



Deep Learning Forecasting of NFL Game Outcomes Relative to Betting Odds

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Betting

- Two types of bets were considered:
 - Over/Under: A “50-50” bet on whether the combined score of both teams will be over or under a target
 - $\text{Away Score} + \text{Home Score} \geq \text{Target}$
 - Spread: A “50-50” on whether the home team will win by at least a given number of points
 - $\text{Home Score} - \text{Away Score} \geq \text{Target}$
- With repeated bets, one can expect to lose 3-4.5%
- Can the outcome of an NFL game be forecasted, and can those forecasts be used to make profitable bets?



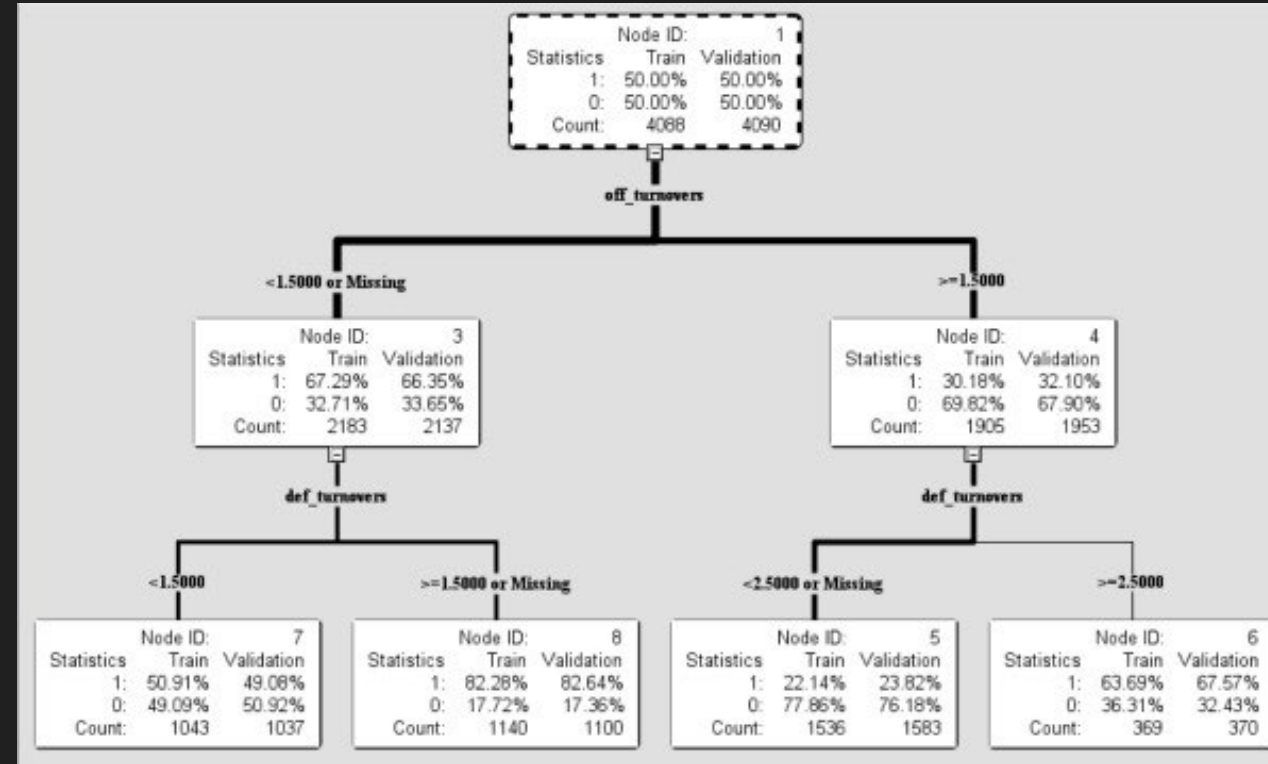
Golec and Tamarkin (1991)

- Used linear regression and F-tests to test for biases in betting odds
- $Y = \beta_1 X_1 + \beta_2 X_2 + \beta_3 X_3 + \beta_4 X_4 + \varepsilon$
 - X_1 is a vector of ones, X_2 is the betting spreads, X_3 is a dummy variable representing whether a team is at home, and X_4 is a dummy variable representing whether a team is favored
 - If the odds are efficient and have no bias, then $\beta_1 = \beta_3 + \beta_4 = 0$ and $\beta_2 = 0$
- All else being equal, bets on underdogs or home teams win more often than those on favorites or visiting teams



Gifford and Bayrak (2023)

- Focused on building binary logistic regression models and decision trees to predict where a team will win based on stats like turnovers, rush yards, and whether the game went to overtime
- They found that a logistic regression could be made that predicts the outcome of a game with a 16.9% misclassification rate (21.6% for decision trees)



