

Machine Learning

Advice for applying machine learning

Deciding what to try next

Debugging a learning algorithm:

Suppose you have implemented regularized linear regression to predict housing prices.

$$J(\theta) = \frac{1}{2m} \left[\sum_{i=1}^{m} (h_{\theta}(x^{(i)}) - y^{(i)})^2 + \lambda \sum_{j=1}^{m} \theta_j^2 \right]$$

However, when you test your hypothesis on a new set of houses, you find that it makes unacceptably large errors in its predictions. What should you try next?

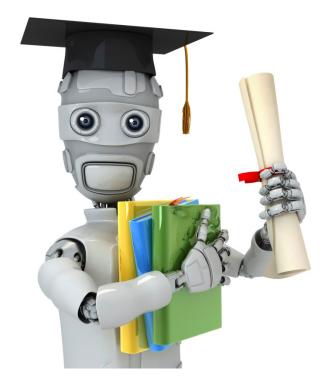
X1, X2, X3, ..., X100

- -> Get more training examples
 - Try smaller sets of features
- -> Try getting additional features
 - Try adding polynomial features $(x_1^2, x_2^2, x_1x_2, \text{etc.})$
 - Try decreasing λ
 - Try increasing λ

Machine learning diagnostic:

Diagnostic: A test that you can run to gain insight what is/isn't working with a learning algorithm, and gain guidance as to how best to improve its performance.

Diagnostics can take time to implement, but doing so can be a very good use of your time.

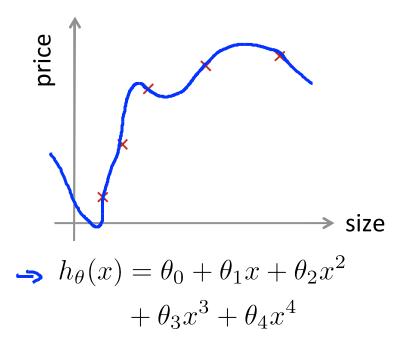


Machine Learning

Advice for applying machine learning

Evaluating a hypothesis

Evaluating your hypothesis

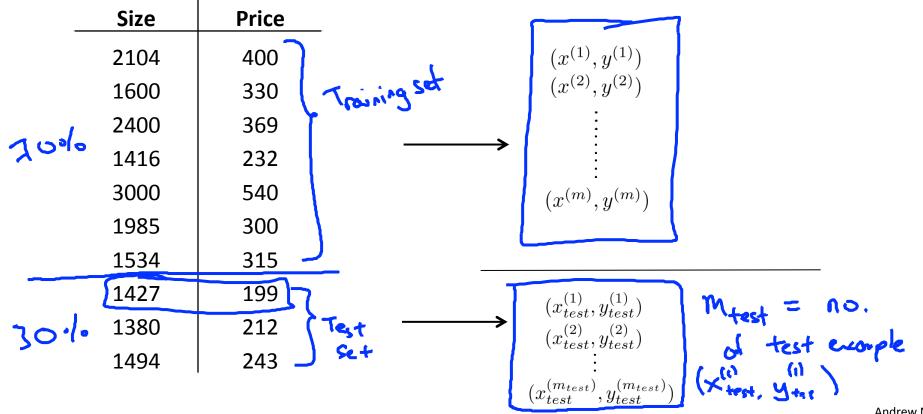


Fails to generalize to new examples not in training set.

```
x_1= size of house x_2= no. of bedrooms x_3= no. of floors x_4= age of house x_5= average income in neighborhood x_6= kitchen size :
```

Evaluating your hypothesis

Dataset:



Andrew Ng

Training/testing procedure for linear regression

 \rightarrow - Learn parameter θ from training data (minimizing training error $J(\theta)$)

- Compute test set error:

$$\frac{1}{1+est}(6) = \frac{1}{2m_{test}} \left(\frac{h_0(x_{test}) - y_{test}}{1+est}\right)^2$$

