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Subject : Laboratory Practice - III

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Assignment No.1

* Title :-

Write a program non-recursive and recursive to calculate Fibonacci numbers and analyze their time and space complexity.

* Objective :-

Students should be able to perform non-recursive and recursive program to calculate Fibonacci numbers and analyze their time and space complexity.

* Prerequisite :-

1. Basic of Python or Java Programming
2. Concept of Recursive and Non-recursive functions.
3. Execution flow of calculate Fibonacci numbers.
4. Basic of Time and Space complexity.



* Theory :-

- Introduction to Fibonacci numbers :-
 - The Fibonacci series, named after Italian mathematician Leonardo Pisano Bogollo, later known as Fibonacci, is a series (sum) formed by Fibonacci numbers denoted as F_n . The numbers in Fibonacci sequence are given as : 0, 1, 1, 2, 3, 5, 8, 13, 21, 38...
 - In a Fibonacci series, every term is the sum of the preceding two terms, starting from 0 and 1. as first and second term. In some old references, the term '0' might be omitted.
- What is the Fibonacci Series?
 - The Fibonacci series is the sequence of numbers (also called Fibonacci numbers), where every number is the sum of the preceding two numbers, such that the first two terms are '0' and '1'.
 - In some older versions of the series, the term '0' might be omitted. A Fibonacci series can thus be given as, 0, 1, 1, 2, 3, 5, 8, 13, 21, 34, ... It can be thus be observed that every



term can be calculated by adding the two terms before it.

- Given the first term, F_0 and second term, F_1 as '0' and '1', the third term here can be given as, $F_2 = 0 + 1 = 1$

Similarly,

$$F_3 = 1 + 1 = 2$$

$$F_4 = 2 + 1 = 3$$

Given a number n , print n -th Fibonacci Number.

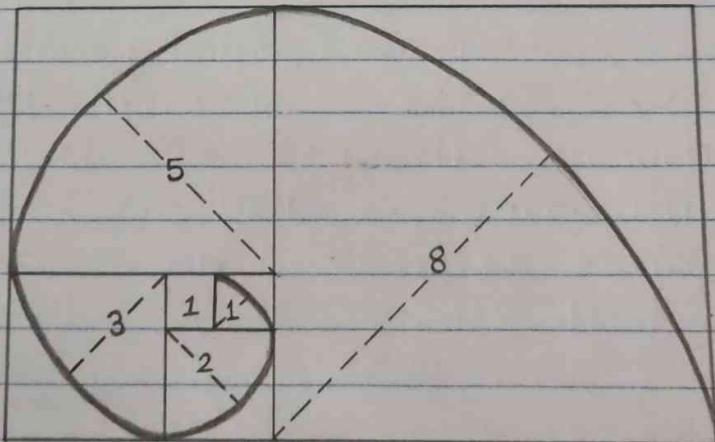


Fig. Fibonacci Number



* Fibonacci Sequence Formula

The Fibonacci sequence of numbers "Fn" is defined using the recursive relation the seed values $F_0=0$ and $F_1=1$:

$$F_n = F_{n-1} + F_{n-2}$$

Here, the sequence is defined using two different parts, such as kick-off and recursive relation.

The kick-off part is $F_0=0$ and $F_1=1$.

The recursive relation part is $F_n = F_{n-1} + F_{n-2}$.

It is noted that the sequence starts with 0 rather than 1. So, F_5 should be the 6th term of the sequence.

* Methods:-

1. Non-recursion:

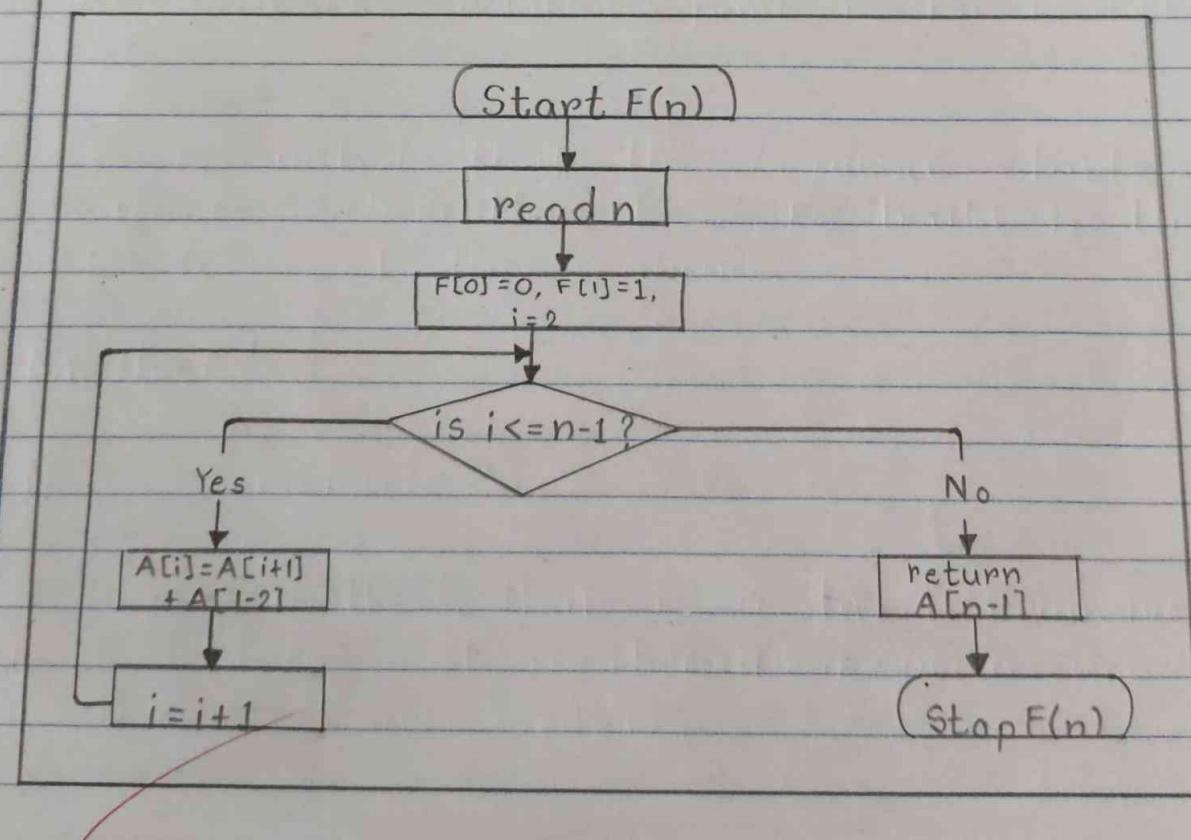
A simple method that is a direct recursive implementation of mathematical recurrence relation is given above.