Model Formulation

- Part 1: Predict proportion of drives ending in touchdowns, field goals, and punts
 - Analyze previous 16 games of each team to determine offensive and defensive outcomes
 - Create 8 time series: touchdown/field goal, home/away, offense/defense
- Part 2: Build team point total distribution using predicted proportions
 - Average respective offense and defense forecasts together
 - Assume drive outcomes are independent
 - Model game outcome with trinomial distribution and Monte Carlo simulation



Part 1: Drive-Level Outcomes

- Models Tested:
 - Least-Squares Regression
 - Holt Exponential Smoothing
 - Recurrent Neural Network (RNN)
 - Long Short-Term Memory (LSTM)
 - Multi-Layer Perceptron (MPL)
 - Transformer Model
- Training Data:
 - Data from the 2020-2023 NFL seasons (regular season games)
 - 1,706 time series built from offensive and defensive drive outcomes



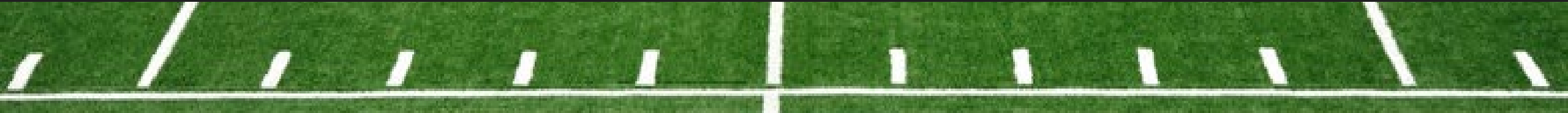
Part 2: Drive-Level Outcomes

- Monte Carlo Simulation for Game Prediction:
 - Use predicted drive-level probabilities (touchdowns, field goals, punts).
 - Trinomial distribution for game outcomes: $X \sim \text{trinomial}(p_{\text{touchdown}}, p_{\text{field goal}}, p_{\text{punt}})$ where $p_{\text{punt}} = 1 - p_{\text{touchdown}} - p_{\text{field goal}}$
- Expected Score: $7 * p_{\text{touchdown}} + 3 * p_{\text{field goal}} + 0 * p_{\text{punt}}$
- Forecast real 2024 game outcomes using data from the 2023 and 2024 NFL seasons



2024 Forecast Results

| Model | TD Perc MAE | FG Perc MAE | Score MAE | Home Line Accuracy | Over/Under Accuracy |
|-----------|----------------|----------------|-----------|-----------------------|------------------------|
| LSR | 0.108 | 0.099 | 7.378 | 0.495 | 0.552 |
| RNN | 0.115 | 0.106 | 8.214 | 0.494 | 0.490 |
| LSTM | 0.108 | 0.098 | 7.367 | 0.490 | 0.500 |
| MLP | 0.116 | 0.105 | 8.480 | 0.454 | 0.516 |
| Transform | 0.107 | 0.101 | 7.581 | 0.495 | 0.516 |
| Holt | 0.132 | 0.120 | 9.512 | 0.469 | 0.485 |



Conclusions and Further Research

- 2024 NFL Forecasting
 - The models were typically off by about 7 points per team in score predictions
 - This variance is somewhat expected given the inherent unpredictability of sports outcomes
- Betting Accuracy
 - The models did not outperform random guesses in predicting over/under or game spread outcomes, generally staying close to a 50/50 chance
 - Some models, like LSR, MPL, and Transform, show promise if their accuracy can be sustained
- Future Enhancements
 - There are opportunities for improvement by adjusting the window length to better account for player injuries
 - Separating offensive and defensive data and incorporating advanced metrics like EPA and DVOA could further refine the models.



References

- [1] M. Gifford and Tuncay Bayrak, “A predictive analytics model for forecasting outcomes in the National Football League games using decision tree and logistic regression,” *Decision Analytics Journal*, vol. 8, pp. 100296–100296, Aug. 2023, doi: <https://doi.org/10.1016/j.dajour.2023.100296>.
- [1] J. Golec, “The degree of inefficiency in the football betting market Statistical tests,” *Journal of Financial Economics*, vol. 30, no. 2, pp. 311–323, Dec. 1991, doi: [https://doi.org/10.1016/0304-405x\(91\)90034-h](https://doi.org/10.1016/0304-405x(91)90034-h).



