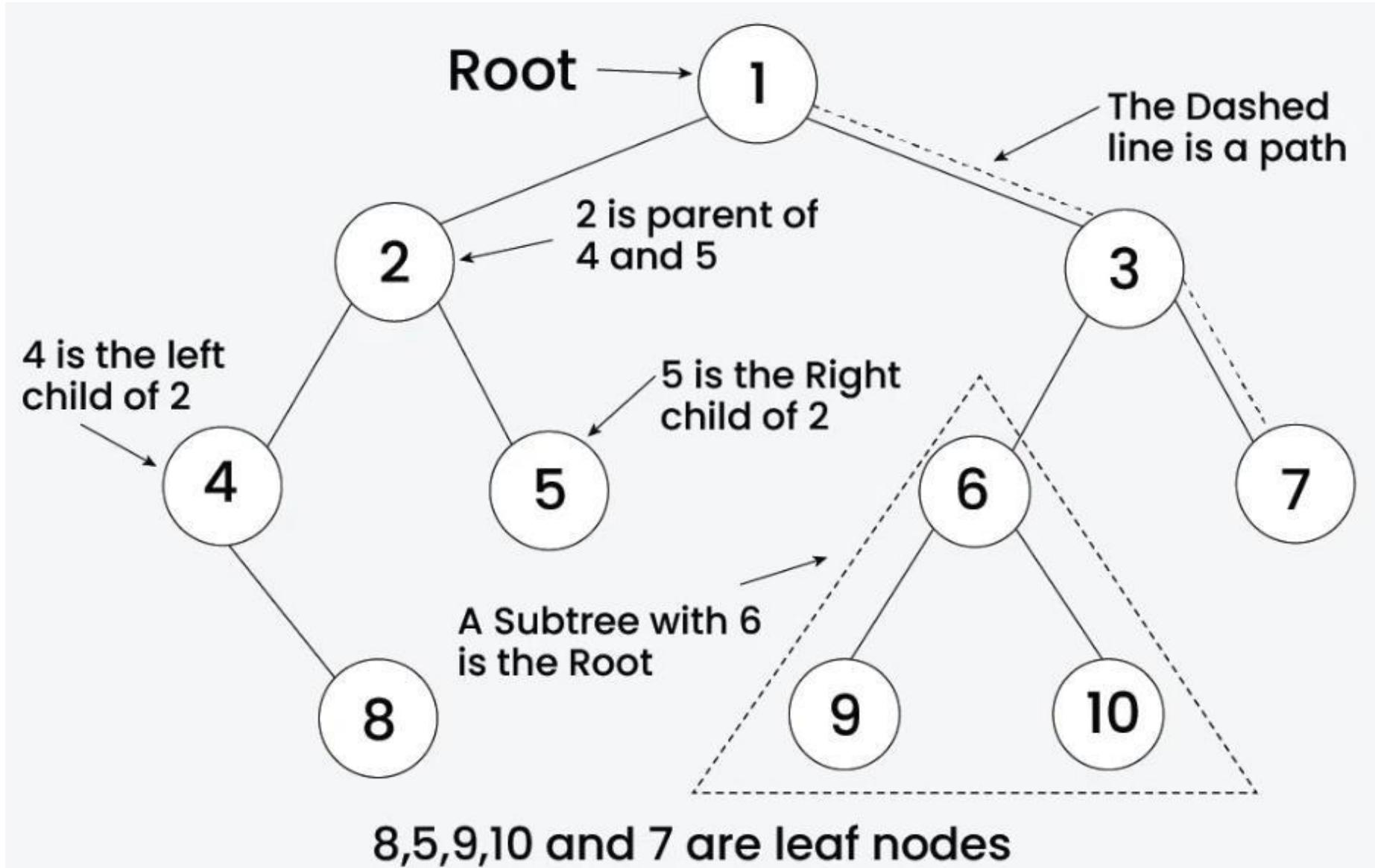
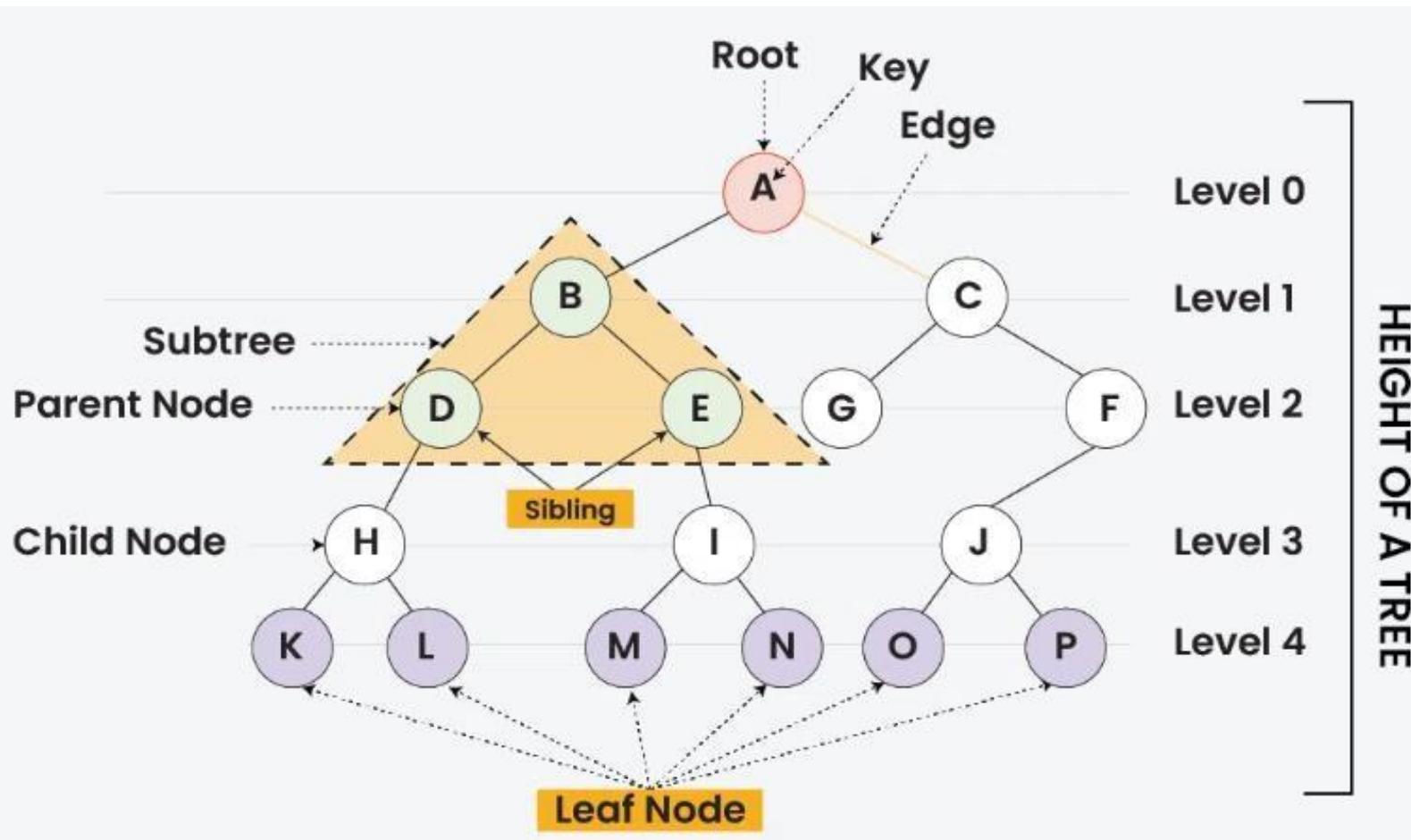


