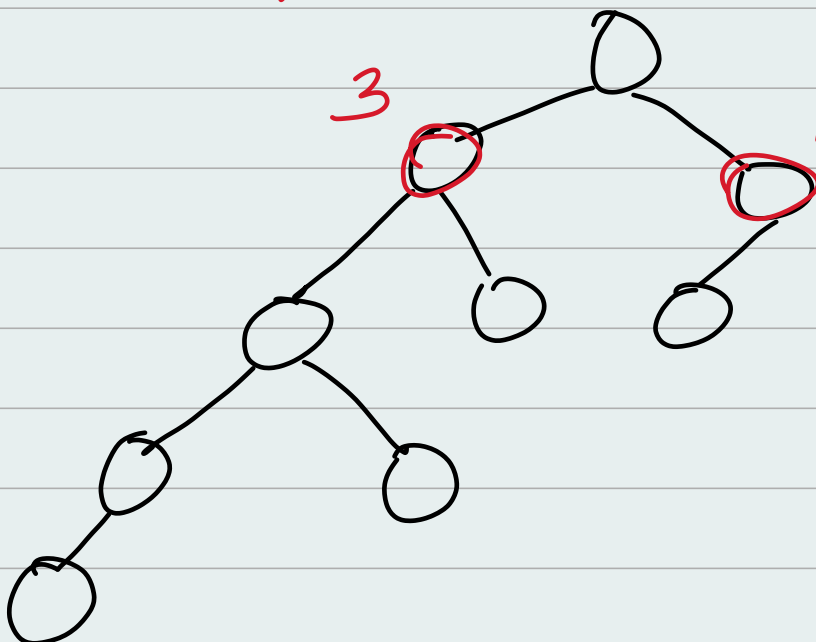
Example:



For every node,  $h(l) - h(r)$   
 $= +1, -1, \text{ or } 0$



\* For every Node in the tree, the difference in height of left and right subtree of that node,  $\leq 1 \Rightarrow$  Balanced Tree.



Not a balanced Tree

Solution?

→ Self balancing binary Tree.

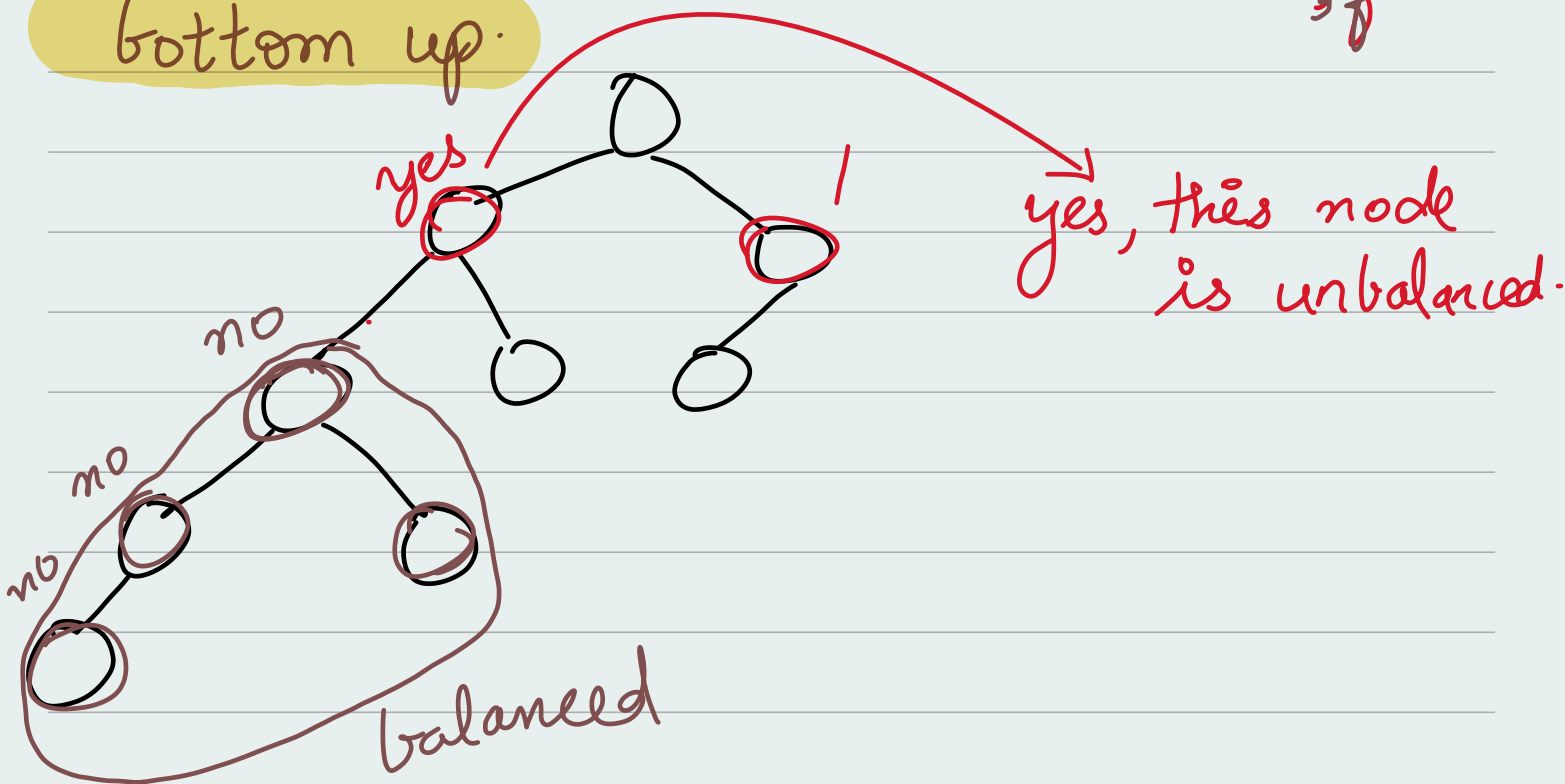
Example: AVL

(Adelson-Velski & Landis)

Algorithm:

① Insert normally node  $n$

② Start from node  $n$  & find the node that makes the tree unbalanced; from bottom up.