2020-2023 Test Fit Results (MAE)

| Model | TD Offense | TD Defense | FG Offense | FG Defense |
|-----------|------------|------------|------------|------------|
| LSR | 0.105 | 0.104 | 0.091 | 0.095 |
| RNN | 0.113 | 0.113 | 0.103 | 0.108 |
| LSTM | 0.110 | 0.104 | 0.091 | 0.095 |
| MLP | 0.115 | 0.116 | 0.101 | 0.108 |
| Transform | 0.121 | 0.105 | 0.094 | 0.095 |
| Holt | 0.135 | 0.140 | 0.118 | 0.120 |



EFIN 301 Presentation



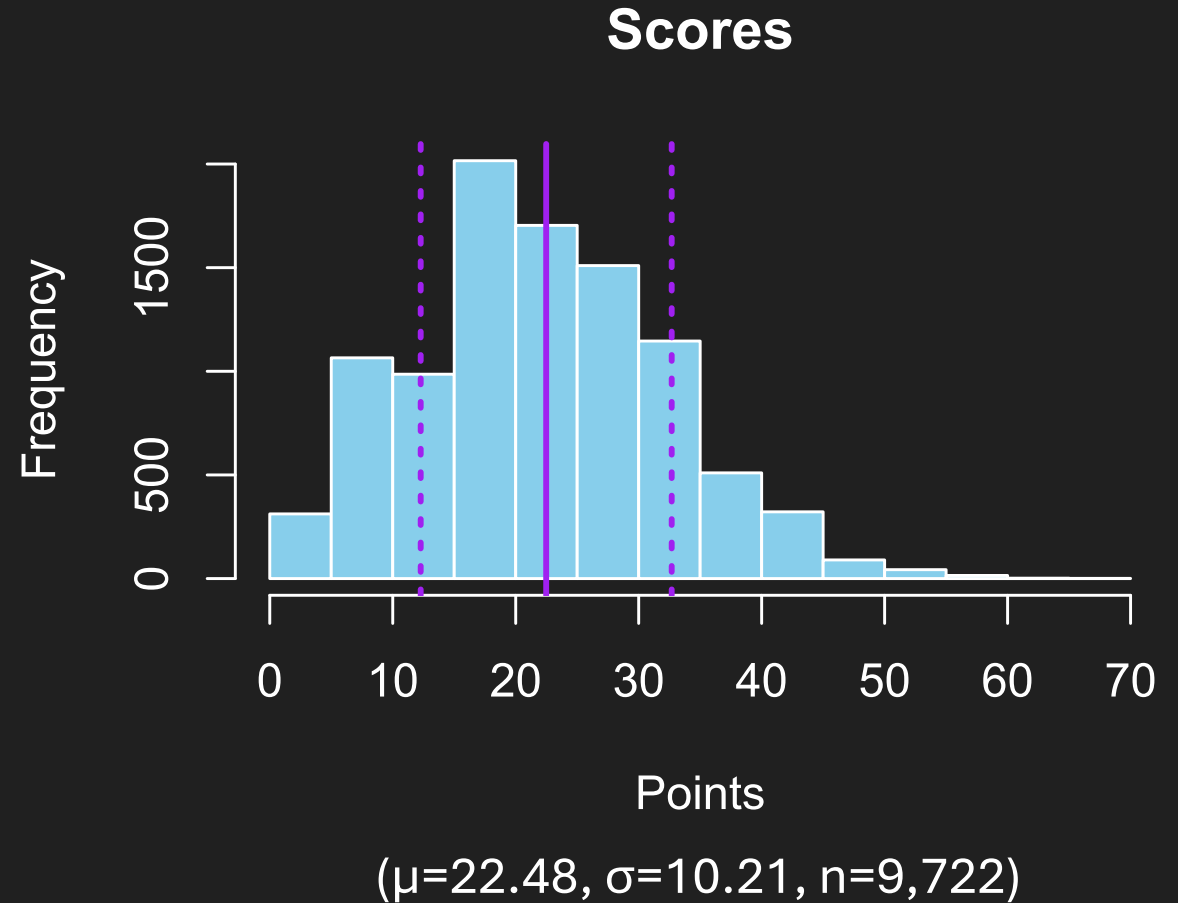
Background

- Sports betting is currently legal in 30 states, Puerto Rico, and the District of Columbia
- Some sites claim to use arbitrage between different oddsmakers to guarantee returns
- Simulation:
 - Using drive-level data, simulate the expected outcomes of a game
 - Using previous drive-level data, predict future drive-level data