First, we'll store 0 and 1 in $F[0]$ and $F[1]$, respectively.

Next, we'll iterate through array positions 2 to $n-1$. At each position i , we store the sum of the two preceding array values in $F[i]$.

Finally, we return the value of $F[n-1]$, giving us the number at position n in the sequence.

Here's a visual representation of this process:





```
# Program to display the Fibonacci sequence  
up to n-th term  nterms = int(input("How  
many terms?"))
```

```
# first two terms
```

```
n1, n2 = 0, 1  
count = 0
```

```
# check if the number of terms is valid  
if nterms <= 0;  
    print ("Please enter a positive integer")
```

```
# if there is only one term, return n1
```

```
elif nterms == 1;
```

```
    print ("Fibonacci sequence upto", nterms, ":")  
    print (n1)
```

```
# generate fibonacci sequence  
else:
```

```
    print ("Fibonacci sequence:")
```

```
    while count < nterms;
```

```
        print (n1)
```

```
        nth = n1 + n2
```

```
# update values
```

```
        n1 = n2
```

```
        n2 = nth
```

~~```
 count+=1.
```~~



\* Output :-

How many terms? 7

Fibonacci sequence :-

0  
1  
1  
2  
3  
5  
8

## 2. Recursion :

Start by defining  $F(n)$  as the function that returns the value of  $F_n$ .

To evaluate  $F(n)$  for  $n > 1$ , we reduce our problem into two smaller problems of the same kind :  $F(n-1)$  and  $F(n-2)$ .

We can further reduce  $F(n-1)$  and  $F(n-2)$  to  $F(n-1)-1$  and  $F(n-1)-2$ ; and  $F((n-2)-1)$  and  $F((n-2)-2)$ , respectively.

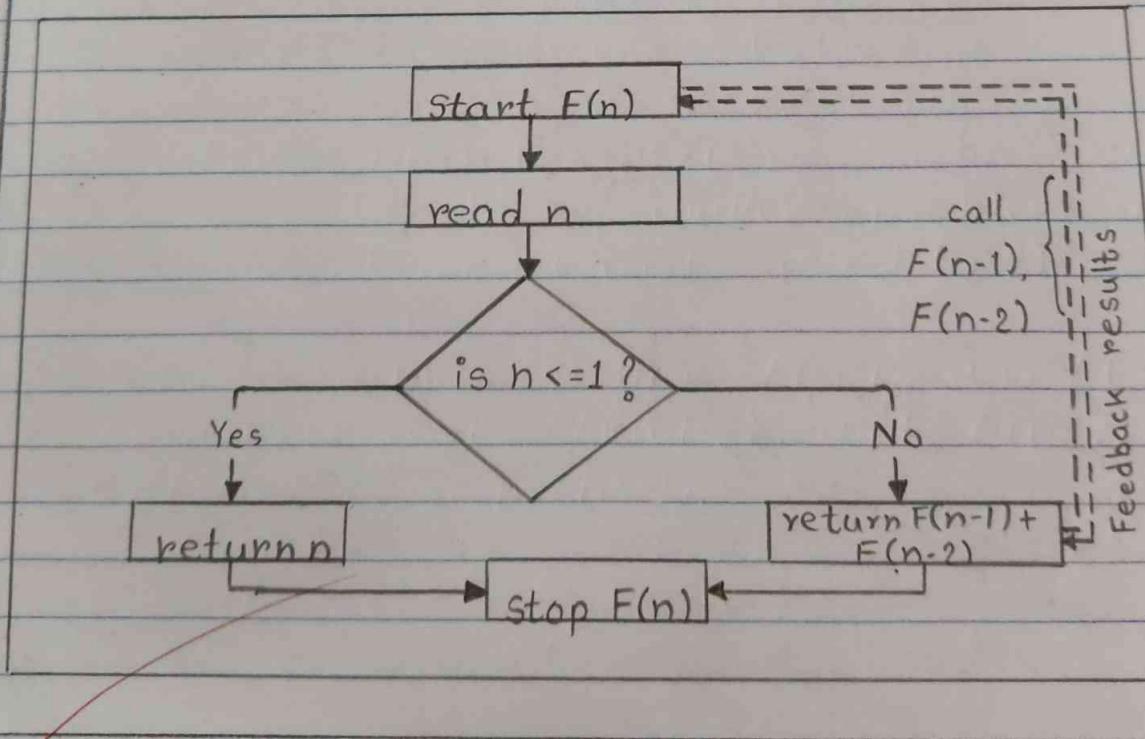


If we repeat this reduction, we'll eventually reach our known base cases and thereby, obtain a solution to  $F(n)$ .

Employing this logic, our algorithm for  $F(n)$  will have two steps;

1. Check if  $n \leq 1$ . If so, return  $n$ .
2. Check if  $n > 1$ . If so, call our function  $F$  with inputs  $n-1$  and  $n-2$ , and return the sum of the two results.

Here's a visual representation of this algorithm:





# Python program to display the Fibonacci Sequence

```
def recur_fibo(n):
 if n <= 1:
 return n
 else:
 return (recur_fibo(n-1) + recur_fibo(n-2))
```

nterms = 7

# check if the number of terms is valid

```
if nterms <= 0:
 print ("Please enter a positive integer")
else:
 print ("Fibonacci Sequence:")
 for i in range (nterms):
 print (recur_fibo(i))
```

### \* Output:

Fibonaci Sequence:

0, 1, 1, 2, 3, 5, 8

\* Conclusion:- In this way we have learned concept of fibonacci series.