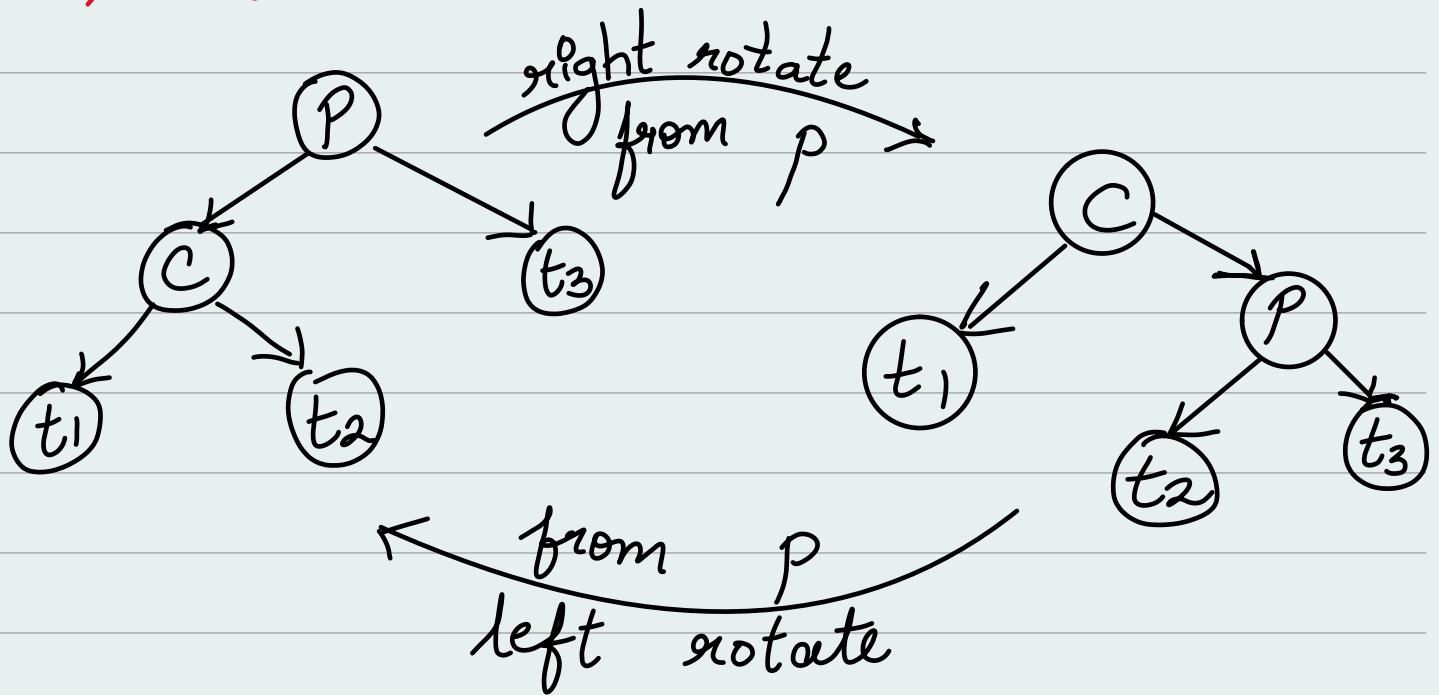


③ Using one of the four Rules;  
rotate

④ On solve the subtree, entire tree above

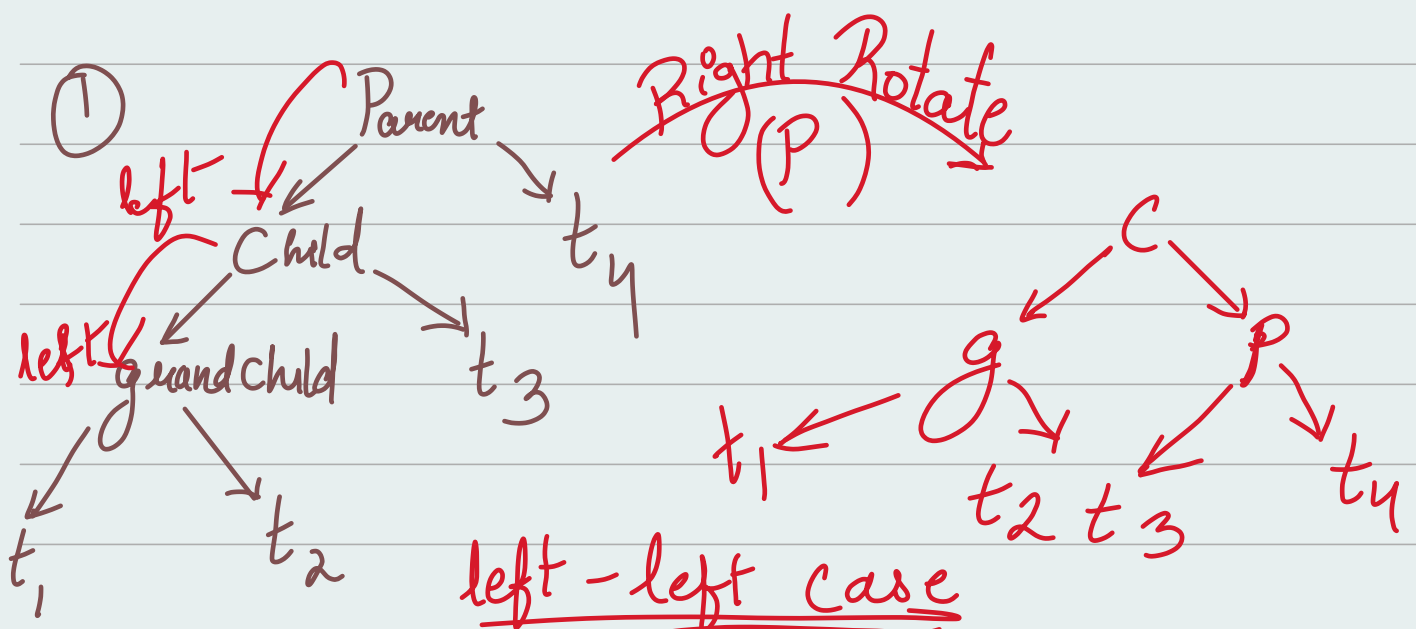
should be balanced in AVL trees.

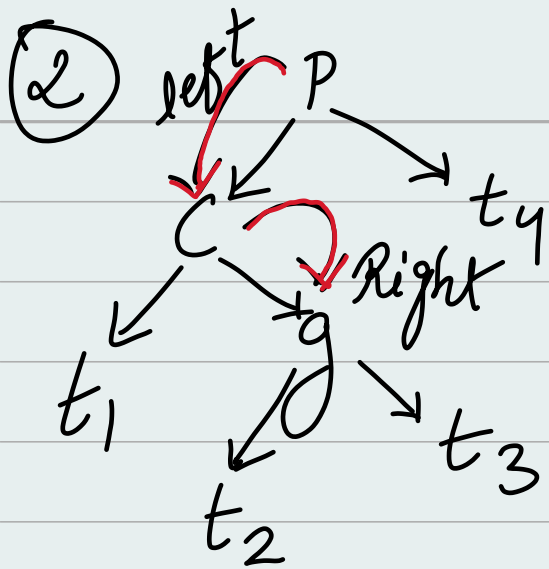
We can solve the above problem either by Right rotation or left rotation.



