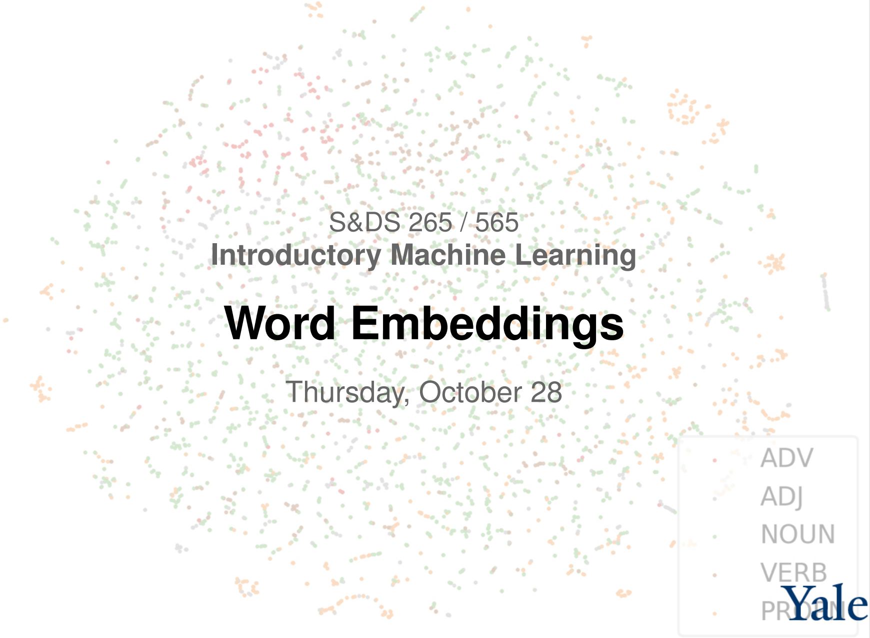
S&DS 265 / 565

Introductory Machine Learning

Word Embeddings

Thursday, October 28



Yale

Shortcomings of word clusters

- Can’t use vector space operations
- Doesn’t give “features” of words
- These are addressed with “distributed representations” (next)

Core idea of embeddings

- Form a language model but replace classes by vectors, one for each word
- Use PMI-like scores to fit the vectors
- Can be applied whenever have cooccurrence data.

Constructing embeddings

Language model is

$$p(w_2 \mid w_1) = \frac{\exp(\phi(w_2)^T \phi(w_1))}{\sum_w \exp(\phi(w)^T \phi(w_1))}.$$

Carry out stochastic gradient descent over the embedding vectors $\phi \in \mathbb{R}^d$ (where $d \approx$ 50–500 is chosen by trial and error)

This is what Mikolov et al. (2014, 2015) did at Google. With a couple of heuristics:

"Distributed representations of words," (2014) "Efficient representations of words in vector space" (2015)

Constructing embeddings

Heuristics used:

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- Second is computational. The bottleneck is computing the denominator in the logistic (softmax) probability.
- Use “negative sampling”: Approximation

$$\sum_w \exp(\phi(w)^T \phi(w_1))$$

$$\approx \exp(\phi(w_2)^T \phi(w_1)) + \sum_{\text{random } w} \exp(\phi(w)^T \phi(w_1))$$

Analogies

These heuristics enable training on very large text collections. Leads to vector representations of words with interesting properties.

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`king` is to `man` as ? is to `woman`

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`Paris` is to `France` as ? is to `Germany`

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For example, analogies:

$\texttt{king}$ is to $\texttt{man}$ as ? is to $\texttt{woman}$

$\texttt{Paris}$ is to $\texttt{France}$ as ? is to $\texttt{Germany}$

$$\phi(\texttt{king}) - \phi(\texttt{man}) \overset{?}{\approx} \phi(\texttt{queen}) - \phi(\texttt{woman})$$

$$\widehat{w} = \arg\min_{w} \|\phi(\texttt{king}) - \phi(\texttt{man}) + \phi(\texttt{woman}) - \phi(w)\|^2$$

Does $\widehat{w} = \texttt{queen}$?

