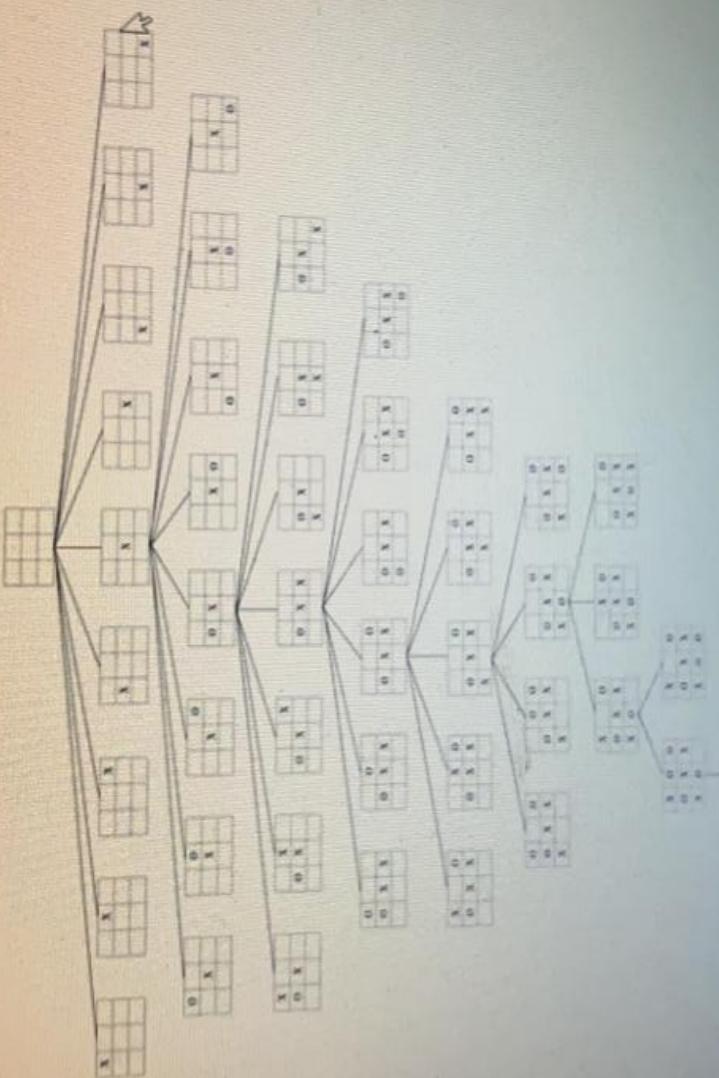


## Approaches to AI

- Pattern recognition: recognition/classification ability
- Image processing/ computer vision: vision aspect
- Natural language processing/speech recognition:  
communication aspect
- Machine learning: generalization
- Knowledge based systems: information storage/ reasoning
- **Search strategies: reasoning/decision making**
- Evolutionary computing: mimics natural evolution
- Neural networks: emulation of human nervous system
- Fuzzy logic: human reasoning process/uncertainty handling
- Expert systems: mimic experts
- Robotics
- Artificial life

VS  
activate Windows.

{Winner - X}



## State space graph

- Keeps track of effects of several alternative sequences of actions; represents all possible states and actions
- A state space is a directed graph  $(V, E)$ ;  $V$ : a set of nodes;  
 $E$ : a set of arcs
  - assumed solutions : nodes of a tree
  - initial state: root of the tree
  - goal state: leaf/ leaves of the tree
- Each arc corresponds to the instance of one of the operators; may have a positive cost associated with it corresponding to the cost of the operator

## 'State Space'



Initial state

Operators



Goal state( $s$ )

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Windows  
to activate Windows

# State space graph

- A search procedure is a strategy for selecting the **order** in which nodes are generated and a given **path** is selected
- A **solution** is a sequence of operators that is associated with a path in a state space from a start node to a goal node
- **State space search** is a process of searching through a state space by making **explicit** a sufficient portion of an **implicit** state space graph to include a goal node
- Initially,  $V = \{S\}$ , when  $S$  is expanded, its successors are generated and those nodes are added to  $V$  and associated arcs are added to  $E$ . This process continues until a goal node is found.

## State space graph

- Node generation is performed by computing the identification/representation code of children nodes from a parent node. Once this is done a child is said to be **generated**.
- A node is **explored** if some of its successors are generated.
- The process of generating all of the children of a parent is known as **expanding** the node.

## Formal Search Problem

4-tuple  $\langle X, S, G, \delta \rangle$

X: set of states

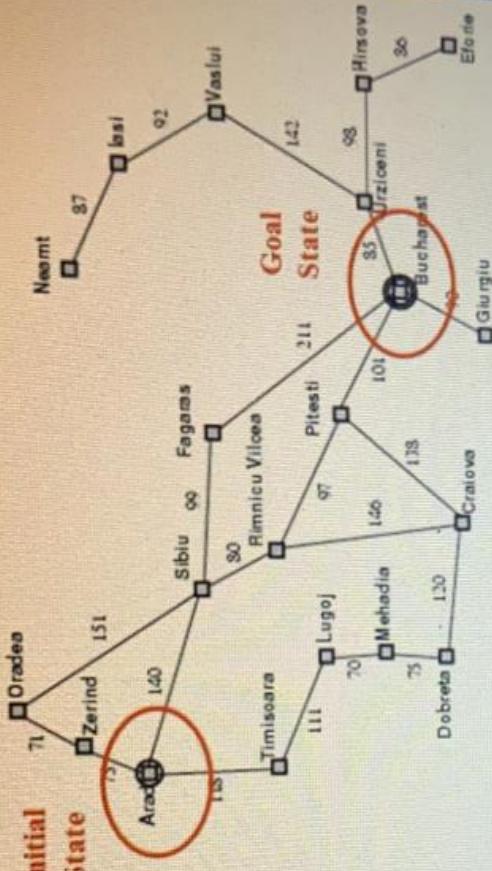
S: start state

G: goal state

$\delta$ : state transition function

# Path Finding Problem

- Formulate goal:
  - be in Bucharest (Romania)
  -
- Formulate problem:
  - **action:** drive between pair of connected cities (direct road)
  - 
  - **state:** be in a city (20 world states)
  -
- Find solution:
  - sequence of cities leading from start to goal state, e.g., **Arad**, **Sibiu**, **Fagaras**, **Bucharest**
  - 
  - **Execution**
    - drive from Arad to Bucharest according to the solution

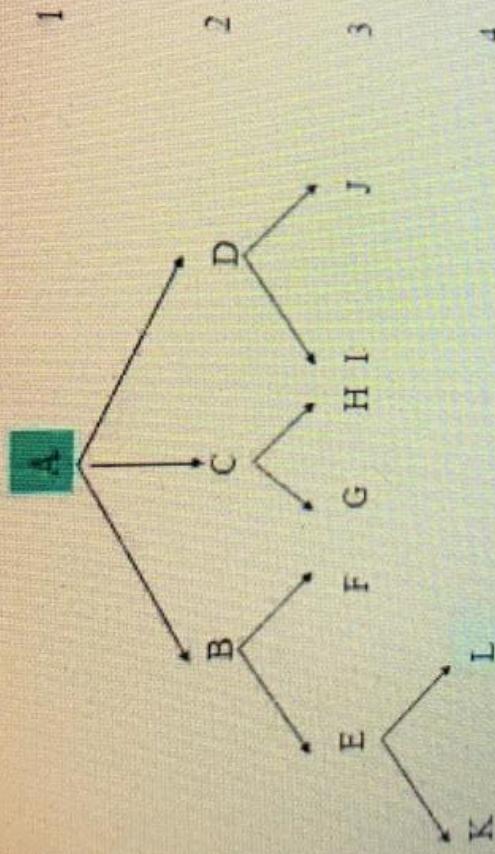


Environment: fully observable (map), deterministic, and the agent knows effects of each action. Is this really the case?

Note: Map is somewhat of a "toy" example. Our real or more states. Far beyond full search, with e.g.  $10^{10}$  actions often still handle those!

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## Example



- A: start state; L: goal state

IBS:

order: iteration 1: A

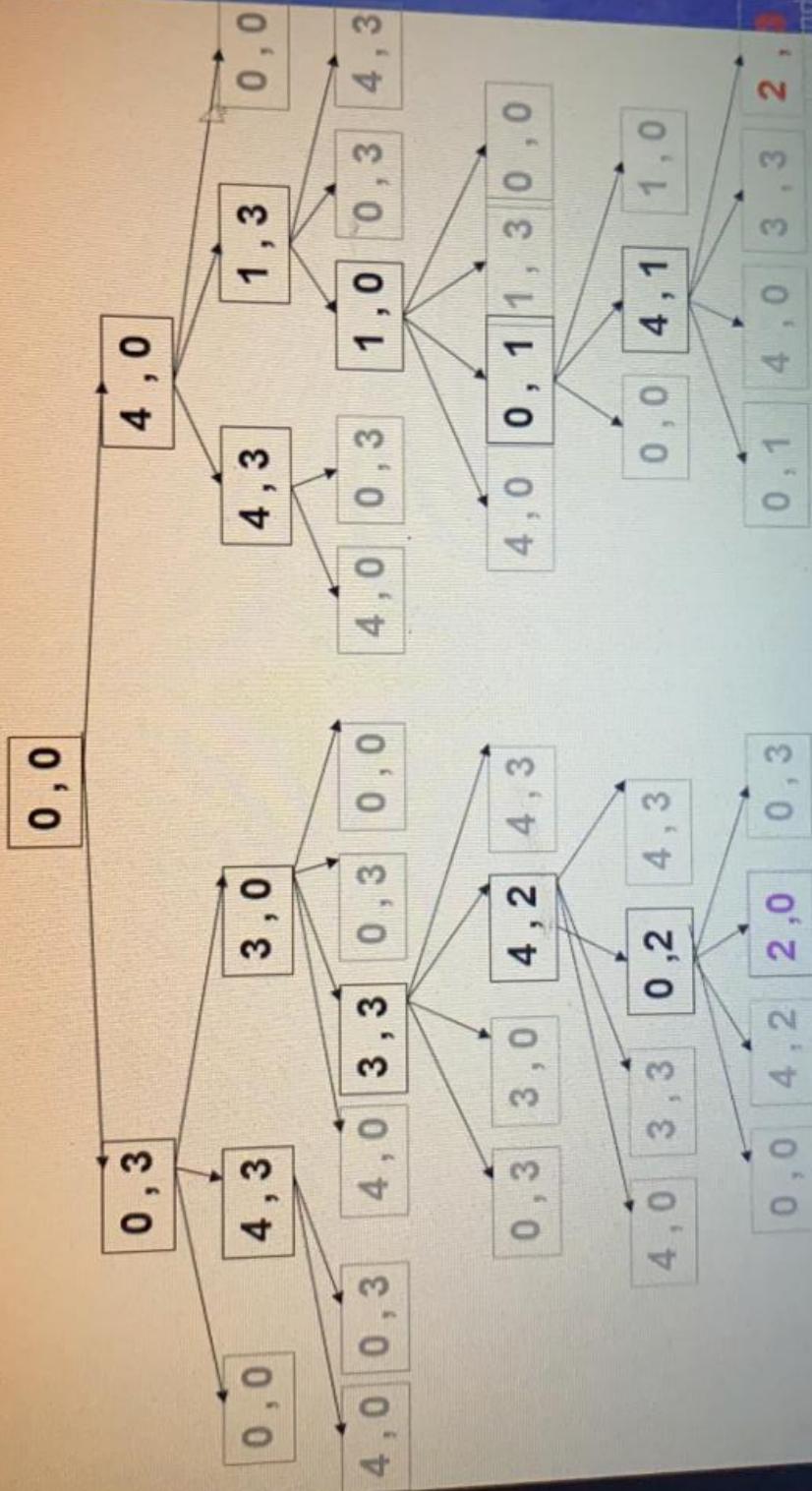
iteration 2: A B E K

iteration 3: A B E K L

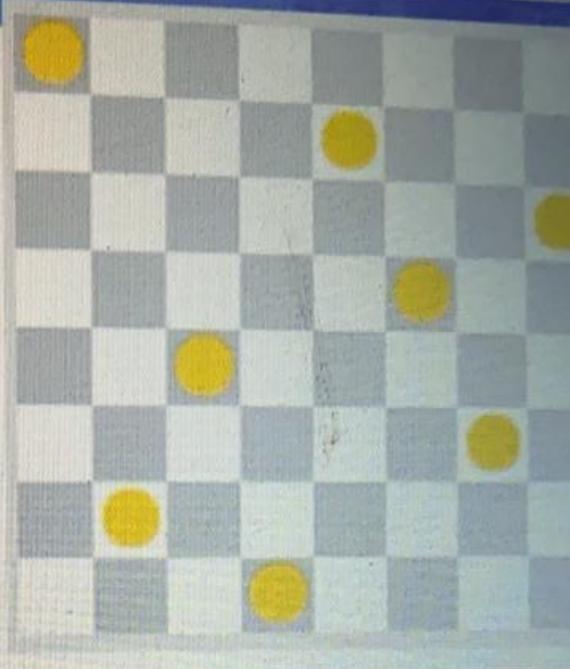
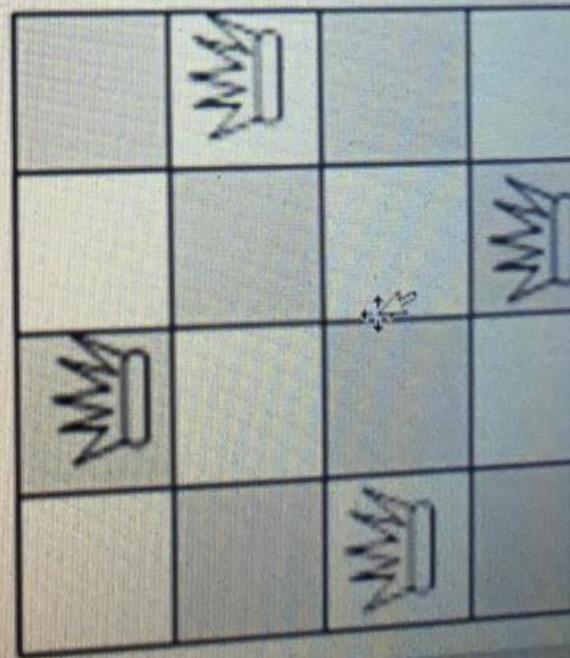
path: A B E L

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## The Water Jugs Problem – Search Tree

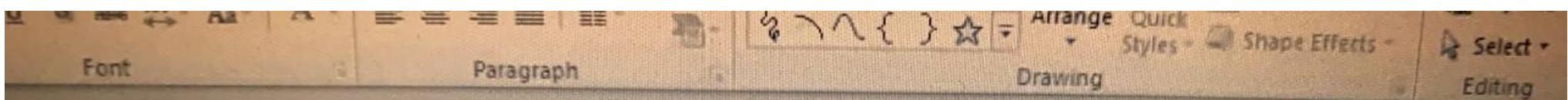


Example:  $n$  queens  
( $n = 4$ ,  $n = 8$ )



## General Graph Searching Algorithm

1. Create a search Tree  $T_r$  consisting solely of the start node  $n_0$ , on an ordered list called OPEN.
2. Create a list called CLOSED that is initially empty
3. If OPEN is empty, exit with failure
4. Select the first node on OPEN, put it in CLOSED. Call this node  $n$
5. If  $n$  is goal node, exit successfully with the solution by tracing a path backward along the arcs in  $T_r$  from  $n$  to  $n_0$ . (Arcs are created in Step 6)
6. Expand node  $n$ , generating a set  $M$  of successors. Install  $M$  as successor of  $n$  in  $T_r$  by creating arcs from  $n$  to each member of  $M$ . Successor will be added to OPEN.
7. Reorder the list OPEN either according to some arbitrary scheme or according to heuristic merit.
8. Go to Step 3



## Evaluating Search Strategies

- Time complexity – How much time is required to find the solution. (#nodes expanded)
- Space complexity – How much space is required to find the solution (maximum size of ‘node-list’ during search)
- Completeness – Is the algorithm guaranteed to find the solution, if one exists?
- Optimality – Does it find an optimal solution (if more than one solutions are present)?

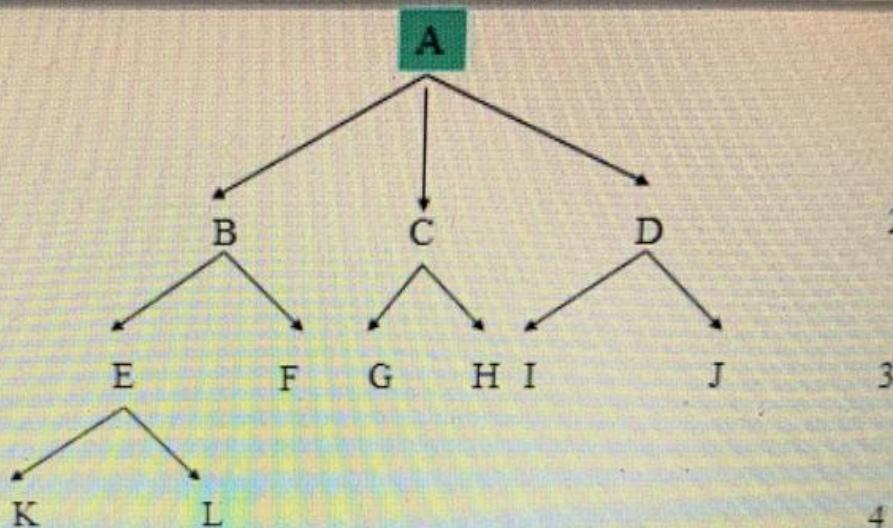
## Example: The Water Jugs Problem

- 2 jugs
  - 4 gallon
  - 3 gallon
- How can you get exactly 2 gallons into the 4 gallon jug?
- Possible operators:
  1. Empty jug
  2. Fill jug from tap
  3. Pour contents from one jug into another



## General Graph Searching Algorithm

1. Create a search Tree  $Tr$ , consisting solely of the start node  $n_0$  on an ordered list called  $OPEN$ .
2. Create a list called  $CLOSED$  that is initially empty
3. If  $OPEN$  is empty, exit with failure
4. Select the first node on  $OPEN$ , put it in  $CLOSED$ . Call this node  $n$
5. If  $n$  is goal node, exit successfully with the solution by tracing a path backward along the arcs in  $Tr$  from  $n$  to  $n_0$  (Arcs are created in Step 6)
6. Expand node  $n$ , generating a set  $M$  of successors. Install  $M$  as successor of  $n$  in  $Tr$  by creating arcs from  $n$  to each member of  $M$ . Successor will be added to  $OPEN$ .
7. Reorder the list  $OPEN$  either according to some arbitrary scheme or according to heuristic merit.
8. Goto Step 3



A: start state; L: goal state

BFS: order: A B C D E F G H I J K L; path: A B E L

DFS: order: A B E K L; path: A B E L

DLS: order: A B E F C G H D I J (considering depth bound as 3)  
no goal found within this bound

Click to add title

*How to execute BFS, DFS, Best first Search then???*

*What do OPEN and CLOSED signify?*

I

*Can we execute other search algorithm also using this framework?*

## Types of search

- Blind/uninformed – no information about goodness of successor state (exhaustive search)

*Breadth first search (BFS), depth first search (DFS),  
depth limited search (DLS), iterative deepening search  
(IDS), iterative broadening search (IBS), bidirectional  
breadth first search (BiBFS), island-driven search*

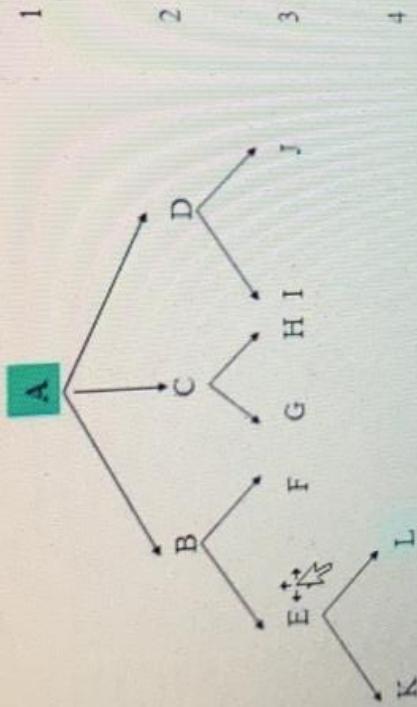
- Uniform cost search (UCS)
- Informed – problem specific information to help focus the search (heuristic search)

*Greedy search, A\* search, iterative deepening A\* (IDA\*)*

## Uninformed search

- **BFS :**
  - ✓ Expands all nodes at depth  $i$  before expanding those at depth  $i+1$
  - ✓ Complete, optimal, time  $\sim O(b^d)$ , space  $\sim O(b^d)$  ( $b$ -branching factor,  $d$  depth of the tree)
- **DFS :**
  - ✓ Generates successors of a node just one at a time; follow one branch, pursue as deep as possible before trying alternatives.
  - ✓ If at dead end, back-up and expand the deepest nodes visited (prune repeated states)
  - ✓ Not complete, not optimal, time  $\sim O(b^d)$ , space  $\sim O(bd)$

## Example



A: start state; L: goal state

BFS: order: A B C D E F G H I J K L; path: A B E L

DFS: order: A B E K L; path: A B E L

DLS: order: A B E F C G H D I J (considering depth bound as 3)  
no goal found within this bound

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## Uninformed Search (contd.)

