



Assignment of Automata  
By,

M. Ammar

BSCS-F19-M63  
Section - B (Morning)

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University of Punjab • Jhelum Campus • September 30<sup>th</sup>, 2020

The background is a dark navy blue. In the top-left corner, there are two overlapping triangles: a blue one and a light green one. In the bottom-left corner, there is a circular inset showing a close-up of a circuit board with various electronic components. In the top-right corner, there is a faint, grey, 3D-rendered pattern of interlocking cubes or a circuit layout.

# Polynomial Solutions

Submitted to: Ma'am Amina

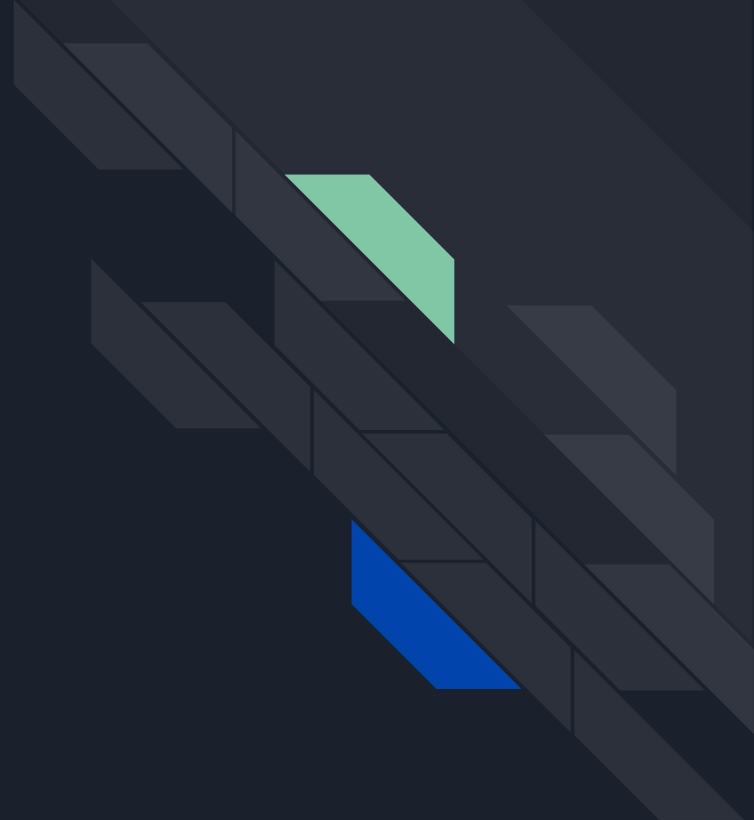


## Polynomial #1

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$$9x^2 + 3y^2 + 7xy - 9$$

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# For $9x^2$

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By Rule #1

- 9 is in POLYNOMIAL

By Rule #2

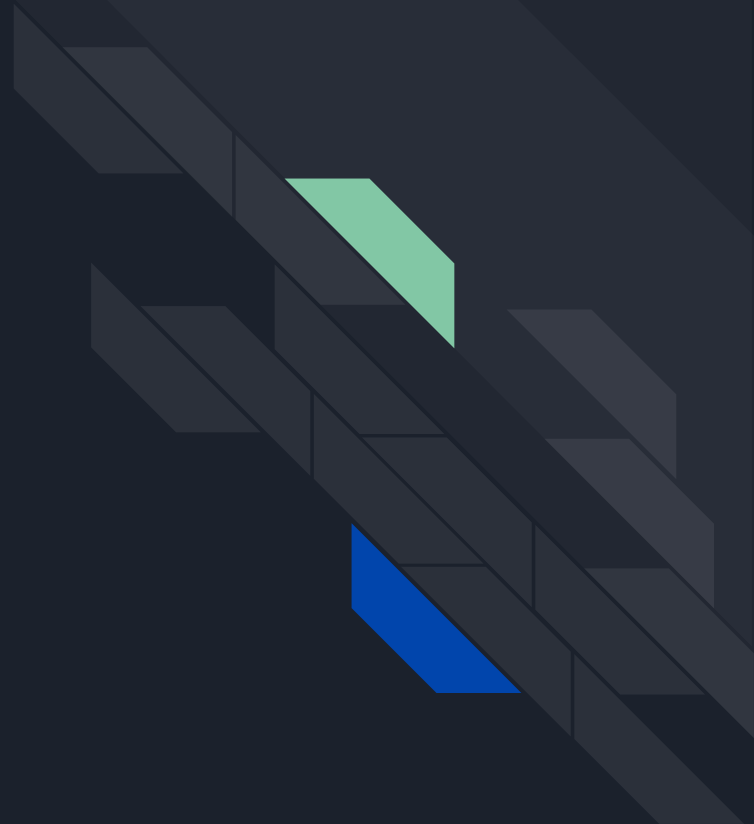
- $x$  is in POLYNOMIAL

By Rule #2

- $x^2$  is in POLYNOMIAL

By Rule #3

- $9x^2$  is in POLYNOMIAL



# For $3y^2$

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By Rule #1