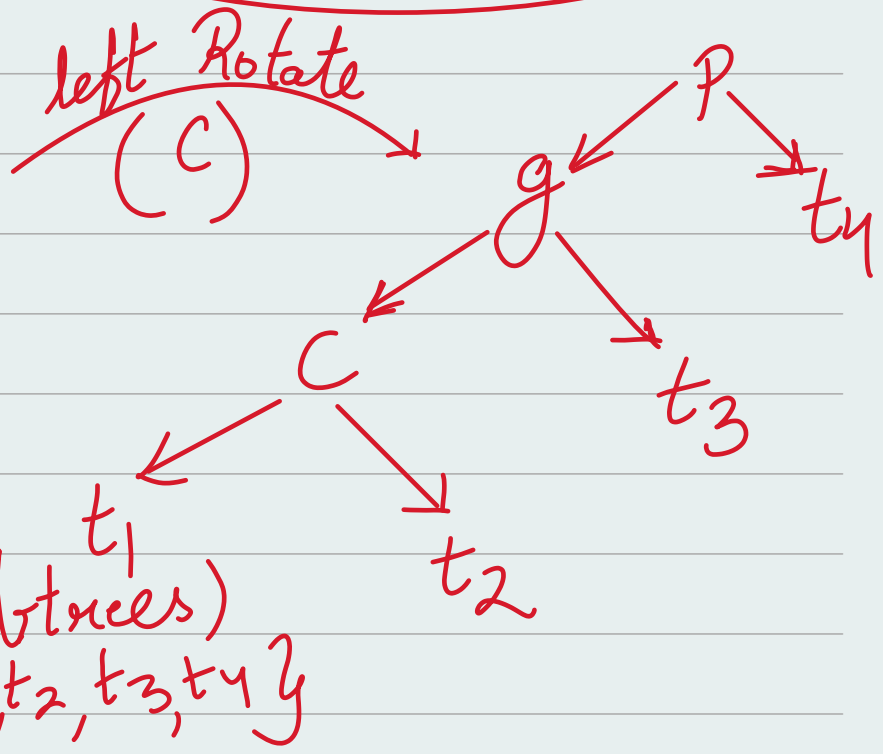
\* Binary Search Tree properties are holding true for this case

4 Rules :

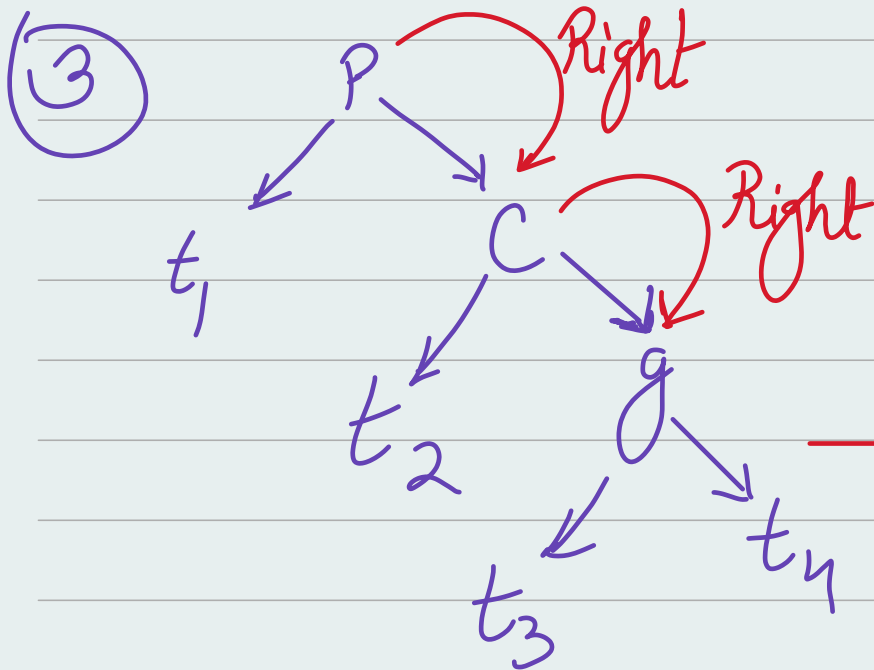




Left-Right Case

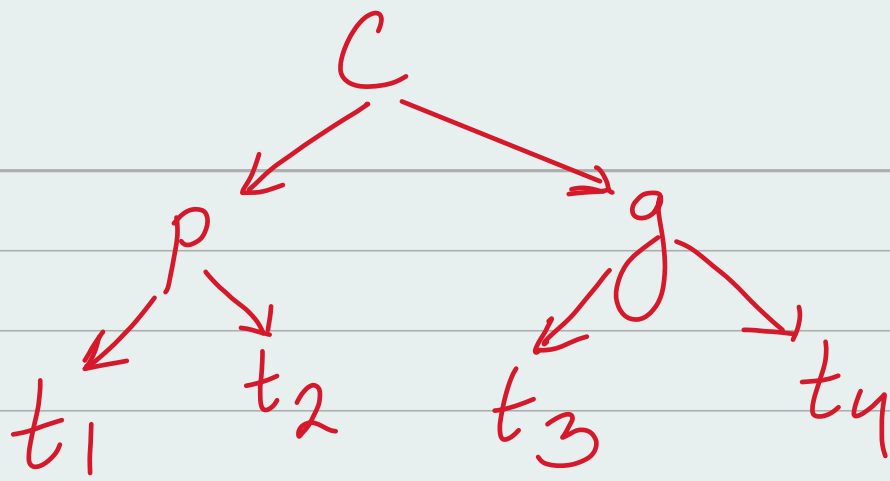


After this Right Rotate p.

