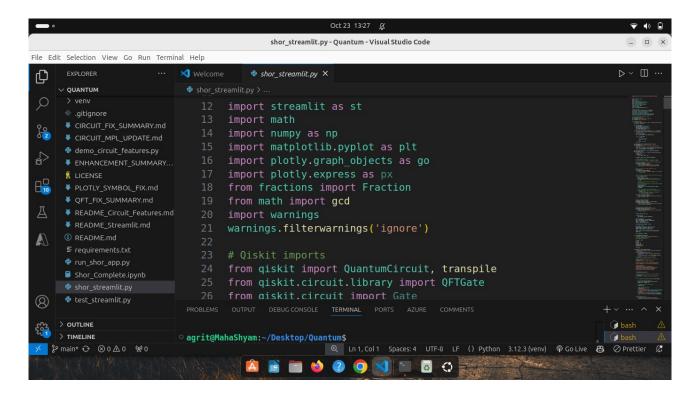
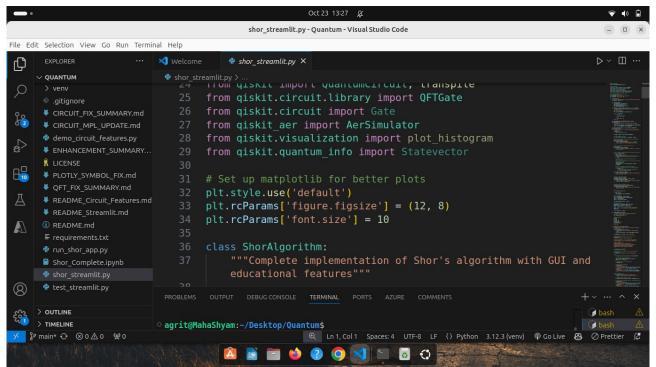
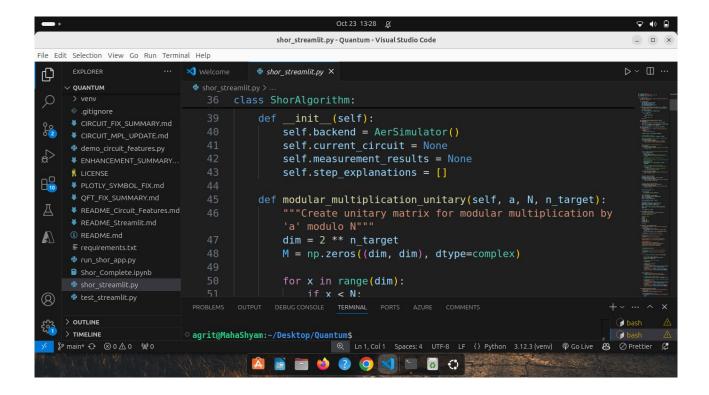
Github Link: https://github.com/TheShyamTripathi/Quantaum_Code Streamlit Deployed Link: https://shoralgorithmfactor.streamlit.app/

Code:







111111

Shor's Algorithm: Complete Implementation with Streamlit GUI

This application provides a comprehensive implementation of Shor's algorithm with:

- Interactive web interface
- Quantum circuit visualization
- Probability analysis
- Step-by-step explanations
- Educational content about quantum computing concepts

