

DISCRETE STRUCTURES (CS21001)

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QUESTION : 1

Show that there are at least six people in California (population: 36 million) with the same three initials who were born on the same day of the year (but not necessarily in the same year). Assume that everyone has three initials.

QUESTION : 2

In a room there are 11 people, none of whom are older than 60 (ages are given in whole numbers only) but each of whom is at least 1 year old. Prove that we can always find two groups of people (with no common person) the sum of whose ages is the same. Can 11 be replaced by a smaller number?

QUESTION : 3

- a) Prove that of any five points chosen within an equilateral side of length 1, there are two whose distance is at most $1/2$.
- b) Prove that of any ten points chosen within an equilateral side of length 1, there are two whose distance is at most $1/3$.
- c) Determine an integer m_n , such that if m_n points are chosen within an equilateral triangle of side 1, there are two whose distance is at most $1/n$.

QUESTION : 4

A 3×7 rectangle is divided into 21 squares each of which is coloured red or black. Prove that the board contains a non-trivial rectangle (not $1 \times k$ or $k \times 1$), whose 4 corner squares are all black or all red.

QUESTION : 5

$2k \times 2k$ grid is divided into $4k^2$ squares and 4 $k \times k$ sub grids. Show that it is impossible to mark k squares in the upper left $k \times k$ sub grids and k squares in lower right $k \times k$ sub grid such that no two marked squares are in the same row, column or diagonal of the $2k \times 2k$ grid.