- **DLS :**
  - to prevent search process running away towards nodes of unbounded depth from start node, a depth bound (say,  $l$ ) is used; no successor is generated whose depth is greater than depth bound  $l$
  - complete, not optimal, time  $\sim O(b^l)$ , space  $\sim O(bl)$
  - assumes that a goal node will be found out within depth  $l$

## Click to add title

- Prove 3 is int
- We know 0 is an int
- $\text{Succ}(\text{int}) = \text{int}$
- $\text{Pred}(\text{int}) = \text{int}$

- 3
- 2
- 1
- 0
- ...
- 5
- 4
- 3
- 2
- 1

## Breadth-First vs. Depth-First search

- Depth-first
  - requires less memory ( $O(bd)$ )
  - may find a solution without searching much of the search space
- Breadth-first
  - will not get trapped exploring a blind alley
  - guaranteed to find solution (if one exists)
  - will find minimal solution (if more than one exist)

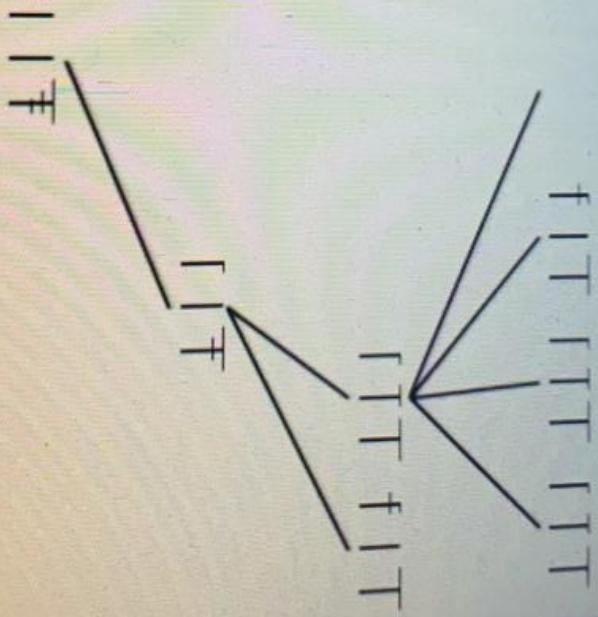
*bfs is computationally expensive than dfs by a factor of  $(I+1)b$*

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## The Towers of Hanoi: DFS



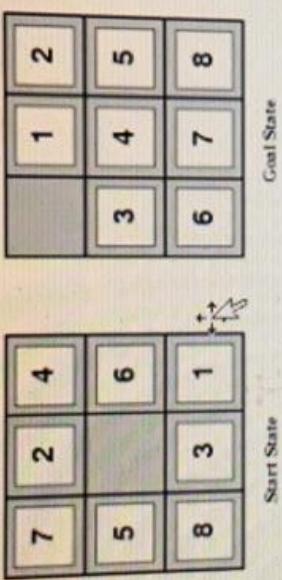
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## Example: The 8-puzzle



- states?
- actions?
- goal test?
- path cost?

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Design English (U.S.)

## Uninformed search (contd.)

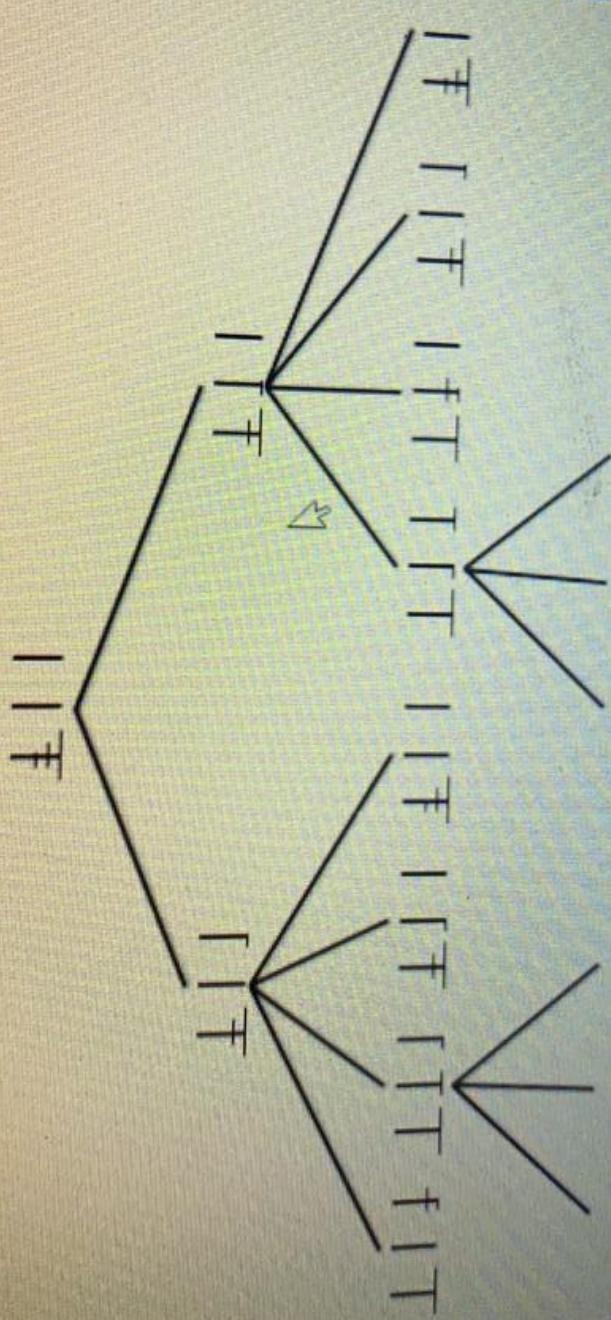
### IDS :

- Successive DFS are conducted, each with depth bound increasing by 1 until a goal node is found
- Complete, optimal, time  $\sim O(b^d)$ , space  $\sim O(bd)$
- Used if search space is deep
- Optimal blind search procedure

### BFS :

- Performs DFS on subgraphs of breadth1, breadth2, ... and so on until a goal node is found
- Complete, not optimal, time  $\sim O(c^d)$ , space  $\sim O(c^d)$       c: breadth
- Used if search space is wide, many goals

## The Towers of Hanoi: BFS



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Text

Symbols

Media

Click to add title

- Bfs:  $(b^{(d+1)} + b^{d+b-3})^{\lceil \frac{2(b-1) \rceil} \rceil}$

## III Time Complexity

- At depth  $j$ , total nodes =  $(b^{(j+1)-1})(b-1)$
- This goes from  $j = 0$  to  $j = d-1$   
$$= (b^{(d+1)-bd-b+d})(b-1)^2$$
  
.....

$$(b^{(d+2)} + b^{(d+1)} + b^2)d + b^2 - 4bd - 5b + 3d + 2)(2^*(b-1)^2)$$

$$\begin{aligned} & (b^{(d+2)} + b^{(d+1)})(2^*(b-1)^2) \\ \text{ID: } & (b+1)^2 b^2 (d+1) (2^*(b-1)^2) \\ \text{DFS: } & b^2 (d+1) 2^*(b-1) \\ \text{ID: } & \frac{\text{dfs}}{\text{time}} = (b-1)(b-1) \end{aligned}$$

## Uninformed search (contd.)

### BiBFS

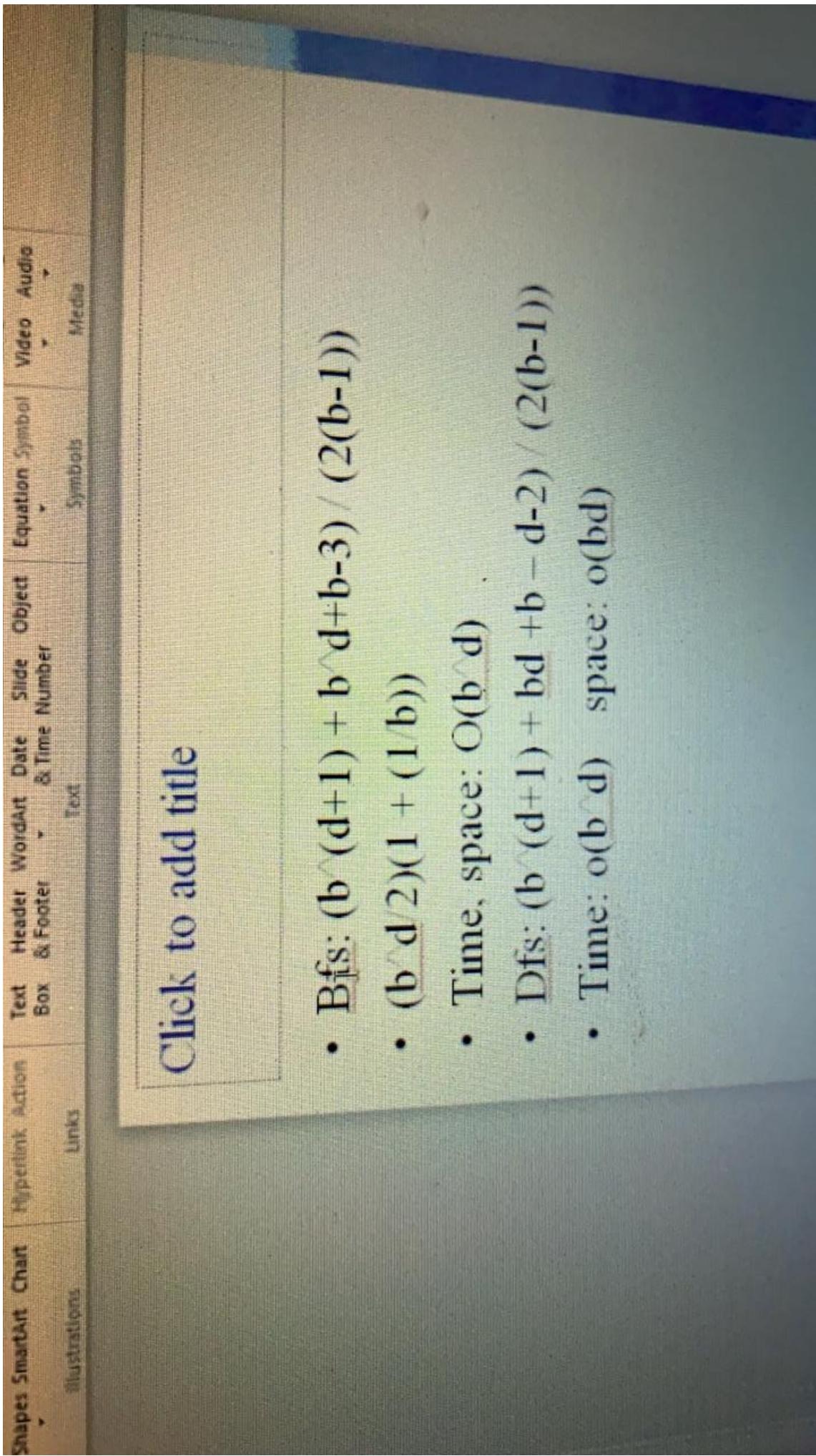
- Search proceeds simultaneously in two directions; both forward from a initial state and backward from a goal state; terminated when the two meet
- Used when S and G configurations are known and operators can be used in reverse manner e.g., 8-puzzle
- Complete, optimal; time:  $O(2b^{d/2})$ ; space:  $O(b^{d/2})$