Training/testing procedure for logistic regression

- Learn parameter heta from training data
- Compute test set error:

$$J_{test}(\theta) = -\frac{1}{m_{test}} \sum_{i=1}^{m_{test}} y_{test}^{(i)} \log h_{\theta}(x_{test}^{(i)}) + (1 - y_{test}^{(i)}) \log h_{\theta}(x_{test}^{(i)})$$

- Misclassification error (0/1 misclassification error):

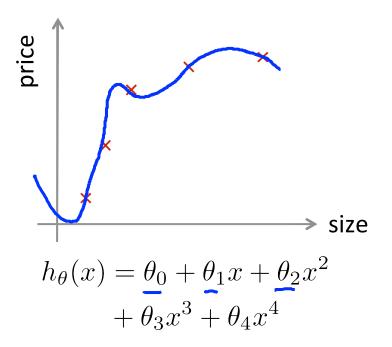


Machine Learning

Advice for applying machine learning

Model selection and training/validation/test sets

Overfitting example



Once parameters $\theta_0, \theta_1, \ldots, \theta_4$ were fit to some set of data (training set), the error of the parameters as measured on that data (the training error $J(\theta)$) is likely to be lower than the actual generalization error.

Model selection

Who def selection
$$\theta_0 = \theta_0 + \theta_1 x$$
 $\theta_0 = \theta_0 + \theta_1 x$ $\theta_0 = \theta_0 + \theta_1 x + \theta_2 x^2$ $\theta_0 = \theta_0 + \theta_1 x + \theta_2 x^2$ $\theta_0 = \theta_0 + \theta_1 x + \dots + \theta_3 x^3$ $\theta_0 = \theta_0 + \theta_1 x + \dots + \theta_3 x^3$ $\theta_0 = \theta_0 + \theta_1 x + \dots + \theta_{10} x^{10}$ $\theta_0 = \theta_0 + \theta_1 x + \dots + \theta_{10} x^{10}$ $\theta_0 = \theta_0 + \theta_1 x + \dots + \theta_{10} x^{10}$ $\theta_0 = \theta_0 + \theta_1 x + \dots + \theta_{10} x^{10}$ $\theta_0 = \theta_0 + \theta_1 x + \dots + \theta_{10} x^{10}$ $\theta_0 = \theta_0 + \theta_1 x + \dots + \theta_{10} x^{10}$ $\theta_0 = \theta_0 + \theta_1 x + \dots + \theta_{10} x^{10}$ $\theta_0 = \theta_0 + \theta_1 x + \dots + \theta_{10} x^{10}$

de degree of polynomial

Choose
$$\theta_0 + \dots \theta_5 x^5$$

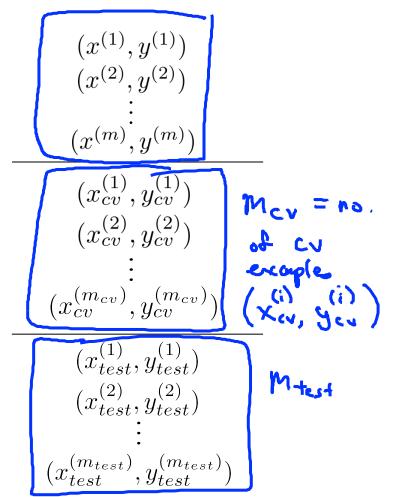
How well does the model generalize? Report test set error $J_{test}(\theta^{(5)})$.

Problem: $J_{test}(\theta^{(5)})$ is likely to be an optimistic estimate of generalization error. I.e. our extra parameter $\underline{d} = \text{degree}$ of polynomial) is fit to test set.

