Collected papers of

Lord Soumadeep Ghosh

Volume 8

# The Ghosh staircase function

### Soumadeep Ghosh

Kolkata, India

#### Abstract

In this paper, I describe the Ghosh staircase function. The paper ends with "The End"

### Introduction

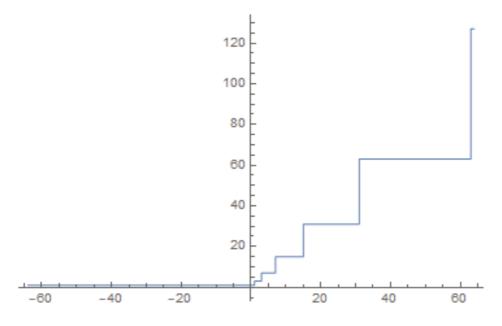
The Ghosh staircase function is the alternative holy grail of functions. In this paper, I describe the Ghosh staircase function.

### The Ghosh staircase function

The Ghosh staircase function is

$$G(x) = \begin{cases} 1 & x \le 1 \\ 2G(\frac{x-1}{2}) + 1 & x > 1 \end{cases}$$

### Plot of the Ghosh staircase function



# The Ghosh pulse function

### Soumadeep Ghosh

Kolkata, India

#### Abstract

In this paper, I describe the Ghosh pulse function. The paper ends with "The End"

### Introduction

The Ghosh pulse function is a useful alternative to the sinc function. In this paper, I describe the Ghosh pulse function.

### The Ghosh pulse function

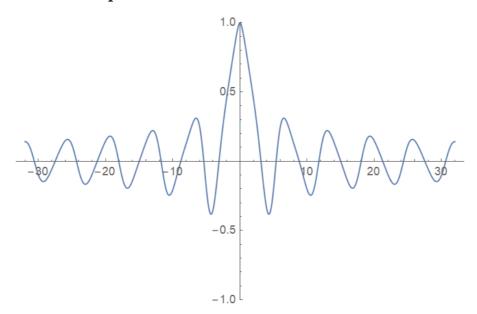
The Ghosh pulse function is

$$P(x) = J_{J_2(|x|)}(|x|)$$

where

 $J_n(x)$  is the Bessel function of the first kind.

### Plot of the Ghosh pulse function



# The Modified V probability density function

#### Soumadeep Ghosh

Kolkata, India

#### Abstract

In this paper, I describe the Modified V probability density function which is never 1. The paper ends with "The  $\operatorname{End}$ "

### Introduction

It is often useful to have a V-shaped probability density function that is never 1. In this paper, I describe the Modified V probability density function which is never 1.

### The Modified V probability density function

The Modified V probability density function is

$$f(x) = \begin{cases} \frac{5(x^2 - 128)(x^2(x^2 - 128)^2 - 8388608)}{5342576161}|x| & |x| \le 1\\ 0 & |x| > 1 \end{cases}$$

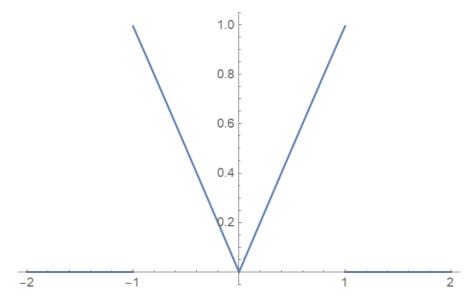
Then

1.  $0 \le f(x) < 1$  for all real x.

$$2. \int_{-\infty}^{\infty} f(x) = 1$$

Thus f(x) is a probability density function which is never 1 for any real x.

### Plot of the Modified V probability density function



# The Ridge probability density function

### Soumadeep Ghosh

Kolkata, India

#### Abstract

In this paper, I describe the Ridge probability density function which is never 1 and also constant for some values. The paper ends with "The End"

### Introduction

It is often useful to have a V-shaped probability density function that is never 1 and also constant for some values. In this paper, I describe the Ridge probability density function which is never 1 and also constant for some values.

### The Ridge probability density function

The Ridge probability density function is

$$f(x) = \frac{8\left(\begin{array}{cc} \left\{ & \min\left(1, \left|\tan\left(\frac{4x}{\pi}\right)\right|\right) & |x| \le 1\\ 0 & |x| > 1 \end{array}\right)}{16 - \pi^2 + 2\pi\log(2)}$$

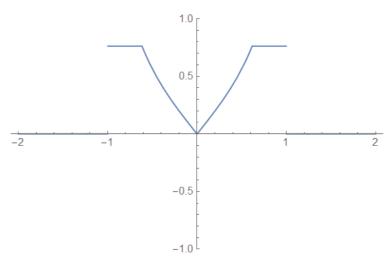
Then

1.  $0 \le f(x) < 1$  for all real x.

$$2. \int_{-\infty}^{\infty} f(x) = 1$$

Thus f(x) is a probability density function which is never 1 for any real x.