- 3 is in POLYNOMIAL

By Rule #2

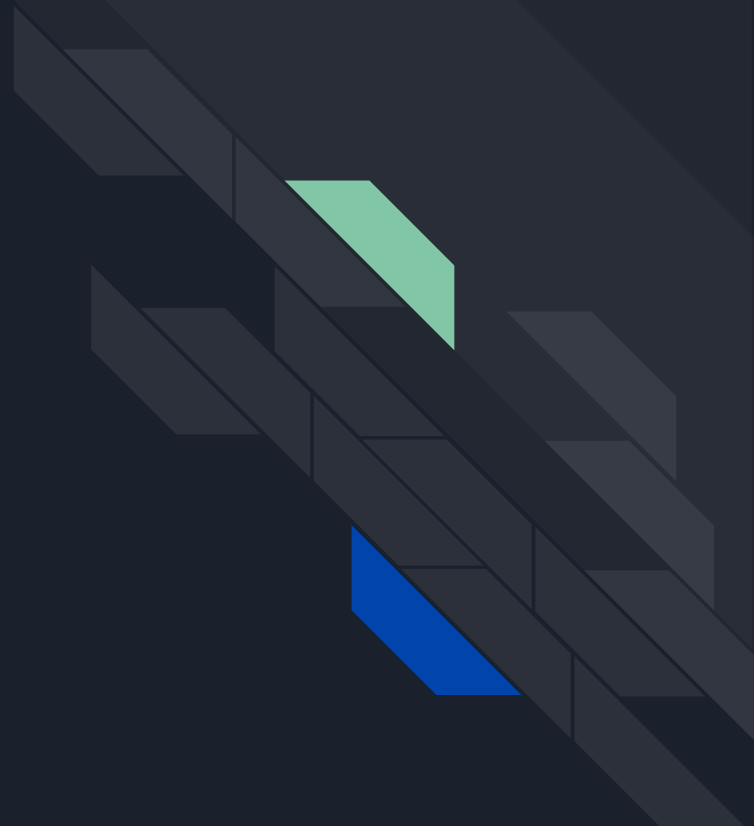
- $y$  is in POLYNOMIAL

By Rule #2

- $y^2$  is in POLYNOMIAL

By Rule #3

- $3y^2$  is in POLYNOMIAL



# For $7xy$

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By Rule #1

- 7 is in POLYNOMIAL

By Rule #2

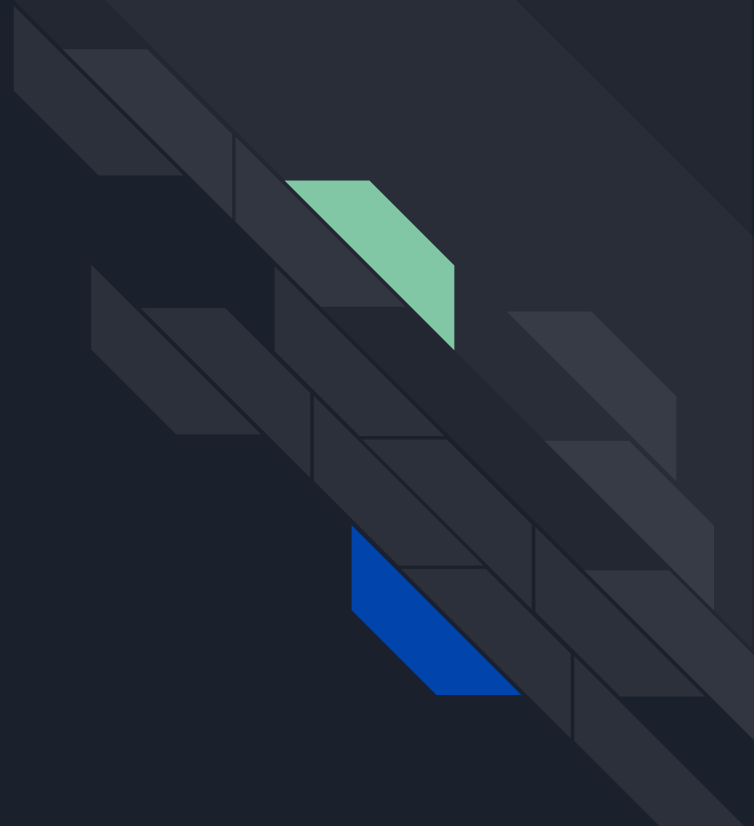
- x is in POLYNOMIAL

By Rule #2

- y is in POLYNOMIAL

By Rule #3

- $7xy$  is in POLYNOMIAL



For:  $9x^2 + 3y^2 + 7xy - 9$

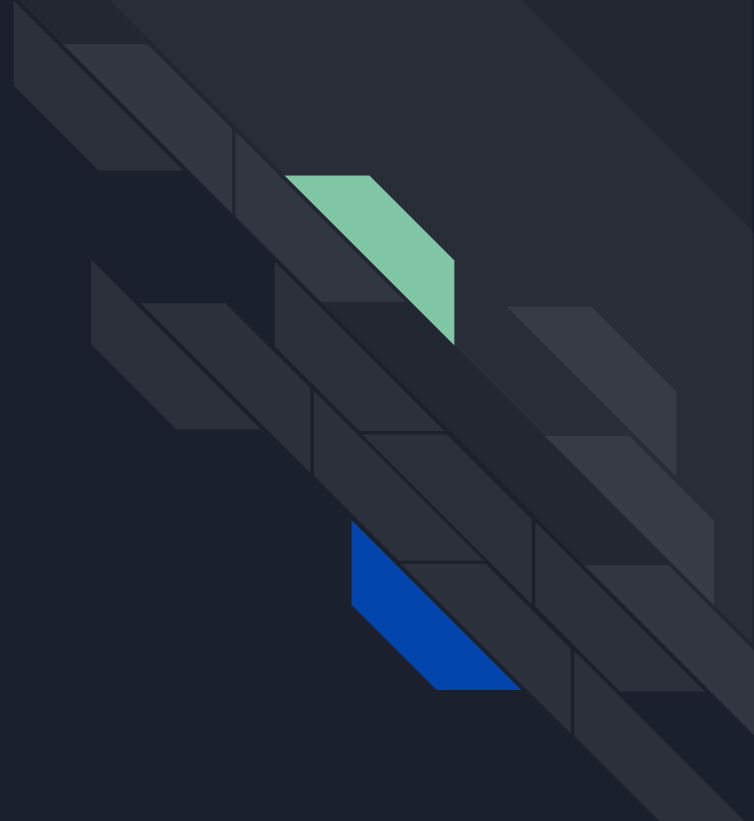
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By Rule #1