Evaluating your hypothesis

Dataset:

_	Size	Price	1
60%	2104	400	
	1600	330	
	• 2400	369 Town	
	1416	232	
	3000	540	7
	1985	300	
20%	1534	315 7 Cross veridation	•
	1427	199	
ζο•	1380	212 } test set	\rightarrow
	1494	243	



Train/validation/test error

Training error:

$$\rightarrow J_{train}(\theta) = \frac{1}{2m} \sum_{i=1} (h_{\theta}(x^{(i)}) - y^{(i)})^2$$

Cross Validation error:

$$J_{cv}(\theta) = \frac{1}{2m_{cv}} \sum_{i=1}^{\infty} (h_{\theta}(x_{cv}^{(i)}) - y_{cv}^{(i)})^2$$

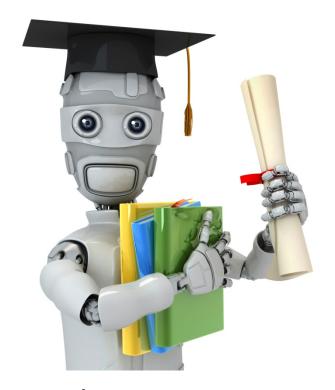
Test error:

$$J_{test}(\theta) = \frac{1}{2m_{test}} \sum_{i=1}^{n} (h_{\theta}(x_{test}^{(i)}) - y_{test}^{(i)})^2$$

Model selection

Pick
$$\theta_0 + \theta_1 x_1 + \cdots + \theta_4 x^4 \leftarrow$$

Estimate generalization error for test set $J_{test}(\theta^{(4)})$

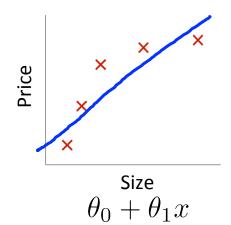


Machine Learning

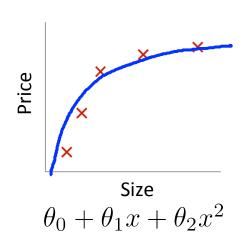
Advice for applying machine learning

Diagnosing bias vs. variance

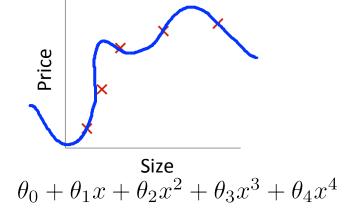
Bias/variance



High bias (underfit) 2=1





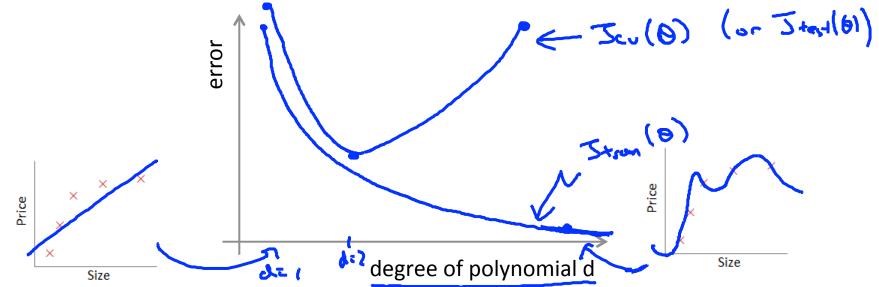


High variance (overfit)

Bias/variance

Training error:
$$J_{train}(\theta) = \frac{1}{2m} \sum_{i=1}^{n} (h_{\theta}(x^{(i)}) - y^{(i)})^2$$

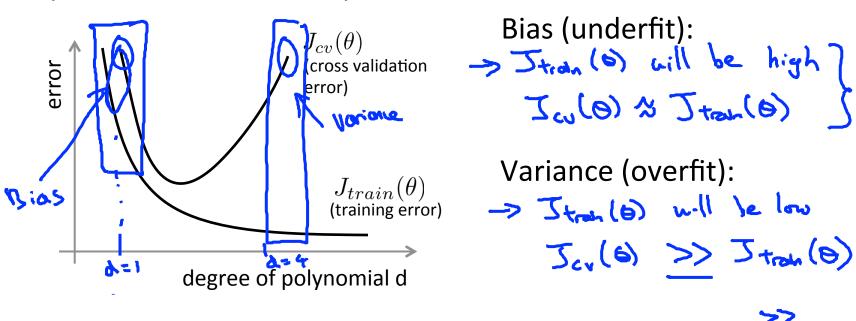
Cross validation error:
$$J_{cv}(\theta) = \frac{1}{2m_{cv}} \sum_{i=1}^{m_{cv}} (h_{\theta}(x_{cv}^{(i)}) - y_{cv}^{(i)})^2$$