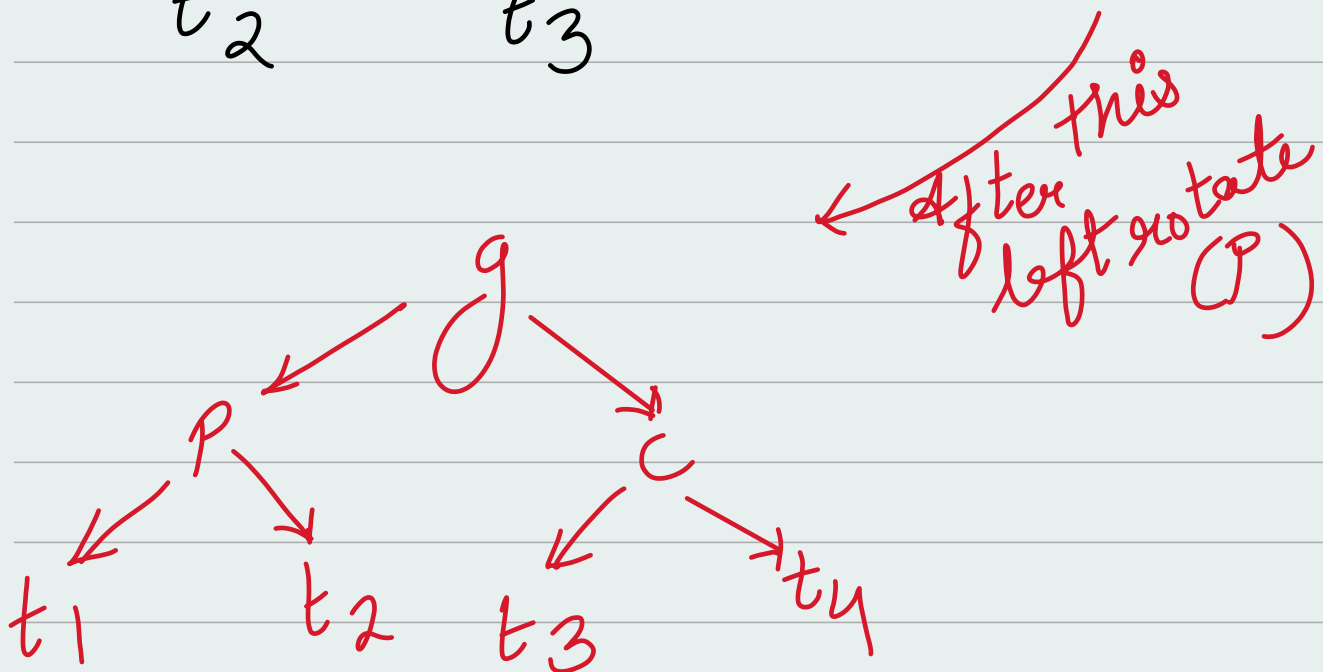
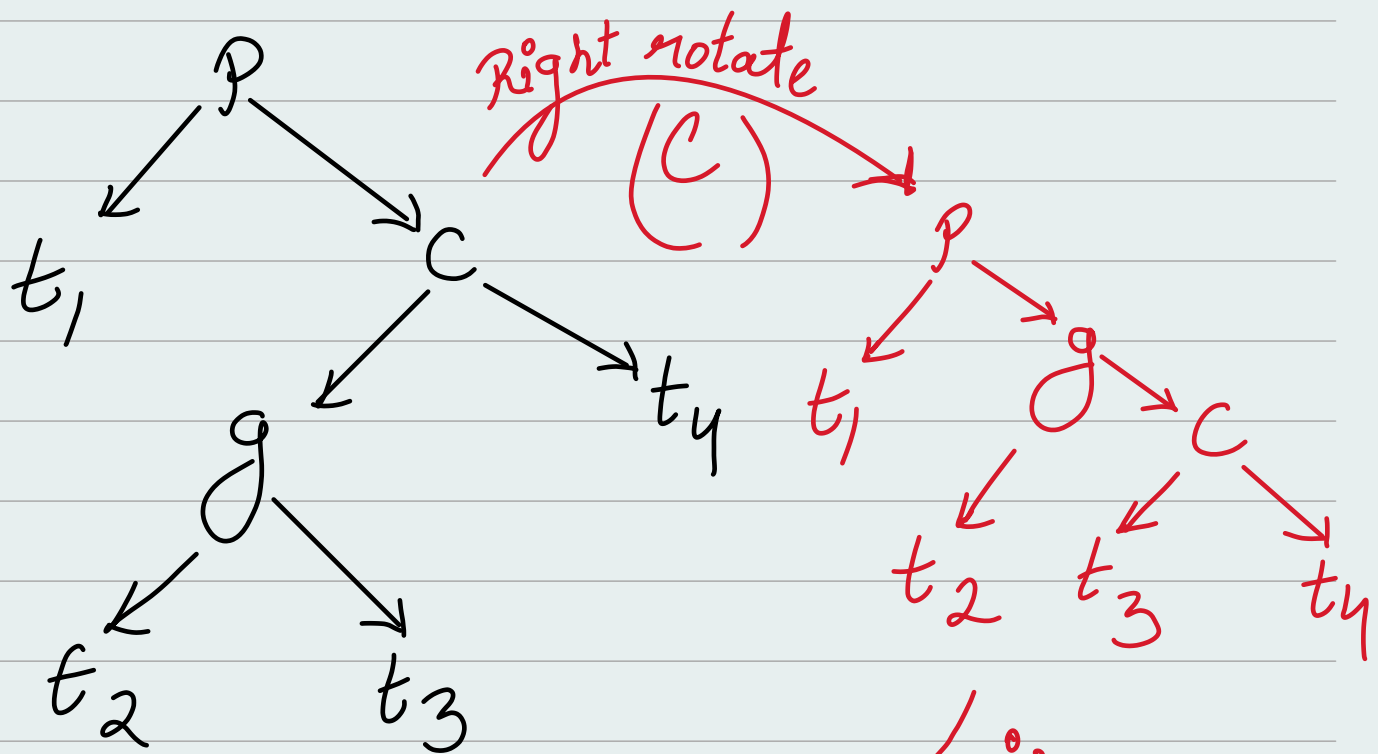


Right-Right Case

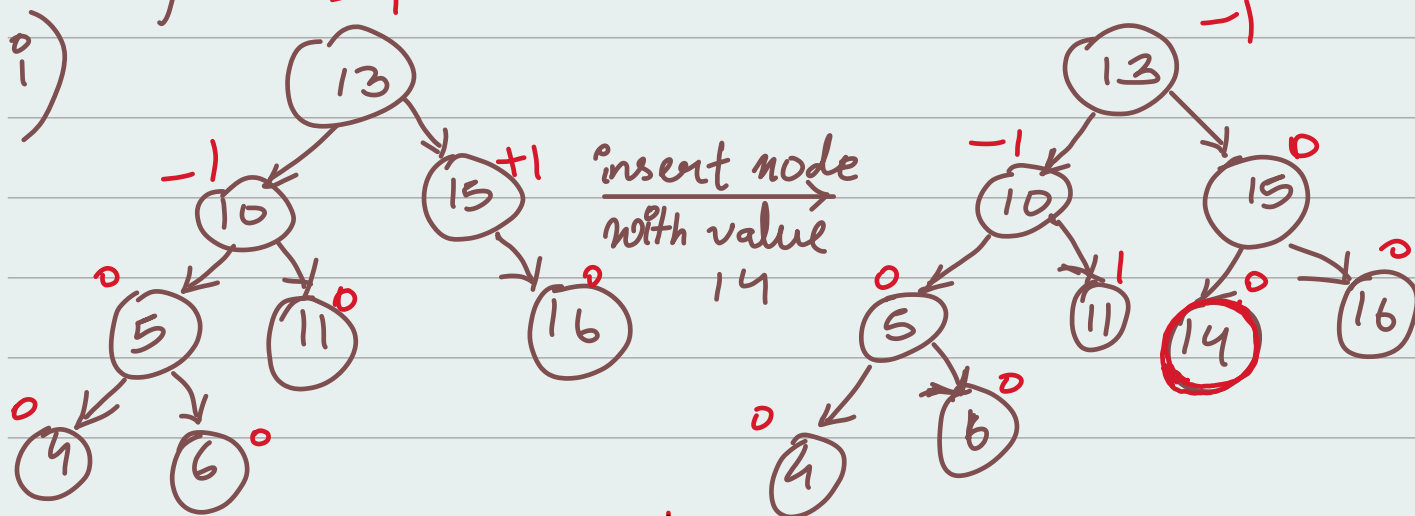
left rotate on (P)