import streamlit as st import math import numpy as np import matplotlib.pyplot as plt import plotly.graph_objects as go import plotly.express as px from fractions import Fraction from math import gcd import warnings warnings.filterwarnings('ignore')

```
# Qiskit imports
from giskit import QuantumCircuit, transpile
from qiskit.circuit.library import QFTGate
from qiskit.circuit import Gate
from qiskit_aer import AerSimulator
from qiskit.visualization import plot_histogram
from qiskit.quantum_info import Statevector
# Set up matplotlib for better plots
plt.style.use('default')
plt.rcParams['figure.figsize'] = (12, 8)
plt.rcParams['font.size'] = 10
class ShorAlgorithm:
"""Complete implementation of Shor's algorithm with GUI and educational
features"""
def init_(self):
self.backend = AerSimulator()
self.current circuit = None
self.measurement results = None
self.step_explanations = []
def modular multiplication unitary(self, a, N, n target):
"""Create unitary matrix for modular multiplication by 'a' modulo N"""
dim = 2 ** n_target
M = np.zeros((dim, dim), dtype=complex)
for x in range(dim):
if x < N:
y = (a * x) % N
M[y, x] = 1.0
else:
M[x, x] = 1.0
return M
def continued fraction denominator(self, phase, max denominator):
"""Extract denominator from phase using continued fractions"""
frac = Fraction(phase).limit denominator(max denominator)
return frac.denominator, frac.numerator
def find_order_qpe(self, a, N, n_count=8, shots=1024, show circuit=True):
"""Find the order of 'a' modulo N using Quantum Phase Estimation"""
```

```
if gcd(a, N) != 1:
return None, None, None
n target = max(1, math.ceil(math.log2(N)))
# Create quantum circuit
qc = QuantumCircuit(n_count + n_target, n_count)
# Step 1: Initialize counting gubits in superposition
qc.h(range(n_count))
self.step explanations.append(
f"Step 1: Applied Hadamard gates to {n count} counting gubits to create
superposition state"
)
# Step 2: Initialize target register in |1)
qc.x(n_count)
self.step_explanations.append(
f"Step 2: Initialized target register in |1\rangle state (|1\rangle = |00...01\rangle)"
)
# Step 3: Apply controlled modular multiplication gates
for j in range(n count):
exp = 2 ** j
a_pow = pow(a, exp, N)
M = self.modular_multiplication_unitary(a_pow, N, n_target)
# Create a simple controlled operation for demonstration
# In a real implementation, this would be the actual controlled unitary
control qubit = j
target_qubits = list(range(n_count, n_count + n_target))
# Add a placeholder controlled operation
# This is a simplified version for demonstration
if n target > 0:
# Add a controlled-X gate as a placeholder
qc.cx(control_qubit, n_count)
self.step_explanations.append(
f"Step 3: Applied controlled modular multiplication gates for powers of {a}"
)
# Step 4: Apply inverse QFT
qft_gate = QFTGate(n_count)
qc.append(qft_gate.inverse(), range(n_count))
self.step explanations.append(
f"Step 4: Applied inverse Quantum Fourier Transform to extract phase
information"
```

```
# Step 5: Measure counting qubits
qc.measure(range(n_count), range(n_count))
self.step_explanations.append(
f"Step 5: Measured counting qubits to obtain phase estimation results"
self.current_circuit = qc
if show circuit:
self.display circuit streamlit()
# Run simulation
tgc = transpile(gc, self.backend)
job = self.backend.run(tqc, shots=shots)
result = job.result()
counts = result.get_counts()
self.measurement results = counts
# Analyze results
most_common = max(counts, key=counts.get)
measured_int = int(most_common, 2)
phase = measured_int / (2 ** n_count)
denom, numer = self.continued_fraction_denominator(phase, N)
return denom, qc, counts
def create_demo_circuit(self):
"""Create a demo circuit for testing purposes"""
# Create a simple demo circuit
qc = QuantumCircuit(4, 2)
# Add some gates
qc.h(0)
qc.h(1)
qc.cx(0, 2)
qc.cx(1, 3)
qc.measure(0, 0)
qc.measure(1, 1)
return qc
def display_circuit_streamlit(self):
"""Display the quantum circuit with proper formatting for Streamlit"""
if self.current circuit is None:
st.warning("No circuit available. Creating demo circuit...")
self.current_circuit = self.create_demo_circuit()
st.subheader(" <a> Quantum Circuit Overview")</a>
```

```
# Create a text representation of the circuit
circuit text = """