Binary Tree

Binary Tree: Definition

- Binary Tree is a non-linear and hierarchical data structure (general tree), where each node has at most two children referred to as the left child and the right child.
- The topmost node in a binary tree is called the **root**, and the bottom-most nodes are called **leaves**.





Binary Tree: Terminologies

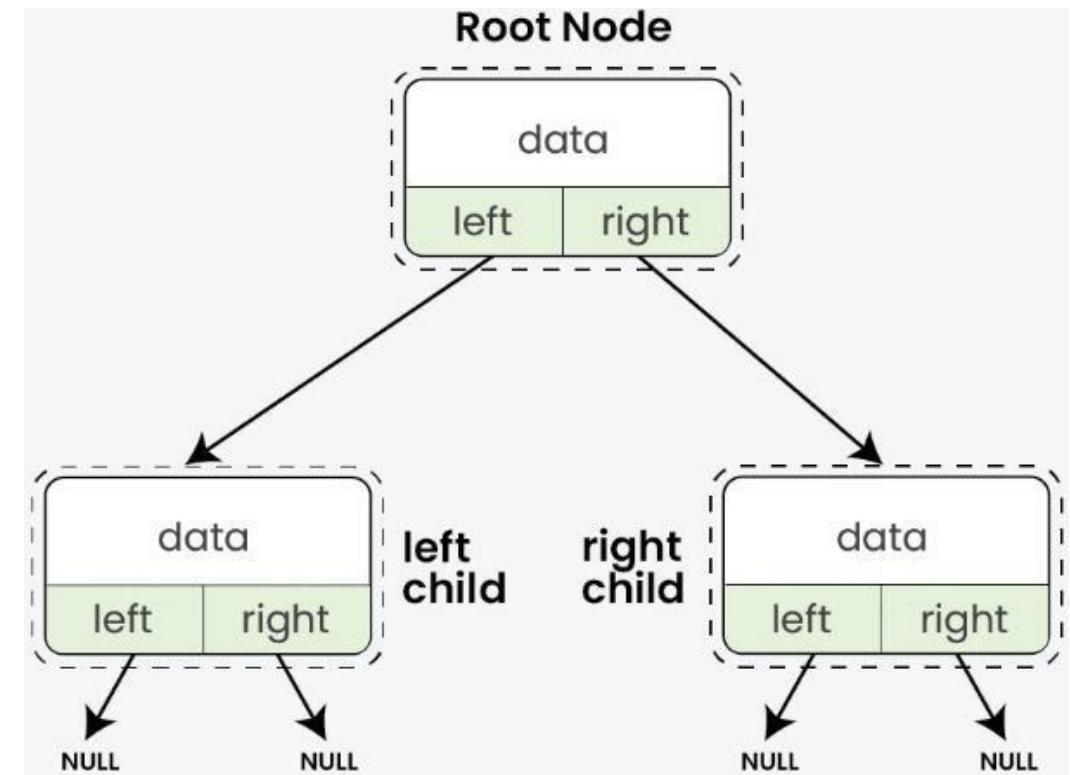
Binary Tree: Representation

```
// Node Structure
struct Node {
    int data;
    Node* left;
    Node* right;

    Node(int value) {
        data = value;
        left = right = nullptr;
    }
};
```