④ Right - left Case

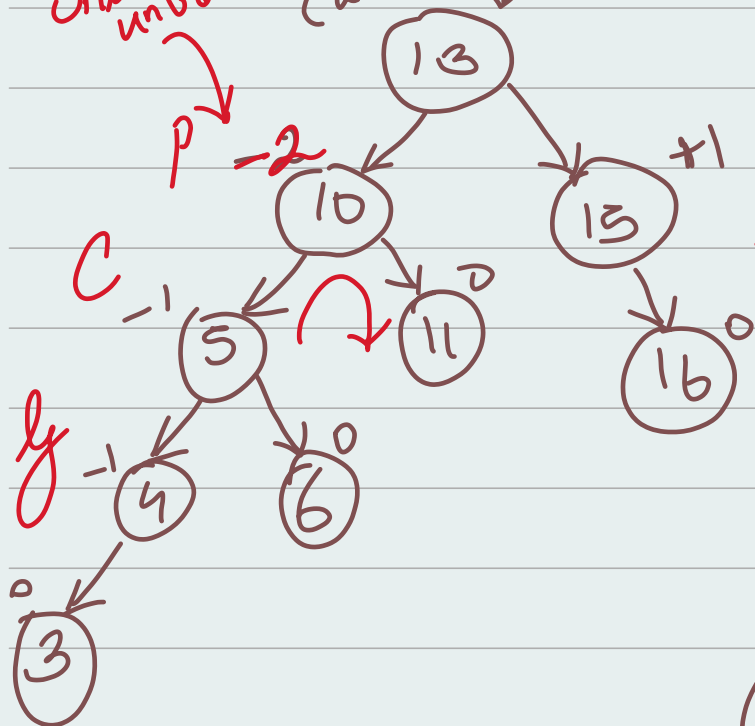


# Example ~

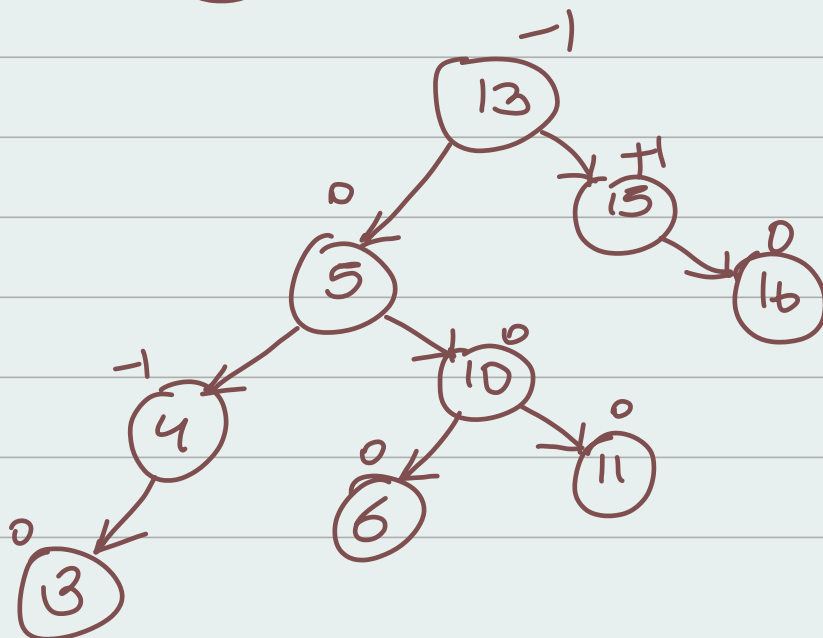


Now, insert node with value 3

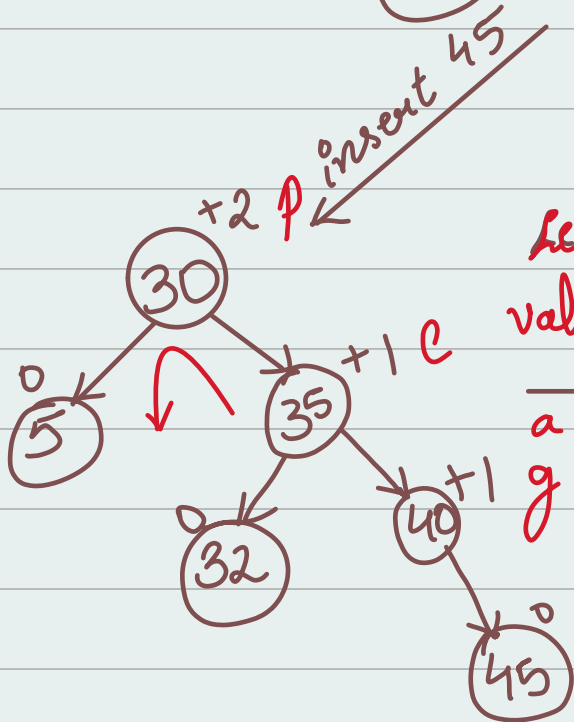
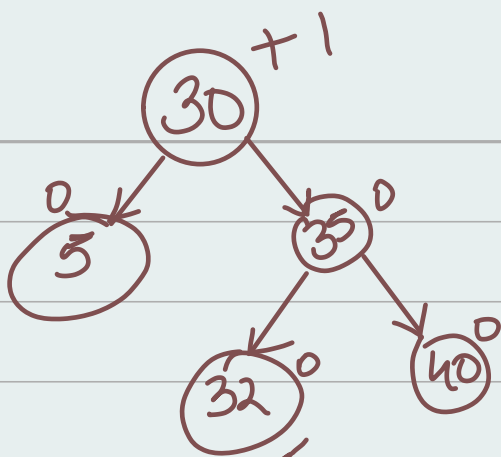
This node made it unbalanced, so AVL.  
 $(2 - 4 = -2)$



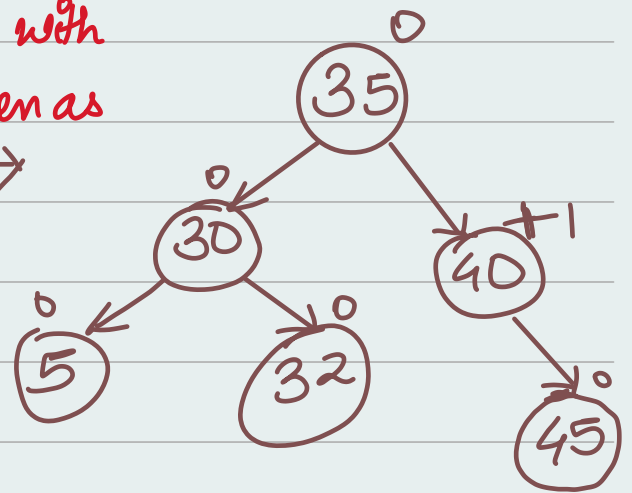
Right Rotate, node with value 10 as pivot.