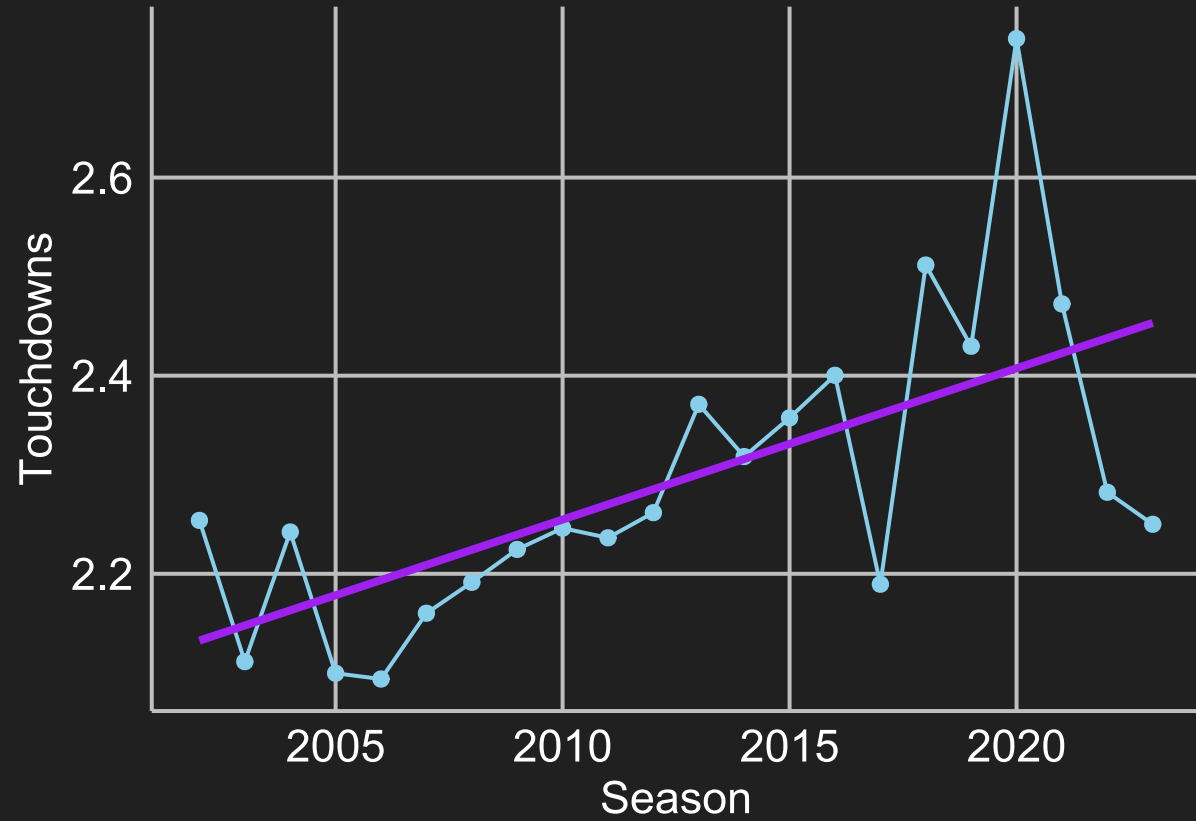


Data

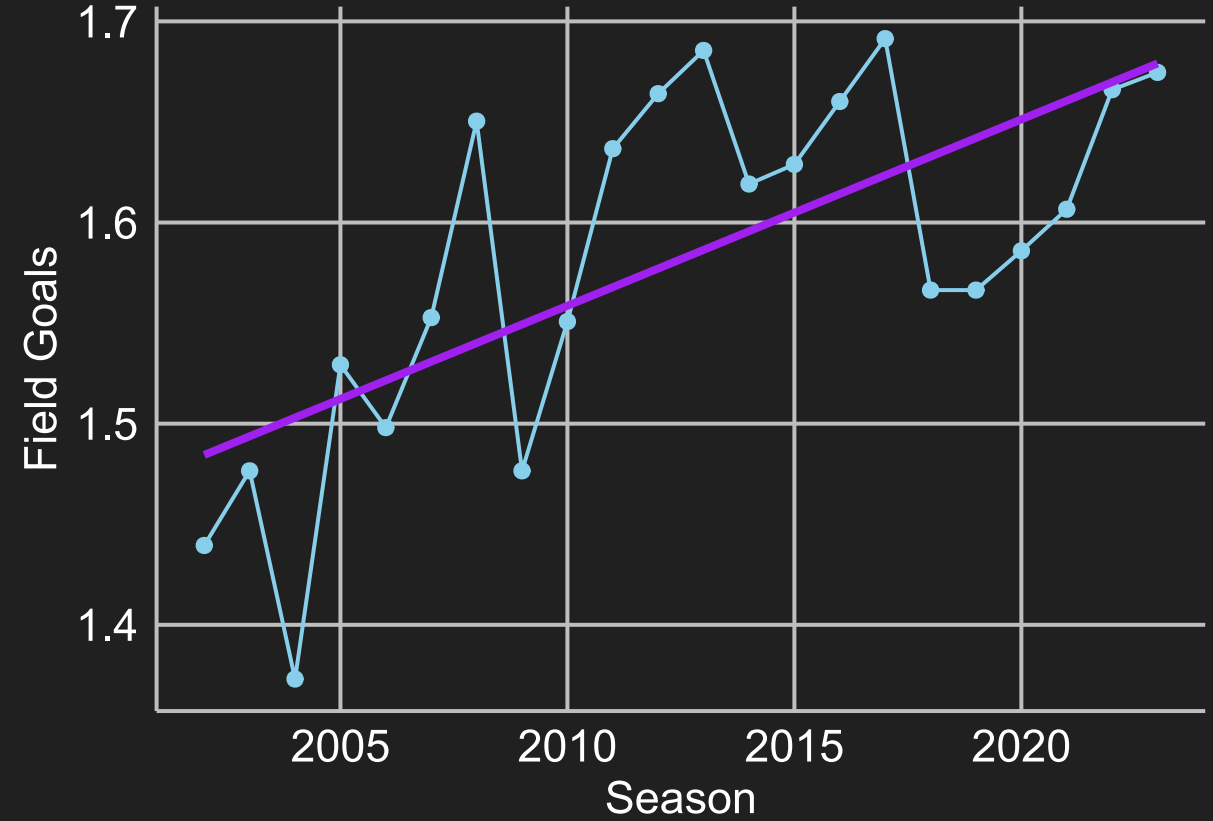
- Drive-level data (offense and defense) on all 32 NFL teams since 2002 (n=704)
 - Touchdowns
 - Field Goals
 - Punts
 - Turnovers
 - Total Drives
- Betting odds and outcomes for all NFL games since 2007 (n=4,861)