Each node in a Binary Tree has three parts:

- Data
- pointer to the left child
- pointer to the right child





Binary Search Tree



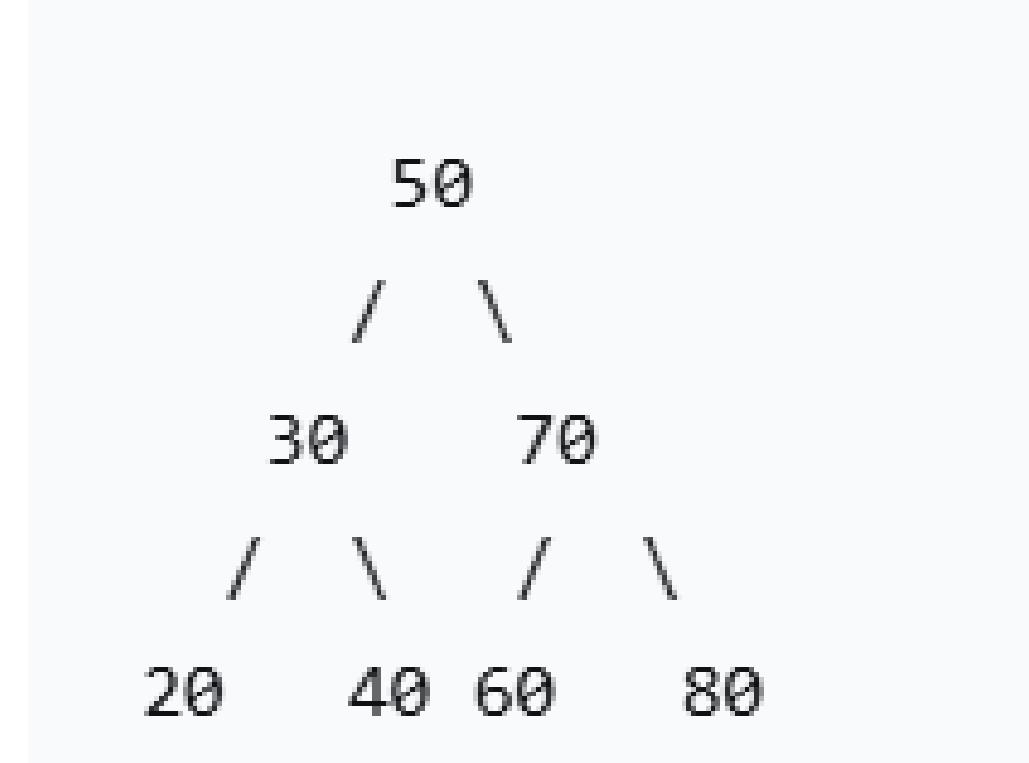
What is a Binary Search Tree?

- A Binary Search Tree is a **node-based binary tree** data structure with the following key properties:
- **Binary Tree Structure:** Each node has at most two children, typically called the **left child** and **right child**.
- **Ordering Property:** For any given node:
 - All values in its **left subtree** are **less than** the node's value.
 - All values in its **right subtree** are **greater than** the node's value.
 - This implies that all values in the tree are **unique** (or if duplicates are allowed, they must be consistently placed, e.g., always in the left or always in the right subtree).