Learned Analogies

Table 8: *Examples of the word pair relationships, using the best word vectors from Table 4 (Skip-gram model trained on 783M words with 300 dimensionality).*

Relationship	Example 1	Example 2	Example 3
France - Paris	Italy: Rome	Japan: Tokyo	Florida: Tallahassee
big - bigger	small: larger	cold: colder	quick: quicker
Miami - Florida	Baltimore: Maryland	Dallas: Texas	Kona: Hawaii
Einstein - scientist	Messi: midfielder	Mozart: violinist	Picasso: painter
Sarkozy - France	Berlusconi: Italy	Merkel: Germany	Koizumi: Japan
copper - Cu	zinc: Zn	gold: Au	uranium: plutonium
Berlusconi - Silvio	Sarkozy: Nicolas	Putin: Medvedev	Obama: Barack
Microsoft - Windows	Google: Android	IBM: Linux	Apple: iPhone
Microsoft - Ballmer	Google: Yahoo	IBM: McNealy	Apple: Jobs
Japan - sushi	Germany: bratwurst	France: tapas	USA: pizza

Mikolov et al., "Distributed representations of words," (2014); "Efficient representations of words in vector space" (2015)

Evaluation Analogies

Type of relationship	Word Pair 1		Word Pair 2	
Common capital city	Athens	Greece	Oslo	Norway
All capital cities	Astana	Kazakhstan	Harare	Zimbabwe
Currency	Angola	kwanza	Iran	rial
City-in-state	Chicago	Illinois	Stockton	California
Man-Woman	brother	sister	grandson	granddaughter
Adjective to adverb	apparent	apparently	rapid	rapidly
Opposite	possibly	impossibly	ethical	unethical
Comparative	great	greater	tough	tougher
Superlative	easy	easiest	lucky	luckiest
Present Participle	think	thinking	read	reading
Nationality adjective	Switzerland	Swiss	Cambodia	Cambodian
Past tense	walking	walked	swimming	swam
Plural nouns	mouse	mice	dollar	dollars
Plural verbs	work	works	speak	speaks

Mikolov et al., “Distributed representations of words,” (2014); “Efficient representations of words in vector space” (2015)

GloVe

Shortly after: Stanford group introduced a computational expedient (with attempt to give a "principled" motivation)

$$\mathcal{O}(\phi) = \sum_{w_1, w_2} f(c_{w_1, w_2}) \left(\phi(w_1)^T \phi(w_2) - \log c_{w_1, w_2} \right)^2$$

where $c_{w,w'}$ are cooccurrence counts.

- A type of regression estimator. Can interpret/relate this to other objectives.
- Main advantage is that SGD can be carried out much more efficiently

Pennington et al., "GloVe: Global vectors for word representation," (2015)

GloVe

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where $c_{w,w'}$ are cooccurrence counts.

- Heuristic weighting function

  $$f(x) = \left(\frac{x}{x_{\text{max}}}\right)^\alpha$$

  where $\alpha = 3/4$ set empirically.
- So $10^{-4} \mapsto 10^{-3}$. Each order of magnitude down gets "boosted" by 1/4-magnitude.

Pennington et al., "GloVe: Global vectors for word representation," (2015)

GloVe site and code

GloVe: Global Vectors for Word Representation

Jeffrey Pennington, Richard Socher, Christopher D. Manning

Introduction

GloVe is an unsupervised learning algorithm for obtaining vector representations for words. Training is performed on aggregated global word-word co-occurrence statistics from a corpus, and the resulting representations showcase interesting linear substructures of the word vector space.

Getting started (Code download)

- Download the code (licensed under the Apache License, Version 2.0)
- Unpack the files: unzip GloVe-1.2.zip
- Compile the source: cd GloVe-1.2 && make
- Run the demo script: ./demo.sh
- Consult the included README for further usage details, or ask a question
- The code is also available on GitHub

Download pre-trained word vectors

- Pre-trained word vectors. This data is made available under the Public Domain Dedication and License v1.0 whose full text can be found at: http://www.opendatacommons.org/licenses/pddl/1.0/.
  - Wikipedia 2014 + Gigaword 5 (6B tokens, 400K vocab, uncased, 50d, 100d, 200d, & 300d vectors, 822 MB download): glove.6B.zip
  - Common Crawl (42B tokens, 1.9M vocab, uncased, 300d vectors, 1.75 GB download): glove.42B.300d.zip
  - Common Crawl (840B tokens, 2.2M vocab, cased, 300d vectors, 2.03 GB download): glove.840B.300d.zip
  - Twitter (2B tweets, 27B tokens, 1.2M vocab, uncased, 25d, 50d, 100d, & 200d vectors, 1.42 GB download): glove.twitter.27B.zip
- Ruby script for preprocessing Twitter data