### Island-Driven Search

- A series of intermediate goals (islands) is identified between start and goal states

$$S \rightarrow I_1 \rightarrow I_2 \rightarrow I_3 \rightarrow \dots \rightarrow I_m \rightarrow G$$

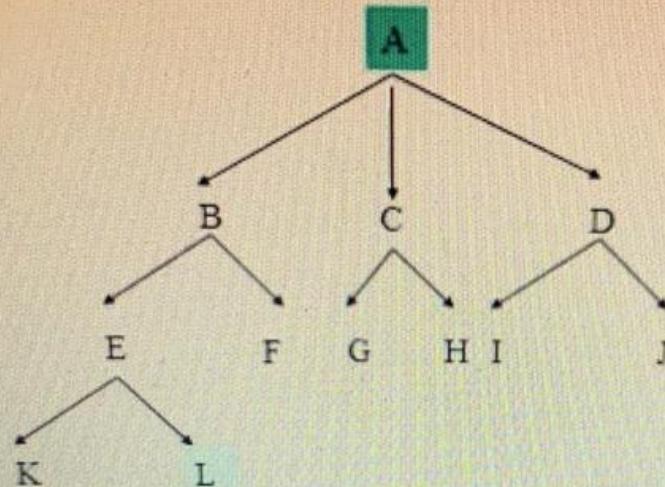
- One large search problem is equivalent to m small search problems
  - time:  $O(mb^{d/m}) \ll b^d$  if islands are evenly spaced



## Uniform Cost Search

- Variant of BFS in which nodes are expanded outward from the start node along the contours of equal cost rather than along the contours of equal depth
- Like Dijkstra's shortest path algorithm
- UCS reduces to BFS if all arc costs are identical
- Complete, optimal, time  $\sim O(b^d)$ , space  $\sim O(b^d)$

## Example



1

2

3

4

- A: start state; L: goal state

IDS:

order: iteration 1: A

iteration 2: A B C D

iteration 3: A B E F C G H D I J

iteration 4: A B E K L

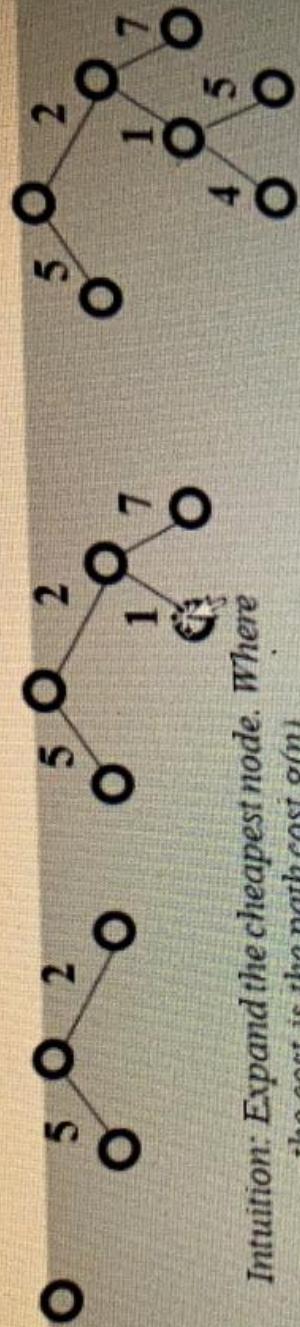
path: A B E L

## Informed Search

- Add domain specific information to select the path
- Controls/guides search processes
  - Heuristic function ( $h$ ) estimates the cost of reaching a goal node from the present state in the search space, small values of  $h \rightarrow$  best node
  - A **heuristic** is a method that might not always find the best solution but is guaranteed to find a **good solution in reasonable time**
- By sacrificing completeness it increases efficiency
  - e.g., 8-puzzle:
    - # tiles misplaced
    - Manhattan distance

# Uniform Cost Search

Enqueue nodes in order of cost



*Intuition: Expand the cheapest node. Where the cost is the path cost  $g(n)$*

**BCSE Third Year Second Semester 2021**

**Class Test 1**

**Artificial Intelligence**

**Full Marks 30**

**Answer all questions. Each question carries 3 marks.**

**State whether the following statements are True or False along with proper explanation / theoretical proof.**

1. Turing Test is a one-sided test.
2. Higher time complexity in finding a solution indicates that the solution thus found will be optimal.
3. "Order" of the nodes visited using any search algorithm is only necessary to find out the "path" of the solution.
4. Two lists, OPEN and CLOSED, are necessary for General Graph Search Algorithm.
5. The average time complexity of any search algorithm is exponential in nature.
6. In certain scenario Iterative Broadening search algorithm can outperform Iterative Deepening search.
7. Bidirectional search strategy is applicable to all sorts of problems.
8. When the temperature tends to infinity, Simulated Annealing algorithm boils down to "random" search
9. Genetic algorithm with population size equal to one is a "random" search algorithm
10. Genetic Algorithm without mutation operator may lead to premature convergence.

**Time: 1 hour**

## Heuristics for 8-puzzle II: Manhattan distance

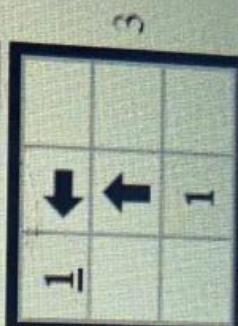
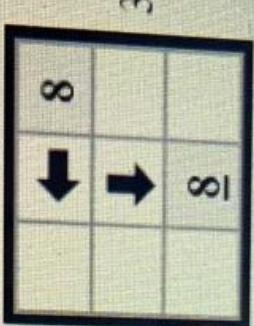
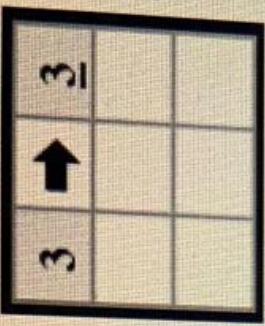
Current State	3	2	8				
	4	5	6				
	7	1					

Distance (not including the blank)

The Manhattan

Distance (not including the blank)

Goal State	1	2	3				
	4	5	6				
	7	8					

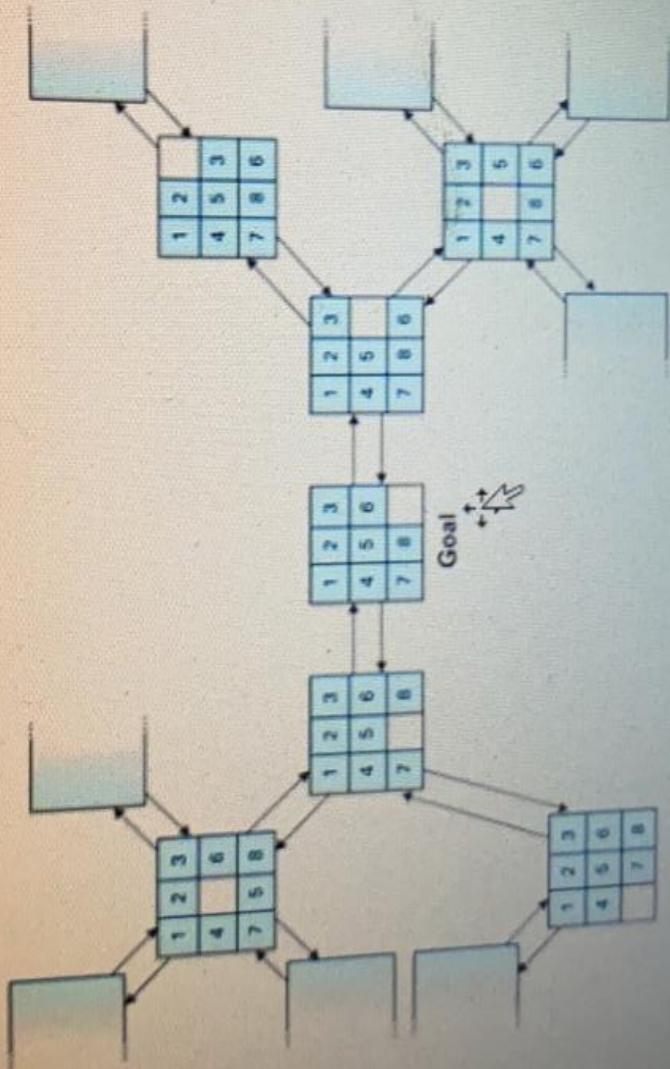


Total 8

In this case, only the "3", "8" and "1" tiles are misplaced, by 2, 3, and 3 squares respectively, so the heuristic function evaluates to 8.