- 9 is in POLYNOMIAL

By Rule #3

- $9x^2 + 3y^2 + 7xy - 9$  is in POLYNOMIAL



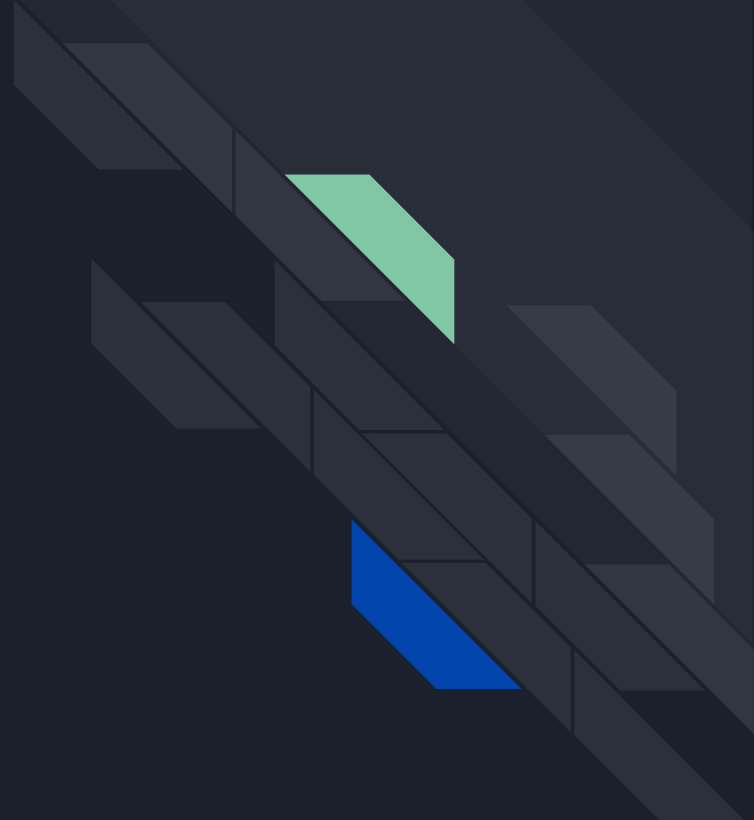


## Polynomial #2

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$$- 3xy^2 + 12x^2 - 7$$

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# For $-3xy^2$

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By Rule #1

- $(-1)3$  is in POLYNOMIAL

By Rule #2

- $x$  is in POLYNOMIAL

By Rule #2

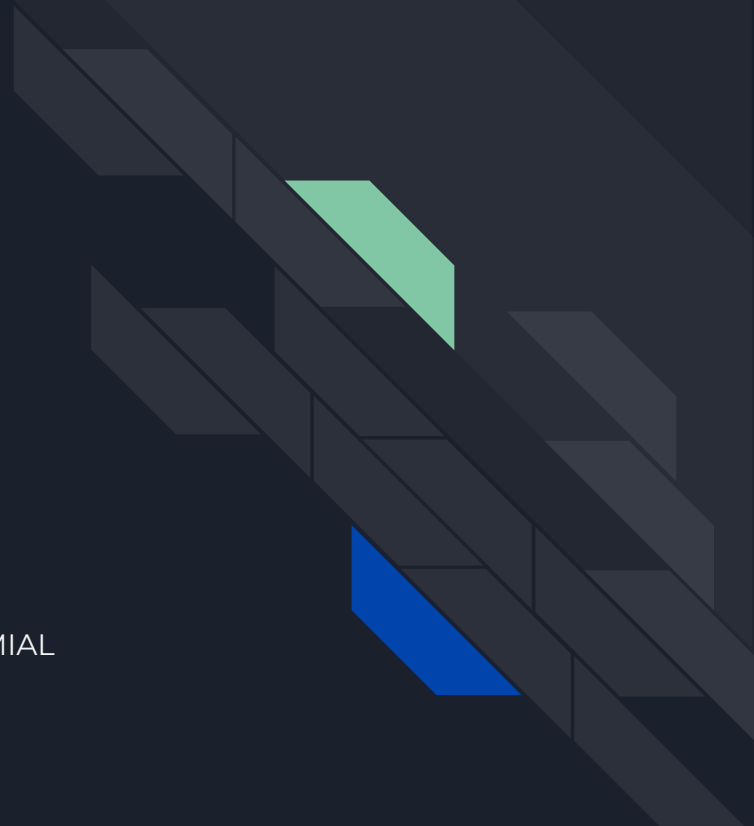
- $y$  is in POLYNOMIAL

By Rule #2

- $y^2$  is in POLYNOMIAL

By Rule #3

- $-3xy^2$  is in POLYNOMIAL



# For $12x^2$

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By Rule #1

- 12 is in POLYNOMIAL

By Rule #2

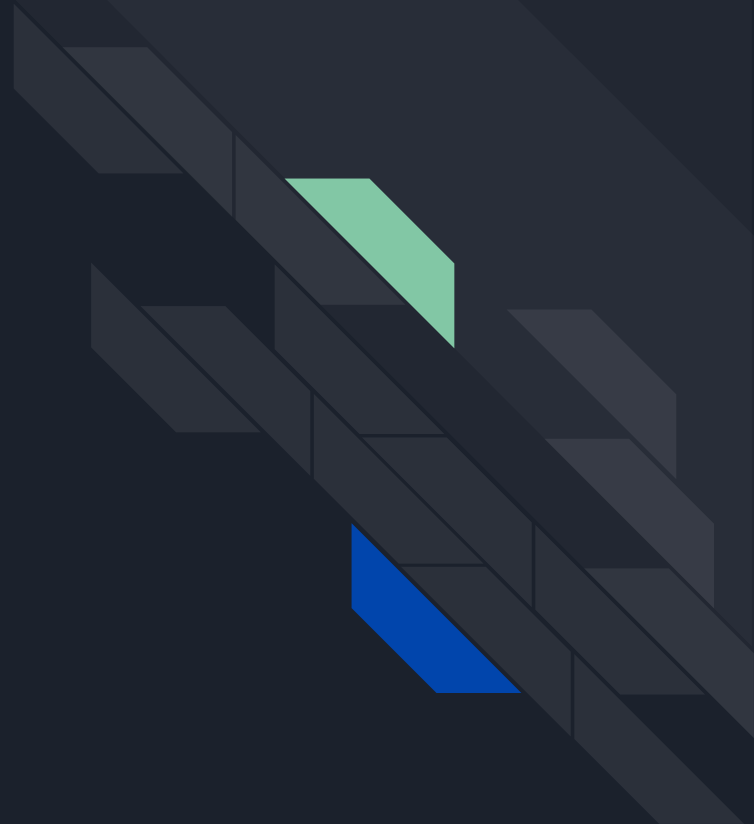