```
import java.io.*;
class FibonacciNonRecursive {
 // Function to print N Fibonacci Numbers
 static void Fibonacci(int N) {
 int num1 = 0, num2 = 1;
 for (int i = 0; i < N; i++) {
 // Print the number
 System.out.print(num1 + " ");
 // Swap
 int num3 = num2 + num1;
 num1 = num2;
 num2 = num3;
 }
 }
 // Driver Code
 public static void main(String args[]) {
 int N = 10;
 Fibonacci(N);
 }
}
```



```
import java.io.*;
class FibonacciRecursive {
 // Function to print the Fibonacci series
 static int fib(int n) {
 if (n <= 1)
 return n;
 return fib(n - 1) + fib(n - 2);
 }
 // Driver Code
 public static void main(String args[]) {
 int N = 10;
 for (int i = 0; i < N; i++) {
 System.out.print(fib(i) + " ");
 }
 }
}
```

```
+1 user@user:~$ javac p.java
user@user:~$ java p
0 1 1 2 3 5 8 13 21 34 user@user:~$ |
```

13

user@user:~

```
user@user:~$ javac p.java
user@user:~$ java p
0 1 1 2 3 5 8 13 21 34 user@user:~$ |
```

## Assignment No. 2.

- \* Title:- Write a program to implement Huffman Encoding using a greedy strategy.
- \* Objective:- Students should be able to understand and solve Huffman Encoding and analyze time and space complexity using a greedy strategy.

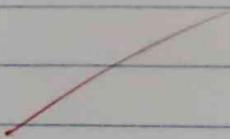
### \* Theory:

- What is a Greedy Method?

- A greedy algorithm is an approach for solving a problem by selecting the best option available at the moment. It doesn't worry whether the current best result will bring the overall optimal result.
- The algorithm never reverse the earlier decision even if the choice is wrong. It works in a top-down approach.
- This algorithm may not produce the best result for all the problems. It's because it always goes for the local best choice to produce the global best result.



- Advantages of Greedy Approach :-
  - The algorithm is easier to describe.
  - This algorithm can perform better than other algorithms (but, not in all cases).
- Disadvantages of Greedy Approach :-
  - As mentioned earlier, the greedy algorithm doesn't always produce the optimal solution. This is the major disadvantage of the algorithm.
  - For example, suppose we want to find the longest path in the graph below from root to leaf.
- Greedy Algorithm :-
  1. To begin with, the solution set (containing answers) is empty.
  2. At each step, an item is added to the solution set until a solution is reached.
  3. If the solution set is feasible, the current item is kept.
  4. Else, the item is rejected and never considered again.





## \* Huffman Encoding

Huffman coding is a lossless data compression algorithm. The idea is to assign variable-length codes to input characters, lengths of the assigned codes are based on the frequency of corresponding characters.

The most frequent character gets the smallest code and the least frequent character gets the largest code. The variable-length codes assigned to input characters are Prefix Codes means the largest code. The variable-length codes assigned to input characters are Prefix Codes means the codes (bit sequences) are assigned in such a way that the code assigned to one character is not prefix of code assigned to any other character. This is how Huffman Coding makes sure that there is no ambiguity when decoding the generated bit stream.

» There are mainly two major parts in Huffman Coding:

- 1) Build a Huffman Tree from input characters.
- 2) Traverse the Huffman Tree and assign codes



to characters.

» Steps to build Huffman Tree:

Input is array of unique characters along with their frequency of occurrences & output is Huffman Tree.

1. Create a leaf nodes for each unique character and build a min heap of all leaf nodes (Min Heap is used as a priority queue. The value of frequency field is used to compare two nodes in min heap. Initially, the leaf frequent character is at root).
2. Extract two nodes with the minimum frequency from the min heap.
3. Create a new internal node with frequency equal to the sum of the two nodes frequencies. Make the first extracted nodes as its left child & the other extracted node as a right child. Add this node to the min heap.
4. Repeat steps #2 and #3 until the heap contains only one node. The remaining node is the root node and the tree

is complete.

#### \* Algorithm for Huffman code:

Input :- Number of message with frequency count.

Output :- Huffman merge tree.

1. Begin
2. Let Q be the priority queue.
3.  $Q = \{ \text{initialize priority queue with frequencies of all symbol or message} \}$
4. Repeat  $n-1$  times.
5. Create a new node Z
6.  $X = \text{exact\_min}(Q)$
7.  $Y = \text{exact\_min}(Q)$
8.  $\text{Frequency}(Z) = \text{Frequency}(X) + \text{Frequency}(Y);$
9. Insert(Z, Q)
10. End repeat
11. Return ( $\text{extract\_min}(Q)$ )
12. End.

#### \* Time Complexity -

$O(n \log n)$  where  $n$  is the number of unique characters. If there are  $n$  nodes,  $\text{extractMin}()$  is called  $2 * (n-1)$  times.  $\text{extractMin}()$  takes  $O(\log n)$  time as it calls  $\text{minHeapify}()$ .



So, overall complexity is  $O(n \log n)$ .

Thus, Overall time complexity of Huffman Coding becomes  $O(n \log n)$ .

If the input array is sorted, there exists a linear time algorithm.

\* Conclusion :-

In this way concept of Huffman Encoding is explored using greedy method.

