



# LEXICAL SYNTAX

## ANALYSIS



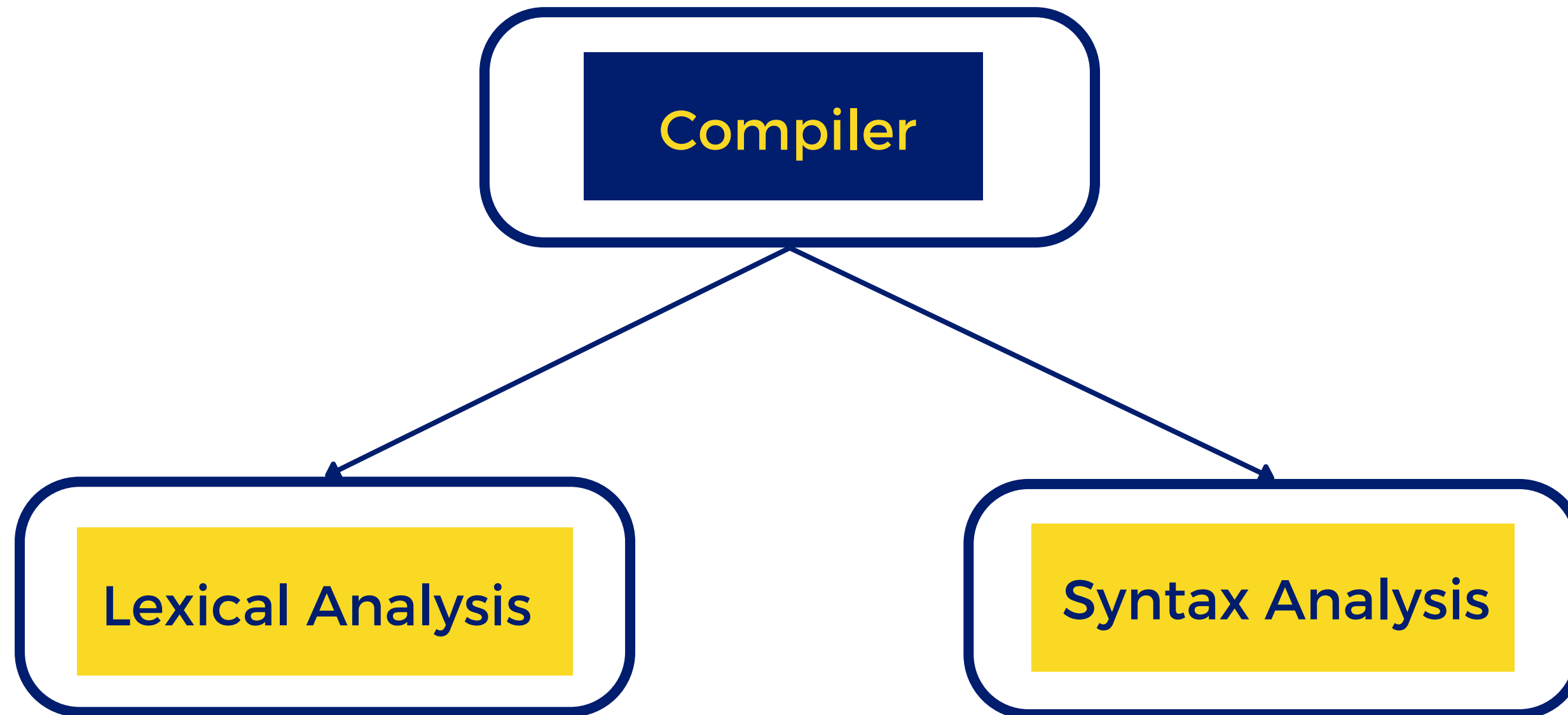
Monzales, Samson, and Tejada



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# INTRODUCTION





# INTRODUCTION



## Why do we separate Lexical and Syntax Analysis?

- Simplicity - lexical analysis is less complex
- Efficiency - lexical analysis can be optimized since it requires more compilation time
- Portability - lexical analyzer is platform dependent whereas syntax analyzer is platform independent



# LEXICAL ANALYSIS

## Lexical Analyzer

- is a **pattern matcher** for **character strings**
- is a “**front-end**” for the **parser**
- Identifies **substrings** of the source program that belong together - **lexemes**
  - Lexemes match a character pattern, which is associated with a lexical category called a **token**



# LEXICAL ANALYSIS

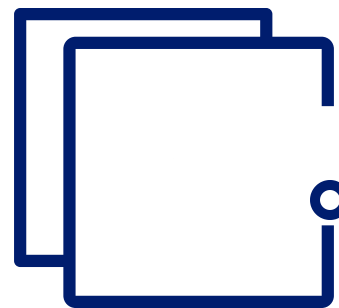
## Lexical Analyzer

- Scans the Pure HLL (High-Level Language) code **line by line**
- Takes **Lexemes** as **input** and produces **Tokens** as **output**
- Removes **comments** and **whitespaces** from the Pure HLL code

# LEXICAL ANALYSIS

## Lexical Analyzer





# LEXICAL

`x = a+b*c;`



Lexical Analysis



Lexemes	Tokens
x	identifier
=	operator
a	identifier
+	operator
b	identifier
*	operator
c	identifier

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# LEXICAL ANALYSIS

## Three approaches to building a lexical analyzer:

- Write a formal description of the tokens and use a software tool that constructs table-driven lexical analyzers given such a description
- Design a state diagram that describes the tokens and write a program that implements the state diagram
- Design a state diagram that describes the tokens and hand-construct a table-driven implementation of the state diagram

# LEXICAL ANALYSIS

## C-Tokens:

- **if:**



- **Identifier:**

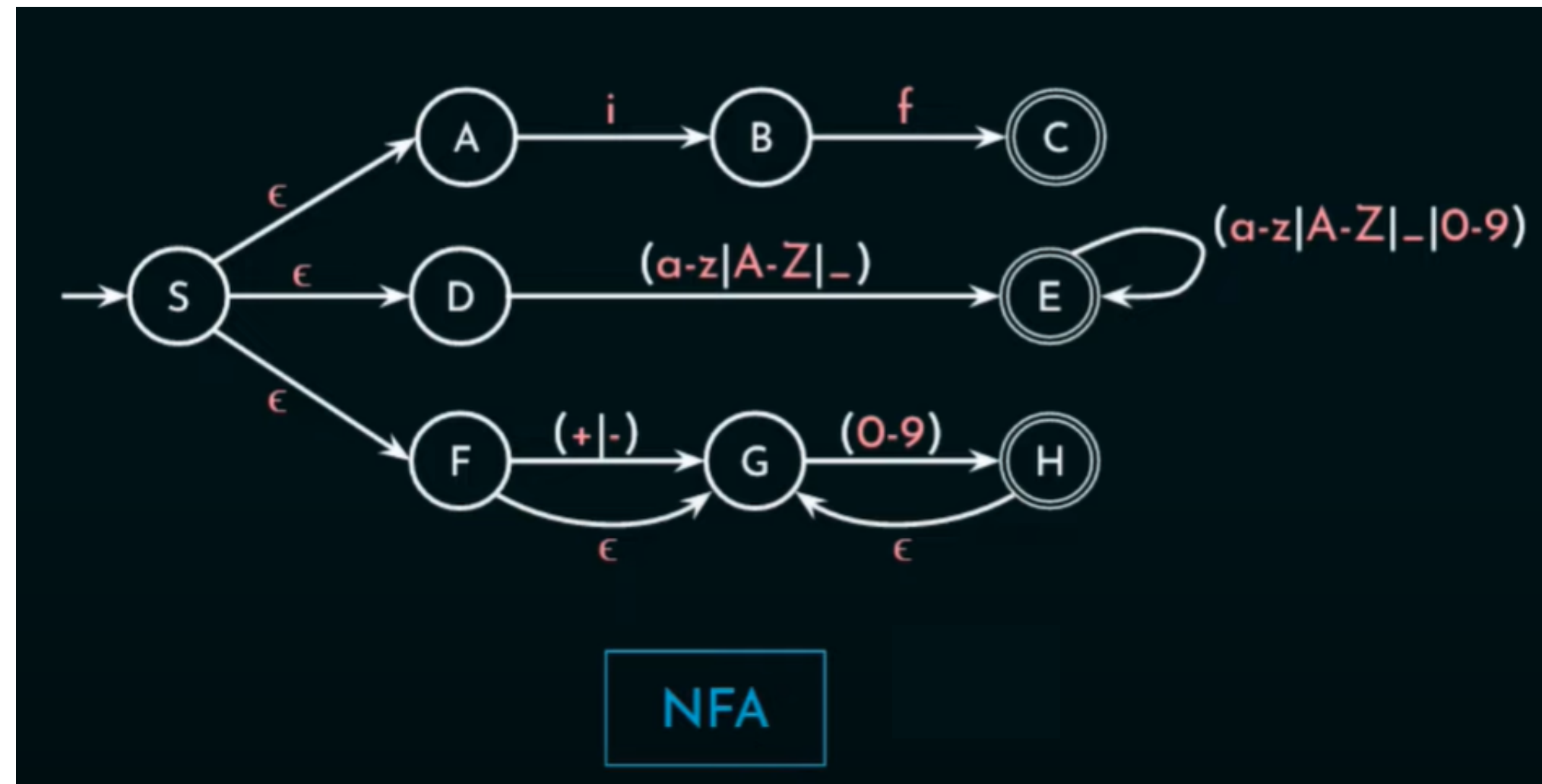


- **Integer:**



# LEXICAL ANALYSIS

State diagram: Non-deterministic Finite Automata (NFA)





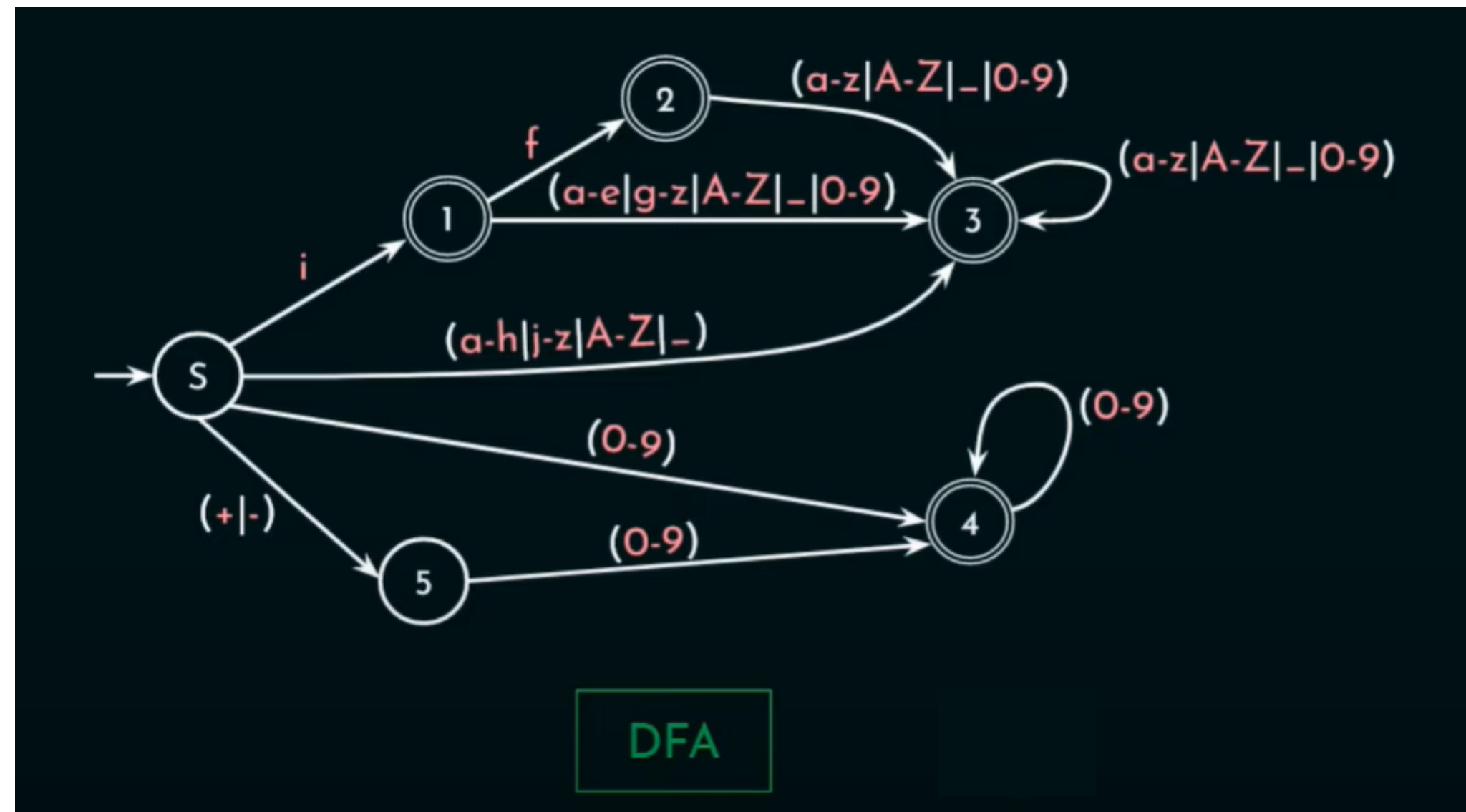
# LEXICAL ANALYSIS

## State Diagram

- **NFA is purely conceptual, so it cannot be implemented.**
- **Hence, conversion to DFA is necessary.**

# LEXICAL ANALYSIS

## State diagram: Deterministic Finite Automata (DFA)





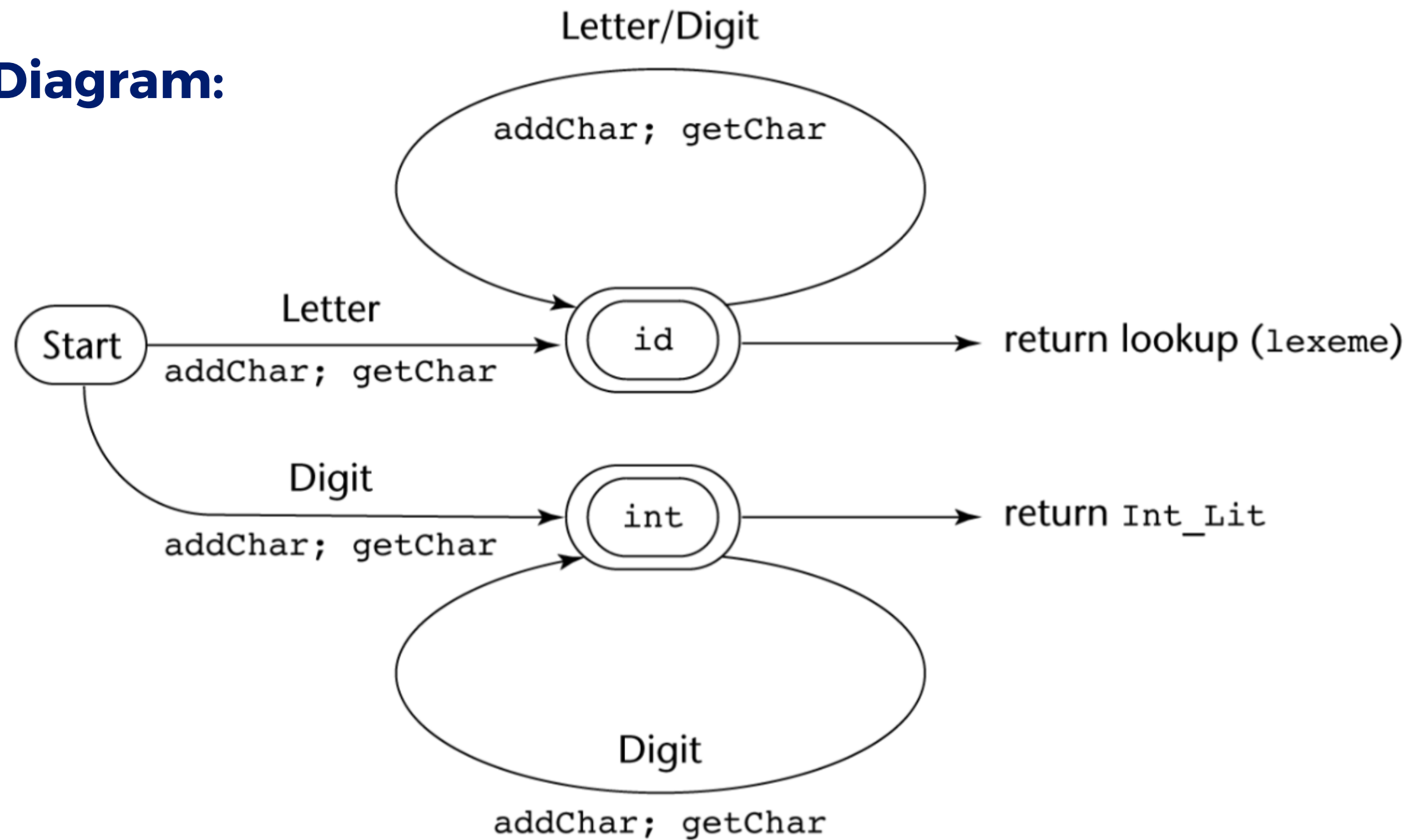
# LEXICAL ANALYSIS

## Convenient utility subprograms:

- **getChar** - gets the next character of input, puts it in
- **nextChar**, determines its class and puts the class in charClass
- **addChar** - puts the character from nextChar into the place the lexeme is being accumulated, lexeme
- **lookup** - determines whether the string in lexeme is a reserved word (returns a code)