Visual Example

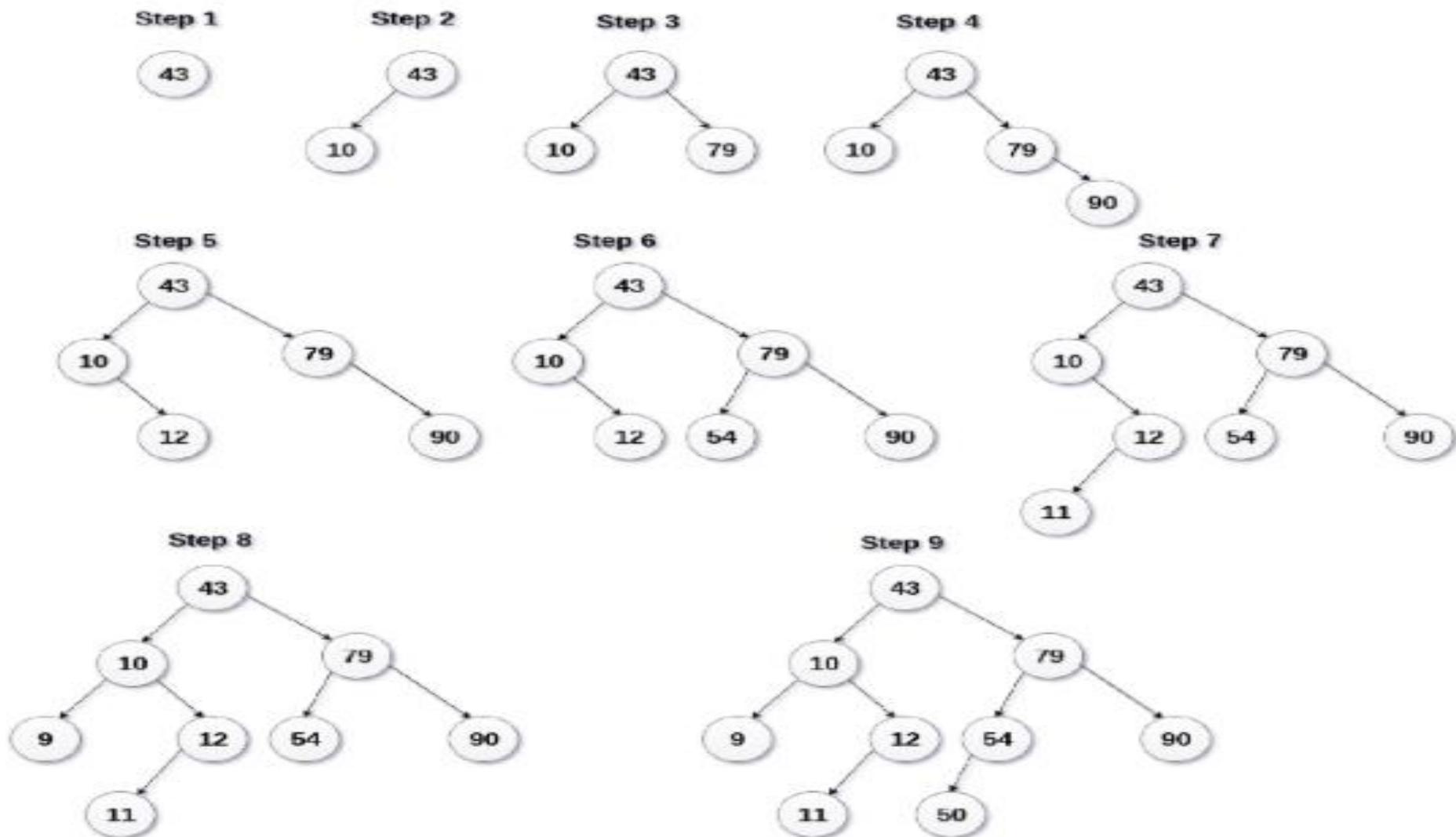
Let's build a BST by inserting the numbers: 50, 30, 70, 20, 40, 60, 80.

- The root is 50.
- The entire left subtree of 50 (30, 20, 40) contains values less than 50.
- The entire right subtree of 50 (70, 60, 80) contains values greater than 50.
- This property holds recursively for every node. For example, node 30 has left child 20 (<30) and right child 40 (>30).



Q. Create the binary search tree using the following data elements. 43, 10, 79, 90, 12, 54, 11, 9, 50 ?

1. Insert 43 into the tree as the root of the tree.
2. Read the next element, if it is lesser than the root node element, insert it as the root of the left sub-tree.
3. Otherwise, insert it as the root of the right of the right sub-tree.



Binary search Tree Creation

Binary Search Tree Operations

Core Operations:

1. Search

Purpose: Find if a value exists

Approach: Start at root, go left if smaller, right if larger.

2. Insertion

Purpose: Add new value while maintaining BST properties

Approach: Find correct position (like search), insert at null location

3. Deletion - Three cases:

No children: Simply remove node

One child: Replace node with its child

Two children: Replace with inorder successor/predecessor

Traversal Operations:

4. In-order Traversal

Order: Left → Root → Right

Result: Returns elements in sorted order

5. Pre-order Traversal

Order: Root → Left → Right

6. Post-order Traversal

Order: Left → Right → Root

1. Search

The **search operation** in a BST finds whether a specific value exists in the tree by leveraging the BST property:

- Left subtree contains smaller values
- Right subtree contains larger values
- This allows us to eliminate half of the remaining tree at each step, making search very efficient.

Algorithm Steps

1. Start at the root node
2. Compare target value with current node's value:
 - If **equal** → Value found
 - If **smaller** → Go to left child
 - If **larger** → Go to right child
3. Repeat until value found or null node reached
4. If null reached → Value not found

```
function search(root, key):  
    current = root  
  
    while current is not NULL:  
        if key == current.value:  
            return true                                // Value found  
        else if key < current.value:  
            current = current.left                     // Search left subtree  
        else:  
            current = current.right                   // Search right subtree  
  
    return false                                 // Value not found
```