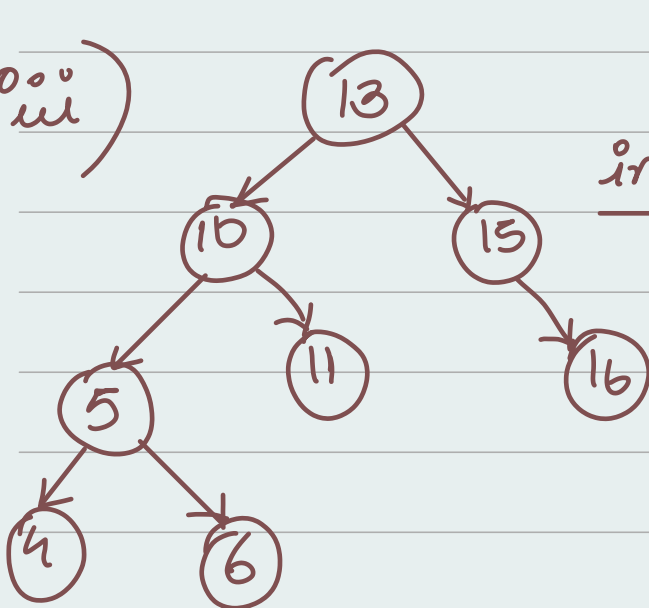
ii)



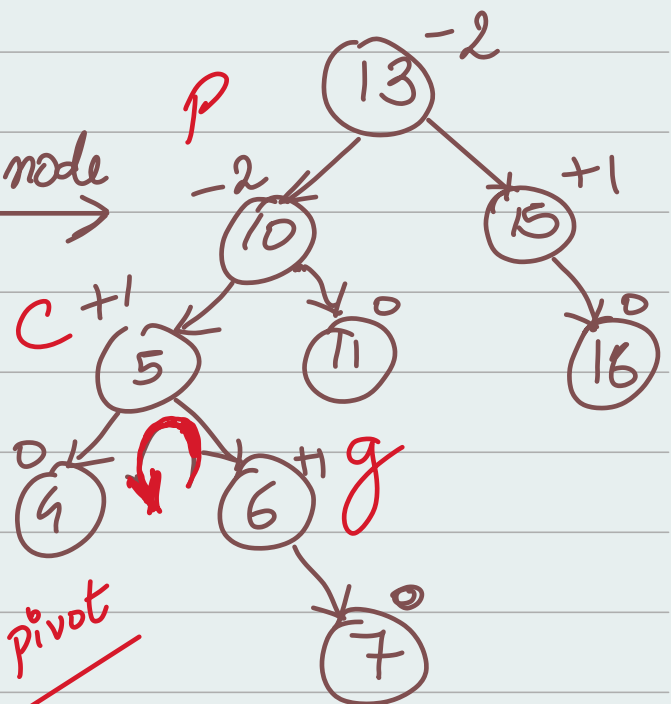
Left rotate, with  
value 30 taken as  
a pivot



iii)

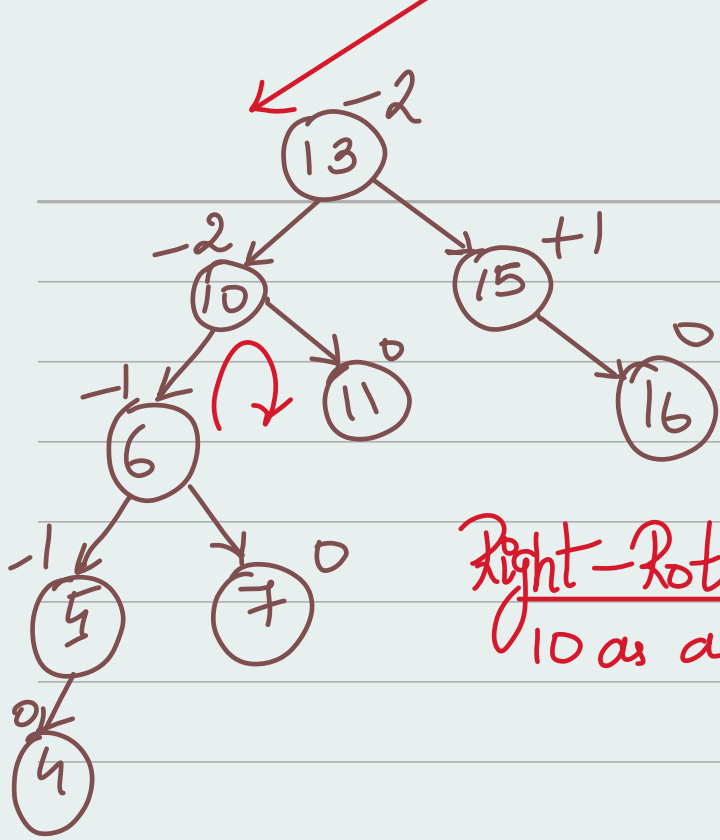


insert node  
7

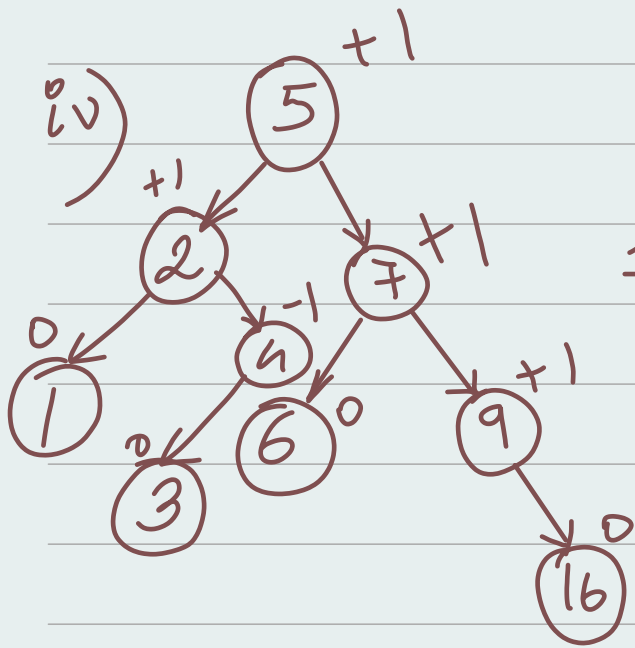
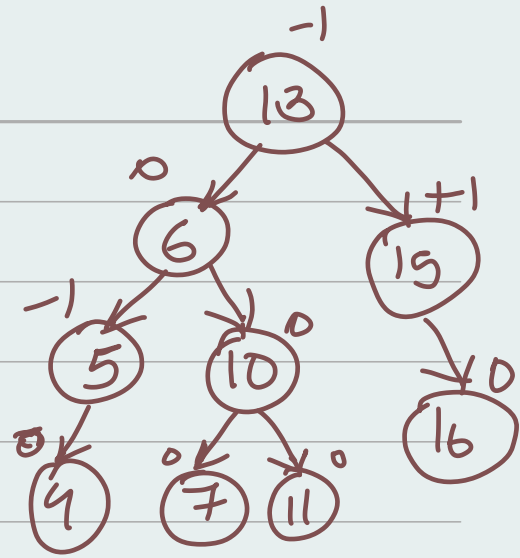