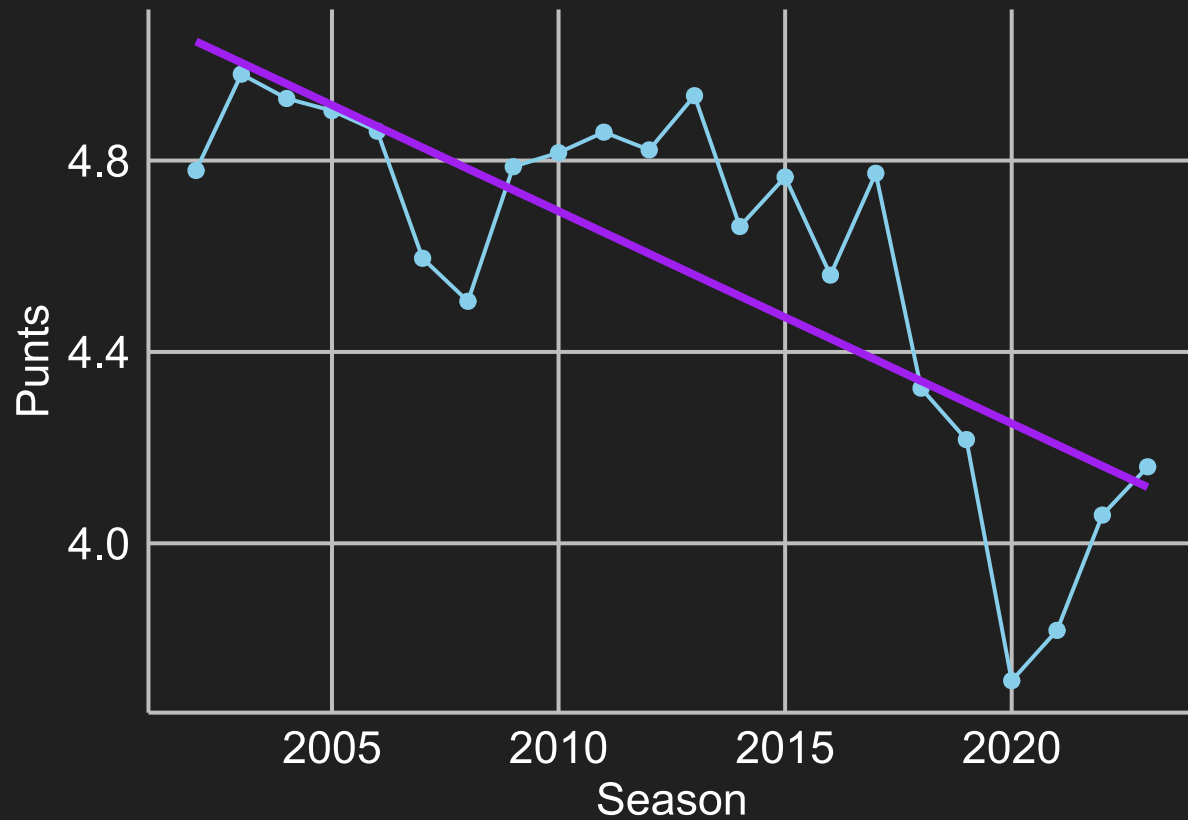
Touchdowns per Team per Game by Season



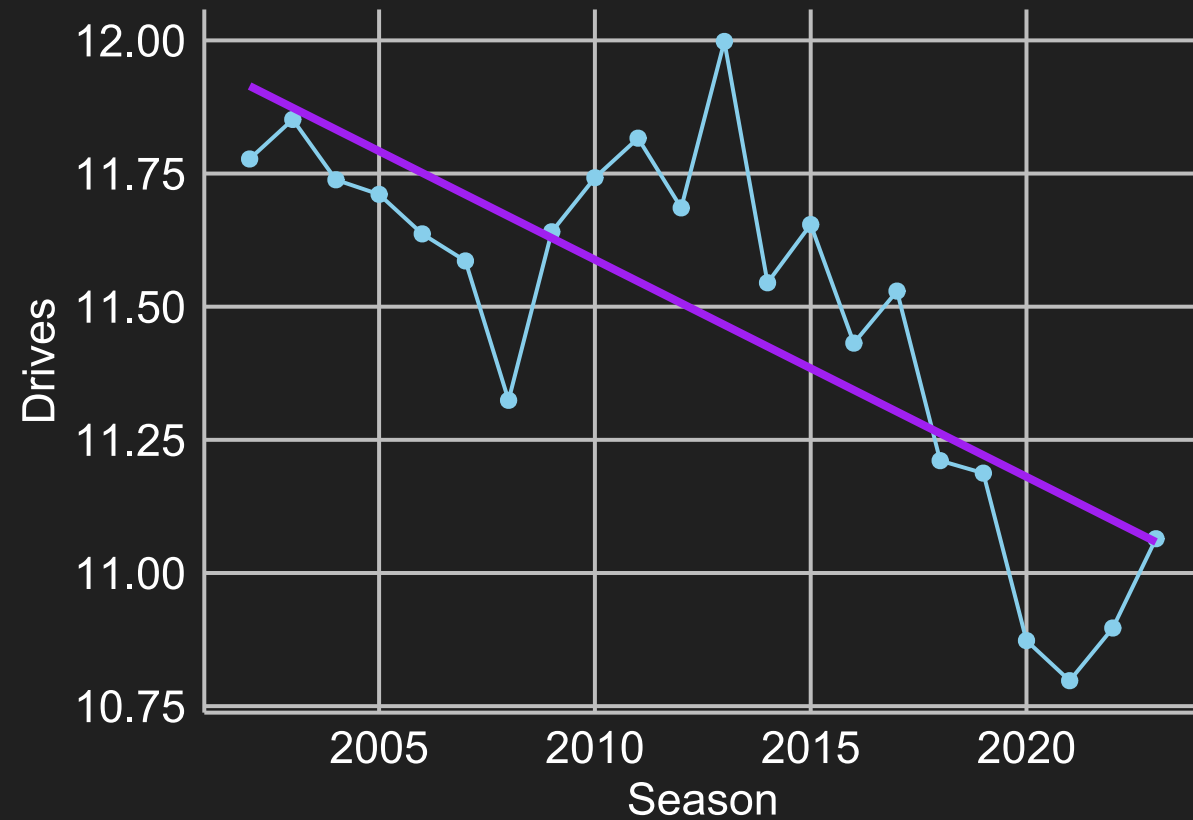
Field Goals per Team per Game by Season