Notation:  $h(n)$        $h(\text{current state}) = 8$

## A small portion of the eight-puzzle's state graph

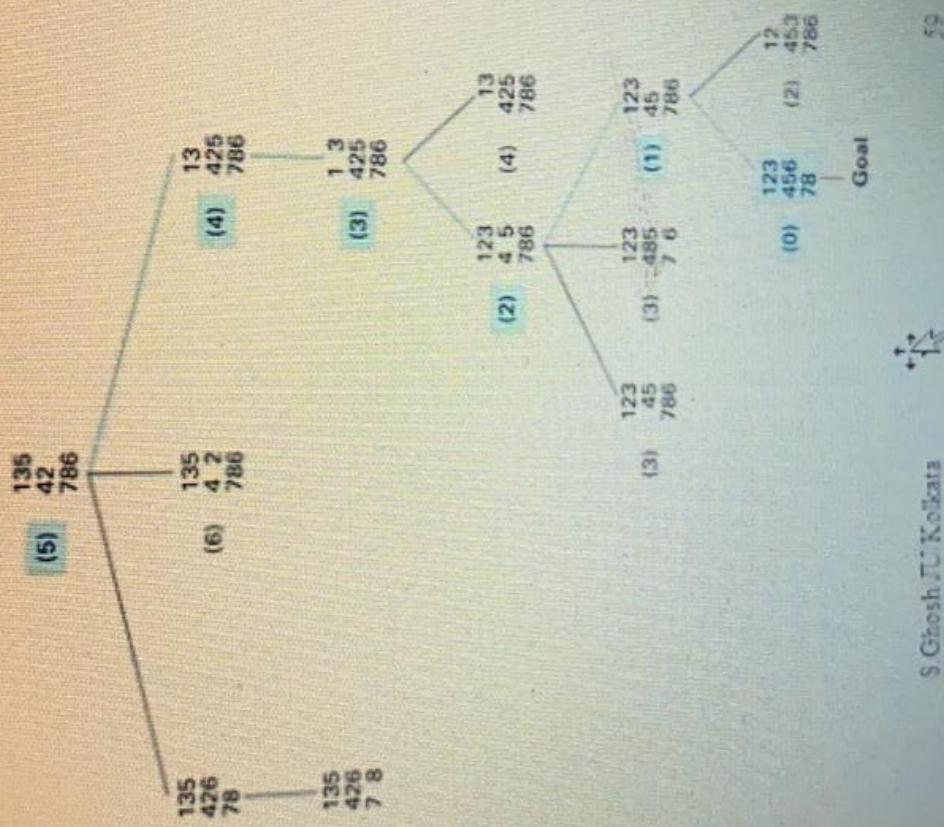


4.2.2021

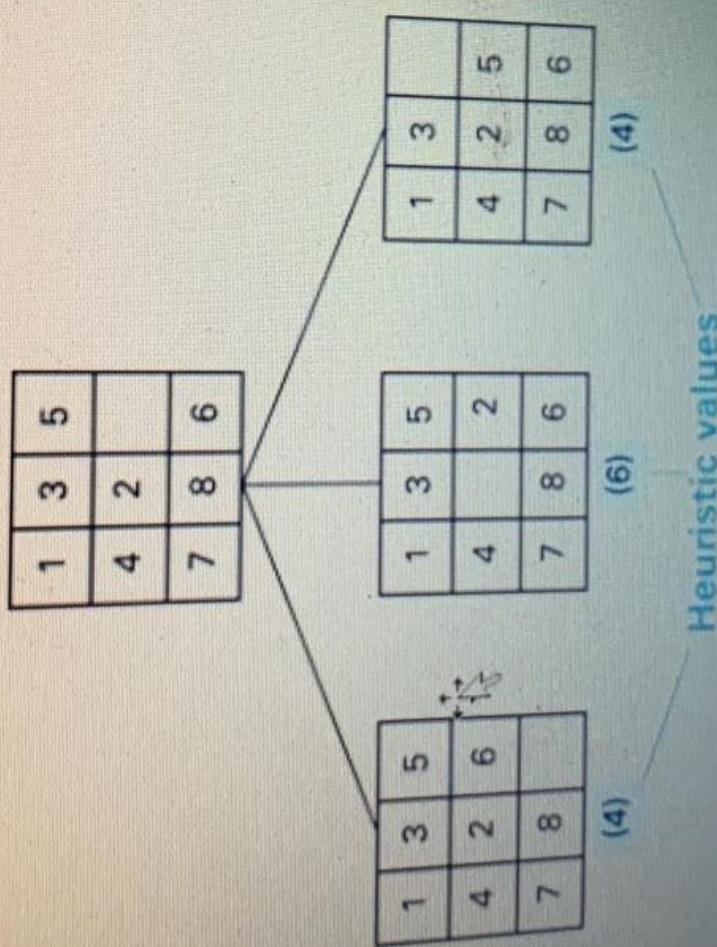
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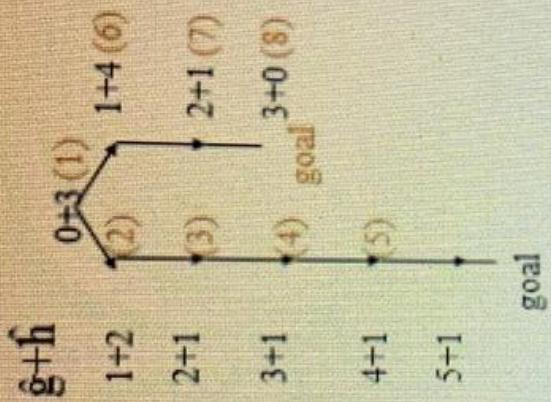
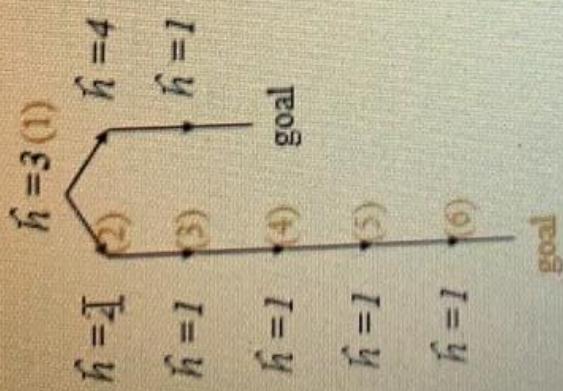
The complete  
search tree  
formed by  
our heuristic  
system



# The beginning of our heuristic search (Greedy): Sliding Tiles



## Example



$f = \hat{f}$   
greedy

$f = \hat{f}$   
 $A^*$

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- A    B    C
- D     $f(D) - g + h$
- Path costs |
- SAD -- 8    SBD --- 9    SCD--- 4

Font Paragraph Drawing

4/3/2021

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## Informed search (contd.)

### Best first greedy search

- Evaluation function ( $f$ ) =  $\hat{h}$
- Shallowest goal may not be reached

A\*

- Evaluation function ( $f$ ) =  $\hat{g} + \hat{h}$   
 $\hat{g}$  = cost of reaching node  $n$  from start node

A\* will always satisfy optimality if the heuristic is admissible

$\hat{h}(n)$  is said to be admissible if

$\hat{h}(n) \leq h(n)$ , for all  $n$  (for minimization problem)

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... go on

in Bucharest  
(Romania)

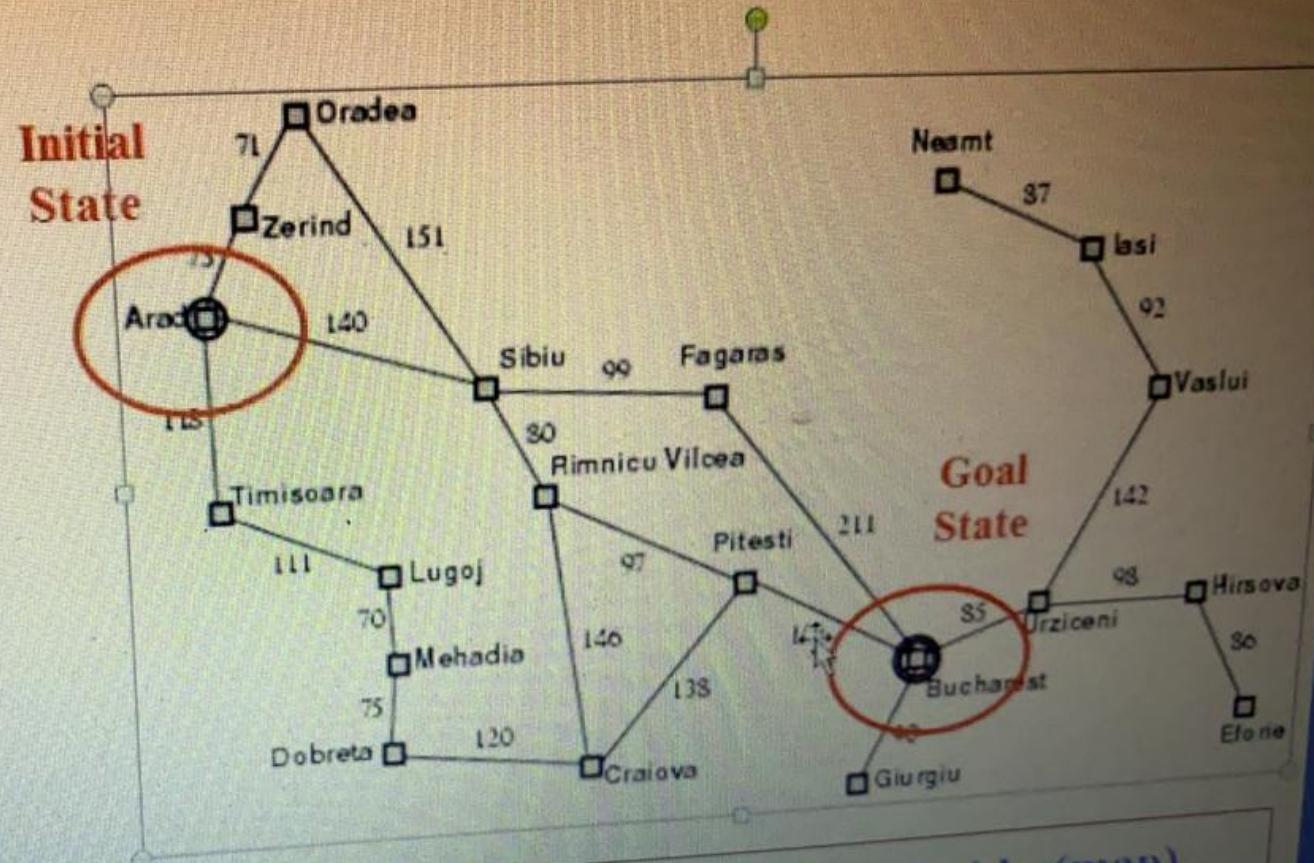
late problem:

Action: drive between  
pair of connected cities  
(not direct road)

State: be in a city  
(20 world states)

A solution:

sequence of cities  
leading from start to  
goal state, e.g., Arad,  
Zerind, Oradea, Sibiu,  
Fagaras.