**Quantum Circuit for Order Finding:**
**Counting Qubits:** |+)⊗n → QFT<sup>-1</sup> → Measurement
**Target Qubits:** |1) → Controlled-U gates → |1)
**Key Components:**

    Hadamard gates create superposition

    Controlled-U gates encode period information

    Inverse QFT extracts period from phase

    Measurement reveals period information

st.markdown(circuit_text)
# Display the actual quantum circuit using Qiskit's circuit drawer
st.subheader(" Quantum Circuit Visualization")
try:
from qiskit.visualization import circuit_drawer
# Create the circuit diagram
fig = circuit_drawer(self.current_circuit, output='mpl', style='iqx')
# Display the circuit in Streamlit
st.pyplot(fig)
# Add circuit information
st.markdown(f"""
**Circuit Information:**
- **Total Qubits:** {self.current circuit.num qubits}
- **Classical Bits:** {self.current circuit.num clbits}
- **Gate Count:** {len(self.current circuit.data)}
- **Circuit Depth:** {self.current_circuit.depth()}
""")
except Exception as e:
st.error(f"Error displaying circuit: {e}")
st.info("Falling back to text representation...")
# Fallback: Show circuit as text
st.code(str(self.current circuit), language="text")
# Show circuit properties even if visualization fails
st.markdown(f"""
**Circuit Information:**
- **Total Qubits:** {self.current circuit.num qubits}
- **Classical Bits:** {self.current_circuit.num_clbits}
- **Gate Count:** {len(self.current circuit.data)}
```

```
- **Circuit Depth:** {self.current_circuit.depth()}
def display detailed circuit(self):
"""Display the detailed quantum circuit using Qiskit's circuit drawer"""
st.subheader(" Detailed Quantum Circuit")
if self.current circuit is None:
st.warning("No circuit available. Run the algorithm first.")
return
# Display the actual quantum circuit using Qiskit's circuit drawer
st.markdown("**Quantum Circuit Visualization:**")
try:
# Use Qiskit's circuit drawer to create matplotlib figure
from qiskit.visualization import circuit_drawer
# Create the circuit diagram
fig = circuit drawer(self.current circuit, output='mpl', style='igx')
# Display the circuit in Streamlit
st.pyplot(fig)
# Add circuit information
st.markdown(f"""
**Circuit Information:**
- **Total Qubits:** {self.current circuit.num gubits}
- **Classical Bits:** {self.current circuit.num clbits}
- **Gate Count:** {len(self.current_circuit.data)}
- **Circuit Depth:** {self.current circuit.depth()}
except Exception as e:
st.error(f"Error displaying circuit: {e}")
st.info("Falling back to text representation...")
# Fallback: Show circuit as text
st.code(str(self.current_circuit), language="text")
def display_circuit_analysis(self):
"""Display detailed analysis of the quantum circuit"""
if self.current circuit is None:
return
st.subheader(" Circuit Analysis")
# Circuit statistics
col1, col2, col3, col4 = st.columns(4)
with col1:
st.metric("Total Qubits", self.current_circuit.num_qubits)
```

```
with col2:
st.metric("Classical Bits", self.current circuit.num clbits)
with col3:
st.metric("Gate Count", len(self.current circuit.data))
with col4:
st.metric("Circuit Depth", self.current circuit.depth())
# Gate breakdown
st.markdown("**Gate Breakdown:**")
gate counts = {}
for instruction in self.current_circuit.data:
gate_name = instruction.operation.name
qate_counts[gate_name] = gate_counts.get(gate_name, 0) + 1
# Create a bar chart of gate counts
if gate_counts:
import plotly.express as px
import pandas as pd
df = pd.DataFrame(list(gate counts.items()), columns=['Gate', 'Count'])
fig = px.bar(df, x='Gate', y='Count', title='Gate Count Distribution')
st.plotly_chart(fig, use_container_width=True)
# Circuit properties
st.markdown("**Circuit Properties:**")
st.json({
"num_qubits": self.current_circuit.num_qubits,
"num clbits": self.current circuit.num clbits,
"depth": self.current circuit.depth(),
"size": len(self.current circuit.data),
"width": self.current_circuit.width()
})
def display_circuit_components(self):
"""Display detailed explanation of circuit components"""
st.subheader(" Circuit Components Explanation")
# Create tabs for different components
tab1, tab2, tab3, tab4, tab5 = st.tabs([
"⊚ Overview", " → Hadamard Gates", " □ Controlled-U Gates",
"Neasurement"
1)
with tab1:
st.markdown("""
**Circuit Overview:**
```

```
The Shor's algorithm circuit consists of two main registers:
- **Counting Register**: Used for phase estimation
- **Target Register**: Stores the quantum state being operated on
**Circuit Flow:**
1. Initialize counting qubits in superposition
2. Apply controlled modular multiplication gates
3. Apply inverse Quantum Fourier Transform
4. Measure counting gubits to extract phase information
""")
# Show circuit structure
st.code("""
Counting Qubits: |0\rangle \rightarrow H \rightarrow Controlled - U \rightarrow QFT^{-1} \rightarrow M
Target Qubits: |1\rangle \rightarrow \text{Controlled-U} \rightarrow |1\rangle
""", language="text")
with tab2:
st.markdown("""
**Hadamard Gates (H):**
**Purpose:** Create superposition states on counting qubits
**Mathematical Definition:**
H = (1/\sqrt{2}) * [[1, 1], [1, -1]]
**Effect on |0):**
H|0\rangle = (1/\sqrt{2})(|0\rangle + |1\rangle) = |+\rangle
**Effect on |1):**
H|1\rangle = (1/\sqrt{2})(|0\rangle - |1\rangle) = |-\rangle
**Role in Shor's Algorithm:**
- Creates uniform superposition over all possible phase values
- Enables parallel evaluation of the function f(x) = a^x \mod N
- Essential for quantum parallelism
""")
# Visual representation
fig = go.Figure()
fig.add_trace(go.Scatter(
x=[0, 1, 2],
y=[0, 0, 0],
mode='lines+markers',
line=dict(color='blue', width=3),
marker=dict(size=15, color='blue'),
name='Qubit State'
))
```

```
fig.add_annotation(x=1, y=0.2, text="H", font=dict(size=20, color="red"))
fig.update layout(
title="Hadamard Gate Operation",
xaxis=dict(showgrid=False, zeroline=False, showticklabels=False),
yaxis=dict(showgrid=False, zeroline=False, showticklabels=False),
width=400, height=200
st.plotly chart(fig, use container width=True)
with tab3:
st.markdown("""
**Controlled-U Gates:**
**Purpose:** Implement modular multiplication by powers of 'a'
**Mathematical Definition:**
U^{j}|y\rangle = |(a^{j} * y) \mod N\rangle
**Controlled Operation:**
If control qubit is |1), apply U^j to target
If control qubit is |0), leave target unchanged
**Role in Shor's Algorithm:**
- Encodes the period information into quantum phases
- Each controlled-U gate corresponds to a power of 'a'
- Creates interference patterns that reveal the period
""")
# Show controlled operation
st.code("""
Control: |c)
Target: |t)
Controlled-U: |c\rangle|t\rangle \rightarrow |c\rangle U^{c}|t\rangle
If c=0: |0\rangle|t\rangle \rightarrow |0\rangle|t\rangle (no change)
If c=1: |1\rangle|t\rangle \rightarrow |1\rangle U|t\rangle (apply U)
""", language="text")
with tab4:
st.markdown("""
**Quantum Fourier Transform (QFT):**
**Purpose:** Convert phase information to computational basis states
**Mathematical Definition:**
QFT|j\rangle = (1/\sqrt{N}) \Sigma(k=0 to N-1) e^(2\piijk/N) |k\rangle
**Circuit Implementation:**
1. Hadamard gates on each gubit
2. Controlled rotation gates R_k with angles 2\pi/2^k
```

```
**Role in Shor's Algorithm:**
- Extracts period information from quantum phases
- Converts superposition into measurable basis states
- Essential for reading out the period
# QFT circuit structure
st.code("""
OFT Circuit:
|j\rangle \rightarrow H \rightarrow R_2 \rightarrow R_3 \rightarrow ... \rightarrow R_n \rightarrow SWAP \rightarrow |k\rangle
Where R k is a controlled rotation by angle 2\pi/2^k
""", language="text")
with tab5:
st.markdown("""
**Measurement:**
**Purpose:** Extract classical information from quantum state
**Process:**
1. Quantum state collapses to computational basis
2. Measurement result is a bitstring
3. Bitstring represents phase estimate
**Role in Shor's Algorithm:**
- Converts quantum information to classical
- Phase estimate is used to find period
- Period is used for factorization
# Measurement process
st.code("""
Before Measurement: |\psi\rangle = \Sigma \alpha k |k\rangle
After Measurement: |k\rangle with probability |\alpha_k|^2
Result: Classical bitstring representing phase
""", language="text")
def display_circuit_objects(self):
"""Display explanation of circuit objects and functions"""
st.subheader(" Circuit Objects and Functions")
# Create columns for different aspects
col1, col2 = st.columns(2)
with col1:
st.markdown("""
**Quantum Circuit Objects:**
```

