

e. $\lim_{n \rightarrow \infty} 3^{2n-1} = \infty$

show that it is monotonic increasing since limit is positive infinity

Prove $a_n \leq a_{n+1}$, if $a_n = 3^{2n-1}$ since $a_1 \leq a_2 \leq a_3 \leq \dots \leq a_k$

$$a_n \leq a_{n+1}$$

$$3^{2n-1} \leq 3^{2(n+1)-1}$$

$$\frac{3^{2n-1}}{3^{2n+1}} \leq 1 \rightarrow 3^{2n-1-2n-1} \leq 1$$

$$3^{-2} \leq 1$$

$$\frac{1}{9} \leq 1$$

When listing the first 5 terms, we get $\{ 3, 27, 243, 2187, 19683 \}$ and it is bounded below at 3. Therefore, $\lim_{n \rightarrow \infty} 3^{2n-1} = \infty$ is monotonic increasing and bounded below at 3