2. Insertion

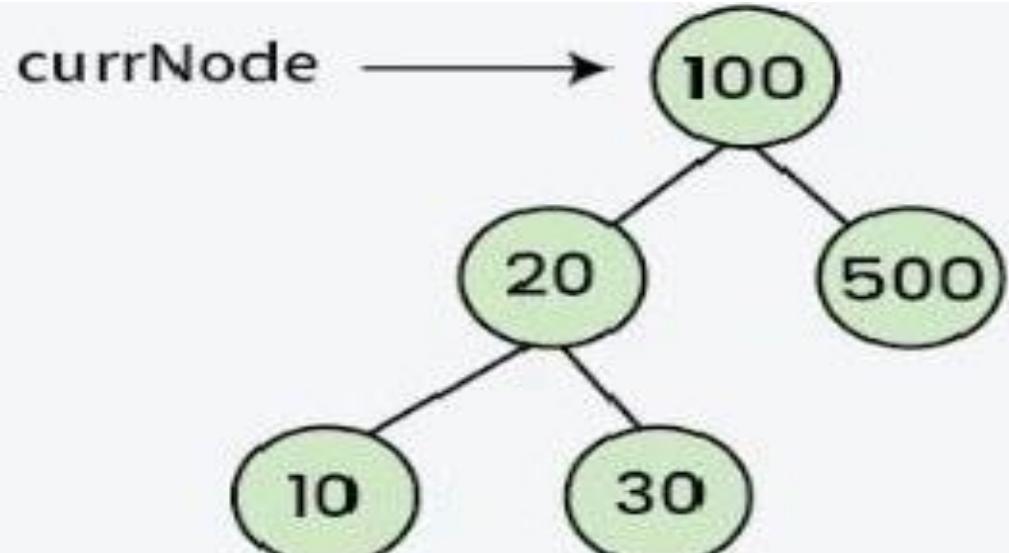
The **insert operation** adds a new value to the BST while maintaining the BST property:

- Left child < Parent < Right child
- The new node is always inserted as a **leaf node**

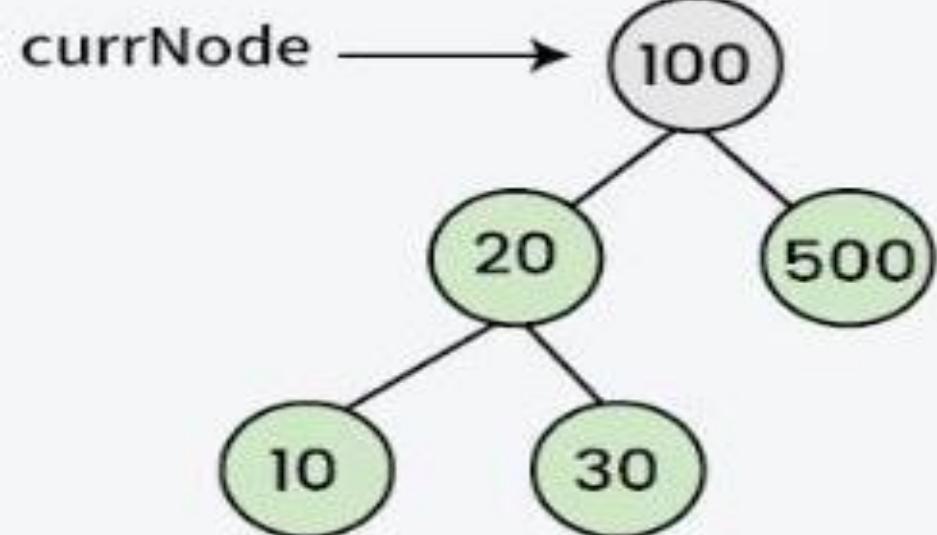
Algorithm Steps

1. Start at the root node
2. Compare new value with current node:
 - If **smaller** → Go to left child
 - If **larger** → Go to right child
3. Repeat until you find a null position
4. Insert new node at that null position

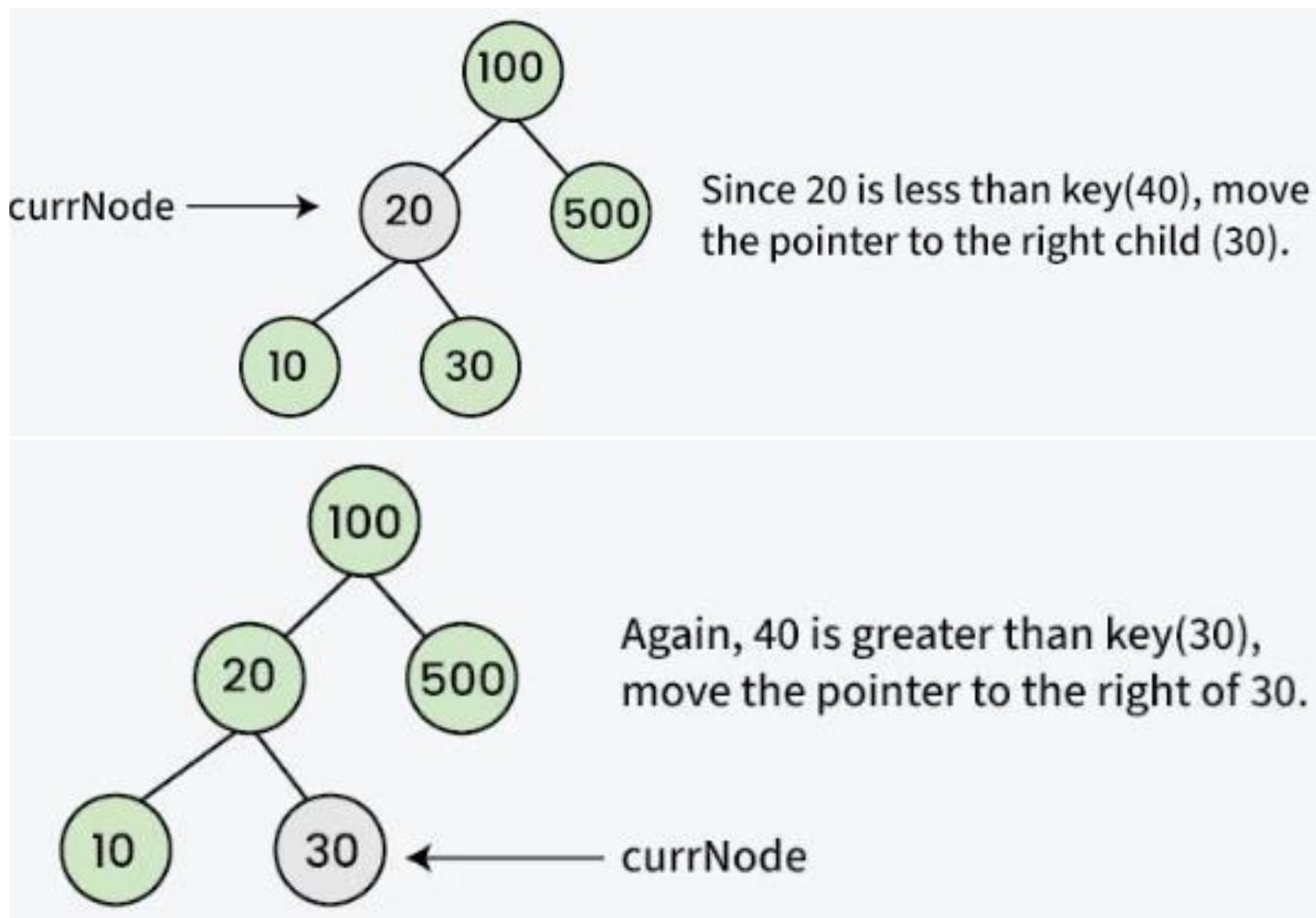
```
FUNCTION insert(root, value):  
    IF root == NULL:  
        root = NEW_NODE(value)  
        RETURN root  
  
    IF value < root.data:  
        root.left = insert(root.left, value)  
    ELSE IF value > root.data:  
        root.right = insert(root.right, value)  
  
    RETURN root
```