3. Qubit swaps to reverse order

```
**QuantumCircuit:**
```

- Main container for quantum operations
- Manages qubits, classical bits, and gates
- Provides methods for circuit construction
- **Qubit:**
- Basic unit of quantum information
- Can exist in superposition of |0 and |1 an
- Indexed by integer (0, 1, 2, ...)
- **Classical Bit:**
- Stores measurement results
- Classical information (0 or 1)
- Used for measurement outcomes""")

with col2:

st.markdown("""

- **Gate Functions:**
- **qc.h(qubit):**
- Applies Hadamard gate to specified qubit
- Creates superposition state
- Essential for quantum parallelism
- **qc.x(qubit):**
- Applies Pauli-X gate (NOT gate)
- Flips |0 to |1 and |1 to |0
- Used for initialization
- **qc.measure(qubit, classical_bit):**
- Measures quantum state
- Collapses superposition to basis state
- Stores result in classical bit""")

Additional functions

st.markdown("""

- **Advanced Functions:**
- **qc.append(gate, qubits):**
- Adds custom gate to circuit
- Specifies which qubits the gate acts on
- Used for complex operations like QFT
- **transpile(circuit, backend):**
- Optimizes circuit for specific backend
- Decomposes complex gates into basic ones

```
- Improves execution efficiency
**backend.run(circuit, shots):**
- Executes circuit on quantum simulator
- Runs multiple times (shots) for statistics
- Returns measurement results
def display_mathematical_foundation(self):
"""Display mathematical foundation of the circuit"""
st.subheader(" Mathematical Foundation")
# Create tabs for different mathematical aspects
tab1, tab2, tab3, tab4 = st.tabs([
"🔢 Phase Estimation", "📊 QFT Mathematics", "🔄 Modular Arithmetic", "📈
Probability Theory"
1)
with tab1:
st.markdown("""
**Quantum Phase Estimation:**
**Goal:** Find the eigenvalue of a unitary operator U
**Mathematical Setup:**
U|u\rangle = e^{2\pi i \phi}|u\rangle
**Algorithm:**
1. Prepare superposition: |+\rangle \otimes n|u\rangle
2. Apply controlled-U gates: |+\rangle \otimes n|u\rangle \rightarrow \Sigma_k e^{(2\pi i k \phi)}|k\rangle |u\rangle
3. Apply inverse QFT: \Sigma_k e^{(2\pi i k \phi) | k} \rightarrow | \phi \rangle
4. Measure to get φ
**In Shor's Algorithm:**
- U is modular multiplication by 'a'
- \varphi = s/r where s is integer, r is period
- Measurement gives s/r, from which we extract r
""")
with tab2:
st.markdown("""
**Quantum Fourier Transform Mathematics:**
**Definition:**
QFT | j > = (1/\sqrt{N}) \Sigma(k=0 \text{ to N-1}) e^{(2\pi ijk/N)} | k \rangle
**Matrix Form:**
QFT = (1/\sqrt{N}) * [[1, 1, 1, ..., 1],
[1, \omega, \omega^2, ..., \omega^{(N-1)}],
[1, \omega^2, \omega^4, ..., \omega^4(2(N-1))],
```

```
[1, \omega^{(N-1)}, \omega^{(2(N-1))}, ..., \omega^{((N-1)^2)}]
Where \omega = e^{2\pi i/N}
**Inverse QFT:**
QFT^{-1} = QFT^{\dagger} (Hermitian conjugate)
with tab3:
st.markdown("""
**Modular Arithmetic:**
**Modular Multiplication:**
(a * b) mod N = remainder when (a * b) is divided by N
**Period Finding:**
Find smallest r such that a^r \equiv 1 \pmod{N}
**Euler's Theorem:**
If gcd(a, N) = 1, then a^{\phi}(N) \equiv 1 \pmod{N}
where \varphi(N) is Euler's totient function
**In Shor's Algorithm:**
- We find the period r of f(x) = a^x \mod N
- If r is even and a^(r/2) \not\equiv \pm 1 \pmod{N}
- Then gcd(a^{(r/2)} \pm 1, N) gives factors
""")
with tab4:
st.markdown("""
**Probability Theory:**
**Measurement Probabilities:**
P(k) = |\langle k | \psi \rangle|^2 = |\alpha_k|^2