# LEXICAL ANALYSIS

## State Diagram:





# LEXICAL ANALYSIS

## Implementation:

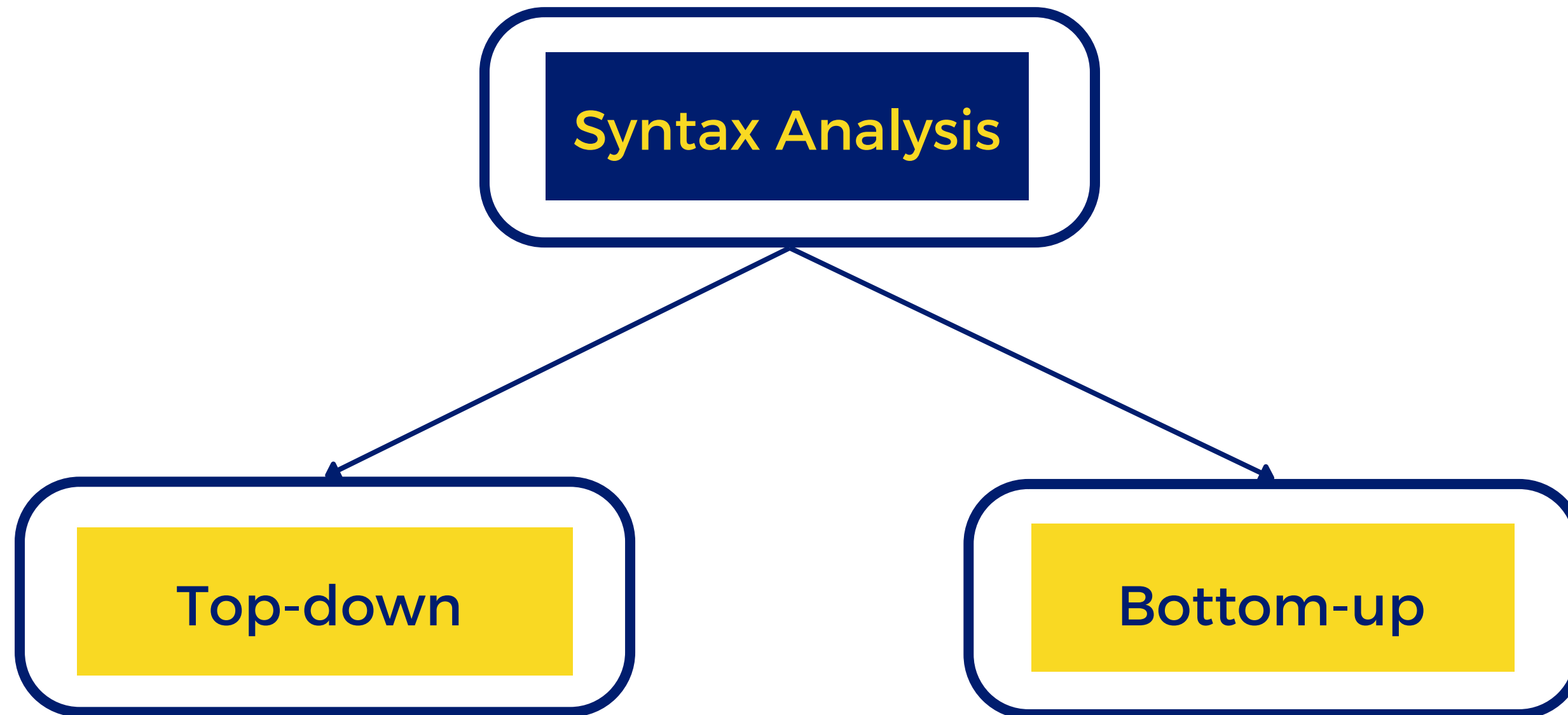
SHOW front.c (pp. 176-181)

Following is the output of the lexical analyzer offront.c when used on **(sum + 47) / total**

Next token is: 25 Next lexeme is (  
Next token is: 11 Next lexeme is sum  
Next token is: 21 Next lexeme is +  
Next token is: 10 Next lexeme is 47  
Next token is: 26 Next lexeme is )  
Next token is: 24 Next lexeme is /  
Next token is: 11 Next lexeme is total  
Next token is: -1 Next lexeme is EOF



# THE PARSING PROBLEM





# THE PARSING PROBLEM

## Two distinct goals of syntax analysis:

1. Check for syntax errors and produce a diagnostic message and recover
2. Produce a complete parse tree, or at least trace the structure of the complete parse tree

# THE PARSING PROBLEM

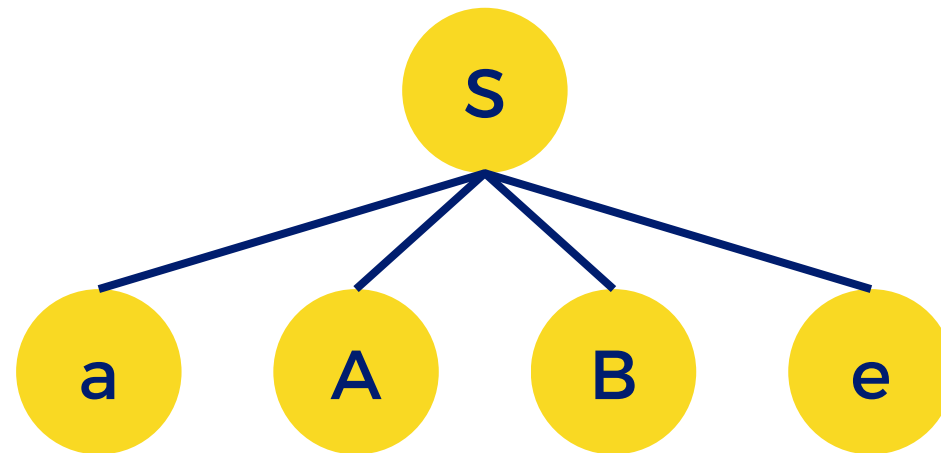
S

Top-down Approach

$S \rightarrow aABe, A \rightarrow Abc \mid a, B \rightarrow d$

aabcde

# THE PARSING PROBLEM

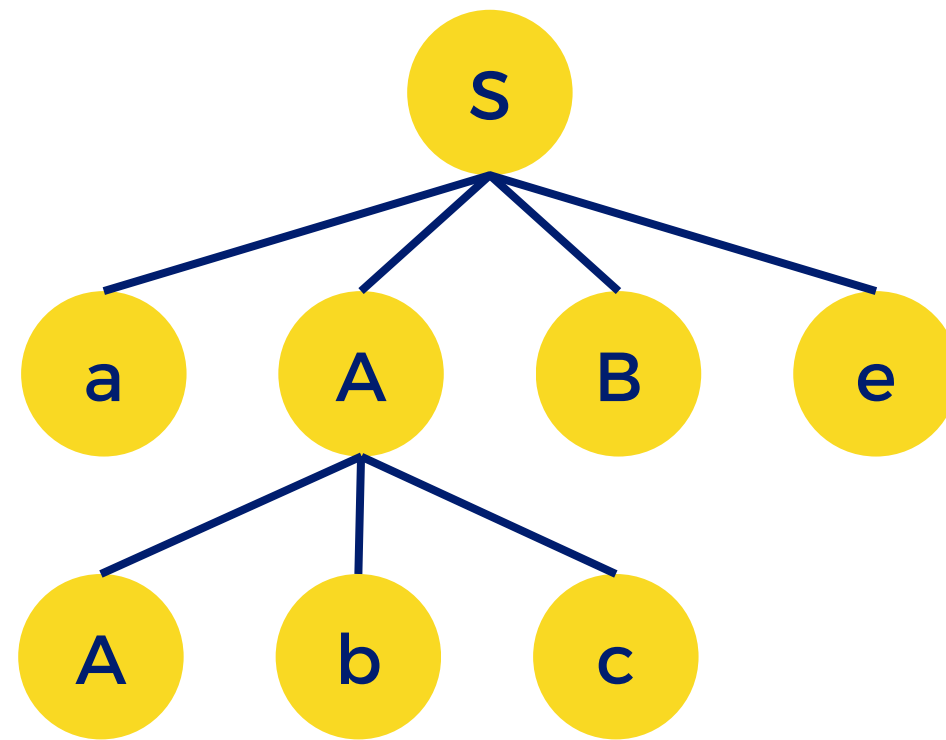


Top-down Approach

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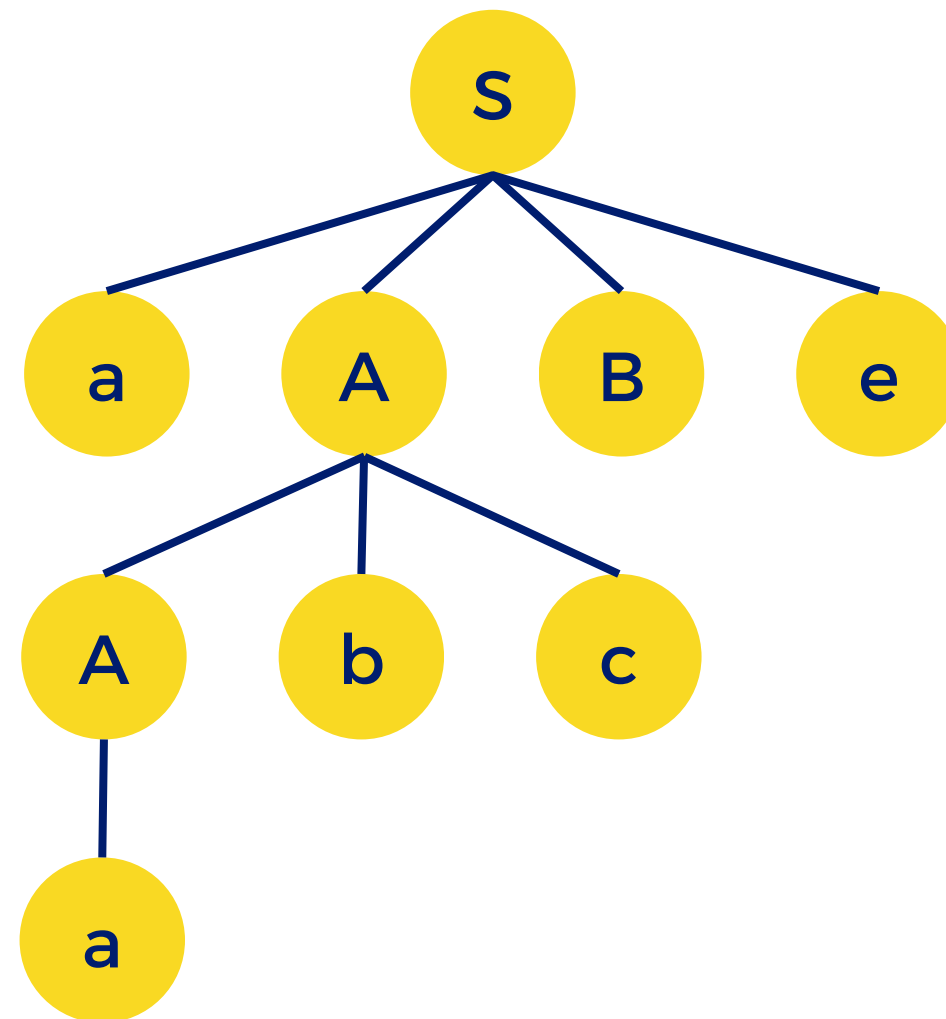


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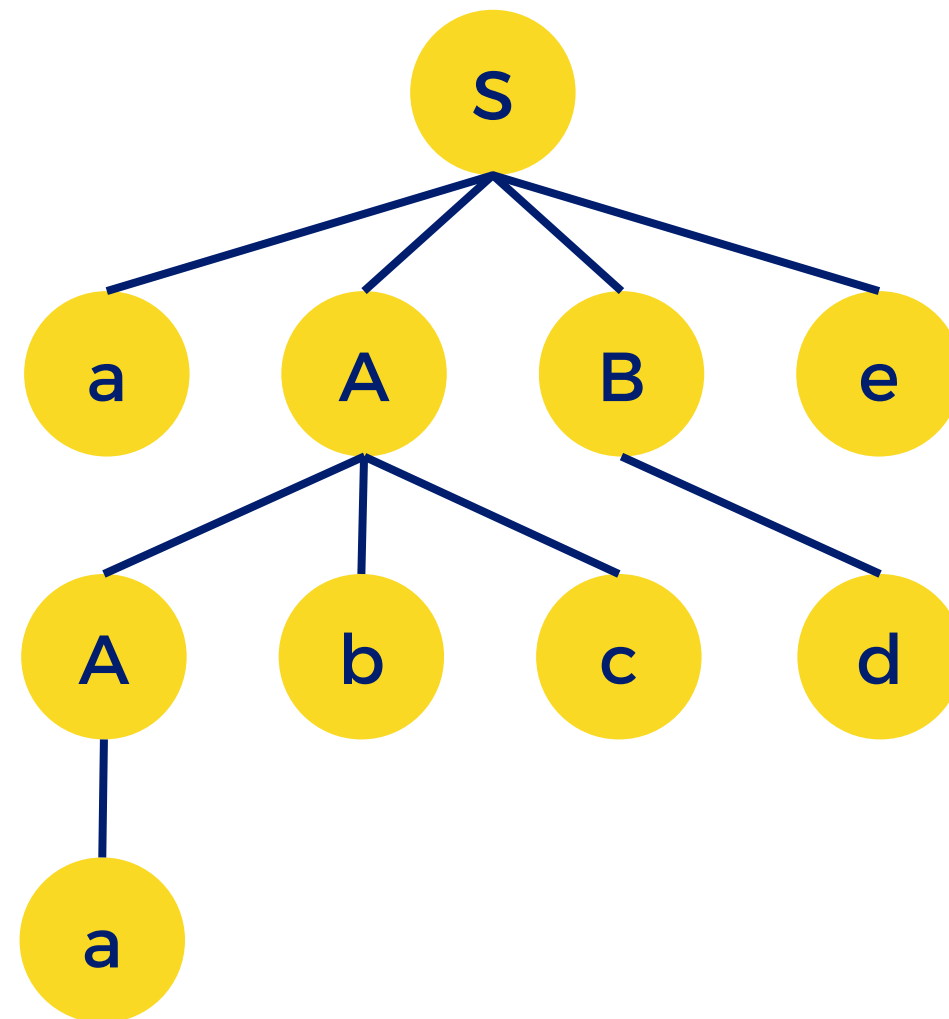