Environment: fully observable (map),  
deterministic, and the agent knows effects  
of each action. Is this really the case?

## Click to add title

- S

- A    B    C

- D     $f(D) = g + h$  (path cost)

- Path costs
- SAD --> 8    SBD --> 9    SCD--> 4
- G = 8 ; G =

• A B C

$$D \quad f(D) = g + h \text{ (path cost)}$$

- Path costs
- SAD -- 8    SBD --- 9    SCD--- 4
- $G = 8$ ;  $G = 8$ ,  $G = 4$
- All paths explore:  $g = \min |$

— 4-5-2021

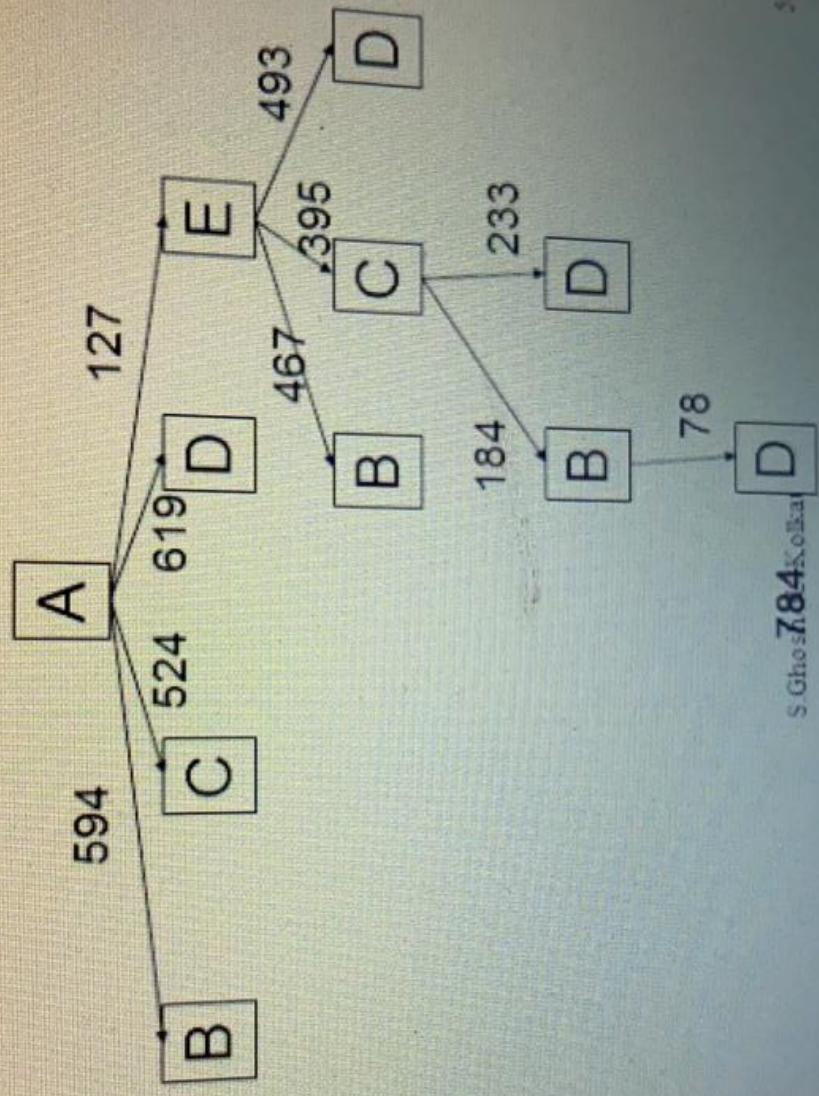
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ck to add notes

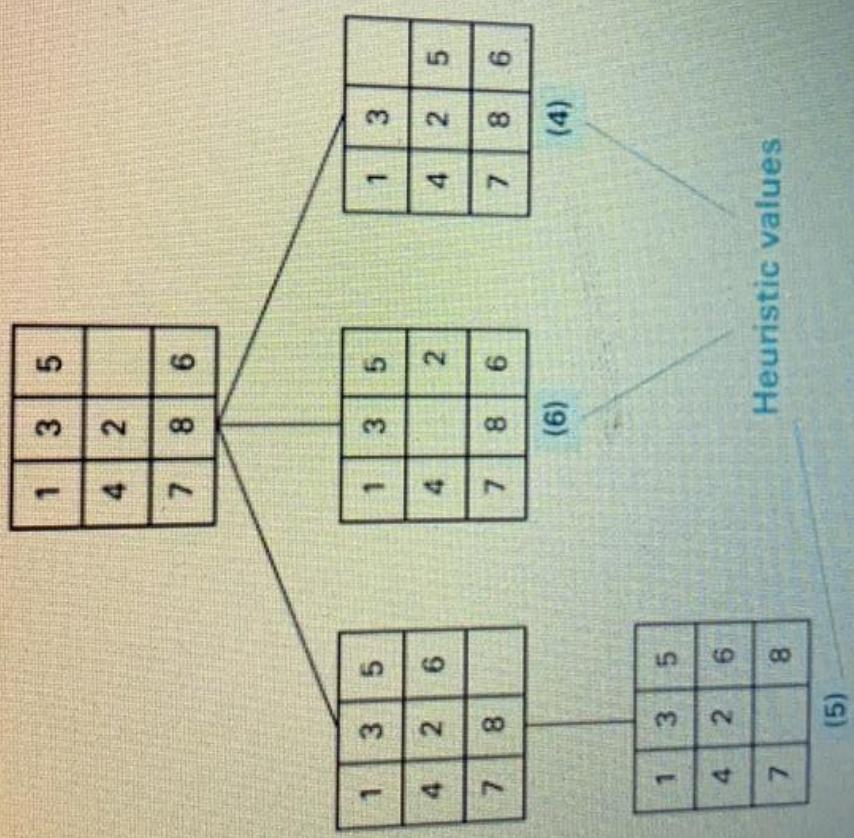
English (U.S.)

## Informed/ Heuristic Search: TSP

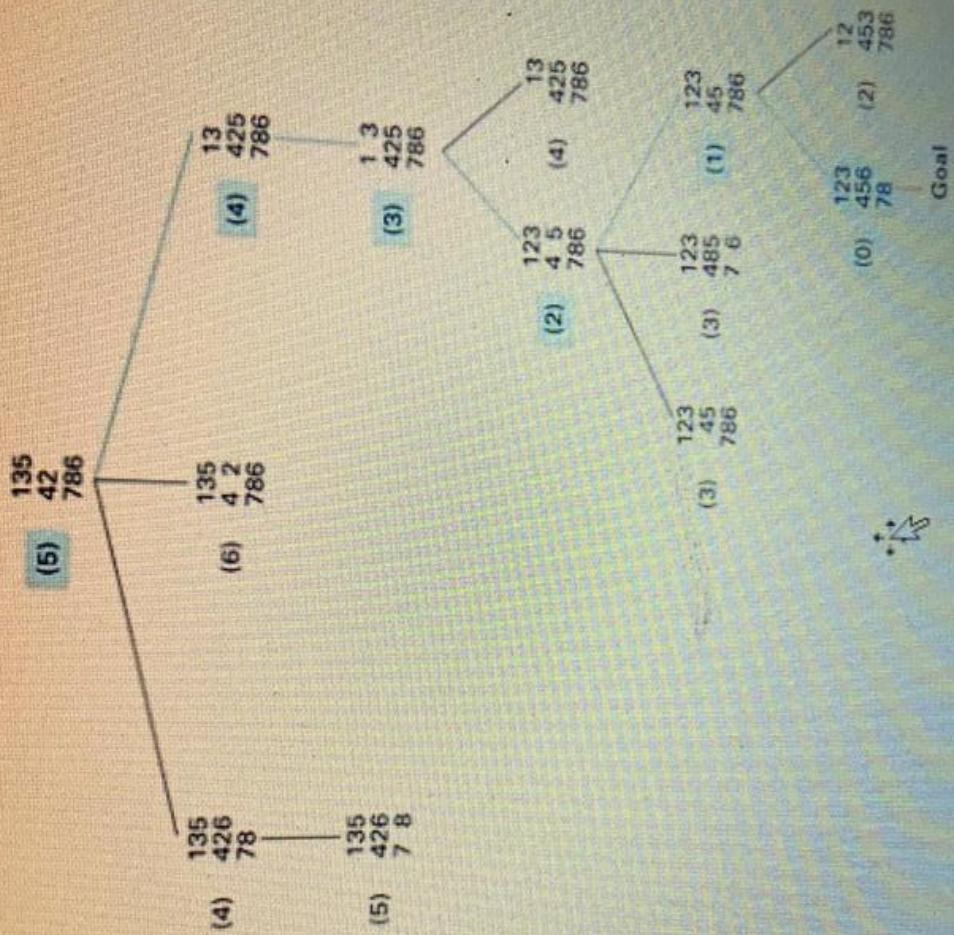
- heuristic = rule of thumb



## The search tree after two passes

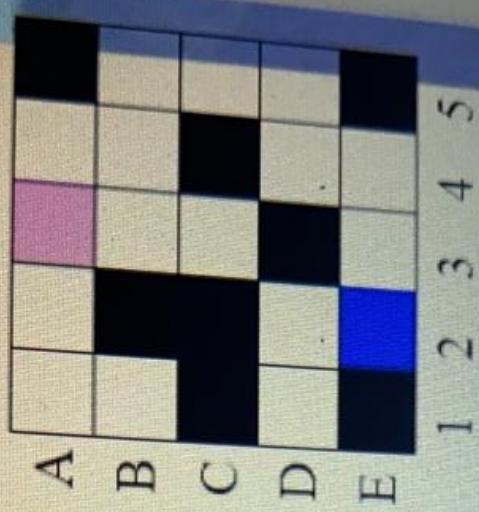


The complete search tree formed by our heuristic system



## A\* : Maze Traversal

**Problem:** To get from square A3 to square E2, one step at a time, avoiding obstacles (black squares).



Operators: (in order)

- go\_left(n)
  - go\_down(n)
  - go\_right(n)
- each operator costs 1.