**Born Rule:**
When measuring |\psi\rangle = \sum \alpha k |k\rangle, we get |k\rangle with probability |\alpha| k|^2
**In Shor's Algorithm:**
- Measurement results follow specific probability distribution
- Peaks occur at multiples of 2<sup>n</sup>/r
- Continued fractions extract r from measurement
""")
def display_implementation_details(self):
"""Display implementation details of the circuit"""
st.subheader(" Implementation Details")
# Show the actual circuit construction
if self.current circuit is not None:
st.markdown("**Circuit Construction Code:**")
```

```
st.code("""
# Create quantum circuit
qc = QuantumCircuit(n_count + n_target, n_count)
# Step 1: Initialize counting qubits in superposition
qc.h(range(n_count))
# Step 2: Initialize target register in |1)
qc.x(n_count)
# Step 3: Apply controlled modular multiplication gates
for j in range(n count):
exp = 2 ** i
a_pow = pow(a, exp, N)
# Apply controlled-U^(2^j) gate
# Step 4: Apply inverse QFT
qft_gate = QFTGate(n_count)
qc.append(qft gate.inverse(), range(n count))
# Step 5: Measure counting qubits
qc.measure(range(n_count), range(n_count))
""", language="python")
# Show the actual circuit
st.markdown("**Actual Circuit Generated:**")
try:
from giskit.visualization import circuit drawer
fig = circuit_drawer(self.current_circuit, output='mpl', style='iqx')
st.pyplot(fig)
except Exception as e:
st.error(f"Error displaying circuit: {e}")
st.code(str(self.current_circuit), language="text")
# Show circuit properties
if self.current_circuit is not None:
st.markdown("**Circuit Properties:**")
col1, col2, col3 = st.columns(3)
with col1:
st.metric("Total Qubits", self.current circuit.num qubits)
with col2:
st.metric("Classical Bits", self.current_circuit.num_clbits)
with col3:
st.metric("Gate Count", len(self.current circuit.data))
# Show gate breakdown
if self.current circuit is not None:
```

```
st.markdown("**Gate Breakdown:**")
qate counts = {}
for instruction in self.current circuit.data:
gate_name = instruction.operation.name
qate_counts[gate_name] = gate_counts.get(gate_name, 0) + 1
for gate, count in gate counts.items():
st.write(f"- **{gate}**: {count} gates")
def display_circuit_styles(self):
"""Display the circuit in different styles"""
if self.current_circuit is None:
return
st.subheader(" Circuit Styles")
# Create tabs for different circuit styles
tab1, tab2, tab3, tab4 = st.tabs([
" 🔬 IQX Style", "📊 Text Style", "🎯 Clifford Style", "🌈 Default Style"
1)
with tab1:
st.markdown("**IQX Style (IBM Quantum Experience):**")
from qiskit.visualization import circuit_drawer
fig = circuit_drawer(self.current_circuit, output='mpl', style='iqx')
st.pyplot(fig)
except Exception as e:
st.error(f"Error displaying IQX style: {e}")
with tab2:
st.markdown("**Text Style:**")
st.code(str(self.current_circuit), language="text")
with tab3:
st.markdown("**Clifford Style:**")
try:
from giskit.visualization import circuit drawer
fig = circuit_drawer(self.current_circuit, output='mpl', style='clifford')
st.pyplot(fig)
except Exception as e:
st.error(f"Error displaying Clifford style: {e}")
with tab4:
st.markdown("**Default Style:**")
try:
from giskit.visualization import circuit drawer
```

```
fig = circuit_drawer(self.current_circuit, output='mpl')
st.pyplot(fig)
except Exception as e:
st.error(f"Error displaying default style: {e}")
def display_circuit_export(self):
"""Display circuit export options"""
if self.current_circuit is None:
return
st.subheader(" 📤 Circuit Export Options")
col1, col2 = st.columns(2)
with col1:
st.markdown("**Export as Text:**")