Top-down Approach

$S \rightarrow aABe, A \rightarrow Abc \mid \boxed{a}, B \rightarrow d$

aabcde

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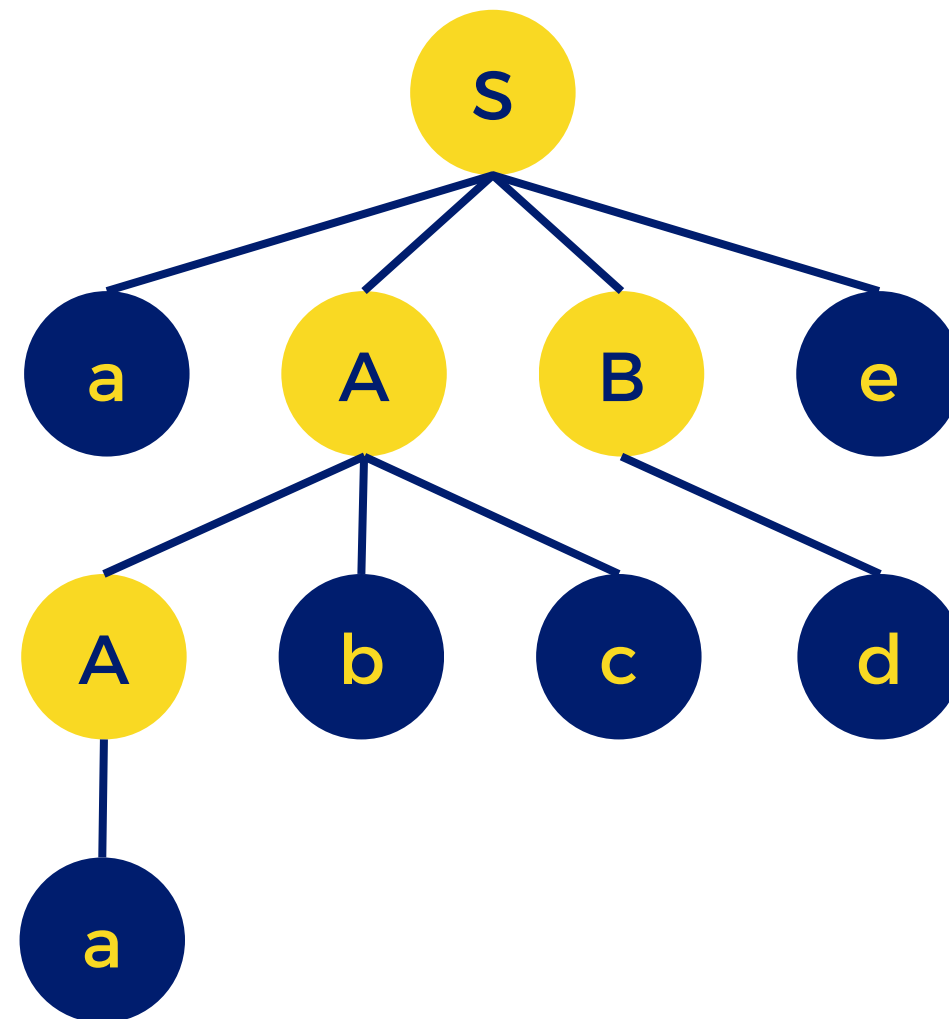