```

import java.util.Comparator;
import java.util.PriorityQueue;
import java.util.Scanner;

class HuffmanCoding {
 // Print Huffman codes
 public static void printCode(HuffmanNode root, String s) {
 if (root.left == null && root.right == null && Character.isLetter(root.c)) {
 System.out.println(root.c + ":" + s);
 return;
 }
 printCode(root.left, s + "0");
 printCode(root.right, s + "1");
 }

 // Main function
 public static void main(String[] args) {
 char[] charArray = { 'a', 'b', 'c', 'd', 'e', 'f' };
 int[] charfreq = { 5, 9, 12, 13, 16, 45 };
 PriorityQueue<HuffmanNode> q = new PriorityQueue<>(6, new MyComparator());

 for (int i = 0; i < charArray.length; i++) {
 HuffmanNode hn = new HuffmanNode();
 hn.c = charArray[i];
 hn.data = charfreq[i];
 hn.left = null;
 hn.right = null;
 q.add(hn);
 }
 }
}

```

HuffmanNode root = null;

```
 while (q.size() > 1) {
 HuffmanNode x = q.poll();
 HuffmanNode y = q.poll();
 HuffmanNode f = new HuffmanNode();
 f.data = x.data + y.data;
 f.c = '-';
 f.left = x;
 f.right = y;
 root = f;
 q.add(f);
 }
 printCode(root, "");
 }
}

class HuffmanNode {
 int data;
 char c;
 HuffmanNode left;
 HuffmanNode right;
}

class MyComparator implements Comparator<HuffmanNode> {
 public int compare(HuffmanNode x, HuffmanNode y) {
 return x.data - y.data;
 }
}
```

User@user:~

```
$ javac p.java
$ java p
```

```
f:0
c:100
d:101
a:1100
b:1101
e:111
```

User@user:~\$ |



### Assignment No. 3.

\* Title :- Write a program to solve a fractional knapsack problem using a greedy method.

\* Objective :- To analyze time and space complexity of fractional Knapsack problem using a greedy method.

\* Theory :-

- Knapsack Problem :

You are given the following :-

- A knapsack (Kind of shoulder bag) with limited weight capacity.
- Few items each having some weight and value.
- The problem states :-

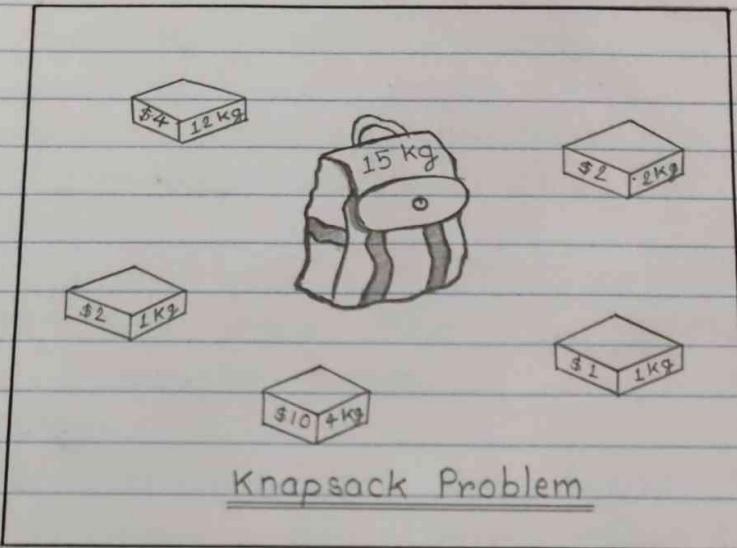
Which items should be placed into the knapsack such that :-

- The value or profit obtained by putting



the items into the knapsack is maximum.

- And the weight limit of the knapsack does not exceed.



#### \* Knapsack Problem Variants:

Knapsack problem has the following two variants

1. Fractional Knapsack Problem
2. 0/1 Knapsack Problem

#### ↔ Knapsack Problem (Fractional):

In Fractional knapsack Problem,

- As the name suggests, items are divisible here.

- We can even put the fraction of any item into the knapsack if taking the complete item is not possible.
- It is solved using the Greedy Method.

### Fractional Knapsack Problem:-

Fractional knapsack problem is solved using greedy method in the following steps-

Step-01 : For each item, compute its value/ weight ratio.

Step-02 : Arrange all the items in decreasing order of their value / weight ratio.

Step -03 : Start putting the items into the knapsack beginning from the item with the highest ratio. as many items as you can into the knapsack.

- Example:- Find the optimal solution for the fractional knapsack problem making use of greedy approach.



Given :-

$$n = 5$$

$$w = 60 \text{ kg}$$

$$(w_1, w_2, w_3, w_4, w_5) = (5, 10, 15, 22, 25)$$

$$(b_1, b_2, b_3, b_4, b_5) = (30, 40, 45, 77, 90)$$

→ Solution -

Step-01: Compute the value / weight ratio for each item -

| Items | Weight | Value | Ratio |
|-------|--------|-------|-------|
| 1     | 5      | 30    | 6     |
| 2     | 10     | 40    | 4     |
| 3     | 15     | 45    | 3     |
| 4     | 22     | 77    | 3.5   |
| 5     | 25     | 90    | 3.6   |

Step-02: Sort all the items in decreasing order of their value / weight ratio.

I<sub>1</sub>, I<sub>2</sub>, I<sub>3</sub>, I<sub>4</sub>, I<sub>5</sub>  
(6) (4) (3.6) (3.5) (3)



Step-03: Start filling the knapsack by putting the items into it one by one.

| Knapsack Weight | Items in Knapsack | Cost |
|-----------------|-------------------|------|
| 60              | Ø                 | 0    |
| 55              | I1                | 30   |
| 45              | I1, I2            | 70   |
| 20              | I1, I2, I5        | 160  |

Now,

- knapsack weight left to be filled is 20kg but item-4 has weight of 22kg.
- Since in fractional knapsack problem, even the fraction of any item can be taken.
- So, knapsack will contain the following items-

$\langle I1, I2, I5, (20/22) I4 \rangle$

Total cost of the knapsack

$$= 160 + (20/22) \times 77$$

$$= 160 + 70$$

$$= 230 \text{ units}$$

## \* Algorithm - Fractional Knapsack:

- Greedy - fractional - knapsack ( $w, v, W$ )

1. for  $i = 1$  to  $n$
2. do  $x[i] = 0$
3. weight = 0
4. While weight <  $W$
5. do  $i = \text{best remaining item}$
6. If weight +  $w[i] \leq W$
7. then  $x[i] = 1$
8. weight = weight +  $w[i]$
9. else
10.  $x[i] = (w - \text{weight}) / w[i]$
11. weight =  $W$
12. return  $x$

## \* Time Complexity -

- The main time taken step is the sorting of all items in decreasing order of their value/weight ratio.
- If the items are already arranged in the required order, then while loop takes  $O(n)$  time.
- The average time complexity of Quick Sort is  $O(n \log n)$ .



- Therefore, total time taken including the sort is  $O(n \log n)$ .

\* Conclusion :-

In this way concept of Fractional Knapsack is explained using greedy method.