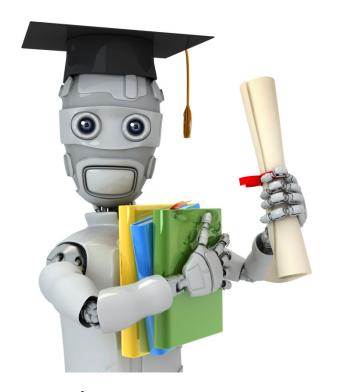


Andrew Ng

Diagnosing bias vs. variance

Suppose your learning algorithm is performing less well than you were hoping. ($J_{cv}(\theta)$ or $J_{test}(\theta)$ is high.) Is it a bias problem or a variance problem?



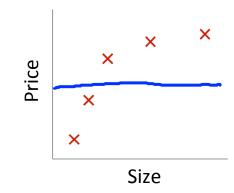


Machine Learning

Advice for applying machine learning

Regularization and bias/variance

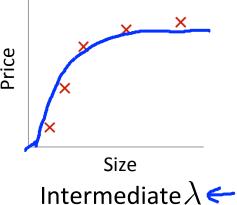
Linear regression with regularization

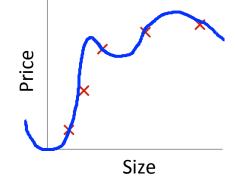


High bias (underfit)

Large $\lambda \leftarrow$

$$\lambda = 10000. \ \theta_1 \approx 0, \theta_2 \approx 0, \dots$$





 \Rightarrow Small λ High variance (overfit)

$$\rightarrow \lambda = 0$$

Choosing the regularization parameter λ

$$h_{\theta}(x) = \theta_{0} + \theta_{1}x + \theta_{2}x^{2} + \theta_{3}x^{3} + \theta_{4}x^{4}$$

$$J(\theta) = \frac{1}{2m} \sum_{i=1}^{m} (h_{\theta}(x^{(i)}) - y^{(i)})^{2} + \frac{\lambda}{2m} \sum_{j=1}^{m} \theta_{j}^{2}$$

$$J_{train}(\theta) = \frac{1}{2m} \sum_{i=1}^{m} (h_{\theta}(x^{(i)}) - y^{(i)})^{2}$$

$$J_{cv}(\theta) = \frac{1}{2m_{cv}} \sum_{i=1}^{m_{cv}} (h_{\theta}(x^{(i)}_{cv}) - y^{(i)}_{cv})^{2}$$

$$J_{test}(\theta) = \frac{1}{2m_{test}} \sum_{i=1}^{m_{test}} (h_{\theta}(x^{(i)}_{test}) - y^{(i)}_{test})^{2}$$

$$J_{test}(\theta) = \frac{1}{2m_{test}} \sum_{i=1}^{m_{test}} (h_{\theta}(x^{(i)}_{test}) - y^{(i)}_{test})^{2}$$

Choosing the regularization parameter λ

Model:
$$h_{\theta}(x) = \theta_0 + \theta_1 x + \theta_2 x^2 + \theta_3 x^3 + \theta_4 x^4$$

$$J(\theta) = \frac{1}{2m} \sum_{i=1}^{m} (h_{\theta}(x^{(i)}) - y^{(i)})^2 + \frac{\lambda}{2m} \sum_{j=1}^{m} \theta_j^2$$

$$Try \lambda = 0 \leftarrow \gamma \longrightarrow \min J(\Theta) \longrightarrow \Theta'' \longrightarrow J_{co}(\Theta'')$$