Top-down Approach

$S \rightarrow aABe$ ,  $A \rightarrow Abc \mid a$ ,  $B \rightarrow d$

aabcde

# THE PARSING PROBLEM



Top-down Approach

$S \rightarrow aABe, A \rightarrow Abc \mid a, B \rightarrow d$

aabcde



# THE PARSING PROBLEM

Bottom-up Approach

$S \rightarrow aABe, A \rightarrow Abc \mid a, B \rightarrow d$

aabcde

a

a

b

c

d

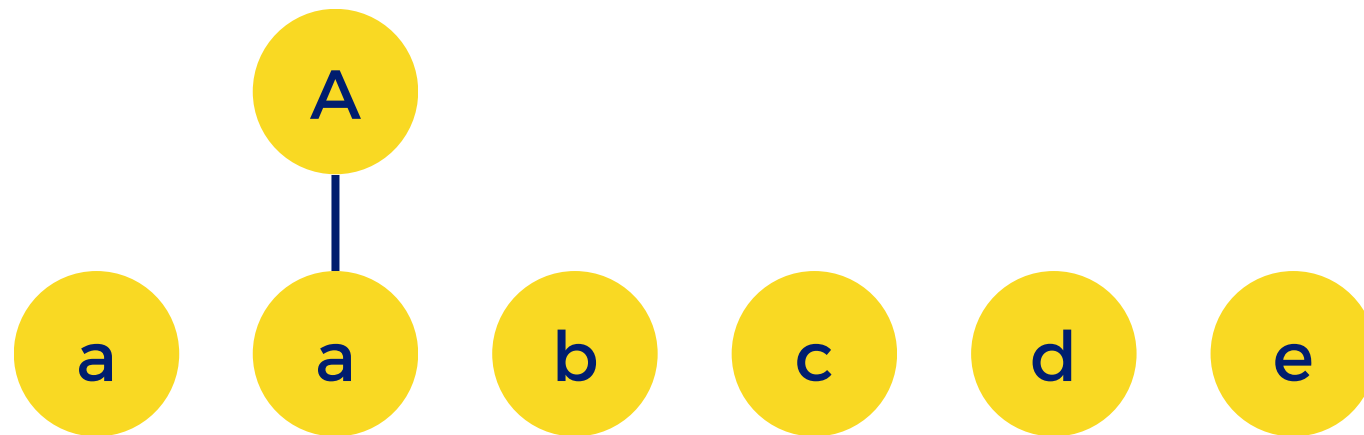
e

# THE PARSING PROBLEM

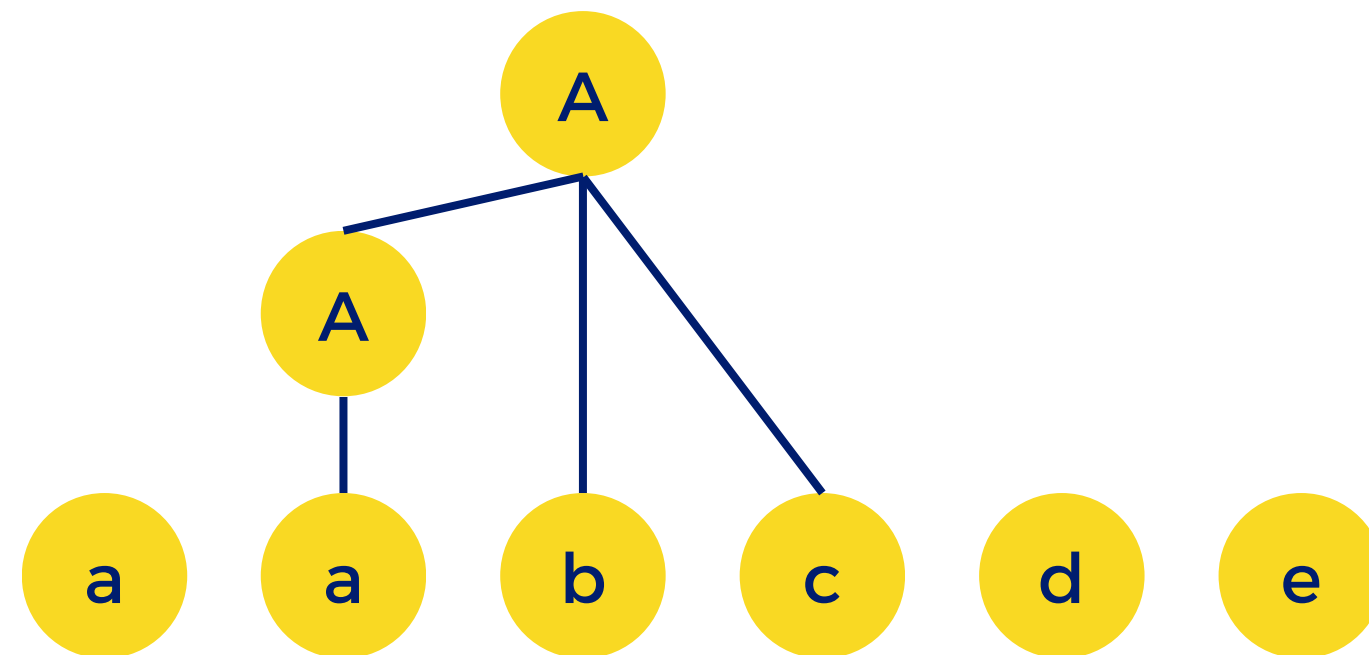
## Bottom-up Approach

$S \rightarrow aABe, A \rightarrow Abc \parallel a, B \rightarrow d$

aabcde



# THE PARSING PROBLEM

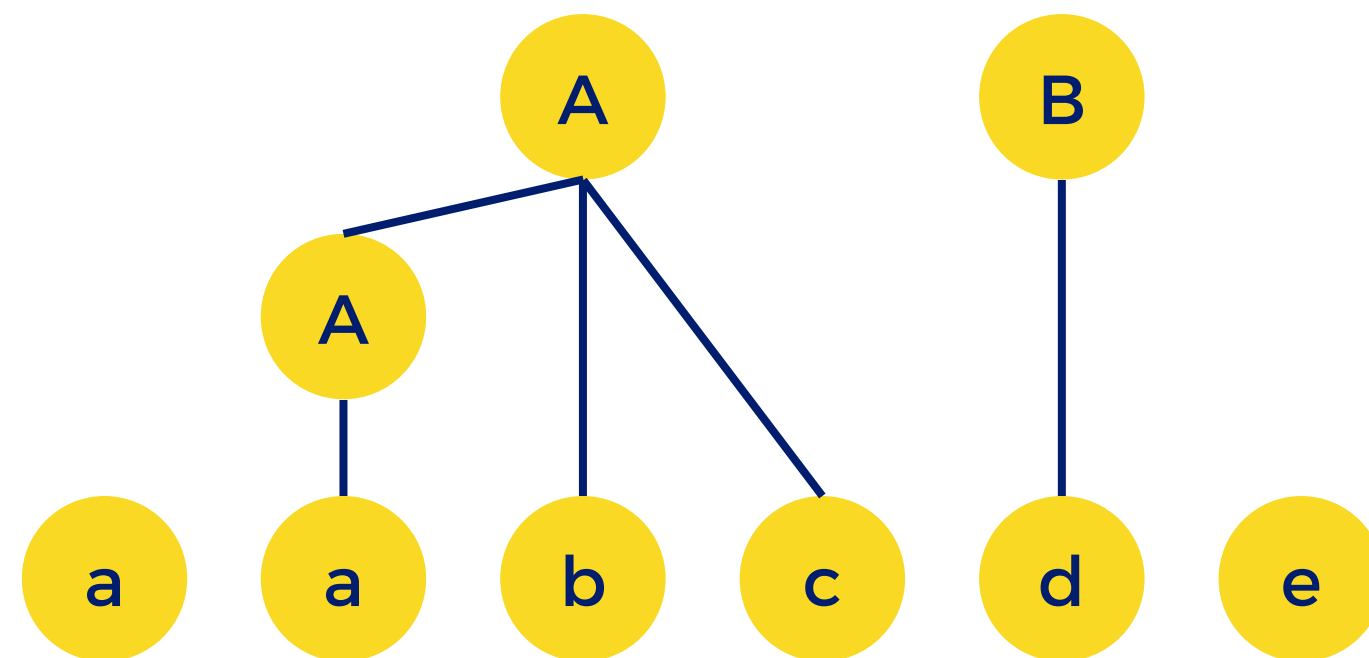


Bottom-up Approach

$S \rightarrow aABe$ ,  $A \rightarrow Abc$ ,  $a$ ,  $B \rightarrow d$

aabcde

# THE PARSING PROBLEM

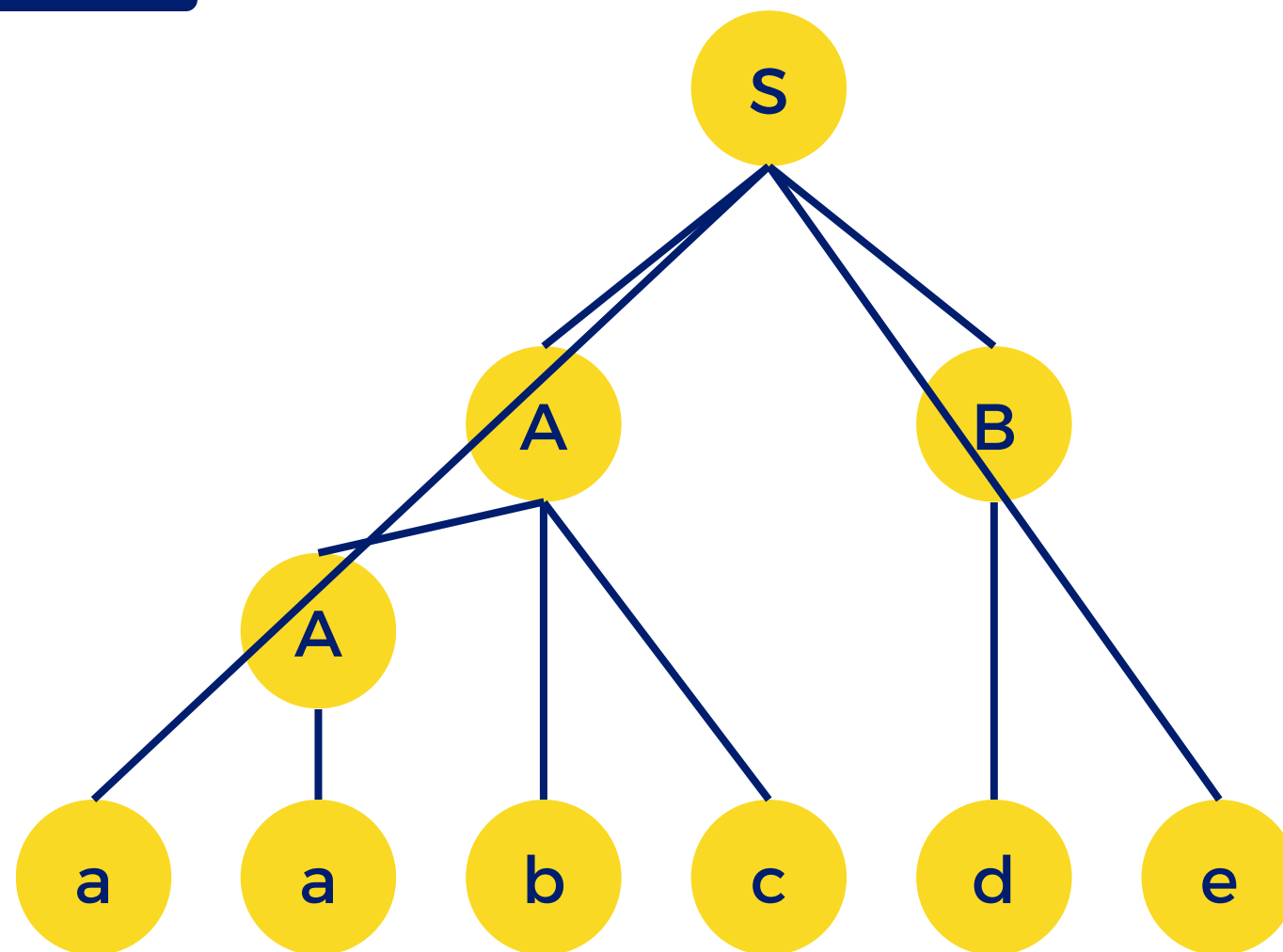


Bottom-up Approach

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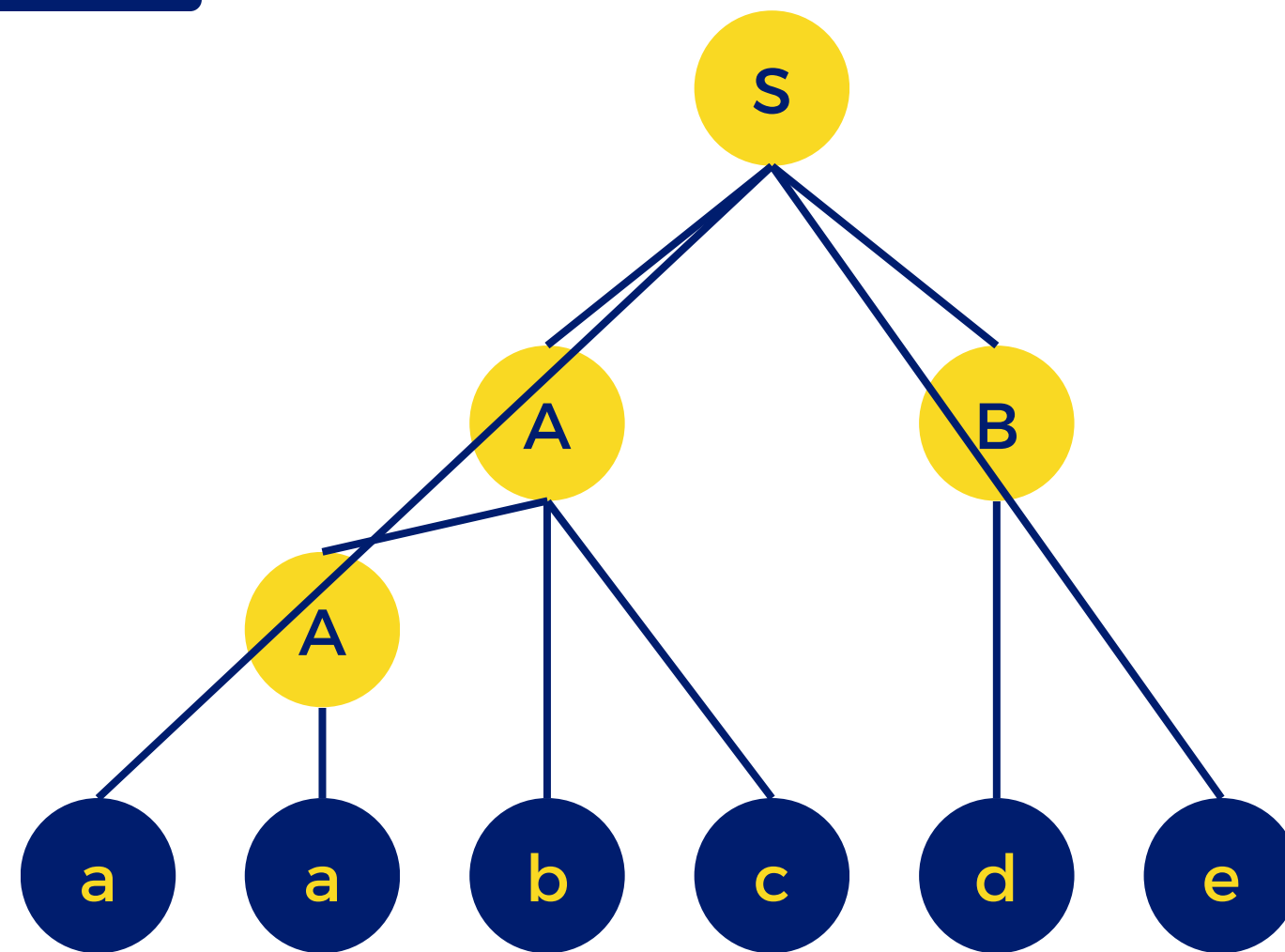


Bottom-up Approach

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aabcde

# THE PARSING PROBLEM



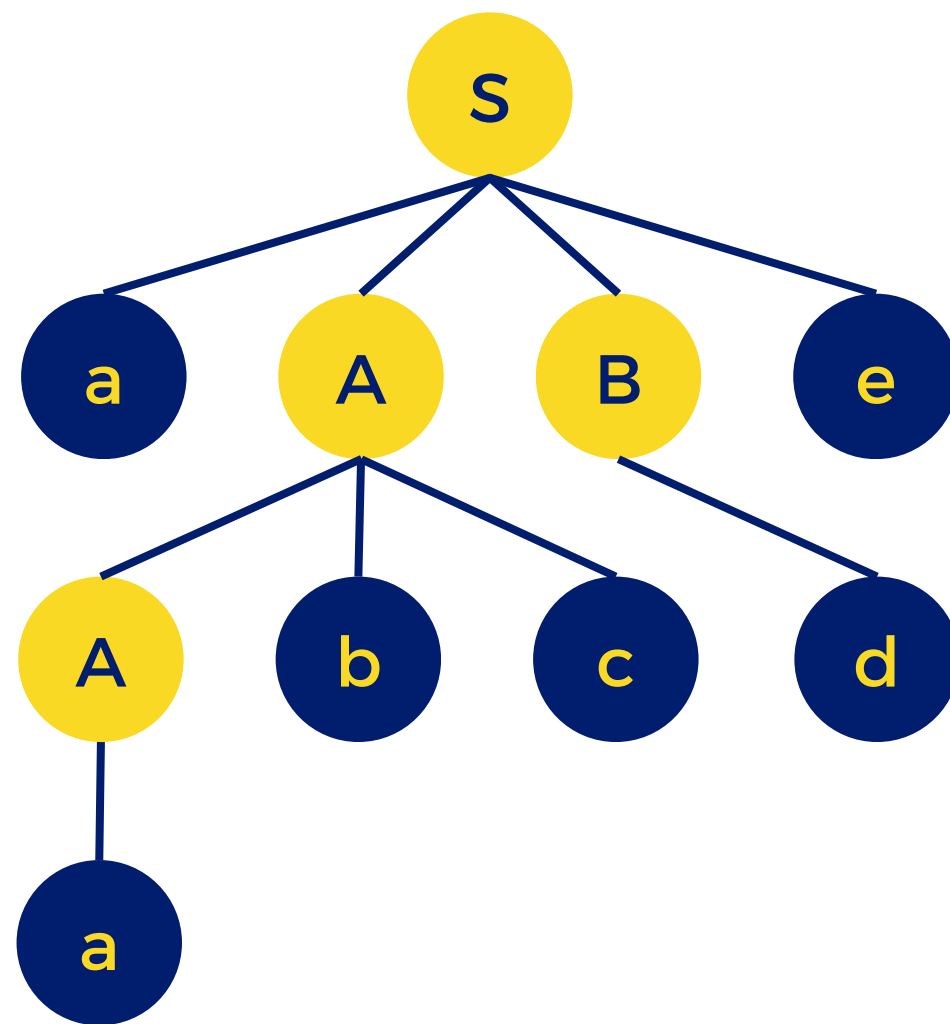
Bottom-up Approach

$S \rightarrow aABe, A \rightarrow Abc \mid a, B \rightarrow d$

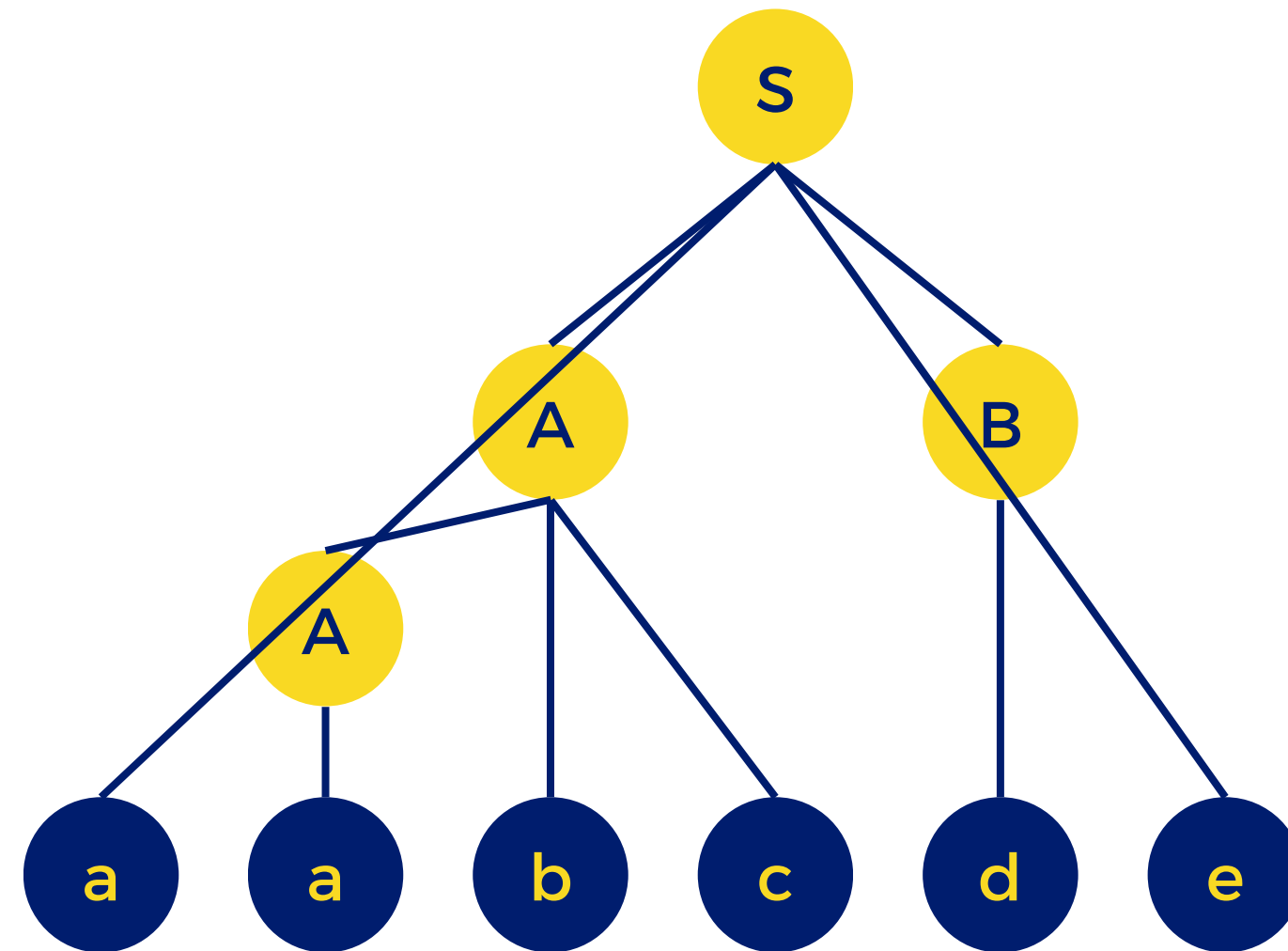
aabcde

# THE PARSING PROBLEM

Top-down Approach



Bottom-up Approach





# THE PARSING PROBLEM

## Time Complexity

Unambiguous grammar =  $O(n^3)$

Commercial Compilers =  $O(n)$





# RECURSIVE-DESCENT PARSING

## Recursive-Descent Parsing (Top-Down)

There is a **subprogram for each nonterminal** in the **grammar**, which can parse sentences that can be generated by that nonterminal value.

**EBNF** is ideally suited for being the basis for a recursive-descent parser, because **EBNF minimizes the number of nonterminals**

**\*EBNF - Extended Backus-Naur form**



# RECURSIVE-DESCENT PARSING

- Assume we have a lexical analyzer named `lex`, which puts the next token code in `nextToken`
- The coding process when there is only one right-hand side (RHS):
  - For each terminal symbol in the RHS, compare it with the next input token; if they match, continue, else there is an error
  - For each nonterminal symbol in the RHS, call its associated parsing subprogram



# RECURSIVE-DESCENT PARSING

A nonterminal that has more than one RHS requires an initial process to determine which RHS it is to parse

- The correct RHS is chosen on the basis of the next token of input (the lookahead)
- The next token is compared with the first token that can be generated by each RHS until a match is found
- If no match is found, it is a syntax error



# RECURSIVE-DESCENT PARSING

## Recursive-Descent Parsing

Given grammar:

$A \rightarrow abC \mid aBd \mid aAD$

$B \rightarrow bB \mid \epsilon$

$C \rightarrow d \mid \epsilon$

$D \rightarrow a \mid b \mid \epsilon$

\*Capital characters - non-terminal

**Input: aaba**

Monzales, Samson, and Tejada

# RECURSIVE-DESCENT PARSING

## Recursive-Descent Parsing

**a a b a**



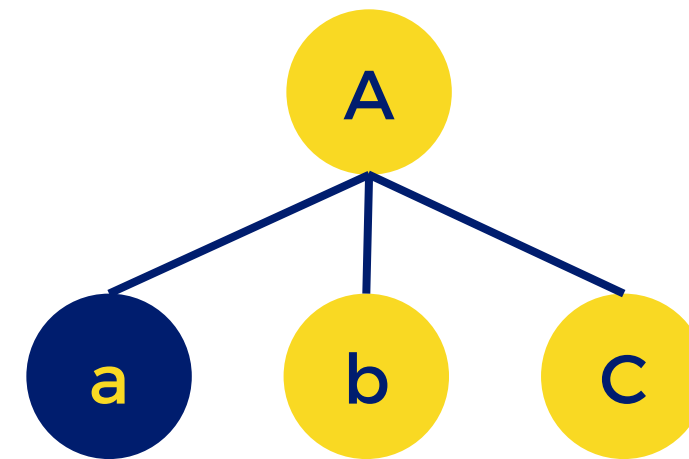
Given grammar:

**A**  $\rightarrow$  **a****b****C** | **a****B****d** | **a****A****D**

**B**  $\rightarrow$  **b****B** |  $\epsilon$

**C**  $\rightarrow$  **d** |  $\epsilon$

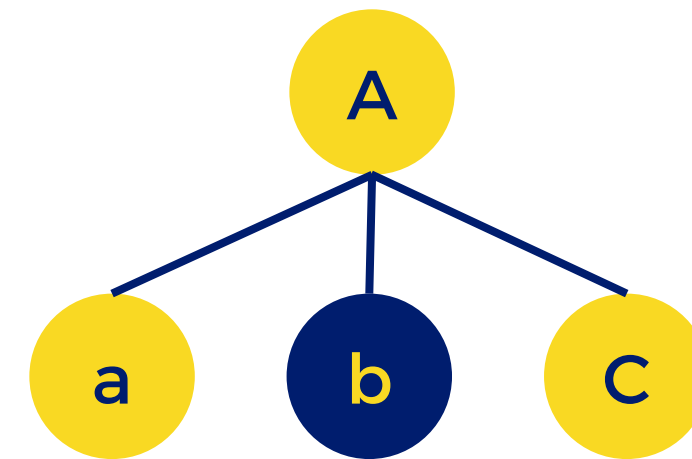
**D**  $\rightarrow$  **a** | **b** |  $\epsilon$



# RECURSIVE-DESCENT PARSING

## Recursive-Descent Parsing

a a b a



Given grammar:

$A \rightarrow abC \mid aBd \mid aAD$

$B \rightarrow bB \mid \epsilon$

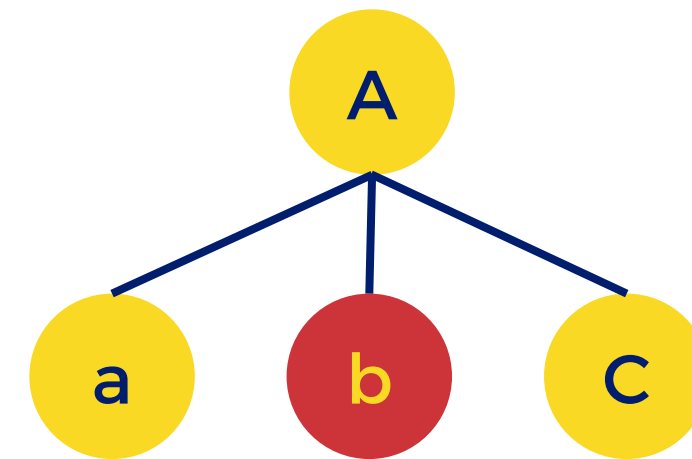
$C \rightarrow d \mid \epsilon$

$D \rightarrow a \mid b \mid \epsilon$

# RECURSIVE-DESCENT PARSING

## Recursive-Descent Parsing

a **a** b a  
↑



Given grammar:

$A \rightarrow \mathbf{abC} \mid \mathbf{aBd} \mid \mathbf{aAD}$

$B \rightarrow \mathbf{bB} \mid \epsilon$

$C \rightarrow \mathbf{d} \mid \epsilon$

$D \rightarrow \mathbf{a} \mid \mathbf{b} \mid \epsilon$

# RECURSIVE-DESCENT PARSING

## Recursive-Descent Parsing

**a a b a**



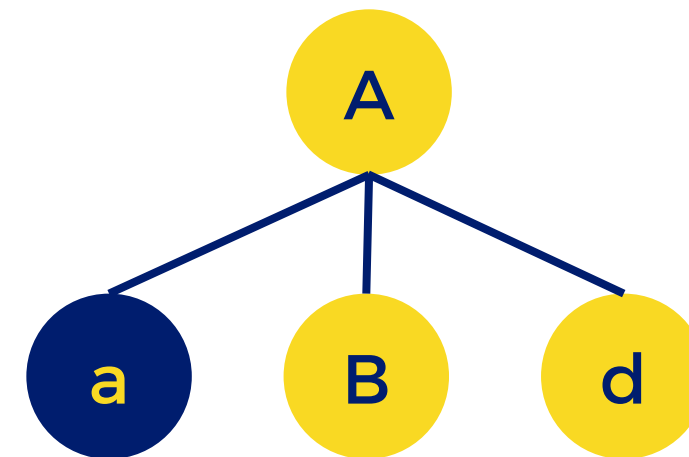
Given grammar:

**A**  $\rightarrow$  abC | **aBd** | aAD

**B**  $\rightarrow$  bB |  $\epsilon$

**C**  $\rightarrow$  d |  $\epsilon$

**D**  $\rightarrow$  a | b |  $\epsilon$





# RECURSIVE-DESCENT PARSING

## Recursive-Descent Parsing

a **a** b a



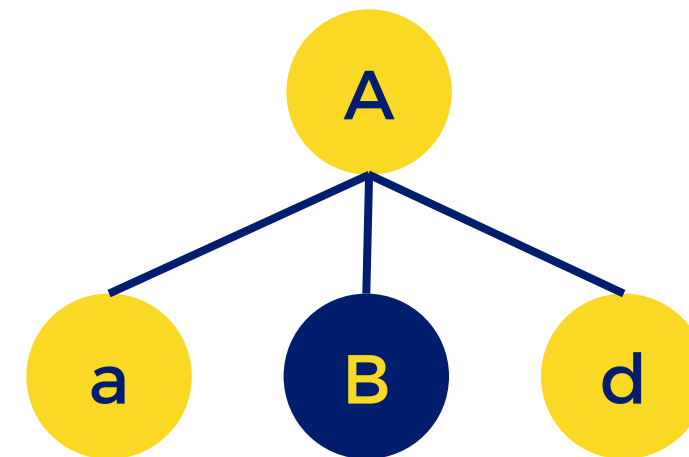
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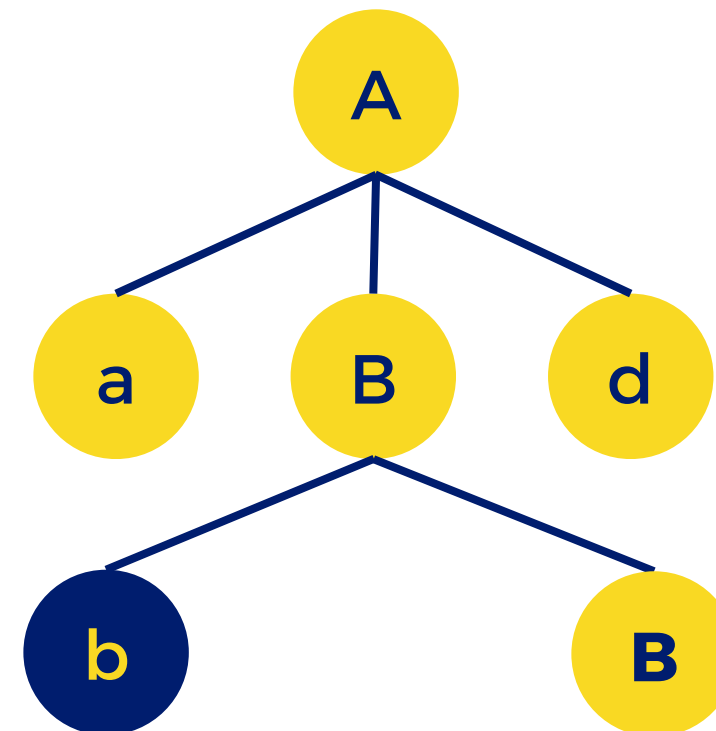
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# RECURSIVE-DESCENT PARSING

## Recursive-Descent Parsing

a **a** b a



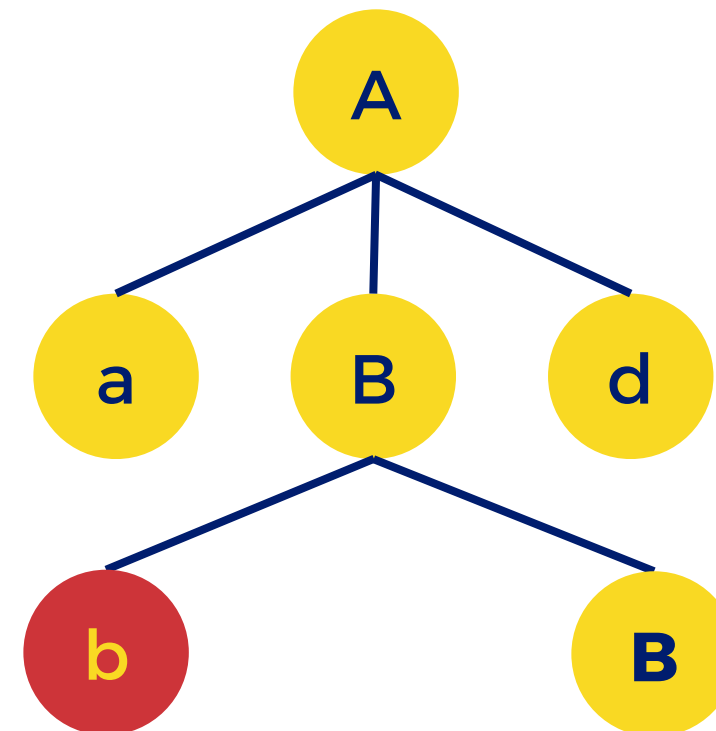
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# RECURSIVE-DESCENT PARSING

## Recursive-Descent Parsing

a **a** b a



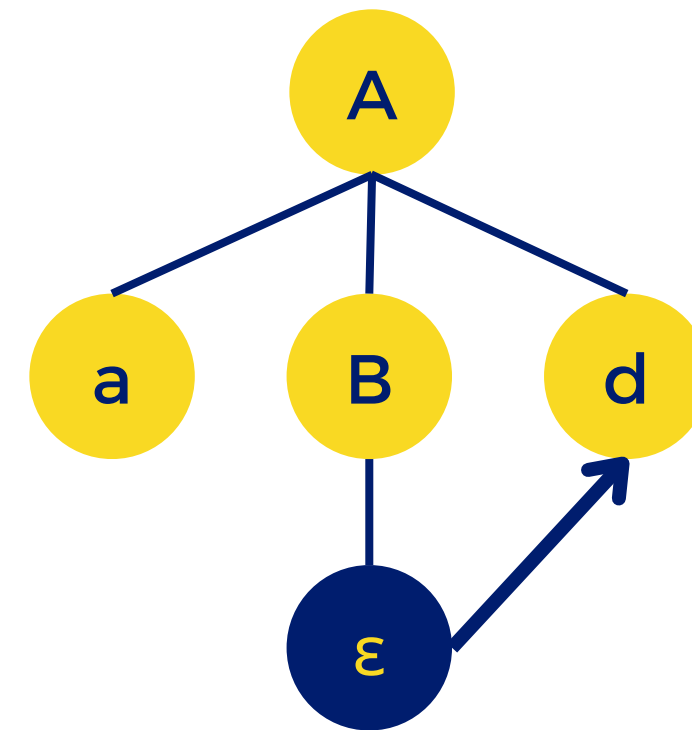
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# RECURSIVE-DESCENT PARSING

## Recursive-Descent Parsing

a **a** b a



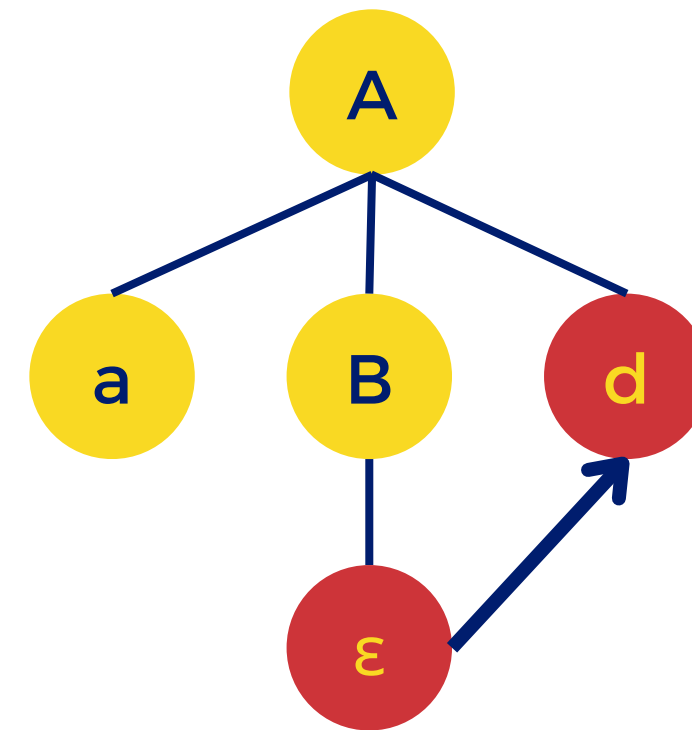
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# RECURSIVE-DESCENT PARSING

## Recursive-Descent Parsing

**a a b a**



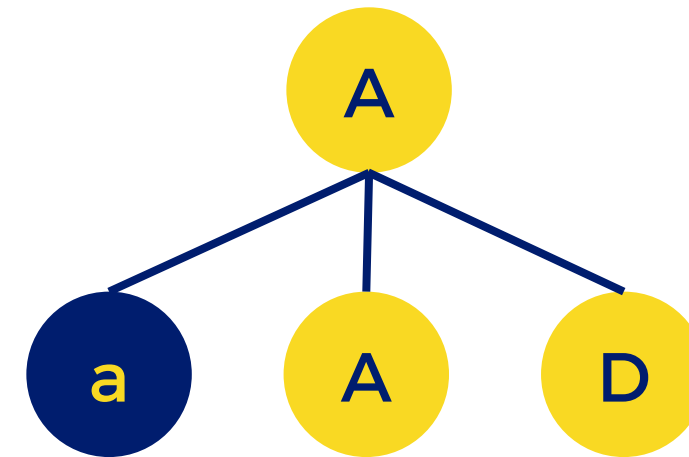
Given grammar:

**A**  $\rightarrow$  abC | aBd | **aAD**

B  $\rightarrow$  bB |  $\epsilon$

C  $\rightarrow$  d |  $\epsilon$

D  $\rightarrow$  a | b |  $\epsilon$



# RECURSIVE-DESCENT PARSING

## Recursive-Descent Parsing

a a b a



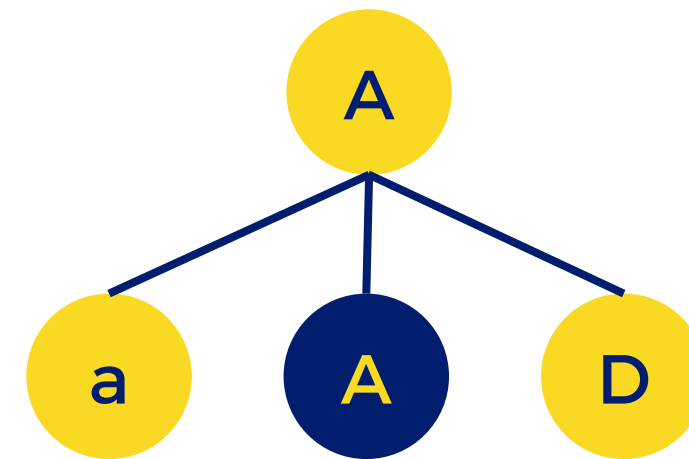
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# RECURSIVE-DESCENT PARSING

## Recursive-Descent Parsing

a a b a



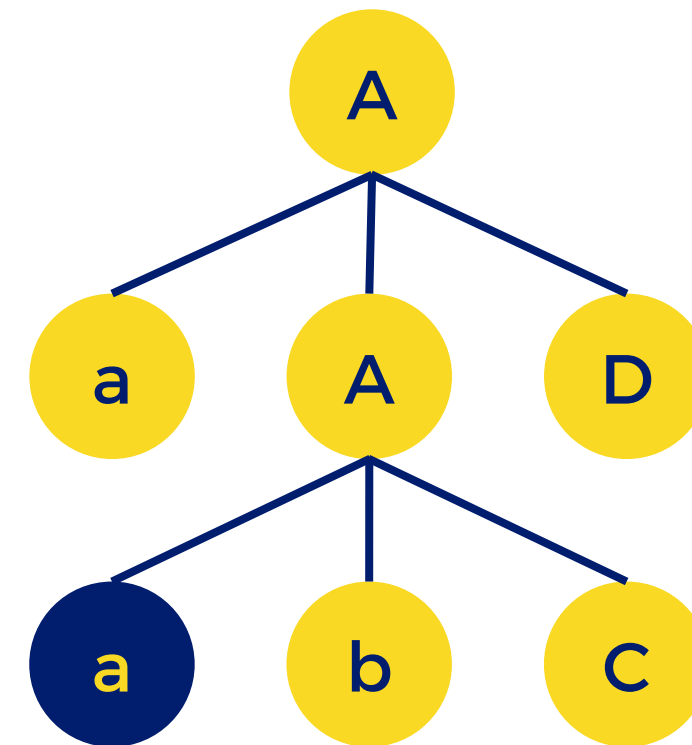
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# RECURSIVE-DESCENT PARSING

## Recursive-Descent Parsing

a a **b** a



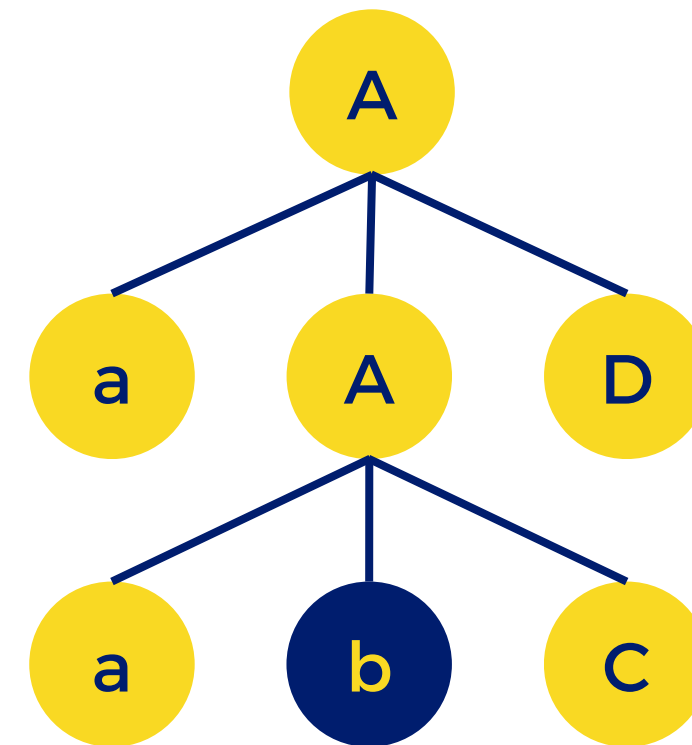
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**A**  $\rightarrow$  **a****b****C** | **a****B****d** | **a****A****D**