```
import java.util.Arrays;
import java.util.Comparator;

public class FractionalKnapsack {
 // Inner class to represent an item with weight, value, and value-to-weight ratio
 static class Item {
 double weight, value, ratio;

 // Constructor to initialize an item with weight, value, and ratio
 public Item(double weight, double value) {
 this.weight = weight;
 this.value = value;
 this.ratio = value / weight;
 }
 }

 // Method to calculate the maximum value that can be carried in the knapsack
 public static double getMaxValue(Item[] items, double capacity) {
 // Sort items by their value-to-weight ratio in descending order
 Arrays.sort(items, new Comparator<Item>() {
 @Override
 public int compare(Item o1, Item o2) {
 return Double.compare(o2.ratio, o1.ratio);
 }
 });

 double totalValue = 0;

 // Iterate through the sorted items
 for (Item item : items) {
 if (capacity == 0) break;
 }
 }
}
```

```
// If the item can be completely added to the knapsack
if (capacity >= item.weight) {
 capacity -= item.weight;
 totalValue += item.value;
} else {
 // If only part of the item can be added to the knapsack
 totalValue += item.value * (capacity / item.weight);
 capacity = 0;
}
}

return totalValue;
}

// Main method
public static void main(String[] args) {
 // Array of items with specified weights and values
 Item[] items = {
 new Item(10, 60),
 new Item(20, 100),
 new Item(30, 120)
 };

 // Knapsack capacity
 double capacity = 50;

 // Calculate the maximum value that can be carried and print the result
 double maxValue = getMaxValue(items, capacity);
 System.out.println("Maximum value in knapsack: " + maxValue);
}
```

```
user@user:~$ javac P.java
user@user:~$ java P
Maximum value in knapsack: 240.0
user@user:~$ |
```



### Assignment No. 4

\* Title: Write a program to solve a 0-1 Knapsack problem using dynamic programming strategy.

\* Objective: To analyze time and space complexity of 0-1 Knapsack problem using dynamic programming.

\* Theory :-

- What is Dynamic Programming?

Dynamic Programming is also used in optimization programs. Like divide and conquer method, Dynamic Programming solves problems by combining the solutions of subproblems.

Dynamic Programming algorithm solves each sub-problem just once and then saves its answer in a table, thereby avoiding the work of re-computing the answer every time.

Two main properties of a problem suggest that the given problem can be solved using Dynamic Programming.



These properties are overlapping sub-problems and optimal substructure.

Dynamic Programming also combines solutions to sub-problems. It is needed repeatedly. The computed solutions are stored in a table, so that they don't have to be re-computed. Hence, this technique is needed where overlapping sub-problem exists.

- Steps of Dynamic Programming Approach:

Dynamic Programming algorithm is designed using the following four steps-

- Characterize the structure of an optimal solution.
- Recursively define the value of an optimal solution.
- Compute the value of an optimal solution, typically in a bottom-up fashion
- Construct an optimal solution from the computed information.



### » Applications of Dynamic Programming Approach :-

- Matrix Chain Multiplication
- Longest common Subsequence
- Travelling salesman Problem

### » Time Complexity :-

- Each entry of the table requires constant time  $O(1)$  for its computation.
- It takes  $O(nw)$  time to fill  $(n+1)(w+1)$  table entries.
- It takes  $O(n)$  time for tracing the solution since tracing process traces the  $n$  rows.
- Thus, overall  $O(nw)$  time is taken to solve 0/1 Knapsack problem using dynamic programming.

\* Conclusion :- In this way we have explored Concept of 0/1 Knapsack using Dynamic approach.

