

Consider a linear transformation $T : \mathbb{R}^2 \rightarrow \mathbb{R}^2$ and the matrix representation of T is \mathbf{M} , where

$$\mathbf{M} = \begin{pmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{pmatrix}.$$

A point $P(x, y)$ on the curve $y = x^2$ is mapped to $P'(5, 0)$ via T . The new coordinates

$$(x', y') = (x \cos \theta - y \sin \theta, x \sin \theta + y \cos \theta)$$

implies the following system of equations

$$x \cos \theta - y \sin \theta = 5$$

$$x \sin \theta + y \cos \theta = 0$$

and as $y = x^2$,

$$x \cos \theta - x^2 \sin \theta = 5$$

$$x \sin \theta + x^2 \cos \theta = 0$$

x must be non-zero. Suppose otherwise, then P would be the origin, and then P' would still be the origin (i.e. P is invariant under T). We have $x = -\tan \theta$, and thus

$$-\sin \theta - \sin \theta \tan^2 \theta = 5.$$

Solving gives $\theta = -1.1314$ radians so $\tan \theta = -2.13$ and note that θ is negative since we are dealing with a clockwise rotation about the origin.