**B**  $\rightarrow$  **b****B** |  $\epsilon$

**C**  $\rightarrow$  **d** |  $\epsilon$

**D**  $\rightarrow$  **a** | **b** |  $\epsilon$



# RECURSIVE-DESCENT PARSING

## Recursive-Descent Parsing

a a b a



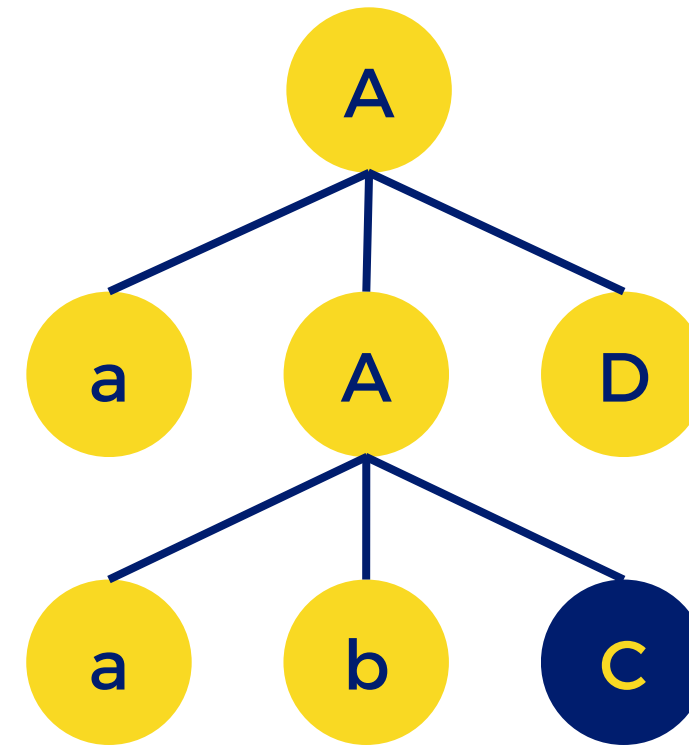
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# RECURSIVE-DESCENT PARSING

## Recursive-Descent Parsing

a a b a



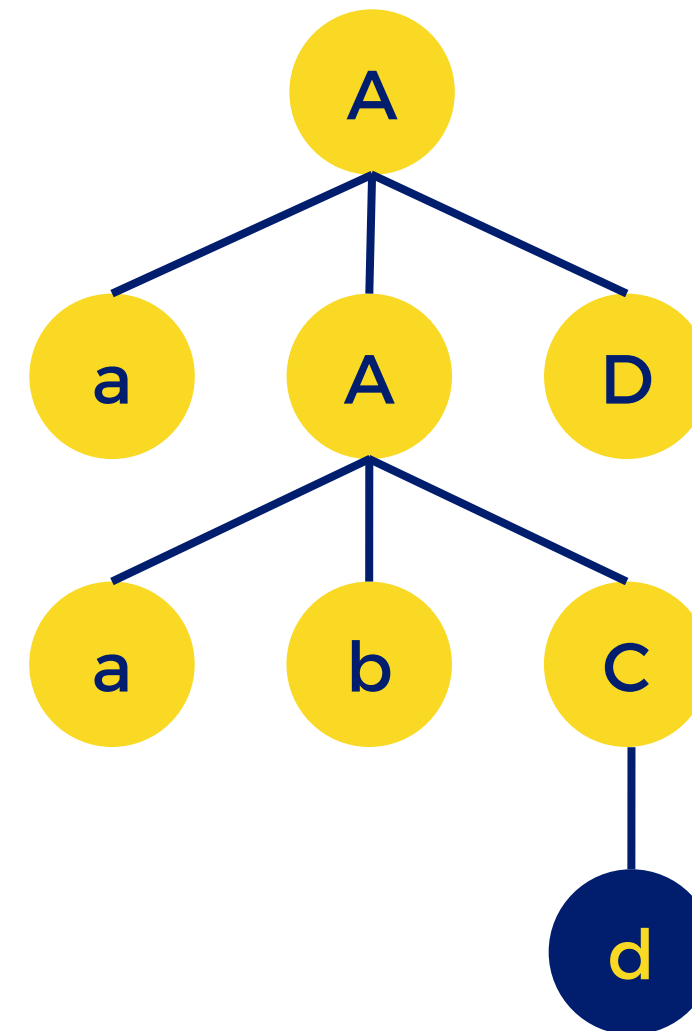
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# RECURSIVE-DESCENT PARSING

## Recursive-Descent Parsing

a a b a



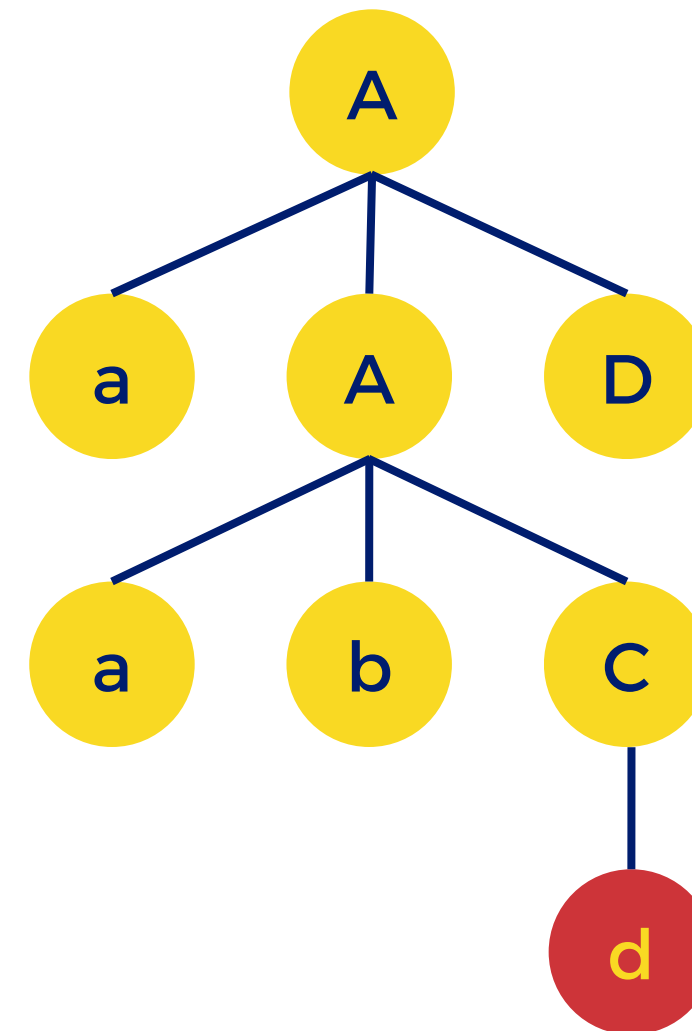
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# RECURSIVE-DESCENT PARSING

## Recursive-Descent Parsing

a a b a



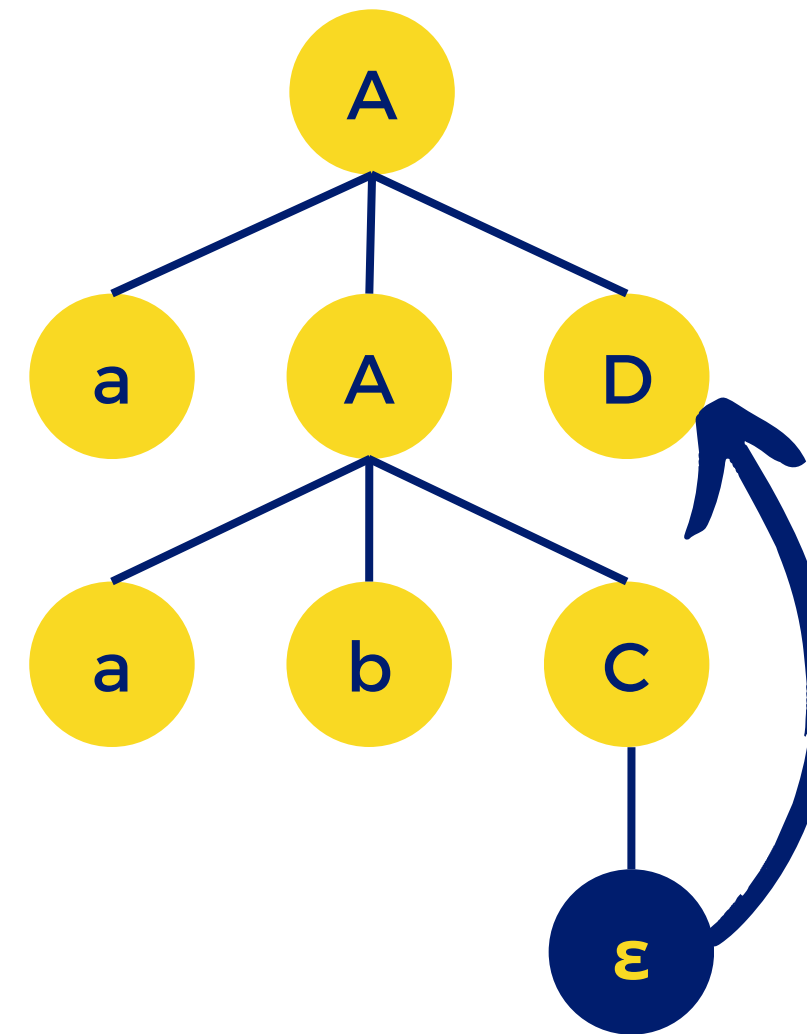
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**B**  $\rightarrow$  **b****B** |  $\epsilon$

**C**  $\rightarrow$  **d** |  $\epsilon$

**D**  $\rightarrow$  **a** | **b** |  $\epsilon$



# RECURSIVE-DESCENT PARSING

## Recursive-Descent Parsing

a a b a



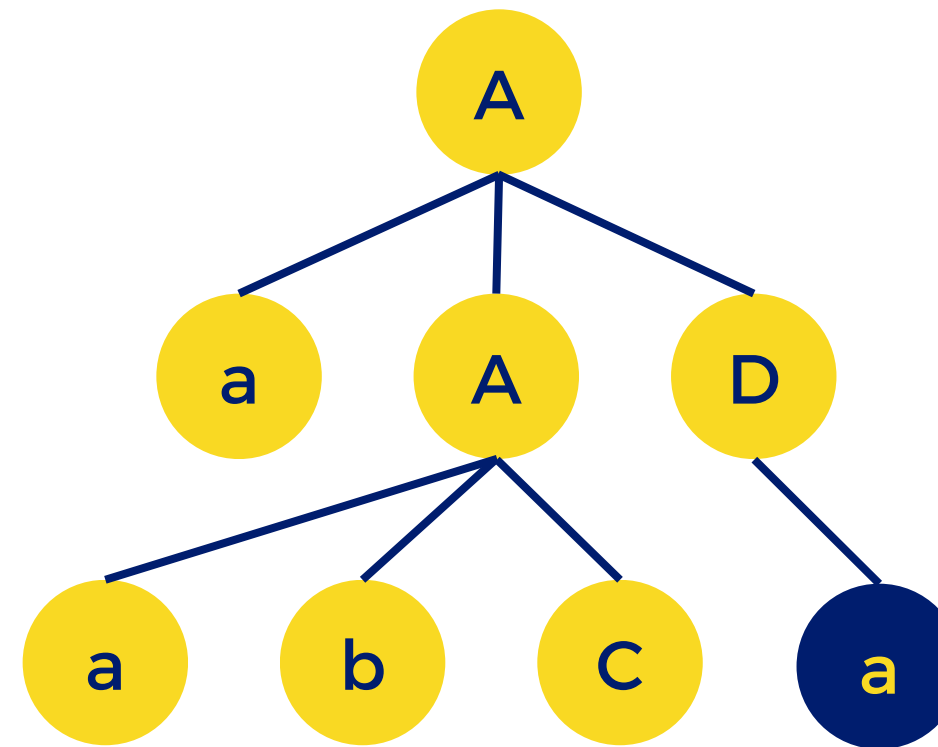
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# RECURSIVE-DESCENT PARSING

## Recursive-Descent Parsing

a a b a

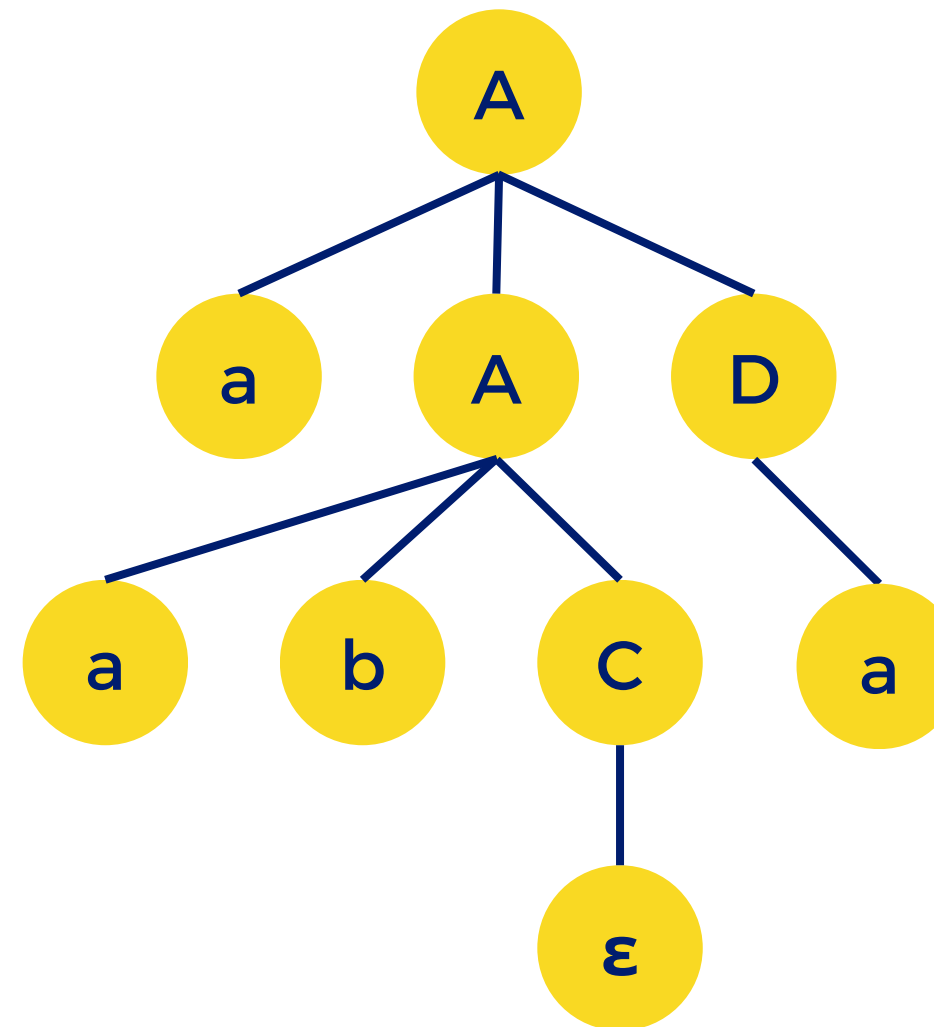
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# RECURSIVE-DESCENT PARSING

## Recursive-Descent Parsing

a a b a

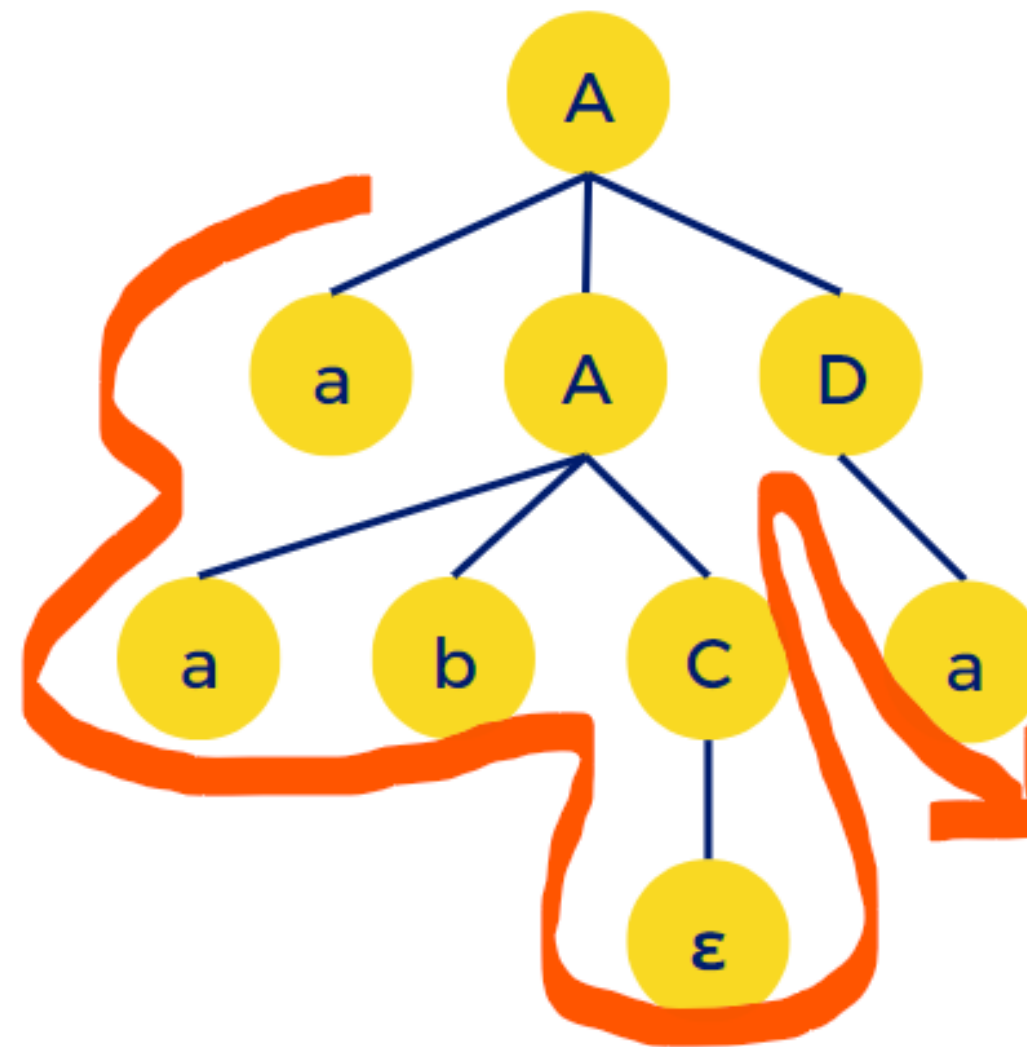
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# RECURSIVE-DESCENT PARSING



## **Problem with Left Recursion:**

If a left recursion is present in any grammar then, during parsing in the syntax analysis part of compilation, there is a chance that the grammar will create an infinite loop. This is because, at every time of production of grammar, A will produce another A without checking any condition.



