Lista 1 - Revisão de álgebra e funções

1. Efetue as operações indicadas e calcule o valor das expressões, simplificando sempre que possível:

a)
$$\frac{(-5)^2 - 4^2 + \left(\frac{1}{5}\right)^0}{3^{(-2)} + 1}$$

b)
$$\left(\sqrt[3]{\frac{6\sqrt{29}}{\sqrt{29}}}\right)^5 \cdot \left(\sqrt[6]{\frac{3\sqrt{29}}{\sqrt{29}}}\right)^5$$

c)
$$\left[\left(\frac{5}{6} - \frac{1}{3} \right)^2 - \frac{1}{5} \right] \div \left\{ \frac{9}{4} - \left[\frac{1}{2} \left(2 - \frac{1}{3} \right) \right] \right\}$$

d)
$$\frac{16^{\frac{3}{4}}}{8^{\frac{1}{3}}} \div \frac{2^4}{8^2}$$

e)
$$\frac{3}{10} - \frac{2}{3} \times \frac{9}{10}$$

f)
$$\left(\frac{5}{16} + \frac{1}{8}\right) \div \left(\frac{5}{4} - \frac{1}{12}\right)$$

g)
$$\left(2 + \frac{1}{3}\right) \div 14 - \left(\frac{1}{9} - \frac{1}{3}\right)$$

h)
$$\frac{1-\frac{3}{2}}{1+\frac{1}{4}} \times \frac{5}{3}$$

2. Aplicando as propriedades das potências, simplifique as expressões:

a)
$$\frac{256.4^9}{8^7}$$

b)
$$\frac{9^3.27^4.3^{-7}}{\frac{1}{3}.243^2}$$

c)
$$\frac{125^6.25^{-3}}{(5^2)^{-3}.25^7}$$

d)
$$\frac{12.10^{-3}.10^{-4}.10^{9}}{3.10^{-1}.10^{4}}$$

3. Simplifique cada expressão:

a)
$$2x^2(x^3)$$

b)
$$(3x)^2 \sqrt[3]{x}$$

$$c) \quad \frac{3x^2}{\left(x^{1/2}\right)^3}$$

d)
$$\frac{5x^4}{(x^2)^3}$$

e)
$$x^{-1}(2x^2)$$

$$f) \quad -\frac{\sqrt{x}}{5x^{-1}}$$

g)
$$\frac{x^4y^3}{x^2y^5}$$

h)
$$\frac{(3x^2)^2y^4}{3y^2}$$

i)
$$\frac{(x^{-3}y^2)^{-4}}{(y^6x^{-4})^{-2}}$$

4. Calcule as seguintes expressões algébricas, simplificando quando possível:

a)
$$(-3a^3x^2)(3ax^3)(-5a^4x^3)$$

b)
$$(3x^4y^2).(-2x^2y^3)-(-4x^6y^5)$$

c)
$$(3x - 2y)(3x + 2y)$$

d)
$$(x+1)^2 - (2x-2)^2 + (x-2)(x+2)$$

e)
$$(28a^4b^3 - 7a^3b^4) \div (-7a^2b^2)$$

f)
$$2(x^2 + x + 1) + 2(x^2 + 2x - 2) - (x^2 + 2x - 3)$$

Lista 1 - Respostas

1. Expressões....

a) 9

b) 32

c) 3/85

d) 16

2. Potências...

a) 32

b) 9

3. Simplificação...

a) $2x^5$

b) $9\sqrt[3]{x^7}$

c) $3\sqrt{x}$

d) $5x^{-2}$

e) 2*x*

4. Álgebra...

a) $45a^8x^8$

b) $-2x^6y^5$

c) $9x^2 - 4y^2$

e) -3/10

f) 3/8

g) 7/18

h) -2/3

c) 625

d) 2/5

f) $-\frac{\sqrt{x^3}}{5}$

g) $\frac{x^2}{y^2}$

h) $3x^4y^2$

i) x^4y^4

d) $-2x^2 + 10x - 7$

e) $-4a^2b + ab^2$

f) $3x^2 + 4x + 1$