- $x$  is in POLYNOMIAL

By Rule #2

- $x^2$  is in POLYNOMIAL

By Rule #3

- $12x^2$  is in POLYNOMIAL



For:  $-3xy^2 + 12x^2 - 7$

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By Rule #1

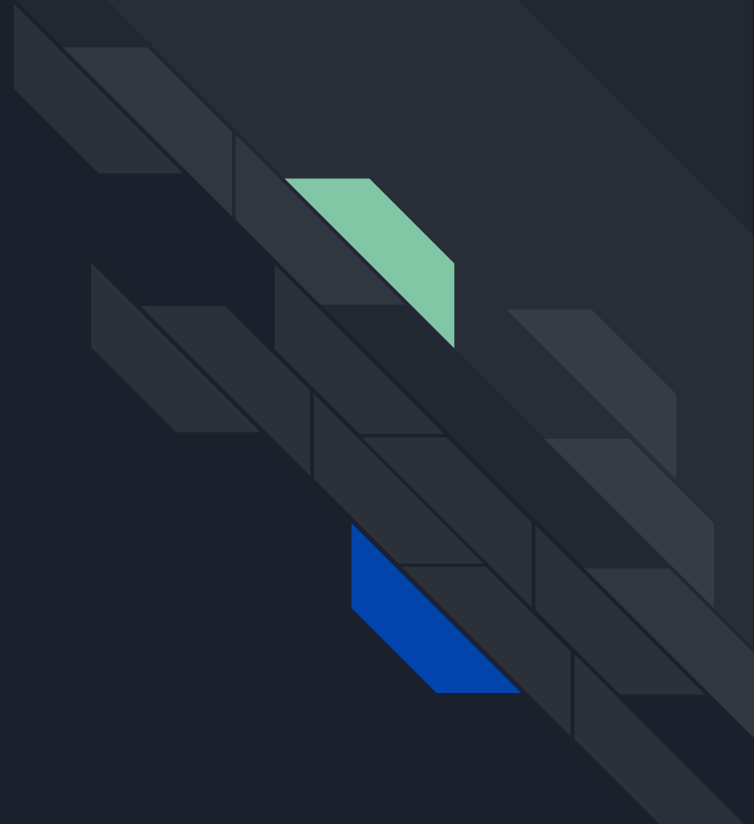
- 7 is in POLYNOMIAL

By Rule #3

- $(-1)7$  is in POLYNOMIAL

By Rule #3

- $-3xy^2 + 12x^2 - 7$  is in POLYNOMIAL





# Arithmetic Expression Solution

Our Expression:

$$(2 + 4) * (7 * (9 - 3) / 4) / 4 * (2 + 8) - 1$$



For:  $(2 + 4) * (7 * (9 - 3) / 4) / 4 * (2 + 8) - 1$


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By Rule #1

- 2, 4, 7, 9, 3, 8, 1 are in AE

By Rule #2

- -3, -1 are in AE
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For:  $(2 + 4)$  ,  $(2 + 8)$