# RECURSIVE-DESCENT PARSING

- The other characteristic of grammars that disallows top-down parsing is the lack of pairwise disjointness
  - The inability to determine the correct RHS on the basis of one token of lookahead
  - Def:  $\text{FIRST}(\alpha) = \{a \mid \alpha \Rightarrow^* a\beta\}$   
(If  $\alpha \Rightarrow^* \epsilon$ ,  $\epsilon$  is in  $\text{FIRST}(\alpha)$ )



# RECURSIVE-DESCENT PARSING

- Pairwise Disjointness Test:
  - For each nonterminal,  $A$ , in the grammar that has more than one RHS, for each pair of rules,  $A \rightarrow \alpha_i$  and  $A \rightarrow \alpha_j$ , it must be true that
$$\text{FIRST}(\alpha_i) \cap \text{FIRST}(\alpha_j) = \varnothing$$

# RECURSIVE-DESCENT PARSING

**Example 1:** Consider the following grammar

$A : a B$

$A : b A b$

$A : B b$

$B : c B$

$B : d$

The FIRST sets for the RHS of A-rules are:  $\text{FIRST}(aB) = \{ a \}$ ,  $\text{FIRST}(bAb) = \{ b \}$ , and  $\text{FIRST}(Bb) = \{ c, d \}$ . These are disjoint and hence PASS the pairwise disjoint test.

The FIRST sets for the RHS of B-rules are:  $\text{FIRST}(cB) = \{ c \}$  and  $\text{FIRST}(d) = \{ d \}$ . These are disjoint and hence PASS the pairwise disjoint test.

# RECURSIVE-DESCENT PARSING

**Example 2:** Consider the following grammar

A : a B  
A : B A b  
B : a B  
B : b

The FIRST sets for the RHS of A-rules are:  $\text{FIRST}(aB) = \{ a \}$  and  $\text{FIRST}(BA b) = \{ a, b \}$ . These are not disjoint and hence FAIL the pairwise disjoint test.

The FIRST sets for the RHS of B-rules are:  $\text{FIRST}(aB) = \{ a \}$  and  $\text{FIRST}(b) = \{ b \}$ . These are disjoint and hence PASS the pairwise disjoint test.

So, the grammar as a whole fails the pairwise disjoint test and hence cannot be parsed using top-down parsers!



# RECURSIVE-DESCENT PARSING

- Left factoring can resolve the problem

Replace

$\langle \text{variable} \rangle \rightarrow \text{identifier} \mid \text{identifier} [\langle \text{expression} \rangle]$

with

$\langle \text{variable} \rangle \rightarrow \text{identifier} \langle \text{new} \rangle$

$\langle \text{new} \rangle \rightarrow \varepsilon \mid [\langle \text{expression} \rangle]$

or

$\langle \text{variable} \rangle \rightarrow \text{identifier} [[\langle \text{expression} \rangle]]$

(the outer brackets are metasymbols of EBNF)

# RECURSIVE-DESCENT PARSING

$A \rightarrow a\alpha1 / a\alpha2 / a\alpha3$

Grammar  
with  
common prefixes

Left Factoring

$A \rightarrow aA'$   
 $A' \rightarrow \alpha1 / \alpha2 / \alpha3$

Left Factored Grammar

# RECURSIVE-DESCENT PARSING

## Problem-01:

Do left factoring in the following grammar-

$$S \rightarrow iEtS / iEtSeS / a$$

$$E \rightarrow b$$



# RECURSIVE-DESCENT PARSING

## Solution-

The left factored grammar is-

$$S \rightarrow iEtSS' / a$$

$$S' \rightarrow eS / \epsilon$$

$$E \rightarrow b$$



# RECURSIVE-DESCENT PARSING



## Problem-02:

Do left factoring in the following grammar-

$$A \rightarrow aAB / aBc / aAc$$

# RECURSIVE-DESCENT PARSING

## Step-01:

$$A \rightarrow aA'$$

$$A' \rightarrow AB / Bc / Ac$$

Again, this is a grammar with common prefixes.

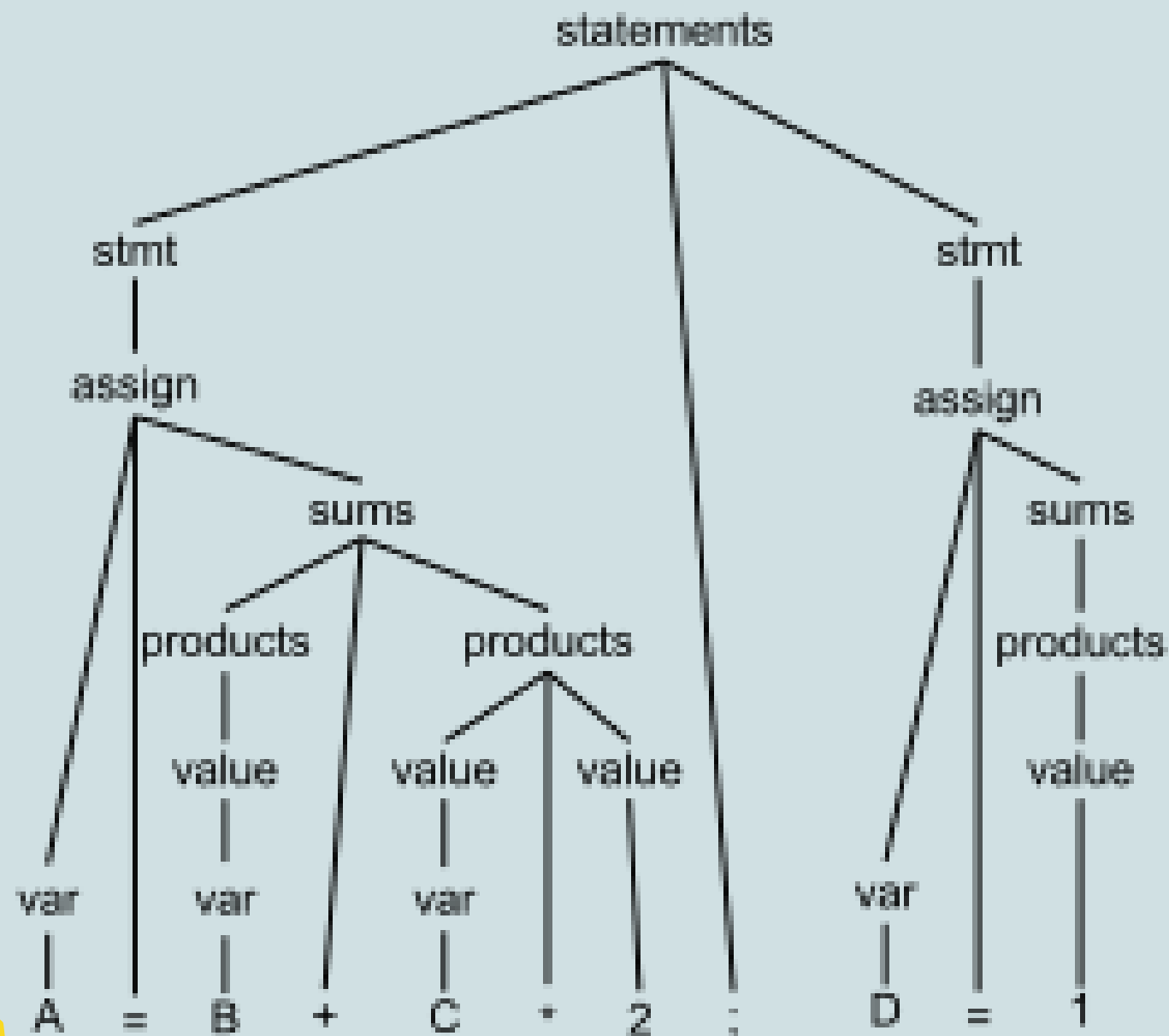
## Step-02:

$$A \rightarrow aA'$$

$$A' \rightarrow AD / Bc$$

$$D \rightarrow B / c$$

# BOTTOM UP PARSING



The parsing problem is finding the correct RHS in a right-sentential form to reduce to get the previous right-sentential form in the derivation.



# BOTTOM UP PARSING



**Right sentential form** a sentential form that occurs in the rightmost derivation of some sentence.

The process of deriving a string by expanding the rightmost non-terminal at each step is called as **rightmost derivation**.

# BOTTOM UP PARSING

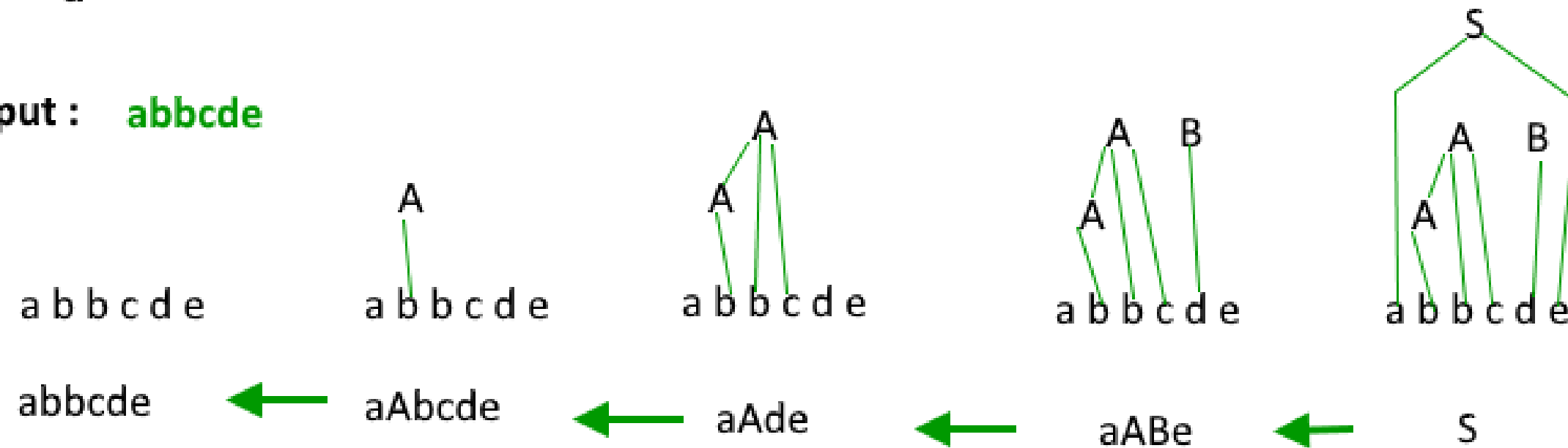
**Handle** - string of symbols to be replaced at each stage of parsing

$S \rightarrow aABe$

$A \rightarrow Abc/b$

$B \rightarrow d$

Input: **abbcde**





# **BOTTOM UP PARSING**

## **LR Parsing Algorithm**

L - left to right scanning of input string

R - start with rightmost derivation



# BOTTOM UP PARSING

- Advantages of LR parsers:
  - They will work for nearly all grammars that describe programming languages.
  - They work on a larger class of grammars than other bottom-up algorithms, but are as efficient as any other bottom-up parser.
  - They can detect syntax errors as soon as it is possible.
  - The LR class of grammars is a superset of the class parsable by LL parsers.

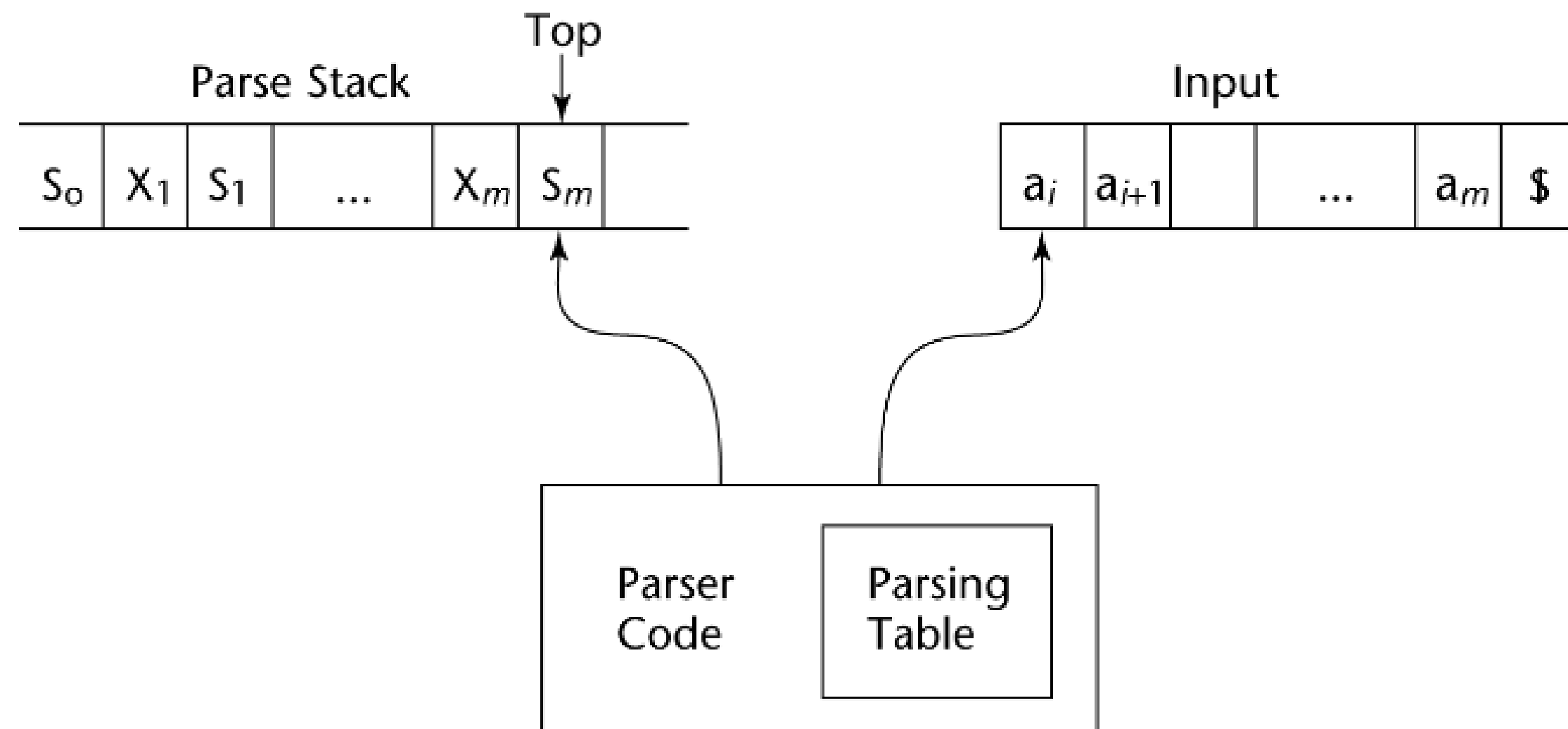




# BOTTOM UP PARSING

- LR parsers must be constructed with a tool
- Knuth's insight: A bottom-up parser could use the entire history of the parse, up to the current point, to make parsing decisions
  - There were only a finite and relatively small number of different parse situations that could have occurred, so the history could be stored in a parser state, on the parse stack

