

#### 4.2.2.c

$S \rightarrow S ( S ) S$

$\mid \epsilon$

String:  $((()()))$

Left most parse:

$S \rightarrow S ( S ) S$

$\rightarrow \epsilon ( S ) S$

$\rightarrow ( S ( S ) S ) S$

$\rightarrow ( S ( S ) S ( S ) S ) S$

$\rightarrow ( \epsilon ( S ) S ( S ) S ) S$

$\rightarrow ( ( \epsilon ) S ( S ) S ) S$

$\rightarrow ( ( ) \epsilon ( S ) S ) S$

$\rightarrow ( ( ) ( \epsilon ) S ) S$

$\rightarrow ( ( ) ( ) \epsilon ) S$

$\rightarrow ( ( ) ( ) ) \epsilon$

$\rightarrow ( ( ) ( ) )$

Right most Parse:

$S \rightarrow S ( S ) S$

$\rightarrow S ( S ) \epsilon \rightarrow S ( S ( S ) S )$

$\rightarrow S ( S ( S ( S ) S ) S )$

$\rightarrow S ( S ( S ) S ( S ) \epsilon )$

$\rightarrow S ( S ( S ) S ( \epsilon ) )$

$\rightarrow S ( S ( S ) \epsilon ( ) )$

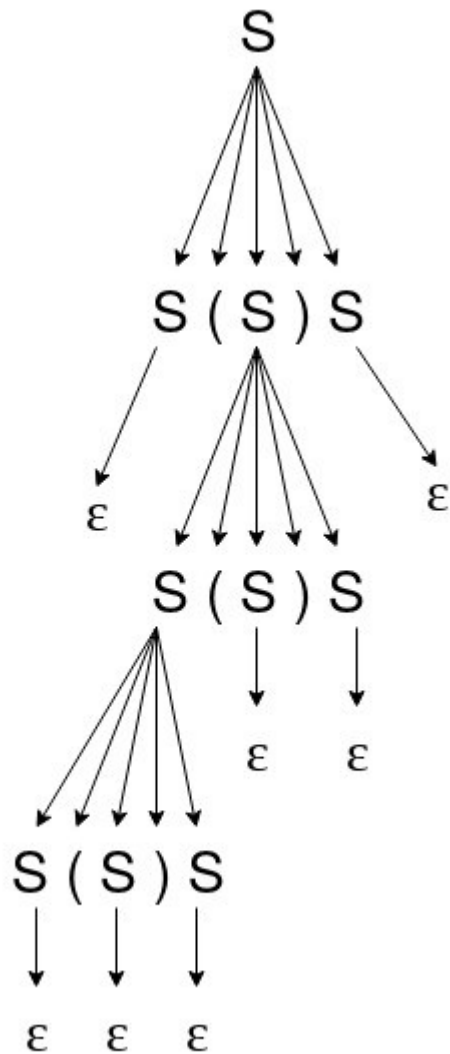
$\rightarrow S ( S ( \epsilon ) ( ) )$

$\rightarrow S ( \epsilon ( ) ( ) )$

$\rightarrow \epsilon ( ( ) ( ) )$

$\rightarrow ( ( ) ( ) )$

Parse Tree:



The grammar is ambiguous since with the input  $((()))$ , we can create two different parse trees with the same grammar.

The Language generates parentheses where every left parentheses closes with a right parentheses.

#### 4.2.3.a

$$S \rightarrow 1 S$$

$$| 01 S$$

$$| \epsilon$$

#### 4.4.1.c

$$S \rightarrow S ( S ) S$$

$$| \epsilon$$

$$S \rightarrow S_R$$

$$S_R \rightarrow \begin{matrix} (S) S S_R \\ | \quad \epsilon \end{matrix}$$

$$\text{First}(S) = \{ (, \epsilon ) \}$$

$$\text{First}(S_R) = \{ (, \epsilon \}$$

$$\text{Follow}(S) = \{ ), (, \$ \}$$

$$\text{Follow}(S_R) = \{ ), (, \$ \}$$

	(	)	\$
S	$S \rightarrow S_R$	$S \rightarrow S_R$	$S \rightarrow S_R$
$S_R$	$S_R \rightarrow (S) S S_R$	$S_R \rightarrow \epsilon$	$S_R \rightarrow \epsilon$