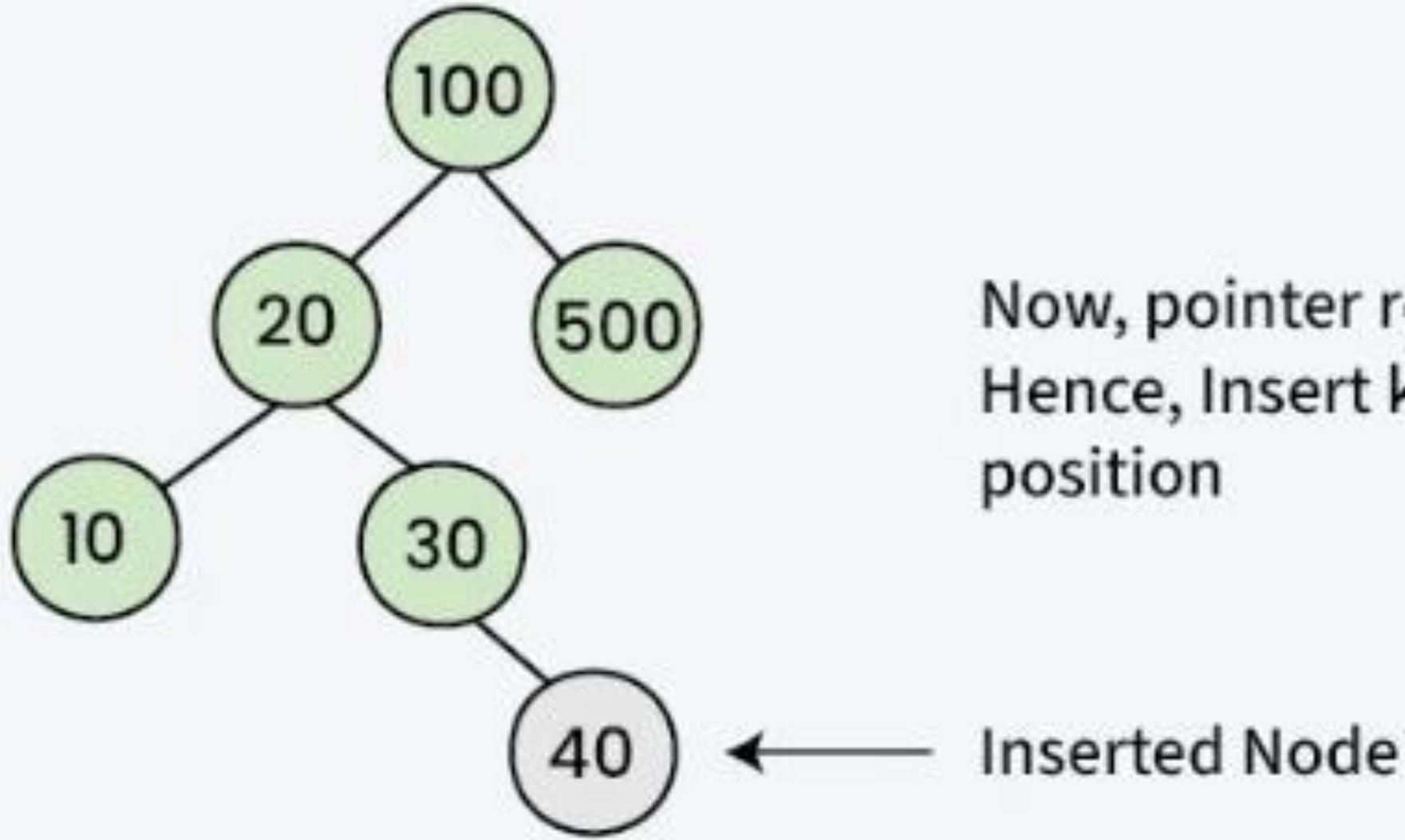


key = 40 (the node to be inserted)