1. Try
$$\lambda = 0 \leftarrow 1$$
 \longrightarrow min $J(\Theta) \rightarrow \Theta'' \rightarrow J_{CU}(\Theta''')$

2. Try $\lambda = 0.01$ \longrightarrow $J_{CU}(\Theta'')$

3. Try $\lambda = 0.02$ \longrightarrow $J_{CU}(\Theta'')$

4. Try $\lambda = 0.04$ \longrightarrow $J_{CU}(\Theta'')$

5. Try $\lambda = 0.08$

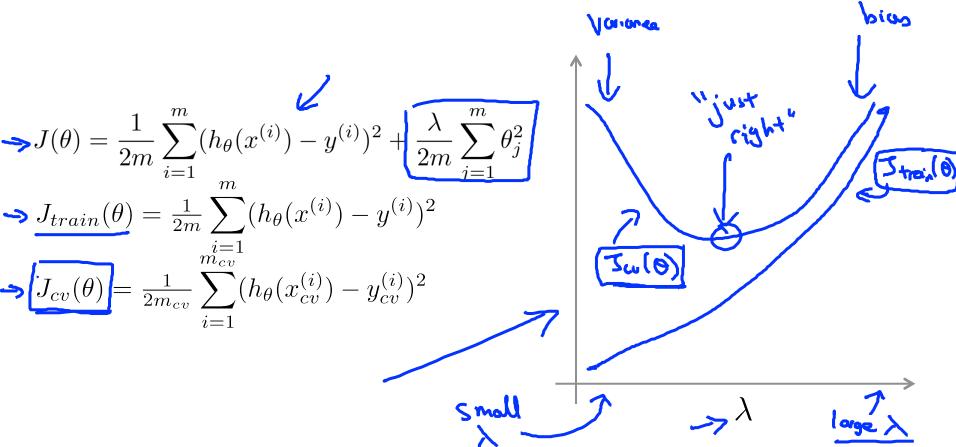
3. Try
$$\lambda = 0.02$$
 \longrightarrow \searrow \searrow \searrow \searrow \swarrow

4. Try
$$\lambda = 0.04$$

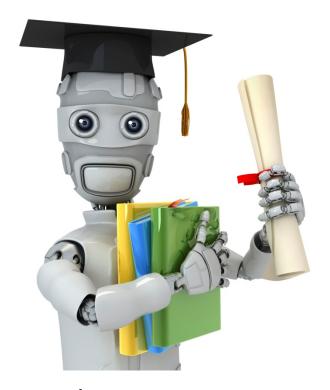
Fry
$$\lambda = 10$$
 Pick (say) $\theta^{(5)}$. Test error: $\sum_{k \in \mathcal{L}} \left(\delta^{(5)} \right)$