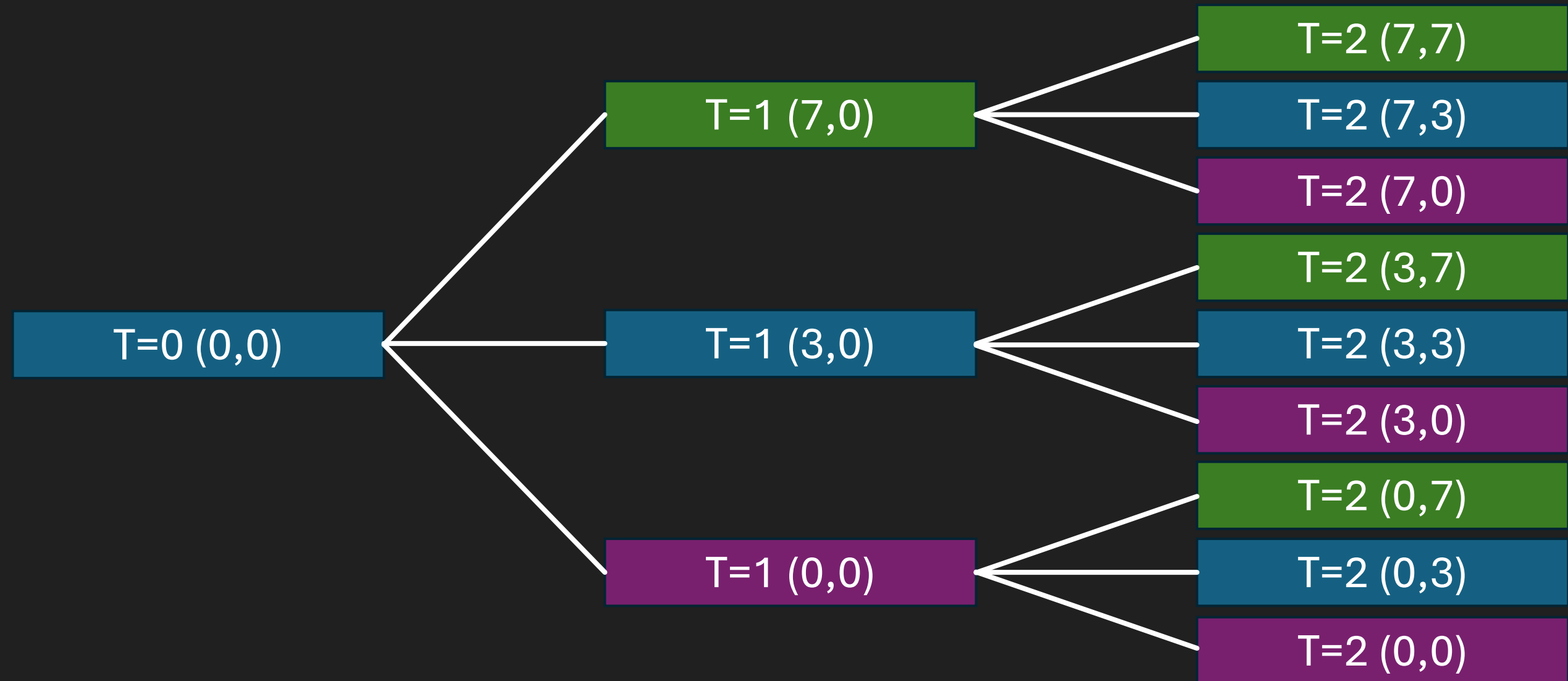


Punts per Team per Game by Season



Drives per Team per Game by Season



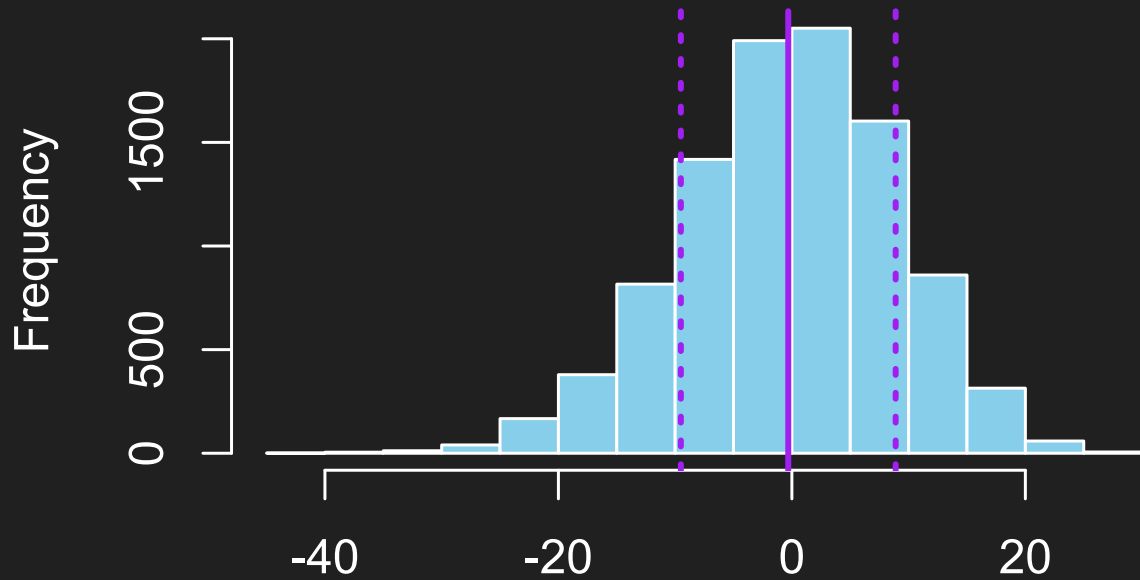


$$\sqrt{td_per_drive_t} = \hat{\beta}_0 + \hat{\beta}_1\sqrt{td_per_drive_{t-1}} + \hat{\beta}_2playoff_{t-1} + \hat{\beta}_3season$$