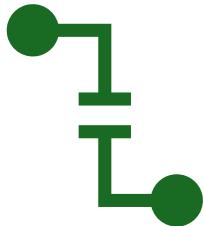
Since 100 is greater than key(40), move the pointer to the left child (20).



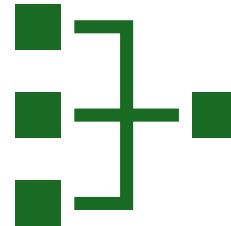


Now, pointer refers to null.
Hence, Insert key(40) at this position

4. Traversing a BST



Traversing a binary tree is the process of visiting each node in the tree exactly once in a systematic way.



There are four different algorithms for tree traversals, which differ in the order in which the nodes are visited:

Pre-order

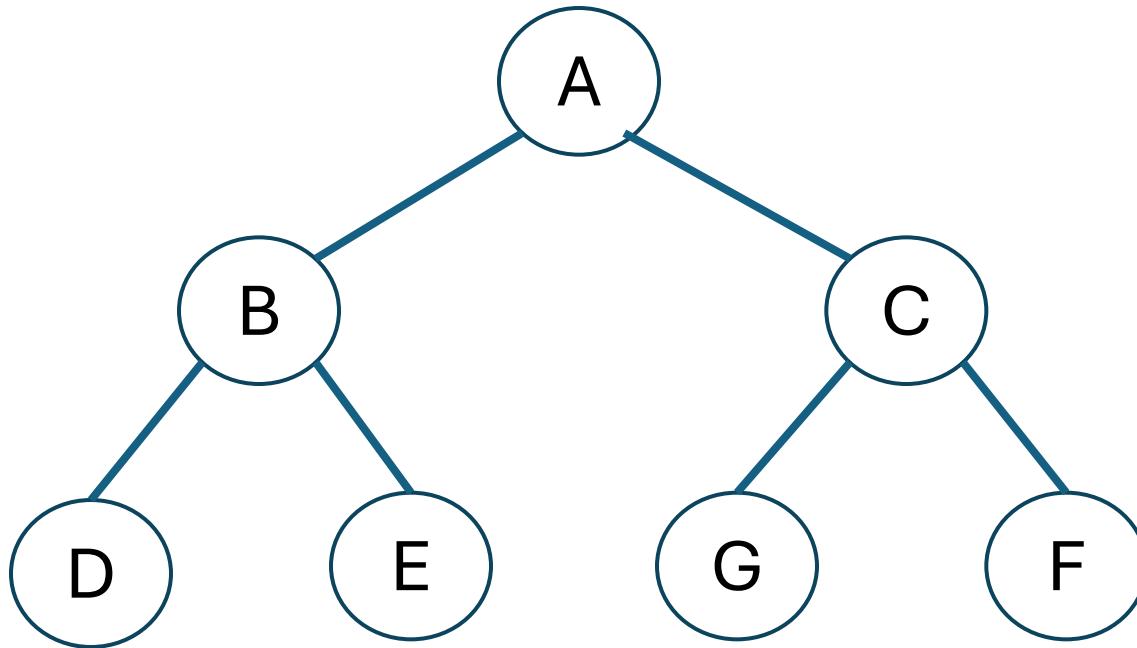
In-order

Post-order

Pre-order

- To traverse a non-empty binary tree in preorder, the following operations are performed recursively at each node.
- The algorithm starts with the root node of the tree and continues by:
 - Visiting the root node
 - Traversing the left subtree
 - Traversing the right subtree
- Implemented by recursive function