### Plot of the Ridge probability density function



# The Generalized Observable Rate Equation and solutions

#### Soumadeep Ghosh

Kolkata, India

#### Abstract

In this paper, I describe the Generalized Observable Rate Equation and solutions. The paper ends with "The End"

#### Introduction

It's a well-known fact that a low interest rate promotes lending and a high interest rate discourages borrowing. Thus, the observable interest rate is somewhere in the middle, neither low nor high. This fact is modeled by the **Generalized Observable Rate Equation (GORE)**. In this paper, I describe the Generalized Observable Rate Equation and solutions.

### The Generalized Observable Rate Equation

The Generalized Observable Rate Equation is

$$\alpha(1 + \frac{r(t)}{t}) + \beta(1 + \frac{\partial r(t)}{\partial t}) + \gamma = 0$$

where

r(t) is interest rate as a function of time  $\alpha$ ,  $\beta$  and  $\gamma$  are constants

### The solution to the Generalized Observable Rate Equation

The solution to the Generalized Observable Rate Equation is

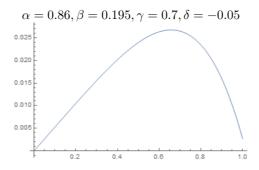
$$r(t) = \delta t^{\alpha/\beta} - \frac{t(-\alpha + \beta + \gamma)}{\beta(1 - \frac{\alpha}{\beta})}$$

where

 $\delta$  is a constant of integration

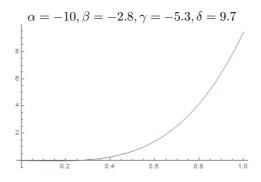
# A particular solution to the Generalized Observable Rate Equation with moderately low interest rate

A particular solution to the Generalized Observable Rate Equation with moderately low interest rate is given by



# A particular solution to the Generalized Observable Rate Equation with moderately high interest rate

A particular solution to the Generalized Observable Rate Equation with moderately high interest rate is given by



### The Airy Peak probability density function

#### Soumadeep Ghosh

#### Kolkata, India

#### Abstract

In this paper, I describe the Airy Peak probability density function which is never 1. The paper ends with "The End"

### Introduction

It is often useful to have an inverted V-shaped probability density function that is never 1. In this paper, I describe the Airy Peak probability density function which is never 1.

### The Airy Peak probability density function

The Airy Peak probability density function is

$$f(x) = \begin{cases} \frac{Ai(|x|)}{\frac{\Gamma(-\frac{1}{3}) \,_{1}F_{2}(\frac{2}{3}; \frac{4}{3}, \frac{5}{3}; \frac{1}{9})}{2 \,_{2} \,_{3}^{5/6}\pi} - \frac{2 \,_{3}^{3} \,_{1}F_{2}(\frac{1}{3}; \frac{2}{3}, \frac{4}{3}; \frac{1}{9})}{\Gamma(-\frac{1}{3})} \end{cases} - 1 \le x \le 1$$

where

Ai(x) is the Airy function

 $_{p}F_{q}(a;b;x)$  is the generalized hypergeometric function

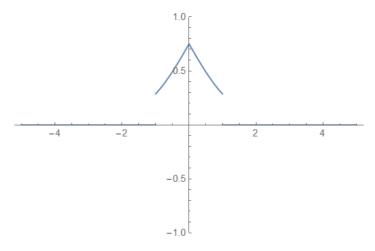
Ther

1.  $0 \le f(x) < 1$  for all real x.

$$2. \int_{-\infty}^{\infty} f(x) = 1$$

Thus f(x) is a probability density function which is never 1 for any real x.

### Plot of the Airy Peak probability density function



# The Airy Valley probability density function

### Soumadeep Ghosh

Kolkata, India

#### Abstract

In this paper, I describe the Airy Valley probability density function which is never 1. The paper ends with "The  $\operatorname{End}$ "

### Introduction

It is often useful to have an alternative V-shaped probability density function that is never 1. In this paper, I describe the Airy Valley probability density function which is never 1.

### The Airy Valley probability density function

The Airy Valley probability density function is

$$f(x) = \begin{cases} \frac{Bi(|x|)}{-\frac{2 \cdot 3^{5/6} \cdot F_2(\frac{1}{3}; \frac{2}{3}, \frac{4}{3}; \frac{1}{9})}{\Gamma(-\frac{1}{3})} - \frac{\Gamma(-\frac{1}{3}) \cdot F_2(\frac{2}{3}; \frac{4}{3}, \frac{5}{3}; \frac{1}{9})}{2 \sqrt[3]{3\pi}} \\ 0 & x < -1 \lor x > 1 \end{cases}$$

where

Bi(x) is the Airy function

 $_{p}F_{q}(a;b;x)$  is the generalized hypergeometric function

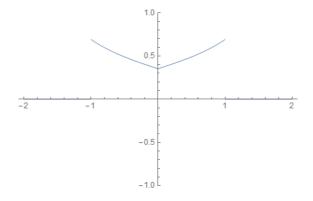
Then

1.  $0 \le f(x) < 1$  for all real x.

$$2. \int_{-\infty}^{\infty} f(x) = 1$$

Thus f(x) is a probability density function which is never 1 for any real x.