Heuristic: Manhattan distance

## Informed Search (contd.)

### IDA\*

- Repeatedly search in DFS fashion over subgraphs with f-cost less than  $\epsilon$ . Less than  $2\epsilon \dots$  until a goal node is found (where,  $\epsilon \leq g(n,m)$  for all  $n,m \in \delta(n)$ )
- Time: in worst case if A\* expands N nodes, IDA\* expands  $O(N^2)$  nodes
- Space:  $O(b(f^*/\epsilon))$ ,  $f^*$ : optimal cost

I

## Informed Search (contd.)

### IDAI

- Repeatedly search in DFS fashion over subgraphs with  $f$ -cost less than  $\varepsilon$ . Less than  $2\varepsilon \dots$  until a goal node is found (where,  $\varepsilon <= g(n,m)$  for all  $n,m \in \delta(n)$ )
- Time: in worst case if A\* expands N nodes, IDA\* expands  $O(N^2)$  nodes
- Space:  $O(b(f^*/\varepsilon))$ ,  $f^*$ : optimal cost

## Admissible Heuristic

$\hat{h}(n)$  : heuristic function (applied to node  $n$ ); estimated distance of node  $n$  from goal node

$h(n)$  : actual distance of node  $n$  from goal node

$\hat{h}(n)$  is admissible if  $\hat{h}(n) \leq h(n)$ , for all  $n$  (for minimization)

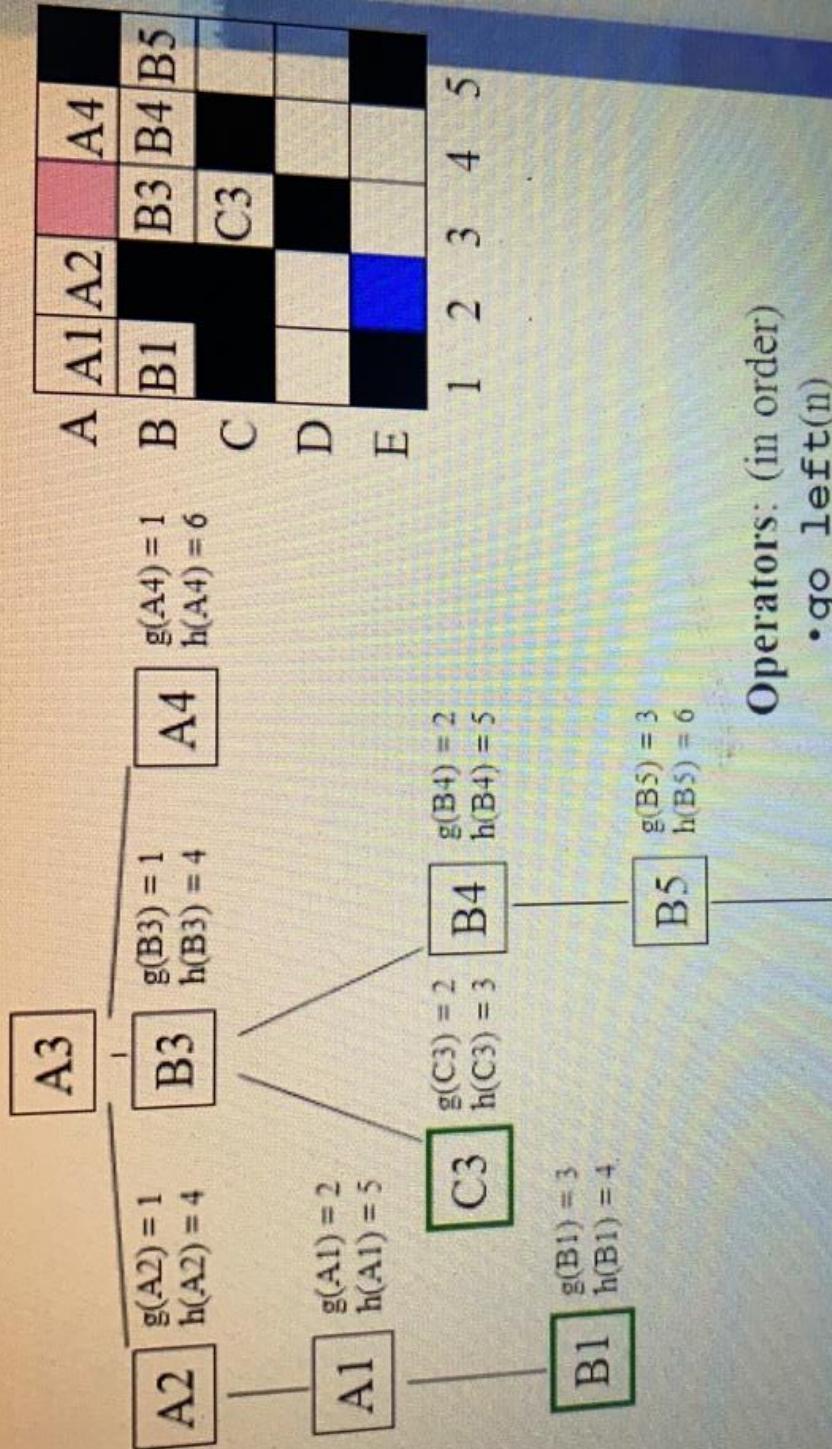
If  $h \geq \hat{h}_1(n) > \hat{h}_2(n)$  then  $\hat{h}_1$  is more informed than  $\hat{h}_2$

Admissibility condition may be relaxed for efficiency but then the obtained solution may not be optimal

$g(n)$	$h(n)$	characteristics
1	0	BFS
Cost	0	UCS
0	0	random search

admissible

$h(n)$



Operators: (in order)

- go\_left(n)
- go\_down(n)
- go\_right(n)

§ GhostrU ~~Each~~ operator costs 1.

66

$\hat{h}(n)$  is admissible if  $\hat{h}(n) \leq h(n)$ , for all  $n$  (for minimization)

If  $h >= \hat{h}_1(n) > \hat{h}_2(n)$  then  $\hat{h}_1$  is more informed than  $\hat{h}_2$

Admissibility condition may be relaxed for efficiency but obtained solution may not be optimal

$g(n)$	$h(n)$	characteristics
1	0	BFS
Cost	0	UCS
0	0	random search
$g(n)$	admissible	optimal path

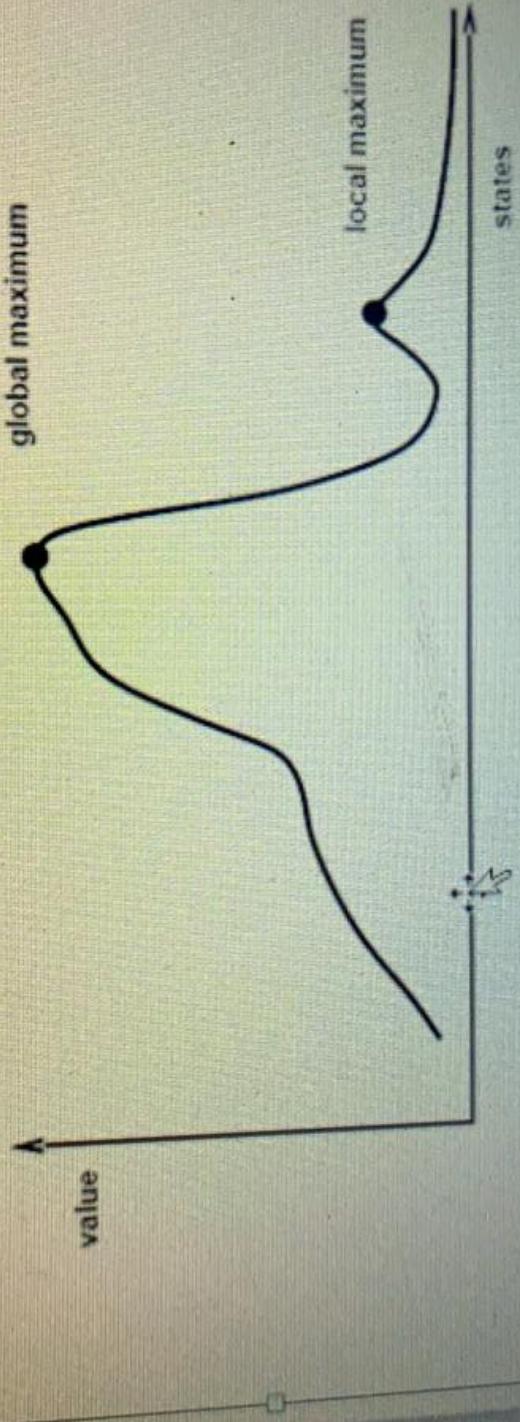
## Iterative Improvement Search

- Every state represents a complete solution to the problem, although not necessarily an optimal one
- Initialize the algorithm at some (random) state, iteratively perturb the current solution, update if any of the tested perturbations yields an improvement
- Never backs up, no search tree

*Hill Climbing, Simulated Annealing, Genetic Algorithm*

# Hill Climbing

Problem: depending on initial state, can get stuck on local maxima



In continuous spaces, problems w/ choosing step size, slow convergence

## Drawbacks of Hill climbing

- Local optima / foothill problem – attracted to local optima
- Plateau problem – nowhere to turn on the flat
- Ridge problem – no available operator to move from the region

## Iterated Hill Climbing (Algorithm)

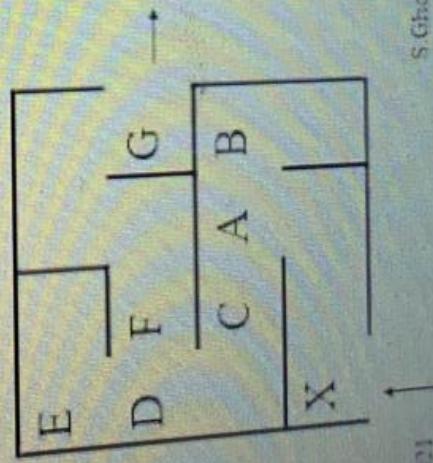
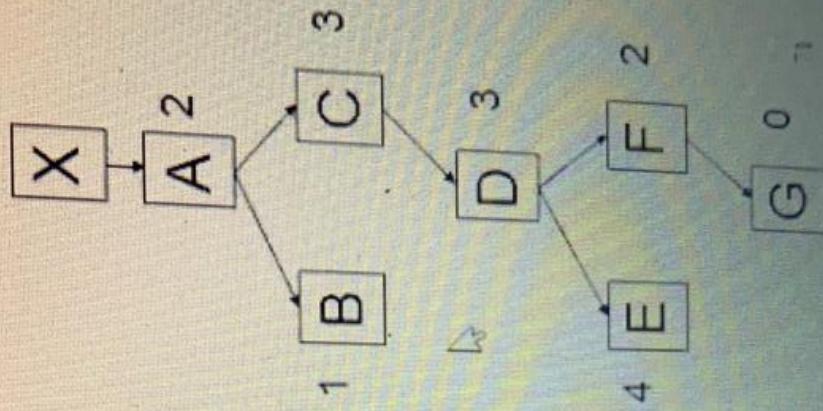
```
begin
    t = 0
repeat
    local = FALSE
    select a random state sc and compute its functional value f(sc)
repeat
    select n new states in the neighborhood of sc (by
    flipping randomly single bit of sc) and compute their functional
    values
    select the state sn from the set of new states with largest
    functional value f(sn)
    If  $f(sc) < f(sn)$  set  $sc = sn$  else  $local = TRUE$ 
    until local
    t = t + 1
until  $t = MAX$ 
end
```