left rotation 5 as a pivot

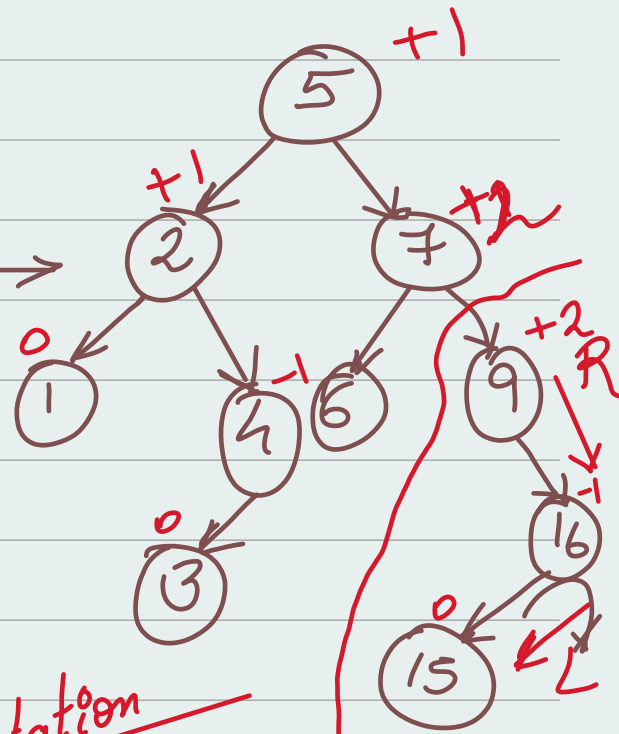




Right-Rotation taking 10 as a pivot

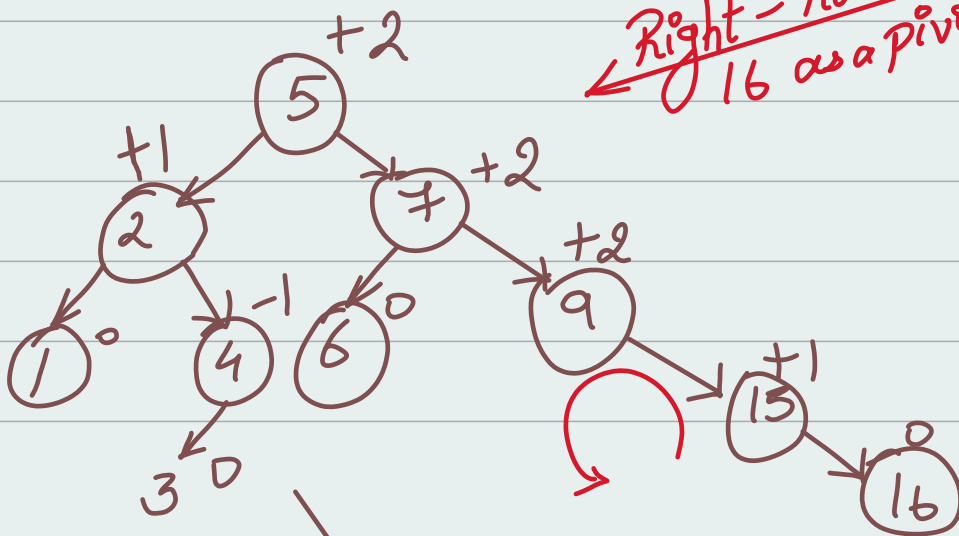


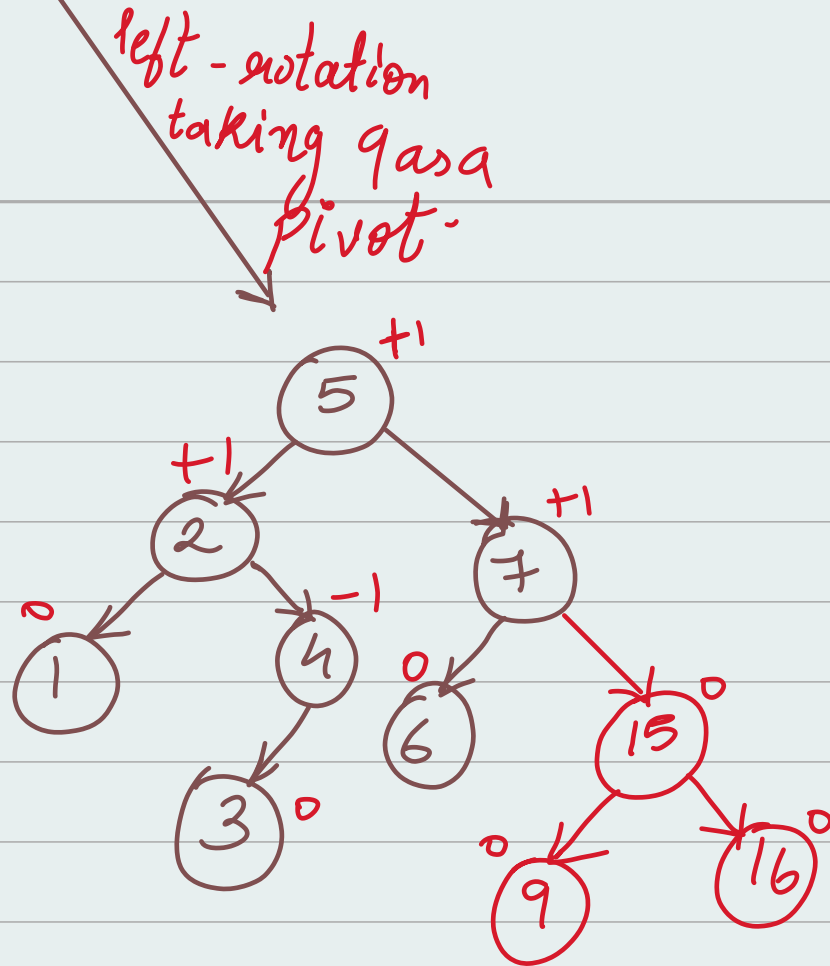
Insert 15



Right-Rotation 16 as a pivot

Solve this  
Then whole tree  
will be  
balanced





→ Time Complexity for adding a node:

→  $\log(N)$  as the tree is balanced.