```

public class KnapsackDP {
 // Function to solve the 0-1 Knapsack problem
 public static int knapsack(int[] weights, int[] values, int capacity) {
 int n = weights.length;
 int[][] dp = new int[n + 1][capacity + 1];

 // Building the DP table
 for (int i = 0; i <= n; i++) {
 for (int w = 0; w <= capacity; w++) {
 if (i == 0 || w == 0) {
 dp[i][w] = 0; // Base case: no items or zero capacity
 } else if (weights[i - 1] <= w) {
 // Include the item or exclude it, choose the maximum value
 dp[i][w] = Math.max(values[i - 1] + dp[i - 1][w - weights[i - 1]], dp[i - 1][w]);
 } else {
 dp[i][w] = dp[i - 1][w]; // Cannot include the item
 }
 }
 }

 // The bottom-right corner contains the maximum profit
 return dp[n][capacity];
 }

 // Main method
 public static void main(String[] args) {
 int[] weights = {10, 20, 30}; // Weights of the items
 int[] values = {60, 100, 120}; // Values of the items
 int capacity = 50; // Maximum capacity of the knapsack

 // Solve the knapsack problem
 }
}

```

```
int maxProfit = knapsack(weights, values, capacity);
System.out.println("Maximum profit: " + maxProfit);
}
}
```

A screenshot of a terminal window with a dark background. The window has a title bar at the top with a close button (X) and several small icons. The terminal prompt is "user@user:~". The user has run the following commands:

```
user@user:~$ javac p.java
user@user:~$ java p
220
user@user:~$ |
```

Below the terminal window, there is a red handwritten mark.



### Assignment No. 5

\* Title :- Write a program for analysis of quick sort by using deterministic and randomized variant.

\* Objective:- To analyze time and space complexity of quick sort by using deterministic and randomized variant.

\* Theory :-

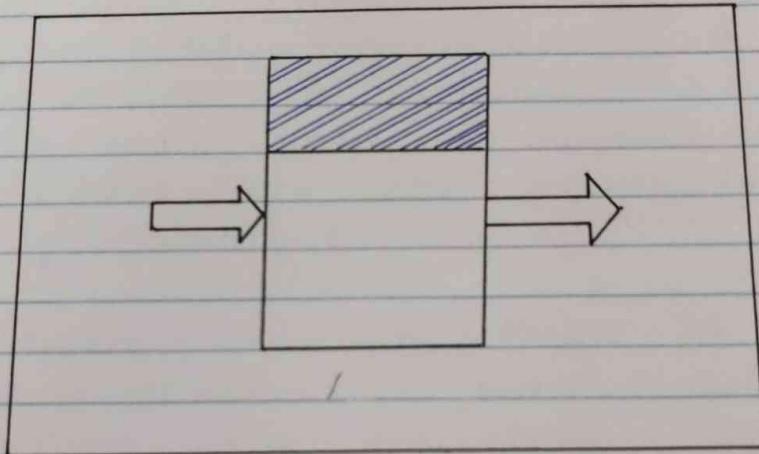
» What is a Randomized Algorithm?

- An algorithm that uses random number to decide what to do next anywhere in its logic is called Randomized Algorithm.
- For example, in Randomized Quick Sort, we use random number to pick the next pivot (or we randomly shuffle the array).
- Typically, this randomness is used to reduce time complexity or space



space complexity in other standard algorithms.

- Randomized algorithm for a problem is usually simpler and more efficient than its deterministic counterpart.
- The output or the running time are functions of the input and random bits chosen.



### \* Types of Randomized Algorithms:-

#### 1. Las Vegas Algorithms:

- These algorithm always produce correct or optimum result.



- Time complexity of these algorithms is based on a random value and time complexity is evaluated as expected value.
- For example, Randomized Quicksort always sorts an input array and expected worst case time complexity of Quicksort is  $O(n \log n)$ .
- A Las Vegas algorithm fails with some probability, but we can tell when it fails. In particular, we can run it again until it succeeds, which means that we can eventually succeed with probability 1.
- Alternatively, we can think of a Las Vegas algorithm as an algorithm that runs for an unpredictable amount of time but always succeeds.

## 2. Monte Carlo Algorithms:

- Produce correct or optimum result with some probability.
- These algorithms have deterministic running time and it is generally easier



to find out worst case time complexity.

- For example Karger's Algorithm produces minimum cut with probability greater than or equal to  $1/n^2$  ( $n$  is number of vertices) and has worst case time complexity as  $O(E)$ .
- A Monte Carlo algorithm fails with some probability, but we can't tell when it fails.
- The polynomial equality-testing algorithm is an example of a Monte Carlo algorithm.

#### \* Randomized Quick Sort Algorithm:

- Randomized algorithm have huge applications in cryptography.
- Load Balancing:
- Number-Theoretic Applications : Primality Testing.
- Data Structure : Hashing, sorting, Searching.



### Analysis of Randomized Quick Sort:

The running time of quicksort depends mostly on the number of comparisons performed in all calls to the Randomized - Partition routine. Let  $X$  denotes the random variable counting the number of comparisons in all to Randomized - Partition.

Let  $z_i$  denote the  $i$ -th smallest element of  $A[1..n]$ ,  
Thus  $A[1..n]$  sorted is  $\langle z_1, z_2, \dots, z_n \rangle$ .

Let  $Z_{ij} = [z_i, \dots, z_j]$  denote that the set of elements between  $z_i$  and  $z_j$ , including these elements.

$X_{ij} = 1(z_i, \dots, z_j)$  denote the set of elements between  $z_i$  and  $z_j$ , including these elements.

$X_{ij} = 1(z_i \text{ is compared to } z_j)$ .

Thus,  $X_{ij}$  is an indicator random variable for the event that the  $i$ -th smallest and the  $j$ -th smallest elements of  $A$  are compared in an execution of quicksort.



### \* Number of Comparisons :-

Since each pair of elements is compared at most once by quicksort, the number  $X$  of comparisons is given by

$$X = \sum_{i=1}^{n-1} \sum_{j=i+1}^n X_{ij}$$

Therefore, the expected number of comparisons is

$$E[X] = \sum_{i=1}^{n-1} \sum_{j=i+1}^n E[X_{ij}] = \sum_{i=1}^{n-1} \sum_{j=i+1}^n \Pr[z_i \text{ is compared to } z_j]$$

### Expected Number of Comparisons.

$$E[X] = \sum_{i=1}^{n-1} \sum_{j=i+1}^n \frac{2}{j-i+1}$$

$$= \sum_{i=1}^{n-1} \sum_{k=1}^{n-1} \frac{2}{k+1}$$

$$< \sum_{i=1}^{n-1} \sum_{k=1}^n \frac{2}{k}$$



$$= \sum_{i=1}^{n-1} O(\log n)$$

$$= O(n \log n)$$

It follows the expected running time to Randomized - Quicksort is  $O(n \log n)$ .

It is unlikely that this algorithm will choose a terribly unbalanced partition each time, so the performance is very good almost all the time.

#### \* Conclusion :-

In this way we have explored concept of quick sort by using deterministic and randomized variant.