## Hill Climbing

- Walk as much uphill as possible
- Move from one point to that adjacent point having highest elevation
- Solution found, but not necessarily an optimal one

## Iterative Improvement Search – Hill Climbing – Maze Problem

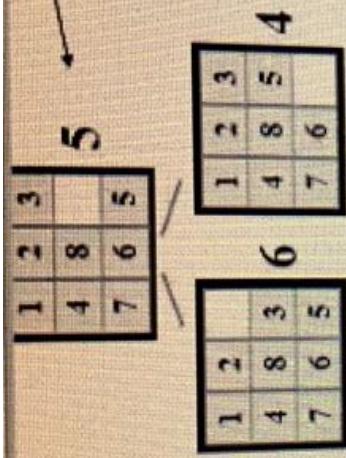
- expand node
- sort children according to Heuristic Evaluation Function
- choose best value



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4.3.2021

1	2	3	
4	8	5	5
7	6	5	



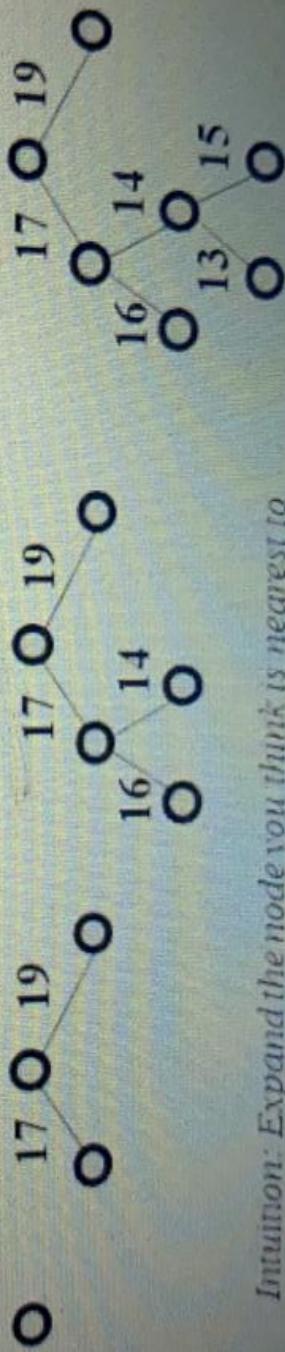
We can use heuristics to guide "hill climbing" search.

In this example, the Manhattan Distance heuristic helps us quickly find a solution to the 8-puzzle.

But "hill climbing" has a problem:

# Hill Climbing Search

Enqueue nodes in order of estimated distance to goal



*Intuition:* Expand the node you think is nearest to goal. Where the estimate of distance to goal is  $h(n)$

Click to add notes

## Simulated Annealing (Algorithm)

```
begin  
    t = tmax  
    select a random state sc and compute its functional value f(sc)  
    while (t >= tmin)  
        for i = 1 to n  
            begin  
                pick an adjacent state sn from sc at random and  
                compute f(sn)  
                If f(sc) >= f(sn) set sc = sn  
                else set sc = sn with probability {exp(- (f(sn) - f(sc))/t)}  
            end  
            decay r  
        end  
    end
```

# Heuristic Search – hill climbing



## Simulated Annealing

- Simulates the concept of annealing of physical systems
- State transition follows Boltzmann distribution
- It is proved that it will reach global optima if  $T$  (temperature) tends to zero and number of alternatives examined at each temperature tends to infinity
- *Escapes local maxima by allowing some bad moves, but gradually decreasing their frequency*

*Drawback: too slow*

## Example 1

Maximize  $f(x) = x^2$

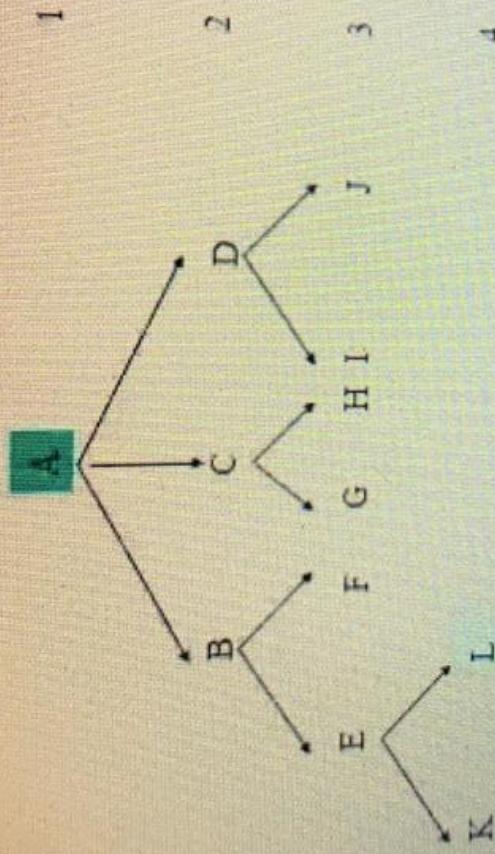
String#	Initial Pop	x-value	$f(x) = x^2$	Expected count (fi/f-av)	Actual count from r-wheel
1	01101	13	169	0.58	1
2	11000	24	576	1.97	2
3	01000	8	64	0.22	0
4	10011	19	361	1.23	1

sum = 1170; average = 293; max = 576

Mating pool      Mate      cross-site  
(after reproduction)      (random select)

New Pop      New Pop      x-value       $f(x) = x^2$

## Example



- A: start state; L: goal state

IBS:

order: iteration 1: A

iteration 2: A B E K

iteration 3: A B E K L

path: A B E L

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# Roulette wheel selection

- Sum the fitness of all the chromosomes of the population. Call it ***total-fitness***.
- Generate a random number ***n*** in [0, ***total-fitness***]
- Return the first chromosome whose fitness when added to the fitness of the preceding population member is greater or equal to ***n***.

## Example:

Let there be five chromosomes with fitness 20, 10, 40, 7, 14  
Then ***total-fitness***=91.

Say, the random number drawn (***n***) is 45.

Select the 3<sup>rd</sup> chromosome (since  $20+10+40 > 45$ ).



# Summary

- All uninformed search techniques are more alike than different.
- Breadth-first has space issues.
  - Depth-first has optimality and completeness issues.
  - Depth-limited search has optimality and completeness (?) issues.
- Iterative deepening is the best uninformed search we have discussed.

Criteria	BFS	Uniform-cost	DFS	Depth-limited	IDS	Bidirectional
Complete?	Yes <sup>#</sup>	Yes <sup>#&amp;</sup>	No	No	Yes <sup>#</sup>	Yes <sup>#+</sup>
Time	$O(b^d)$	$O(b^{1+[C^*/\epsilon]})$	$O(b^m)$	$O(b^l)$	$O(b^d)$	$O(b^{d/2})$
Space	$O(b^d)$	$O(b^{1+[C^*/\epsilon]})$	$O(bm)$	$O(bl)$	$O(bd)$	$O(b^{d/2})$
Optimal?	Yes <sup>\$</sup>	Yes	No	No	Yes <sup>\$</sup>	Yes <sup>\$+</sup>

*b:* Branching factor

*d:* Depth of the shallowest goal

*l:* Depth limit

*m:* Maximum depth of search tree

*e:* The lower bound of the step cost

<sup>#</sup>: Complete if *b* is finite

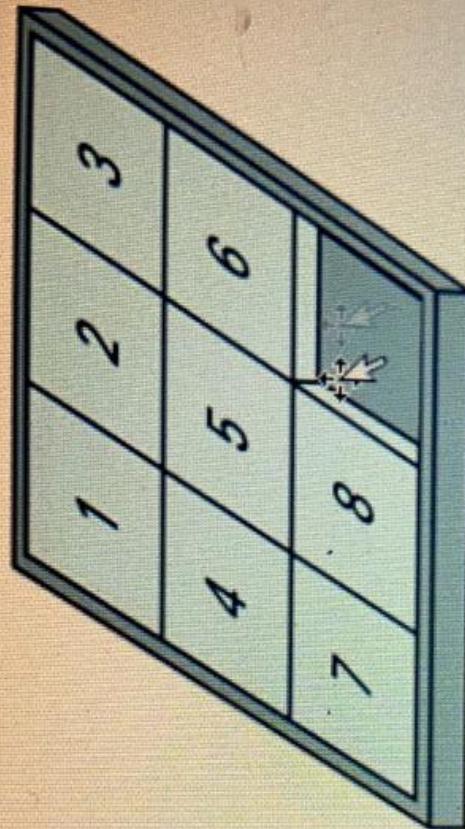
<sup>&</sup>: Complete if step cost  $\geq e$

<sup>\$</sup>: Optimal if all step costs are identical

<sup>+</sup>: If both direction use BFS

## The Eight-Puzzle (Sliding Tiles) Problem

1	3	5
4	2	
7	8	6



Note: finding **optimal** solution of  $n$ -puzzle family is NP-hard!

Also, from certain states you can't reach the goal.

Total number of states  $9! = 362,880$  (more interesting space;  
not all connected... only half can reach goal state)

S.Ghosh JU/Kolkata

4.2.2021

## Introduction to Search

- Search is the operational task that characterizes the AI programs best. Almost every AI program depends on a search procedure to perform its prescribed functions.
- Problems are typically defined in terms of **states** and a solution corresponds to a **goal state**.
- Solving a problem then amounts to searching through different states until one or more goal states are found.
  - e.g., chess: 20 alternative moves for each board configuration  
    >100 different configurations

Therefore  $> 20^{100}$  moves !!! *Is it possible to evaluate all?*

*eliminate questionable states, look ahead*

3.19.2021 S.Ghosh,IIT Kharagpur