Citing GloVe

Jeffrey Pennington, Richard Socher, and Christopher D. Manning. 2014. GloVe: Global Vectors for Word Representation. [pdf] [bib]

Highlights

1. **Nearest neighbors**

   The Euclidean distance (or cosine similarity) between two word vectors provides an effective method for measuring the linguistic or semantic similarity of the corresponding words. Sometimes, the nearest neighbors according to this metric reveal rare but relevant words that lie outside an average human's vocabulary. For example, here are the closest words to the target word *frog*:

   0. *frog*
   1. frogs
   2. toad
   3. litoria
   4. leptodactylidae
   5. rana
   6. lizard
   7. eleutherodactylus

3. litoria

4. leptodactylidae

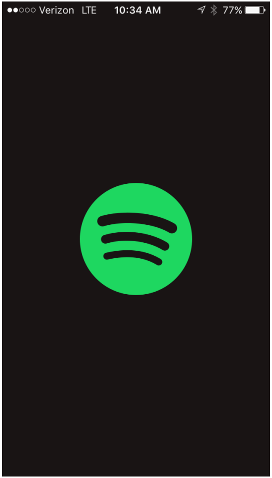
5. rana

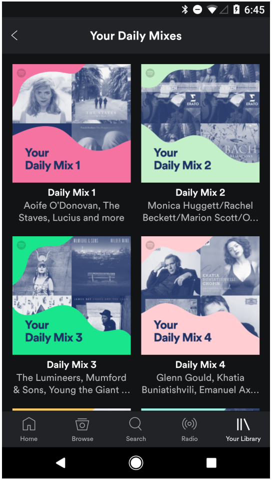
7. eleutherodactylus

2. **Linear substructures**

   The similarity metrics used for nearest neighbor evaluations produce a single scalar that quantifies the relatedness of two words. This simplicity can be problematic since two given words almost always exhibit more intricate relationships than can be captured by a single number. For example, *man* may be regarded as similar to *woman* in that both words describe human beings; on the other hand, the two words are often considered opposites since they highlight a primary axis along which humans differ from one another.

Recommendation via Embedding





species2vec: A novel method for species representation

Boyan Angelov

doi: https://doi.org/10.1101/461996

This article is a preprint and has not been certified by peer review [what does this mean?].

Abstract Full Text Info/History Metrics Preview PDF

Abstract

Word embeddings are omnipresent in Natural Language Processing (NLP) tasks. The same technology which defines words by their context can also define biological species. This study showcases this new method - species embedding (species2vec). By proximity sorting of 6761594 mammal observations from the whole world (2862 different species), we are able to create a training corpus for the skip-gram model. The resulting species embeddings are tested in an environmental classification task. The classifier performance confirms the utility of those embeddings in preserving the relationships between species, and also being representative of species consortia in an environment.

Visualisation

In [10]:
```
m = gensim.models.KeyedVectors.load_word2vec_format('reptilia.vec')
```

In [11]:
```
len(m.vocab)
```

Out[11]:
```
7397
```

In [15]:
```
m.most_similar(u'Alligator_mississippiensis')
```

Out[15]:
```
[(u'Sternotherus_bonevalleyensis', 0.8425856828689575),
 (u'Apalone_ferox', 0.8147842884063721),
 (u'Macrochelys_suwanniensis', 0.8063992261886597),
 (u'Deirochelys_reticularia', 0.7871163487434387),
 (u'Terrapene_putnami', 0.7841686010360718),
 (u'Chelydra_floridana', 0.7829421758651733),
 (u'Alligator_mefferdi', 0.7742743492126465),
 (u'Macrochelys_temminckii', 0.7682404518127441),
 (u'Trachemys_inflata', 0.7563525438308716),
 (u'Deirochelys_carri', 0.755811333656311)]
```

In [16]:
```
%matplotlib inline

def tsne_plot(model):
    "Creates and TSNE model and plots it"
    labels = []
```

Notebook

Let's go to the Python notebook!

Embedding embeddings: t-SNE

- How can we visualize the embeddings?

