

### 3. WRITTEN PROBLEMS.

(a) `def foo1(lst):`  
 $i = \text{len}(\text{lst}) // 2 \rightarrow \theta[1]$   
`for j in range(len(lst) - 1):`  
 $0[1][\text{lst}[j], \text{lst}[j+1] = \text{lst}[j+1], \text{lst}[j]$   
`if i + j <= j:`  
`break`  
 $i // 2$

$\text{len}(\text{lst})$  is always +ve.  $\therefore i$  is always +ve.  
 But, it eventually  $i // 2$  will reach 0.  
 In that case  $i + j = j$  and we will break  
 out of the for loop. So, we have to find  
 out how much time it takes for  $i$  to become 0?  
 $\theta(\log n)$

(b) `def foo2(lst):`  
 $n = \text{len}(\text{lst})$   
`for i in range(n - 1):`  
 $j = i + 1$   
`while j > 1:`  
 $\text{lst}[j] = 3 * j - 1$   
`if  $\text{lst}[j] > \text{lst}[j-1] / 2$ :`  
 $j = 1$   
`else:`  
 $j = j - 3$  ]  $\rightarrow$  if only this  
 part happens,  
 then too  
 it runs  
 roughly  $O(n^2)$  times.

if only this part happens, it happens only in  $O(n^2)$

Ans case =  $O(n^2)$

def sum-list (lst, low, high):  
 print ("sum-list, low=", low, "high=", high)  
 if low == high:  
 return lst[low]

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else:

sum-of-rest = sum-list (lst, low+1, high)

total-sum = lst[low] + sum-of-rest

return total sum

I = [1, 2, 3, 4, 5, 6, 7, 8] low = 0, high = 7

### REQUIRED OUTPUT

sum-list, low = 0, high = 7

sum-list, low = 1, high = 7

" " " 2, high = 7

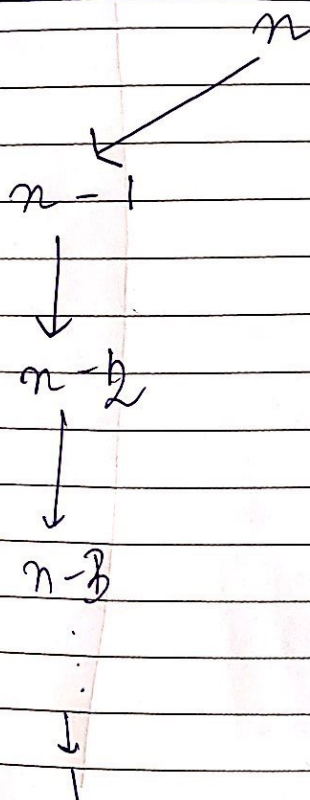
" " " 3 " "

" " " 4 "

" " " 5 "

" " " 6 "

" " " 7 "



in each node, apart from the recursive step, only  $O(1)$  is done and number of nodes will be  $\text{len}(\text{list})$ .  
 $\therefore O(n)$  is the running time.



def sum\_list2 (lst, low, high):

point ("sum-list2, low=", low, "high=", high, "sep=")

if low == high:

return lst [low]

else:

mid = (low + high) // 2

leftsum = sum\_list2 (lst, low, mid)

rightsum = sum\_list2 (lst, mid + 1, high)

totalsum = leftsum + rightsum

return totalsum

Input = [1, 2, 3, 4, 5, 6, 7, 8]

low = 0 | high = 7

REQUIRED OUTPUT

sum-list2, low = 0, high = 7

sum-list2, low = 0, high = 3

sum-list2, low = 0, high = 1

sum-list2, low = 0, high = 0

sum-list2, low = 2, high = 3

sum-list2, low = 4, high = 7

sum-list2, low = 0, high = 7

sum-list2, low = 0, high = 3

" " 0 " 1

" " 0 " 0

" " 1 " 1

" " 2 " 3

" " 2 " 2

" " 3 " 3

" " 4 " 7

" " 4 " 5

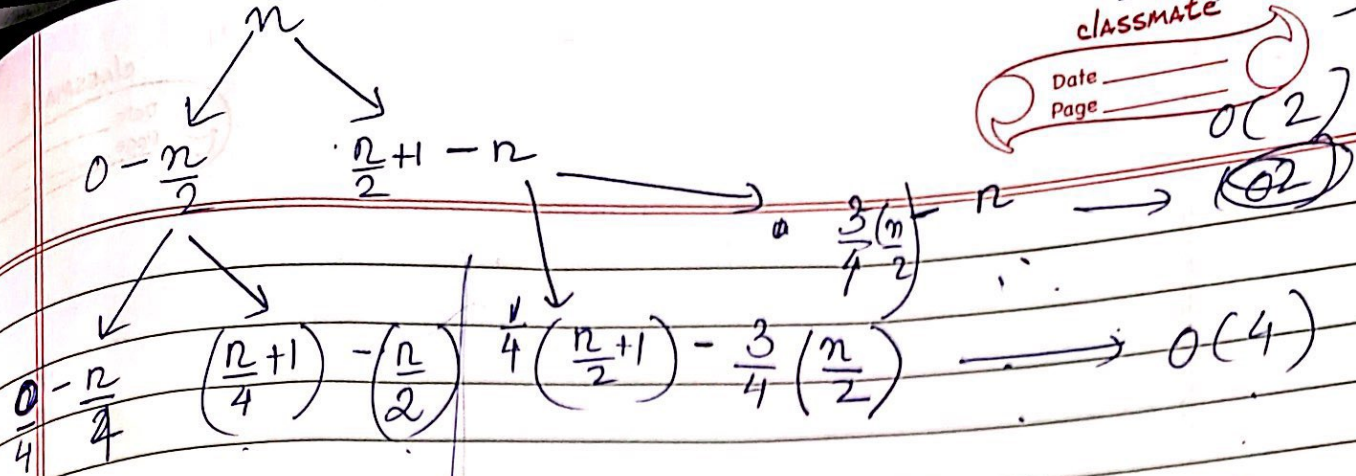
" " 4 " 4

" " 5 " 5

" " 6 " 7

" " 6 " 6

" " 7 " 7



$\therefore$  Here instead of counting the nodes, we count how much work is done at each level.

$\therefore$  Total work:

$$1 + 2 + 4 + 8 \dots$$

$$S = a(1 - r^n)$$

$$= \frac{1 - r}{1 - r} (1 - 2^{\log_2 n}) = \frac{(1 - 2^{\log_2 n})}{(1 - 2)} \approx O(n)$$

low-high  
therefore  
depth of the  
tree is  $\log n$