- $td_per_drive_t$: Number of touchdowns scored per drive in season t
- $playoff_t$: A dummy variable representing whether a team made the playoffs in season t
- $season$: The season to account for time trends

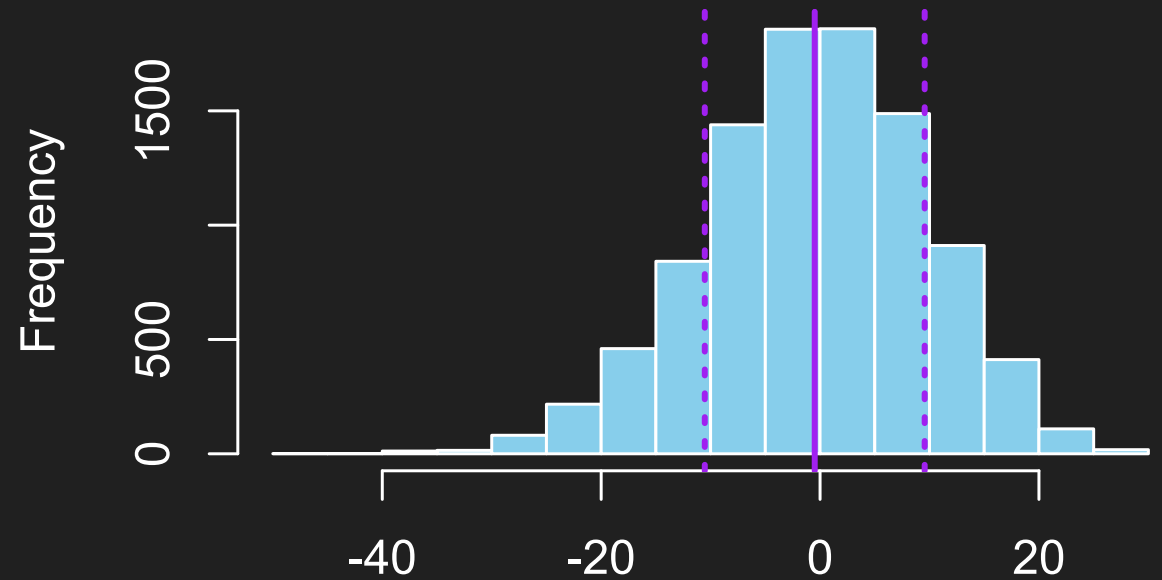


Error



Simulated - Actual
($\bar{x} = -0.31$, $S_x = 9.20$, $n = 9,722$)

Errors (Forecasted)



Simulated - Actual
($\bar{x} = -0.49$, $S_x = 10.04$, $n = 9,722$)



Over/Under Bet Returns

| Difference in Odds | Percent of Games (in 1 Season) | Returns | Returns (Dynamic) |
|--------------------|--------------------------------|---------|-------------------|
| >0% | 100% (272) | -3.9% | -4.4% |
| >5% | 77.5% (211) | -3.5% | -4.1% |
| >10% | 44.0% (120) | -5.3% | -5.0% |
| >20% | 8.4% (23) | -4.0% | -4.4% |
| >25% | 2.3% (6) | -1.1% | -2.3% |
| >30% | 0.5% (1) | -26.5% | -26.6% |



Money Line Bet Returns

| Difference in Odds | Percent of Games (in 1 Season) | Returns | Returns (Dynamic) |
|--------------------|--------------------------------|---------|-------------------|
| >0% | 100% (272) | -3.0% | -4.3% |
| >5% | 76.3% (208) | -3.9% | -4.6% |
| >10% | 53.2% (145) | -7.0% | -6.1% |
| >20% | 18.3% (50) | -8.5% | -6.4% |
| >25% | 8.2% (22) | 1.9% | 3.0% |
| >30% | 3.4% (9) | 1.8% | 3.8% |



Spread Bet Returns

| Difference in Odds | Percent of Games (in 1 Season) | Returns | Returns (Dynamic) |
|--------------------|--------------------------------|---------|-------------------|
| >0% | 100% (272) | -11.5% | -0.6% |
| >5% | 97.1% (264) | -11.7% | -0.6% |
| >10% | 91.5% (249) | -11.2% | -0.4% |
| >20% | 77.3% (210) | -5.6% | 2.8% |
| >25% | 68.2% (186) | 0.5% | 7.1% |
| >30% | 58.2% (158) | 8.6% | 13.2% |



Conclusions

- The model is better at determining the difference between the teams' scores than determining the combined score
- Scaling bets based on expected returns may or may not increase returns/decrease losses
- There is a Goldilocks zone of differences to exploit
- Football games are inherently difficult to accurately predict