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Embedding embeddings: t-SNE

- How can we visualize the embeddings?
- We're in a very high dimensional space
- Could use PCA—this will tend to distort more
- Many visualization techniques exist. A currently popular one is t-SNE: "Student-t Stochastic Neighborhood Embedding"

t-SNE

Here's the idea behind t-SNE:

- Form a language model using the embeddings

Pronounced: **tee**-snee

t-SNE

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- Form a language model using the embeddings
- Scale and symmetrize, giving a matrix $P = [P_{ij}]$

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- Represent word i by $y_i \in \mathbb{R}^2$. Use a heavy-tailed distribution (Student-t)

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t-SNE

Here's the idea behind t-SNE:

- Form a language model using the embeddings
- Scale and symmetrize, giving a matrix $P = [P_{ij}]$
- Represent word i by $y_i \in \mathbb{R}^2$. Use a heavy-tailed distribution (Student-t)
- Select y_i using stochastic gradient descent

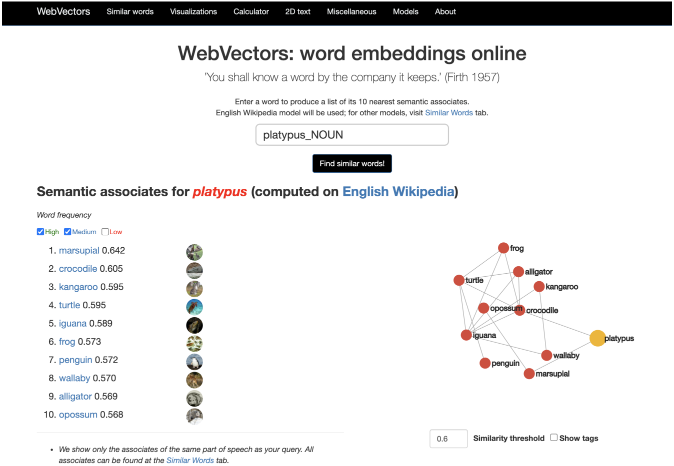
Pronounced: **tee**-snee

t-SNE: More info and examples

`https://lvdmaaten.github.io/tsne/`
`http://cs.stanford.edu/people/karpathy/tsnejs/`

Note: This is just a visualization technique, to give intuition for the high dimensional embedding

Embedding / Visualization Examples



http://vectors.nlpl.eu/explore/embeddings/en/

Summary: Word embeddings

- Word embeddings are vector representations of words, learned from cooccurrence statistics
- The models can be viewed in terms of logistic regression and class-based bigram models
- Surprising semantic relations are encoded in linear relations
- Various heuristics have been introduced to get scalability
- Embeddings improve with more data
- t-SNE is an algorithm for visualizing embeddings

extra slides (optional)

t-SNE: Detailed algorithm

For each word w_i compute a language model

$$P_{j\,|\,i} \propto \exp\left(-\frac{\|\phi(w_i)-\phi(w_j)\|^2}{2h_i^2}\right)$$

That is:

$$P_{j\,|\,i} = \frac{\exp\left(-\frac{\|\phi(w_i)-\phi(w_j)\|^2}{2h_i^2}\right)}{\sum_k \exp\left(-\frac{\|\phi(w_i)-\phi(w_k)\|^2}{2h_i^2}\right)}$$

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Choose the bandwith h_i so that the perplexity is, say, 10. This puts the probabilities all on the same scale.

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t-SNE: Detailed algorithm

For each word w_i compute a language model

$$P_{j\,|\,i} \propto \exp\left(-\frac{\|\phi(w_i) - \phi(w_j)\|^2}{2h_i^2}\right)$$

Now form

$$P_{ij} = \frac{1}{2}\left(P_{j\,|\,i} + P_{i\,|\,j}\right)$$

as a simple way of symmetrizing.

t-SNE: Detailed algorithm

Now form Student-t distribution depending on the visualization vectors $y_i \in \mathbb{R}^2$:

$$Q_{ij} \propto \left(1 + \|y_i - y_j\|^2\right)^{-1}$$

t-SNE: Detailed algorithm

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That is:

$$Q_{ij} = \frac{\left(1 + \|y_i - y_j\|^2\right)^{-1}}{\sum_{k \neq \ell} \left(1 + \|y_k - y_\ell\|^2\right)^{-1}}$$

This has fatter tails than a Gaussian

t-SNE: Detailed algorithm

Finally, run stochastic gradient descent (SGD) over the vectors y_i to optimize:

$$
\begin{aligned}
\widehat{y} &= \arg\min \sum_{ij} P_{ij} \log P_{ij} / Q_{ij} \\
&= \arg\max \sum_{ij} P_{ij} \log Q_{ij}
\end{aligned}
$$

Interpretation: if $\phi(w_i)$ is very close to $\phi(w_j)$ then y_i will be close to y_j.
(long distances may be stretched further...)