Pre-order



Pre-order A, B, D, E, C, G, F

Pre-order Implementation

- Implement by recursive function

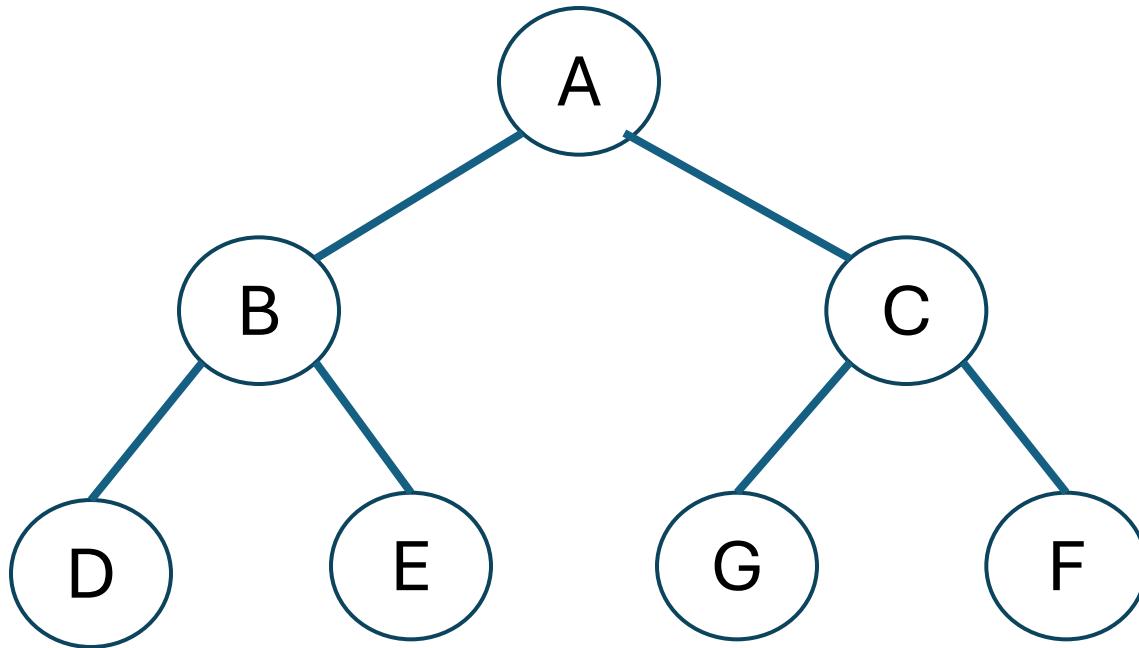
Example

```
void print_preorder(node *root) {  
    if (root) {  
        printf("%d ", root->data);  
        print_preorder(root->left);  
        print_preorder(root->right);  
    }  
}
```

In-order

- To traverse a non-empty binary tree in **in-order**, the following operations are performed recursively at each node.
- The algorithm starts with the root node of the tree and continues by,
 - Traversing the left subtree
 - Visiting the root node
 - Traversing the right subtree

In-order



In-order: **D, B, E, A, G, C,**
F

In-order Implementation

- Implement by recursive function

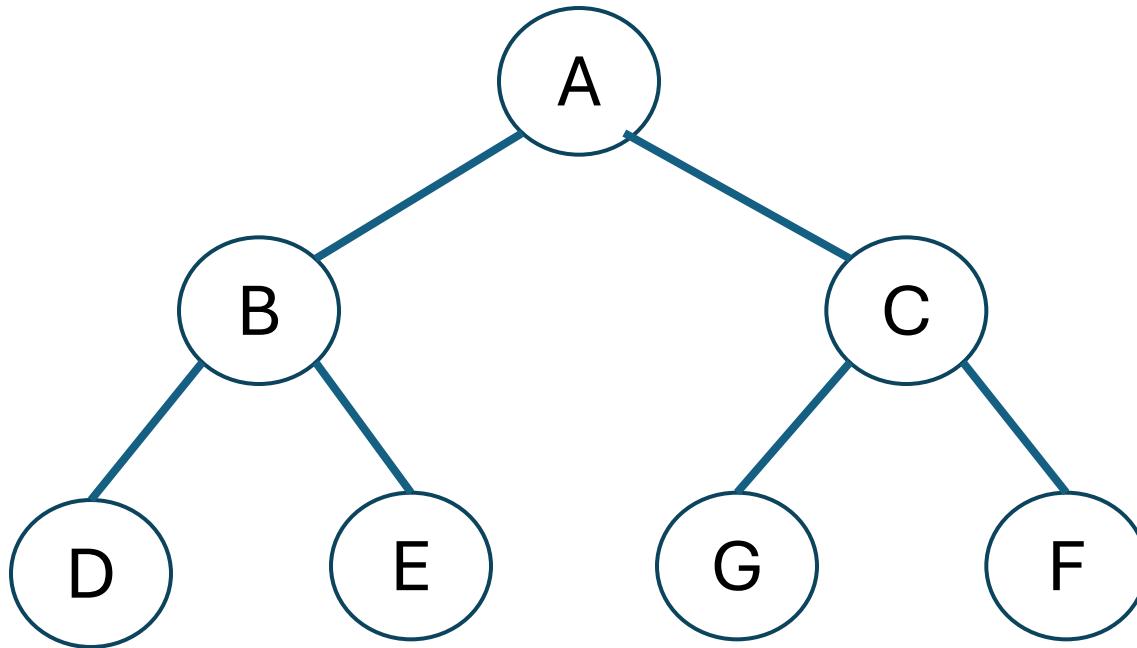
Example

```
void print_inorder(node *root) {  
    if (root) {  
        print_inorder(root->left);  
        printf("%d ", root->data);  
        print_inorder(root->right);  
    }  
}
```

Post-order

- To traverse a non-empty binary tree in **post-order**, the following operations are performed recursively at each node.
- The algorithm starts with the root node of the tree and continues by,
 - Traversing the left subtree
 - Traversing the right subtree
 - Visiting the root node
- Implemented by recursive function

Post-order



Post-order: D, E, B, G, F, C, A

post-order Implementation

- Implement by recursive function

Example

```
void print_postorder(node *root) {  
    if (root) {  
        print_postorder(root->left);  
        print_postorder(root->right);  
        printf("%d ", root->data);  
    }  
}
```