Andrew Ng

Bias/variance as a function of the regularization parameter $\,\lambda\,$



Andrew Ng



Machine Learning

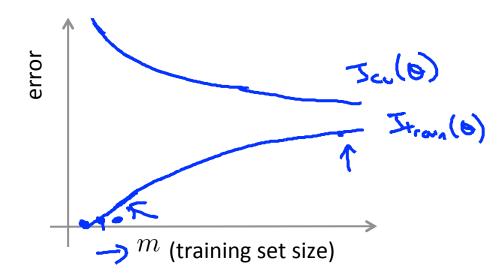
Advice for applying machine learning

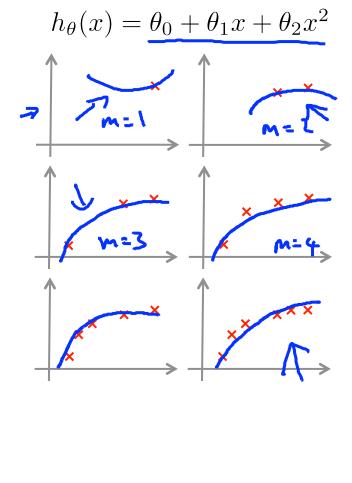
Learning curves

Learning curves

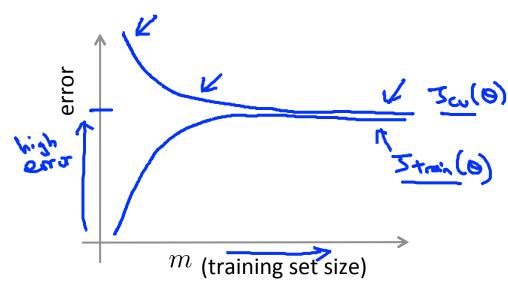
$$J_{train}(\theta) = \frac{1}{2m} \sum_{i=1}^{m} (h_{\theta}(x^{(i)}) - y^{(i)})^2$$

$$J_{cv}(\theta) = \frac{1}{2m_{cv}} \sum_{i=1}^{m_{cv}} (h_{\theta}(x_{cv}^{(i)}) - y_{cv}^{(i)})^2$$

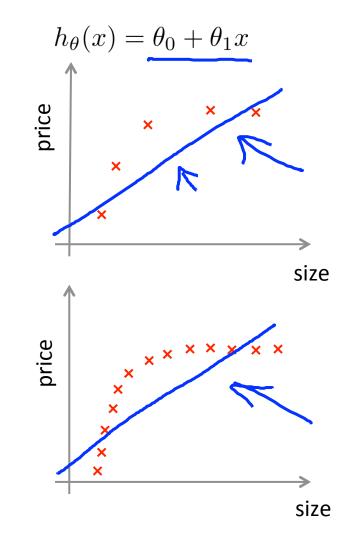




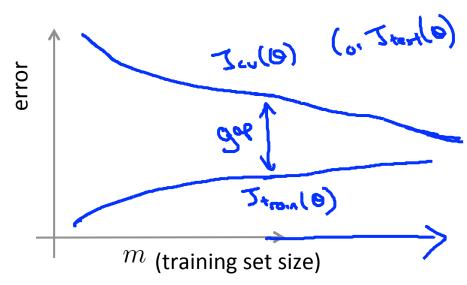
High bias



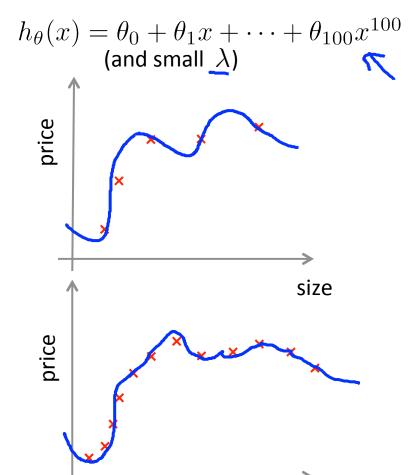
If a learning algorithm is suffering from high bias, getting more training data will not (by itself) help much.



High variance



If a learning algorithm is suffering from high variance, getting more training data is likely to help. \leftarrow



size



Machine Learning

Advice for applying machine learning

Deciding what to try next (revisited)

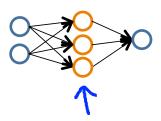
Debugging a learning algorithm:

Suppose you have implemented regularized linear regression to predict housing prices. However, when you test your hypothesis in a new set of houses, you find that it makes unacceptably large errors in its prediction. What should you try next?

- Get more training examples -> fixe high vorione
- Try smaller sets of features -> Fixe high voice
- Try getting additional features -> free high bias
- Try adding polynomial features $(x_1^2, x_2^2, x_1x_2, \text{etc}) \rightarrow \{$
- Try decreasing λ fixes high high
- Try increasing λ -> fixes high variance

Neural networks and overfitting

"Small" neural network (fewer parameters; more prone to underfitting)



Computationally cheaper

"Large" neural network (more parameters; more prone to overfitting) Computationally more expensive.

Use regularization (λ) to address overfitting.

