## Homework #5 due April 28 Friday 18.30

(1) Let M be the PDA defined by  $Q = \{q, q_0, q_1, q_2\}$ ,  $\Sigma = \{a,b\}$ ,  $\Gamma = \{a\}$ ,  $F := \{q, q_1\}$ .

$$\delta(q_0, a, Z_0) = \{(q, Z_0)\}$$

$$\delta(q, a, Z_0) = \{(q, aZ_0)\}$$

$$\delta(q, a, a) = \{(q, aa)\}$$

$$\delta(q\,,\,b\,,\,a)=\{(q_1,e)\}$$

$$\delta(q_1, b, a) = \{(q_1, e)\}$$

$$\delta(q_1\,,\,b,\,Z_0\,)=\{(q_2,\,e)\}$$

- a) Describe the language accepted by M.
- b) Trace all computations of the strings aab, abb, aba in M.
- c) Show that *aaabb*,  $aaab \in L(M)$ .
- (2) Construct PDAs that accept each of the following languages.

$$a) \{a^{i}b^{j} \mid 0 \leq i \leq j\}$$

$$b) \{a^{\dot{i}}c^{\dot{j}}b^{\dot{i}} \mid i,j \geq 0\}$$

$$d) \{a^{i}b^{j}c^{k} / i+k=j\}$$

$$e) \quad \{a^{i}b^{j} \mid 0 \le i \le j \le 2i\}$$

$$f) \{a^{i+j}b^ic^j / i,j > 0\}$$

(3)  $L = \{w \in \{a, b\}^* \mid at \ least \ one \ prefix \ of \ w \ contains \ strictly \ more \ b$ 's than a's.}.

For example, baa, abb, abbbaa are in L, but aab, aabbab are not in L.

- a) Construct a PDA that accepts  $\boldsymbol{L}$  by final state.
- b) Construct a PDA that accepts L by empty stack.
- (4) From the main text Exercises 6.2.6, 6.3.2, 6.3.4