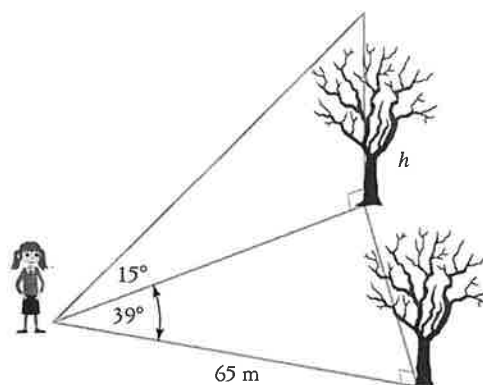
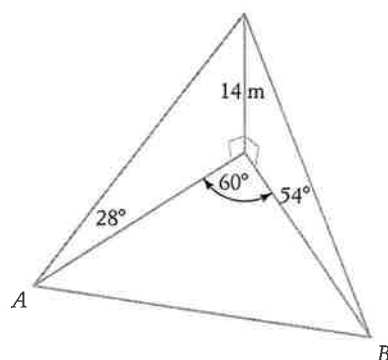


**WORKSHEET**

# 3D trigonometry

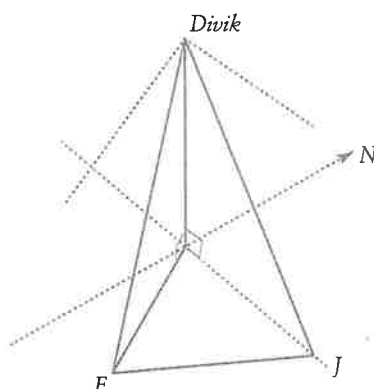
- 1 Isabella stands in a field and observes that the angle between the lines to the bases of 2 trees is  $39^\circ$ , while the angle of elevation to one tree is  $15^\circ$ . If Isabella is 65 metres from the other tree, find the height  $h$  of the first tree.

- 2 Find the distance from A to B.



- 3 Divik is looking out of a window 35 m above the ground. He sees his friend James east of him at an angle of depression of  $34^\circ$ . His friend Fahmid is at a bearing of  $150^\circ$  at an angle of depression of  $41^\circ$ .

- a Show these details on this diagram.

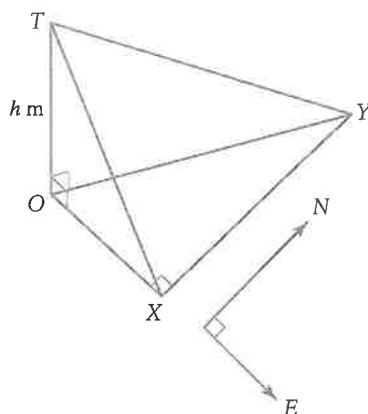


- b Find the distance between Fahmid and James.

- 4 Annelise walks 1000 metres due north along a road from point  $X$  to point  $Y$ . The point  $X$  is due east of a tower  $OT$ , where  $T$  is the top of the tower. The height of the tower above point  $O$  is  $h$  metres.

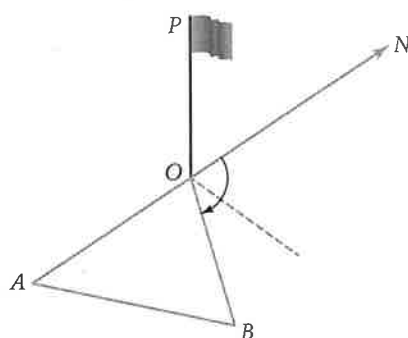
When Annelise stood at  $X$ , the angle of elevation was  $18^\circ$ . From point  $Y$ , the angle of elevation to the top of the tower is  $12^\circ$ .

- a Add all the given information to this diagram.



- b Show that  $OX = h \cot 18^\circ$ .
- c Show that  $OY = h \cot 12^\circ$ .
- d Using  $\triangle OXY$ , show that  $h^2 = \frac{1000^2}{\cot^2 12^\circ - \cot^2 18^\circ}$ .
- e Hence, find the value of  $h$ , correct to one decimal place.
- 5 From a point  $A$  due south of a flagpole, the angle of elevation of the top of the pole  $P$ , is  $38^\circ$ . From another point  $B$ , on a bearing of  $117^\circ$  from the pole, the angle of elevation of  $P$  is  $36^\circ$ . The distance  $AB$  is 110 metres. Let  $h$  be the height of the flagpole.

- a Add all the given information to this diagram.



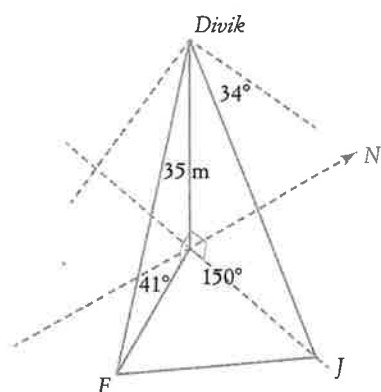
- b Show that  $OA = h \cot 38^\circ$  and  $OB = h \cot 36^\circ$ .
- c Hence find, correct to one decimal place, the height of the flagpole.

**Answers**

1 22.4 m

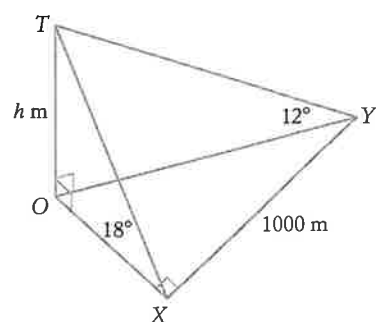
2 23 m

3 a



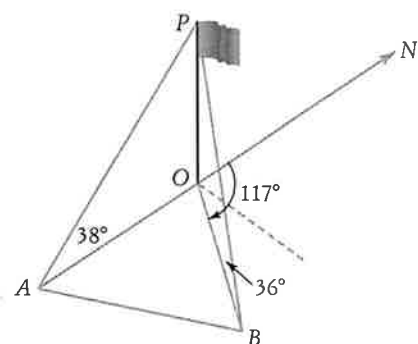
b 47.2 m

4 a



e 281.0 m

5 a



c 79.1 m