# **Solving Quadratics**

A quadratic function has three terms:  $ax^2 + bx + c$ . a, b, and c are known as the *coeffcients*. The coefficients can be any constant, except that a can never be zero. (If a is zero, it is a linear function, not a quadratic.)

When you have an equation with a quadratic function on one side and a zero on the other, you have a quadratic equation. For example:

$$72x^2 - 12x + 1.2 = 0$$

How can you find the values of x that will make this equation true?

You can always reduce a quadratic equation so that the first coefficient is 1, so that your equation looks like this:

$$x^2 + bx + c = 0$$

For example, if you are asked to solve  $4x^2 + 8x - 19 = -2x^2 - 7$ 

$$4x^2 + 8x - 19 = -2x^2 - 7$$

$$6x^2 + 8x - 12 = 0$$

$$x^2 + \frac{4}{3}x - 2 = 0$$

Here,  $b = \frac{4}{3}$  and c = -2.

$$x^2 + bx + c = 0$$
 when

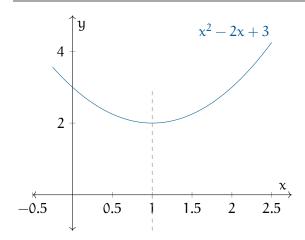
$$x=-\frac{b}{2}\pm\frac{\sqrt{b^2-4c}}{2}$$

What does this mean?

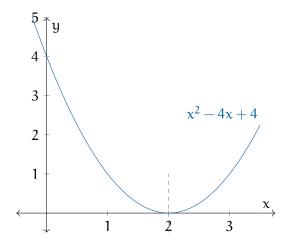
For any b and c, the graph of  $x^2 + bx + c$  is a parabola that goes up on each end. Its low point is at  $x = -\frac{b}{2}$ .

If there are no real roots  $(b^2 - 4c < 0)$ , which means the parabola never gets low enough to cross the x-axis:

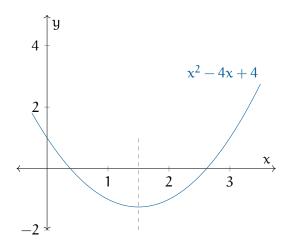
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If there is one real root  $(b^2 - 4c = 0)$ , it means that the parabola just touches the x-axis.



If there are two real roots  $(b^2-4c>0)$ , it means that the parabola crosses the x-axis twice as it dips below and then returns:



#### **Exercise 1** Roots of a Quadratic

Working Space —

In the last chapter, you found that the function for the height of your flying hammer is:

$$p = -\frac{1}{2}9.8t^2 + 12t + 2$$

At what time will the hammer hit the ground?

Answer on Page 5	

#### 1.1 The Traditional Quadratic Formula

If the last explanation was a little tricky to understand the quadratic formula is a nifty tool.

The Quadratic Formula

$$ax^2 + bx + c = 0$$
 when

$$x = \frac{-b \pm \sqrt{b^2 - 4\alpha c}}{2\alpha}$$

This is a draft chapter from the Kontinua Project. Please see our website (https://kontinua.org/) for more details.

## Answers to Exercises

### **Answer to Exercise 1 (on page 3)**

For what t is  $-4.9t^2 + 12t + 2 = 0$ ? Start by dividing both sides of the equation by -4.9.

$$t^2 - 2.45t - 0.408 = 0$$

The roots of this are at

$$x = -\frac{b}{2} \pm \frac{\sqrt{b^2 - 4c}}{2} = -\frac{-2.45}{2} \pm \frac{\sqrt{(-2.45)^2 - 4(-0.408)}}{2} = 1.22 \pm 1.36$$

We only care about the root after we release the hammer (t>0).

1.22 + 1.36 = 2.58 seconds after releasing the hammer, it will hit the ground.