### Plot of the Airy Valley probability density function



### The Alternative Ridge probability density function

### Soumadeep Ghosh

#### Kolkata, India

#### Abstract

In this paper, I describe the Alternative Ridge probability density function which is never 1 and also constant for some values. The paper ends with "The End"

### Introduction

It is often useful to have an alternative V-shaped probability density function that is never 1 and also constant for some values. In this paper, I describe the Alternative Ridge probability density function which is never 1 and also constant for some values.

### The Alternative Ridge probability density function

The Alternative Ridge probability density function is

$$f(x) = \begin{cases} \frac{6\min(1,|x|+x^2)}{19-5\sqrt{5}} & -1 \le x \le 1\\ 0 & x < -1 \lor x > 1 \end{cases}$$

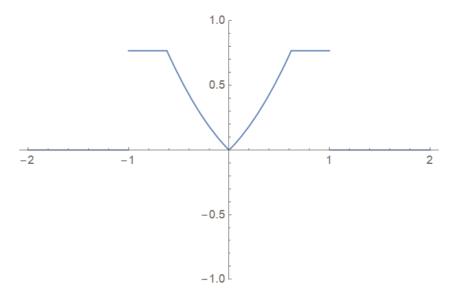
Then

1.  $0 \le f(x) < 1$  for all real x.

$$2. \int_{-\infty}^{\infty} f(x) = 1$$

Thus f(x) is a probability density function which is never 1 for any real x.

### Plot of the Alternative Ridge probability density function



# The Umbrella probability density function

### Soumadeep Ghosh

Kolkata, India

#### Abstract

In this paper, I describe the Umbrella probability density function which is never 1. The paper ends with "The End"

### Introduction

In this paper, I describe the Umbrella probability density function which is never 1.

### The Umbrella probability density function

The Umbrella probability density function is

$$f(x) = \begin{array}{cc} \frac{480}{877} \left(1 - \frac{x^4}{64} - \frac{x^2}{4}\right) & -1 \le x \le 1\\ 0 & x < -1 \lor x > 1 \end{array}$$

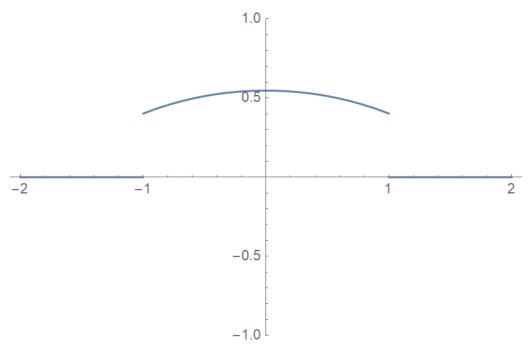
Then

1.  $0 \le f(x) < 1$  for all real x.

$$2. \int_{-\infty}^{\infty} f(x) = 1$$

Thus f(x) is a probability density function which is never 1 for any real x.

# Plot of the Umbrella probability density function



# The Dome probability density function

#### Soumadeep Ghosh

#### Kolkata, India

#### Abstract

In this paper, I describe the Dome probability density function which is never 1. The paper ends with "The End"

### Introduction

In this paper, I describe the Dome probability density function which is never 1.

### The Dome probability density function

The Dome probability density function is

$$f(x) = \frac{2}{3} \max(0, (x+1)(\frac{3}{2} - \frac{9}{8}(x+\frac{1}{3})))$$

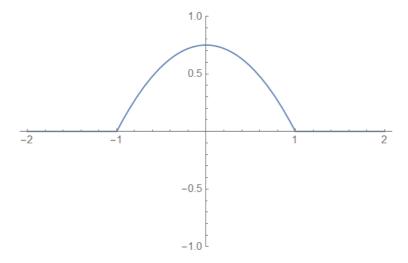
Then

1.  $0 \le f(x) < 1$  for all real x.

$$2. \int_{-\infty}^{\infty} f(x) = 1$$

Thus f(x) is a probability density function which is never 1 for any real x.

### Plot of the Dome probability density function



# The Uniform probability density function

### Soumadeep Ghosh

Kolkata, India

#### Abstract

In this paper, I describe the Uniform probability density function which is never 1. The paper ends with "The  $\operatorname{End}$ "

### Introduction

In this paper, I describe the Uniform probability density function which is never 1.

### The Uniform probability density function

The Uniform probability density function is

$$f(x) = \begin{cases} & \frac{1}{2} & -1 \le x \le 1 \\ & 0 & x < -1 \lor x > 1 \end{cases}$$

Then

1.  $0 \le f(x) < 1$  for all real x.

$$2. \int_{-\infty}^{\infty} f(x) = 1$$

Thus f(x) is a probability density function which is never 1 for any real x.

# Plot of the Uniform probability density function

