

# Differential Equations

Differential equations are equations involving an unknown function and its derivatives. They play a crucial role in mathematics, physics, engineering, economics, and other disciplines due to their ability to describe change over time or in response to changing conditions.

## 1.1 Ordinary Differential Equations

An ordinary differential equation (ODE) involves a function of a single independent variable and its derivatives. The order of an ODE is determined by the order of the highest derivative present in the equation. An example of a first-order ODE is:

$$\frac{dy}{dx} + y = x \quad (1.1)$$

Here,  $y$  is the function of the independent variable  $x$ , and  $\frac{dy}{dx}$  represents its first derivative.

## 1.2 Partial Differential Equations

Partial differential equations (PDEs), on the other hand, involve a function of multiple independent variables and their partial derivatives. An example of a PDE is the heat equation, a second-order PDE:

$$\frac{\partial u}{\partial t} = \alpha \frac{\partial^2 u}{\partial x^2} \quad (1.2)$$

In this equation,  $u = u(x, t)$  is a function of the two independent variables  $x$  and  $t$ ,  $\frac{\partial u}{\partial t}$  is the first partial derivative of  $u$  with respect to  $t$ , and  $\frac{\partial^2 u}{\partial x^2}$  is the second partial derivative of  $u$  with respect to  $x$ .

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*This is a draft chapter from the Kontinua Project. Please see our website (<https://kontinua.org/>) for more details.*



# Answers to Exercises





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