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Taking  $(2+4)$

By Rule #3

- $+$  is a valid Arithmetic Operation
  - So,  $(2+3)$  is in AE
- 

Taking  $(2+8)$

By Rule #3

- $+$  is a valid Arithmetic Operation
- So,  $(2+8)$  is in AE

For:  $(9 - 3)$

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Taking  $(9 - 3)$

By Rule #2

- $(-1)3$  is in AE

By Rule #3

- $9 + (-1)3$  is in AE
- So,  $(9 - 3)$  is in AE



For:  $(2 + 4) * (7 * (9 - 3) / 4) / 4 * (2 + 8) - 1$

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By Rule #3

- $(7 * (9 - 3))$  is in AE
- $(7 * (9 - 3) / 4)$  is in AE
- $((7 * (9 - 3) / 4) / 4)$  is in AE

By Rule #3

- $(2 + 4) * ((7 * (9 - 3) / 4) / 4)$  is in AE
  - $((7 * (9 - 3) / 4) / 4) * (2 + 8)$  is in AE
  - $(2 + 4) * ((7 * (9 - 3) / 4) / 4) * (2 + 8)$  is in AE
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By Rule #3


- $(2 + 4) * ((7 * (9 - 3) / 4) / 4) * (2 + 8) - 1$   
is in AE



# Recursive Language

Problems






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Consider the language  $S^* = \{a, b\}$ .  
How many words this language have of length 2, 3, and  $n$ ?

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- Language will have  $2^2 = 4$  words of  $S^*$ , of Length 2
- Language will have  $2^3 = 8$  words of  $S^*$ , of Length 3
- Language will have  $2^n$  words of  $S^*$ , of Length  $n$



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Consider the language  $S^* = \{aa, b\}$ .  
How many words this language have of length 4 & 5?


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#### Length 4

- $L_1 = \{aaaa, aabb, baab, bbaa, bbbb\}$
- Words = 5

#### Length 5

- $L_2 = \{aaaab, aabaa, baaaa, bbbbb, aabbb, bbbba, bbaab, baabb\}$
- Words = 8



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Consider the language  $S^* = \{ab, ba\}$ .  
Write all the words that have 7 or fewer letters.


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#### Length 4

- $L_1 = \{aaaa, aabb, baab, bbaa, bbbb\}$
- Words = 5

#### Length 5

- $L_2 = \{aaaab, aabaa, baaaa, bbbbb, aabbb, bbbba, bbaab, baabb\}$
- Words = 8



Consider the language  $S^* = \{ab, ba\}$ .  
Write all the words that have 7 or fewer letters.

---

$$L_1 = \{ab, ba\}$$

$$L_2 = \{abab, abba, baab, baba\}$$


$$L_3 = \{ababab, ababba, abbaab, abbaba, baabab, baabba, babaab, bababa\}$$

So, our required Language is  $L$ , which is

$$L = L_1 L_2 L_3$$

Can any word in this Language contain the substrings: aaa, or bbb?

No, Because none of the given substrings are valid strings, if they are from ALPHABET  $S^*$



Consider the language  $S^* = \{a, ab, ba\}$ .  
Write all the words that have 7 or fewer letters.

---

Our required Language is L, which is

$L = \{ \Lambda, a, ab, ba, aa, aab, aba, ab, abab, abba, baba, baa, baab, aaa, aaab, aaba, ababab, ababa, abaabba, abaab, baaba, baaba, ababa, baaab, ababab, ababba, abbaab, abbaba, baabab, baabba, babaab, bababa, \dots, bababaa \}$

Is the String: ( abbbba ) a word in this language?

No, Because substring is valid strings, if they are not from ALPHABET  $S^*$



$S^* = \{ aa, aba, baa \}$

Show the words aabaa, baaabaaa, baaaaababaaaa are all in this language

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For aabaa

- (aa)(baa)

For baaabaaa

- (baa)(aba)(aa)

For baaaaababaaaa

- (baa)(aa)(aba)(baa)(aa)

Can any word in this Language be interpreted as a string of elements from S in two different ways?

Can any word in this Language have an odd total number of “a”s?

No, because all the given words can only be interpreted as only one way

No, because language has always even number of “a”s, so the a word will also has even number of a’s

# The End