```
import java.util.Random;

public class QuickSortAnalysis {
 // Deterministic QuickSort
 public static void deterministicQuickSort(int[] arr, int low, int high) {
 if (low < high) {
 int pi = partition(arr, low, high);
 deterministicQuickSort(arr, low, pi - 1);
 deterministicQuickSort(arr, pi + 1, high);
 }
 }

 // Randomized QuickSort
 public static void randomizedQuickSort(int[] arr, int low, int high) {
 if (low < high) {
 int pi = randomizedPartition(arr, low, high);
 randomizedQuickSort(arr, low, pi - 1);
 randomizedQuickSort(arr, pi + 1, high);
 }
 }

 // Partition method used in deterministic QuickSort
 private static int partition(int[] arr, int low, int high) {
 int pivot = arr[high]; // Pivot element
 int i = low - 1; // Index of smaller element

 for (int j = low; j < high; j++) {
 if (arr[j] < pivot) {
 i++;
 swap(arr, i, j);
 }
 }
 }
}
```

```
 }

 swap(arr, i + 1, high);

 return i + 1;
 }

 // Randomized partition for Randomized QuickSort
 private static int randomizedPartition(int[] arr, int low, int high) {

 Random rand = new Random();

 int randomIndex = low + rand.nextInt(high - low + 1);

 swap(arr, randomIndex, high); // Move random element to the end

 return partition(arr, low, high);
 }

 // Utility method to swap elements in the array
 private static void swap(int[] arr, int i, int j) {

 int temp = arr[i];

 arr[i] = arr[j];

 arr[j] = temp;
 }

 // Utility method to generate a random array
 public static int[] generateRandomArray(int size, int range) {

 Random rand = new Random();

 int[] arr = new int[size];

 for (int i = 0; i < size; i++) {

 arr[i] = rand.nextInt(range);
 }

 return arr;
 }

 // Method to copy an array (used to ensure same input for both variants)
```

```
public static int[] copyArray(int[] arr) {
 int[] newArr = new int[arr.length];
 System.arraycopy(arr, 0, newArr, 0, arr.length);
 return newArr;
}

// Main method to analyze the performance
public static void main(String[] args) {
 int size = 10000; // Size of the array
 int range = 10000; // Range of random numbers

 // Generate a random array for testing
 int[] originalArray = generateRandomArray(size, range);

 // Test Deterministic QuickSort
 int[] arr1 = copyArray(originalArray);
 long startTime = System.nanoTime();
 deterministicQuickSort(arr1, 0, arr1.length - 1);
 long endTime = System.nanoTime();
 System.out.println("Deterministic QuickSort time: " + (endTime - startTime) + " ns");

 // Test Randomized QuickSort
 int[] arr2 = copyArray(originalArray);
 startTime = System.nanoTime();
 randomizedQuickSort(arr2, 0, arr2.length - 1);
 endTime = System.nanoTime();
 System.out.println("Randomized QuickSort time: " + (endTime - startTime) + " ns");
}
```

```
user@user:~$ javac p.java
user@user:~$ java p
Deterministic QuickSort time: 4387768 ns
Randomized QuickSort time: 7189222 ns
user@user:~$ |
```



## Assignment No. 6 Mini Project

### \* Title :-

Implementation of Naive String Matching and Rabin-Karp Algorithm for String Matching.

### \* Objective :-

- To implement the Naive string matching algorithm and Rabin-Karp algorithm for string matching.
- To observe the difference in the working of both algorithms for the same input.

### \* Theory :-

#### » Naive String Matching Algorithm :-

The Naive string matching algorithm is a simple string matching algorithm that checks for a pattern in a text by sliding the pattern over the text one character at a time. It has a time complexity



of  $O((n-m+1) * m)$ , where  $n$  is the length of the text and  $m$  is the length of the pattern.

### » Rabin - Karp Algorithm :-

The Rabin - Karp algorithm is a string searching algorithm that uses hashing to find any one of a set of pattern strings in a text. It has an average time complexity of  $O(n+m)$ , making it more efficient than the Naive algorithm for large texts.

### \* Implementation :-

#### » Naive String Matching Algorithm:

```
def naive_string_matching(text, pattern):
 n = len(text)
 m = len(pattern)
 for i in range(n-m+1):
 match = True
 for j in range(m):
 if text[i+j] != pattern[j]:
```



```
match = False
break
if match
return i
return -1.
```

### » Rabin - Karp Algorithm:

```
def rabin_karp(text, pattern):
 n = len(text)
 m = len(pattern)
 d = 256
 q = 101
 pattern_hash = 0
 text_hash = 0
 h = 1

 for _ in range(m-1):
 h = (h * d) % q

 for i in range(m):
 pattern_hash = (d * pattern_hash +
 ord(pattern[i])) % q
 text_hash = (d * text_hash +
 ord(text[i])) % q
 for i in range(n-m+1):
 if pattern_hash == text_hash
 match = True
 for j in range(m):
 if text[i+j] != pattern[j]:
 match = False
 break
 if match:
 return i
 return -1
```



if  $\text{text}[i + j] \neq \text{pattern}[j]$ :  
    match = False  
    break

if match  
return i

if  $i < n - m$ :  
    text\_hash = (d + (text\_hash - ord(text[i])))  
    if text\_hash <= hash < 0: text  
        hash < 0  
    text\_human += a

return -1.

#### \* Conclusion:

We have successfully demonstrated the Naive String matching algorithm and the Rabin-Karp algorithm for String matching.

# mini-projet-group-b-1

October 15, 2024

```
[36]: #Name: Shriharsh J. Deshmukh
#Roll No. 71 Div. 'A'
```

```
[37]: # Import necessary libraries
import pandas as pd
import numpy as np
import matplotlib.pyplot as plt
from sklearn.model_selection import train_test_split
from sklearn.linear_model import LinearRegression
from sklearn.metrics import mean_squared_error
```

```
[38]: # Load the dataset
df = pd.read_csv('Stock_data.csv')
```

```
[39]: # Perform EDA
print(df.head())
print(df.info())
print(df.describe())
```

|   | Date       | Open   | High   | Low    | Last   | Close  | Total Trade | Quantity | \ |
|---|------------|--------|--------|--------|--------|--------|-------------|----------|---|
| 0 | 2018-09-28 | 234.05 | 235.95 | 230.20 | 233.50 | 233.75 |             | 3069914  |   |
| 1 | 2018-09-27 | 234.55 | 236.80 | 231.10 | 233.80 | 233.25 |             | 5082859  |   |
| 2 | 2018-09-26 | 240.00 | 240.00 | 232.50 | 235.00 | 234.25 |             | 2240909  |   |
| 3 | 2018-09-25 | 233.30 | 236.75 | 232.00 | 236.25 | 236.10 |             | 2349368  |   |
| 4 | 2018-09-24 | 233.55 | 239.20 | 230.75 | 234.00 | 233.30 |             | 3423509  |   |

Turnover (Lacs)

|   |          |
|---|----------|
| 0 | 7162.35  |
| 1 | 11859.95 |
| 2 | 5248.60  |
| 3 | 5503.90  |
| 4 | 7999.55  |

```
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 2035 entries, 0 to 2034
Data columns (total 8 columns):
 # Column Non-Null Count Dtype
 --- --
 0 Date 2035 non-null object
```

```

1 Open 2035 non-null float64
2 High 2035 non-null float64
3 Low 2035 non-null float64
4 Last 2035 non-null float64
5 Close 2035 non-null float64
6 Total Trade Quantity 2035 non-null int64
7 Turnover (Lacs) 2035 non-null float64
dtypes: float64(6), int64(1), object(1)
memory usage: 127.3+ KB
None
 Open High Low Last Close \
count 2035.000000 2035.000000 2035.000000 2035.000000 2035.000000
mean 149.713735 151.992826 147.293931 149.474251 149.45027
std 48.664509 49.413109 47.931958 48.732570 48.71204
min 81.100000 82.800000 80.000000 81.000000 80.95000
25% 120.025000 122.100000 118.300000 120.075000 120.05000
50% 141.500000 143.400000 139.600000 141.100000 141.25000
75% 157.175000 159.400000 155.150000 156.925000 156.90000
max 327.700000 328.750000 321.650000 325.950000 325.75000
Total Trade Quantity Turnover (Lacs)
count 2.035000e+03 2035.000000
mean 2.335681e+06 3899.980565
std 2.091778e+06 4570.767877
min 3.961000e+04 37.040000
25% 1.146444e+06 1427.460000
50% 1.783456e+06 2512.030000
75% 2.813594e+06 4539.015000
max 2.919102e+07 55755.080000

```

```
[40]: # Plot the stock prices over time
plt.figure(figsize=(10,6))
plt.plot(df['Date'], df['Close'])
plt.title('Stock Prices Over Time')
plt.xlabel('Date')
plt.ylabel('Close Price')
plt.show()
```



```
[41]: # Prepare the data for time series analysis
df['Date'] = pd.to_datetime(df['Date'])
df.set_index('Date', inplace=True)

[42]: # Split the data into training and testing sets
train_data, test_data = train_test_split(df, test_size=0.2, random_state=42)

[43]: # Develop the predictive model
X_train = train_data.drop('Close', axis=1)
y_train = train_data['Close']
X_test = test_data.drop('Close', axis=1)
y_test = test_data['Close']

model = LinearRegression()
model.fit(X_train, y_train)

[43]: LinearRegression()

[44]: # Make predictions on the test data
predictions = model.predict(X_test)

[45]: # Evaluate the model
mse = mean_squared_error(y_test, predictions)
print(f'Mean Squared Error: {mse:.2f}')
```

Mean Squared Error: 0.16

```
[46]: future_data = pd.DataFrame({
 'Open': [100],
 'High': [120],
 'Low': [80],
 'Last': [110], # Assuming this value based on domain knowledge
 'Total Trade Quantity': [10000], # You need to provide a reasonable value
 'Turnover (Lacs)': [50.5] # Similarly, include a value for turnover
)
```

```
[47]: future_prediction = model.predict(future_data)
print(f'Predicted Stock Price: {future_prediction[0]:.2f}')
```

Predicted Stock Price: 108.71

~~old~~