# BOTTOM UP PARSING





# BOTTOM UP PARSING

## Bottom up parsers make use of Shift-Reduce Algorithms

- Shift-Reduce Algorithms
  - Reduce is the action of replacing the handle on the top of the parse stack with its corresponding LHS
  - Shift is the action of moving the next token to the top of the parse stack



# BOTTOM UP PARSING

- LR parsers are table driven, where the table has two components, an ACTION table and a GOTO table
  - The ACTION table specifies the action of the parser, given the parser state and the next token
    - Rows are state names; columns are terminals
  - The GOTO table specifies which state to put on top of the parse stack after a reduction action is done
    - Rows are state names; columns are nonterminals

# BOTTOM UP PARSING

1.  $E \rightarrow E + T$
2.  $E \rightarrow T$
3.  $T \rightarrow T * F$
4.  $T \rightarrow F$
5.  $F \rightarrow (E)$
6.  $F \rightarrow id$

State	Action						Goto		
	id	+	*	(	)	\$	E	T	F
0	S5		S4				1	2	3
1		S6				accept			
2		R2	S7		R2	R2			
3		R4	R4		R4	R4			
4	S5			S4			8	2	3
5		R6	R6		R6	R6			
6	S5			S4				9	3
7	S5			S4					10
8		S6			S11				
9		R1	S7		R1	R1			
10		R3	R3		R3	R3			
11		R5	R5		R5	R5			

# BOTTOM UP PARSING

- Initial configuration:  $(S_0, a_1 \dots a_n \$)$
- Parser actions:
  - If  $\text{ACTION}[S_m, a_i] = \text{Shift } S$ , the next configuration is:  
 $(S_0 X_1 S_1 X_2 S_2 \dots X_m S_m a_i S, a_{i+1} \dots a_n \$)$
  - If  $\text{ACTION}[S_m, a_i] = \text{Reduce } A \rightarrow \beta$  and  $S = \text{GOTO}[S_{m-r}, A]$ , where  $r = \text{the length of } \beta$ , the next configuration is  
 $(S_0 X_1 S_1 X_2 S_2 \dots X_{m-r} S_{m-r} AS, a_i a_{i+1} \dots a_n \$)$
  - If  $\text{ACTION}[S_m, a_i] = \text{Accept}$ , the parse is complete and no errors were found.
  - If  $\text{ACTION}[S_m, a_i] = \text{Error}$ , the parser calls an error-handling routine.

# BOTTOM UP PARSING

- 1.  $E \rightarrow E + T$
- 2.  $E \rightarrow T$
- 3.  $T \rightarrow T * F$
- 4.  $T \rightarrow F$
- 5.  $F \rightarrow (E)$
- 6.  $F \rightarrow id$

State	Action						Goto		
	id	+	*	(	)	\$	E	T	F
0	S5		S4				1	2	3
1		S6				accept			
2		R0	S7		R2	R0			
3		R4	R4		R4	R4			
4	S5			S4			8	2	3
5		R6	R6		R6	R6			
6	S5			S4				9	3
7	S5			S4					10
8		S6			S11				
9		R1	S7		R1	R1			
10		R3	R3		R3	R3			
11		R5	R5		R5	R5			

id + id \* id \$

0						lexeme
						state

# BOTTOM UP PARSING

- 1.  $E \rightarrow E + T$
- 2.  $E \rightarrow T$
- 3.  $T \rightarrow T * F$
- 4.  $T \rightarrow F$
- 5.  $F \rightarrow (E)$
- 6.  $F \rightarrow id$

State	Action						Goto		
	id	+	*	(	)	\$	E	T	F
0	S5		S4				1	2	3
1		S6				accept			
2		R0	S7		R2	R0			
3		R4	R4		R4	R4			
4	S5			S4			8	2	3
5		R6	R6		R6	R6			
6	S5			S4				9	3
7	S5			S4					10
8		S6			S11				
9		R1	S7		R1	R1			
10		R3	R3		R3	R3			
11		R5	R5		R5	R5			

± id \* id \$

0	id					lexeme
	5					state



# BOTTOM UP PARSING

- 1.  $E \rightarrow E + T$
- 2.  $E \rightarrow T$
- 3.  $T \rightarrow T * F$
- 4.  $T \rightarrow F$
- 5.  $F \rightarrow (E)$
- 6.  $F \rightarrow id$

State	Action						Goto		
	id	+	*	(	)	\$	E	T	F
0	S5		S4				1	2	3
1		S6				accept			
2		R0	S7		R2	R0			
3		R4	R4		R4	R4			
4	S5			S4			8	2	3
5		R6	R6		R6	R6			
6	S5			S4				9	3
7	S5			S4					10
8		S6			S11				
9		R1	S7		R1	R1			
10		R3	R3		R3	R3			
11		R5	R5		R5	R5			

± id \* id \$

0	F					lexeme
	3					state

# BOTTOM UP PARSING

- 1.  $E \rightarrow E + T$
- 2.  $E \rightarrow T$
- 3.  $T \rightarrow T * F$
- 4.  $T \rightarrow F$
- 5.  $F \rightarrow (E)$
- 6.  $F \rightarrow id$

State	Action						Goto		
	id	+	*	(	)	\$	E	T	F
0	S5		S4				1	2	3
1		S6				accept			
2		R0	S7		R2	R0			
3		R4	R4		R4	R4			
4	S5			S4			8	2	3
5		R6	R6		R6	R6			
6	S5			S4				9	3
7	S5			S4					10
8		S6			S11				
9		R1	S7		R1	R1			
10		R3	R3		R3	R3			
11		R5	R5		R5	R5			

± id \* id \$

0	T					lexeme
	2					state

# BOTTOM UP PARSING

- 1.  $E \rightarrow E + T$
- 2.  $E \rightarrow T$
- 3.  $T \rightarrow T * F$
- 4.  $T \rightarrow F$
- 5.  $F \rightarrow (E)$
- 6.  $F \rightarrow id$

State	Action						Goto		
	id	+	*	(	)	\$	E	T	F
0	S5		S4				1	2	3
1		S6				accept			
2		R0	S7		R2	R0			
3		R4	R4		R4	R4			
4	S5			S4			8	2	3
5		R6	R6		R6	R6			
6	S5			S4				9	3
7	S5			S4					10
8		S6			S11				
9		R1	S7		R1	R1			
10		R3	R3		R3	R3			
11		R5	R5		R5	R5			

± id \* id \$

0	E					lexeme
	1					state

# BOTTOM UP PARSING

- 1.  $E \rightarrow E + T$
- 2.  $E \rightarrow T$
- 3.  $T \rightarrow T * F$
- 4.  $T \rightarrow F$
- 5.  $F \rightarrow (E)$
- 6.  $F \rightarrow id$

State	Action						Goto		
	id	+	*	(	)	\$	E	T	F
0	S5		S4				1	2	3
1		S6				accept			
2		R0	S7		R2	R0			
3		R4	R4		R4	R4			
4	S5			S4			8	2	3
5		R6	R6		R6	R6			
6	S5			S4				9	3
7	S5			S4					10
8		S6			S11				
9		R1	S7		R1	R1			
10		R3	R3		R3	R3			
11		R5	R5		R5	R5			

id \* id \$

0	E	+				lexeme
	1	6				state

# BOTTOM UP PARSING

- 1.  $E \rightarrow E + T$
- 2.  $E \rightarrow T$
- 3.  $T \rightarrow T * F$
- 4.  $T \rightarrow F$
- 5.  $F \rightarrow (E)$
- 6.  $F \rightarrow id$

State	Action						Goto		
	id	+	*	(	)	\$	E	T	F
0	S5		S4				1	2	3
1		S6				accept			
2		R0	S7		R2	R0			
3		R4	R4		R4	R4			
4	S5			S4			8	2	3
5		R6	R6		R6	R6			
6	S5			S4				9	3
7	S5			S4					10
8		S6			S11				
9		R1	S7		R1	R1			
10		R3	R3		R3	R3			
11		R5	R5		R5	R5			

\* id \$

0	E	+	id			lexeme
	1	6	5			state

# BOTTOM UP PARSING

- 1.  $E \rightarrow E + T$
- 2.  $E \rightarrow T$
- 3.  $T \rightarrow T * F$
- 4.  $T \rightarrow F$
- 5.  $F \rightarrow (E)$
- 6.  $F \rightarrow id$

State	Action						Goto		
	id	+	*	(	)	\$	E	T	F
0	S5		S4				1	2	3
1		S6				accept			
2		R0	S7		R2	R0			
3		R4	R4		R4	R4			
4	S5			S4			8	2	3
5		R6	R6		R6	R6			
6	S5			S4				9	3
7	S5			S4					10
8		S6			S11				
9		R1	S7		R1	R1			
10		R3	R3		R3	R3			
11		R5	R5		R5	R5			

\* id \$

0	E	+	F			lexeme
	1	6	3			state

# BOTTOM UP PARSING

- 1.  $E \rightarrow E + T$
- 2.  $E \rightarrow T$
- 3.  $T \rightarrow T * F$
- 4.  $T \rightarrow F$
- 5.  $F \rightarrow (E)$
- 6.  $F \rightarrow id$

State	Action						Goto		
	id	+	*	(	)	\$	E	T	F
0	S5		S4				1	2	3
1		S6				accept			
2		R0	S7		R2	R0			
3		R4	R4		R4	R4			
4	S5			S4			8	2	3
5		R6	R6		R6	R6			
6	S5			S4				9	3
7	S5			S4					10
8		S6			S11				
9		R1	S7		R1	R1			
10		R3	R3		R3	R3			
11		R5	R5		R5	R5			

\* id \$

0	E	+	T			lexeme
	1	6	2			state

# BOTTOM UP PARSING

- 1.  $E \rightarrow E + T$
- 2.  $E \rightarrow T$
- 3.  $T \rightarrow T * F$
- 4.  $T \rightarrow F$
- 5.  $F \rightarrow (E)$
- 6.  $F \rightarrow id$

State	Action						Goto		
	id	+	*	(	)	\$	E	T	F
0	S5		S4				1	2	3
1		S6				accept			
2		R0	S7		R2	R0			
3		R4	R4		R4	R4			
4	S5			S4			8	2	3
5		R6	R6		R6	R6			
6	S5			S4				9	3
7	S5			S4					10
8		S6			S11				
9		R1	S7		R1	R1			
10		R3	R3		R3	R3			
11		R5	R5		R5	R5			

id \$

0	E	+	T	*		lexeme
	1	6	2	7		state



# BOTTOM UP PARSING

1.  $E \rightarrow E + T$
2.  $E \rightarrow T$
3.  $T \rightarrow T * F$
4.  $T \rightarrow F$
5.  $F \rightarrow (E)$
6.  $F \rightarrow id$

State	Action						Goto		
	id	+	*	(	)	\$	E	T	F
0	S5		S4				1	2	3
1		S6				accept			
2		R0	S7		R2	R0			
3		R4	R4		R4	R4			
4	S5			S4			8	2	3
5		R6	R6		R6	R6			
6	S5			S4				9	3
7	S5			S4					10
8		S6			S11				
9		R1	S7		R1	R1			
10		R3	R3		R3	R3			
11		R5	R5		R5	R5			

\$

0	E	+	T	*	id	lexeme
	1	6	2	7	5	state

# BOTTOM UP PARSING

- 1.  $E \rightarrow E + T$
- 2.  $E \rightarrow T$
- 3.  $T \rightarrow T * F$
- 4.  $T \rightarrow F$
- 5.  $F \rightarrow (E)$
- 6.  $F \rightarrow id$

State	Action						Goto		
	id	+	*	(	)	\$	E	T	F
0	S5		S4				1	2	3
1		S6				accept			
2		R0	S7		R2	R0			
3		R4	R4		R4	R4			
4	S5			S4			8	2	3
5		R6	R6		R6	R6			
6	S5			S4				9	3
7	S5			S4					10
8		S6			S11				
9		R1	S7		R1	R1			
10		R3	R3		R3	R3			
11		R5	R5		R5	R5			

\$

0	E	+	T	*	F	lexeme
	1	6	2	7	3	state

# BOTTOM UP PARSING

- 1.  $E \rightarrow E + T$
- 2.  $E \rightarrow T$
- 3.  $T \rightarrow T * F$
- 4.  $T \rightarrow F$
- 5.  $F \rightarrow (E)$
- 6.  $F \rightarrow id$

State	Action						Goto		
	id	+	*	(	)	\$	E	T	F
0	S5		S4				1	2	3
1		S6				accept			
2		R0	S7		R2	R0			
3		R4	R4		R4	R4			
4	S5			S4			8	2	3
5		R6	R6		R6	R6			
6	S5			S4				9	3
7	S5			S4					10
8		S6			S11				
9		R1	S7		R1	R1			
10		R3	R3		R3	R3			
11		R5	R5		R5	R5			

\$

0	E	+	T			lexeme
	1	6	2			state

# BOTTOM UP PARSING

- 1.  $E \rightarrow E + T$
- 2.  $E \rightarrow T$
- 3.  $T \rightarrow T * F$
- 4.  $T \rightarrow F$
- 5.  $F \rightarrow (E)$
- 6.  $F \rightarrow id$

State	Action						Goto		
	id	+	*	(	)	\$	E	T	F
0	S5		S4				1	2	3
1		S6				accept			
2		R0	S7		R2	R0			
3		R4	R4		R4	R4			
4	S5			S4			8	2	3
5		R6	R6		R6	R6			
6	S5			S4				9	3
7	S5			S4					10
8		S6			S11				
9		R1	S7		R1	R1			
10		R3	R3		R3	R3			
11		R5	R5		R5	R5			

\$

0	E					lexeme
	1					state

# BOTTOM UP PARSING

- 1.  $E \rightarrow E + T$
- 2.  $E \rightarrow T$
- 3.  $T \rightarrow T * F$
- 4.  $T \rightarrow F$
- 5.  $F \rightarrow (E)$
- 6.  $F \rightarrow id$

State	Action						Goto		
	id	+	*	(	)	\$	E	T	F
0	S5		S4				1	2	3
1		S6				accept			
2		R0	S7		R2	R0			
3		R4	R4		R4	R4			
4	S5			S4			8	2	3
5		R6	R6		R6	R6			
6	S5			S4				9	3
7	S5			S4					10
8		S6			S11				
9		R1	S7		R1	R1			
10		R3	R3		R3	R3			
11		R5	R5		R5	R5			

\$

0	E					lexeme
	1					state

accept



# SUMMARY

**Syntax analysis** is normally based on a formal syntax description of the language being implemented, commonly using BNF.

## Parts of Syntax Analysis:

- Lexical Analysis
- Syntax Analysis

## Reasons for Separating Lexical and Syntax Analysis:

- Simplicity
- Efficiency
- Portability



## SUMMARY

- **Lexical Analyzer** is a pattern matcher that isolates **lexemes**, which is the basic lexical unit of a language.
- **Lexemes** are categorized by **tokens**.

### Goals of Syntax Analysis:

- detect syntax errors and provide diagnostic message if an error exists
- produce a parse tree which would be used for code generation

### Approaches to Syntax Analysis:

- Top-Down Approach
- Bottom Up Approach



## SUMMARY

- **Top Down Approach:** Given a sentential form,  $xA\alpha$ , the parser must choose the correct A-rule to get the next sentential form in the leftmost derivation, using only the first token produced by A. Commonly uses Recursive Descent parsing algorithm. Subprogram driven.
- **Bottom Up Approach:** The parsing problem is finding the correct RHS in a right-sentential form to reduce to get the previous right-sentential form in the derivation. Table driven.





**THANK YOU VERY  
MUCH FOR LISTENING**



Monzales, Samson, and Tejada

