**Problem 1** — Algorithms often have the following properties:

- the steps are stated unambiguously so that there is no question how the algorithm proceeds
- the algorithm is *deterministic* so that repeating the algorithm on the same input produces the same output
- the algorithm is *finite* because it terminates after a finite number of steps have been performed
- the algorithm produces *correct* output for a given input

For the following algorithm, for each property listed above, determine whether the algorithm exhibits this property:

```
unsigned max3(unsigned a, unsigned b, unsigned c)

unsigned result = a;

if (b > result)

result = b;

if (c > result)

result = c;

return result;

}
```

Answer: This algorithm is unambiguous because the syntax for the operations is well-understood. It is deterministic because it always produces the same output for a given input. It is finite because the number of lines of code executed (including the header) is strictly between 3 and 7 inclusive. It is correct because for all possible valid input combinations it does in fact return a value equal to the maximum input value.

**Problem 2** — Repeat problem 1 for the following algorithm. This algorithm empirically checks the correctness of Goldbach's conjecture, which states (in a modern interpretation) that every even number greater than 2 is the sum of two prime numbers. Assume has\_prime\_addends is a valid function that correctly determines whether its argument has two prime addends.

```
bool goldbach()

unsigned value = 4;

bool ok = true;

while (ok)

{

if (!has_prime_addends(value))
```

```
{
            ok = false;
10
         else
11
         {
12
            value += 2;
13
         }
14
       }
15
       return ok;
16
    }
17
```

Answer: This algorithm is unambiguous because the syntax for the operation is well-understood. But it's non-deterministic since it does not produces the same output for a given input, also it is infinite because it will never reached the terminated condition if the given input is bigger than 2. And this algorithm is not correct since it does not produces correct output for a given input.

**Problem 3** — What is the hexadecimal representation of  $724_{10}$ ?

Answer: The first few powers of 16 are:

$$16^0 = 1$$
  
 $16^1 = 16$   
 $16^2 = 256$   
 $16^3 = 4096$ 

Thus we have:

$$724$$

$$-2 \times 256 = 512$$

$$212$$

$$-13 \times 16 = 208$$

$$4$$

$$-4 \times 1 = 2$$

$$0$$

And thus we have  $724_{10} = 2d4_{16}$ .

**Problem 4** — Based on the hexadecimal value found in the previous solution, what is the binary representation of  $724_{10}$ ?

Answer: According to the previous solution, we have the hex value 0x2d4. So we could convert the hex to binary one digit by one digit. So here is a binary to hex table:

0000 = 0	1000 = 8
0001 = 1	1001 = 9
0010 = 2	1010 = a
0011 = 3	1011 = b
0100 = 4	1100 = c
0101 = 5	1101 = d
0110 = 6	1110 = e
0111 = 7	1111 = f

Since  $2_{16} = 0010$ ,  $d_{16} = 1101$  and  $4_{16} = 0100$ . So the binary of  $724_{10} = 0010$  1101 0100.

## **Problem 5** — What is the decimal representation of 0x2b3a?

Answer: According to the table above, we could know that b in decimal is 11 and a in decimal is 10. So we have the following

$$2b3a_{16} = 2 \cdot 16^{3} + 11 \cdot 16^{2} + 3 \cdot 16^{1} + 10 \cdot 16^{0}$$

$$= 2 \cdot 4096 + 11 \cdot 256 + 3 \cdot 16 + 10$$

$$= 8192 + 2816 + 48 + 10$$

$$= 11066$$

So, the decimal representation of 0x2b3a is 11066.