→ Rotation Time complexity is constant because we only fix a subtree and cause of this whole tree will be solved automatically.  
 $O(1)$ .

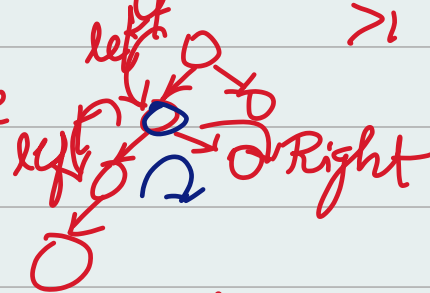
$$= \log(N) + O(1)$$

$$\text{Ans} = O(\log N)$$

Code : for left-left case

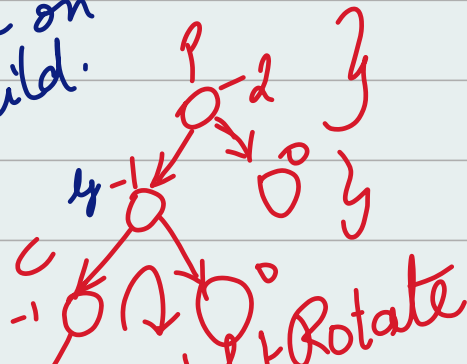
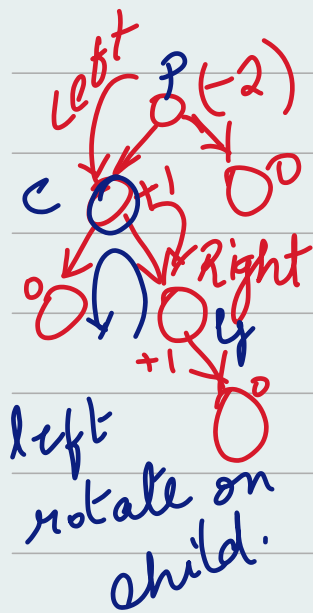
```
node height = Math.max(
    height(node.left), height(
        node.right)) + 1;
return rotate(node);
```

```
private Node rotate(Node node) {
    if (height(node.left) - height(node.right) > 1) {
        // left heavy case
```



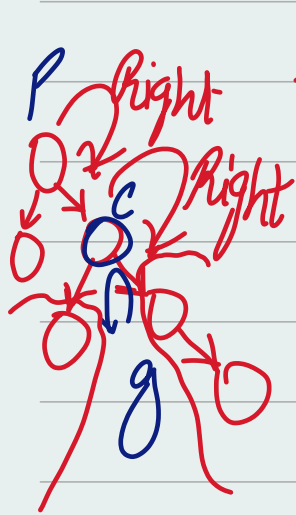
```
if (height(node.left.left) -
    height(node.left.right) > 0) {
    // left-left case
    return rightRotate(node);
}
```

```
if (height(node.left.left) - height(
    node.left.right) < 0) {
    node.left = leftRotate(node.left);
    return rightRotate(node);
}
```



if right

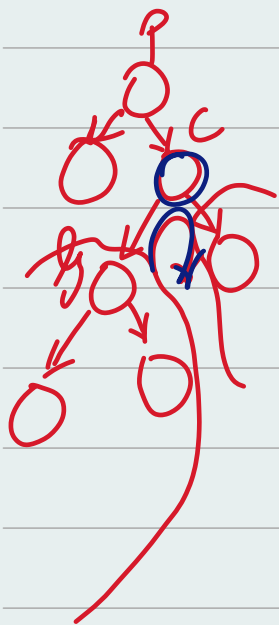
return node;



if (height (node . left) - height  
(node . right) < -1) {  
// right heavy

if (height (node . right . left) -  
height (node . right . right)  
≤ 0) {

// right - right case  
return leftRotate (node);



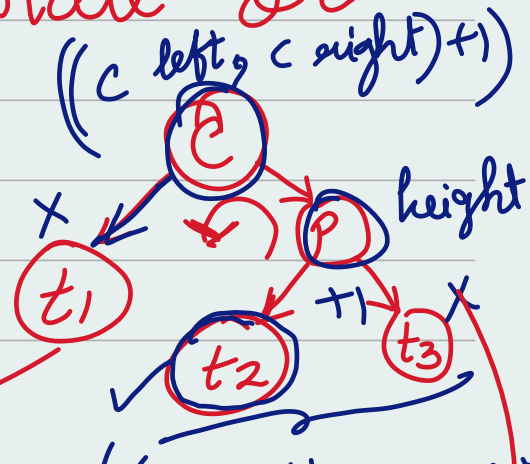
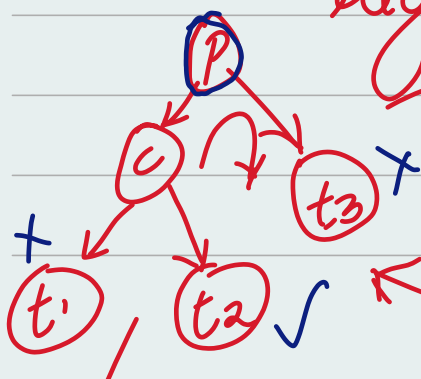
}

i) (height (node . right . left) -  
height (node . right . right) > 0) {  
node . right = rightRotate (node . right);  
return leftRotate (node);

}

return node;

// Now create left rotate or  
right rotate.



$t_2$  will change to  $t_1$  node

((p.left; p.right) + 1)

```
public Node rightRotate (Node p) {  
    Node c = p.left;  
    Node t = c.right;
```

```
    c.right = p;  
    p.left = t;
```

// Now update the height.

```
p.height = Math.max(height(p.left),  
    height(p.right) + 1);
```

```
c.height = Math.max(height(c.left),  
    height(c.right) + 1);  
return c;
```

```
public Node leftRotate (Node c) {  
    Node p = c.right;  
    Node t = p.left;
```

```
    p.left = c;  
    c.right = t;
```

// Now update the height

```
c.height = Math.max(height(c.left),  
    height(c.right) + 1);
```

```
p.height = Math.max(height(p.left),
```

```
        height(P.right) + 1);  
    return P;  
}
```

```
class Main {
```

```
    public static void main(String[]  
                             args) {
```

```
        AVL tree = new AVL();
```

```
        for (int i = 0; i < 1000; i++) {  
            tree.insert(i);  
        }
```

```
        System.out.println(tree.height()),  
    }
```