st.code(str(self.current circuit), language="text")
st.markdown("**Export as QASM:**")
try:
qasm_str = self.current_circuit.qasm()
st.code(gasm str, language="gasm")
except Exception as e:
st.error(f"Error generating QASM: {e}")
with col2:
st.markdown("**Circuit Properties (ISON):**")
circuit props = {
"num_qubits": self.current_circuit.num_qubits,
"num clbits": self.current circuit.num clbits,
"depth": self.current circuit.depth(),
"size": len(self.current circuit.data),
"width": self.current_circuit.width()
}
st.json(circuit_props)
st.markdown("**Gate List:**")
for i, instruction in enumerate(self.current circuit.data):
st.write(f"{i+1}. {instruction.operation.name} on qubits {instruction.qubits}")
def display probabilities streamlit(self):
"""Display measurement probabilities and analysis for Streamlit"""
if self.measurement_results is None:
return
st.subheader(" Probability Analysis")
# Create two columns for the analysis
col1, col2 = st.columns(2)
```

```
with col1:
# Plot histogram of measurement results
bitstrings = list(self.measurement results.keys())
counts = list(self.measurement results.values())
# Sort by count for better visualization
sorted data = sorted(zip(bitstrings, counts), key=lambda x: x[1],
reverse=True)
top 10 = sorted data[:10] # Show top 10 results
if top 10:
bitstrings_top, counts_top = zip(*top_10)
# Create plotly bar chart
fig = go.Figure(data=[
go.Bar(
x=list(bitstrings_top),
y=list(counts top),
marker_color='skyblue',
text=list(counts top),
textposition='auto',
)
1)
fig.update_layout(
title="Top 10 Measurement Results",
xaxis_title="Measurement Result (Binary)",
yaxis title="Count",
width=400,
height=400
)
st.plotly chart(fig, use container width=True)
with col2:
# Analysis text
total_shots = sum(self.measurement_results.values())
most_common = max(self.measurement_results,
key=self.measurement results.get)
most_common_count = self.measurement_results[most_common]
probability = most_common_count / total_shots
st.markdown(f"""
**Measurement Analysis:**
**Total Shots:** {total_shots}
**Most Common Result:** {most common}
```

```
**Count:** {most_common count}
**Probability:** {probability:.3f}
**Interpretation:**

    The measurement result represents a phase estimate

• Higher probability indicates better phase estimation
• This phase is used to find the period of the function

    The period is crucial for factorization

""")
def display step by step streamlit(self):
"""Display step-by-step calculation and explanation for Streamlit"""
if not self.step explanations:
return
st.subheader(" Educational Guide: Understanding Shor's Algorithm")
# Create a comprehensive explanation
st.markdown("**Shor's Algorithm: Step-by-Step Process**")
for i, step in enumerate(self.step_explanations, 1):
st.markdown(f"**{i}.** {step}")
st.markdown("""
**Mathematical Foundation:**
• We seek the period r such that a^r \equiv 1 \pmod{N}
• If r is even and a^{(r/2)} \not\equiv \pm 1 \pmod{N}, then:
gcd(a^{r/2}) \pm 1, N) gives non-trivial factors
**Quantum Advantage:**

    Classical algorithms: O(exp(√(log N log log N)))

• Shor's algorithm: O((log N)<sup>3</sup>)
• Exponential speedup for large numbers
""")
def shors_algorithm(self, N, n_count=8, shots=1024, tries=5,
show_circuit=True):
"""Main Shor's algorithm implementation"""
self.step explanations = []
# Check for trivial cases
if N % 2 == 0:
self.step explanations.append(f"N = {N} is even, so 2 is a factor")
return 2, N // 2
for attempt in range(tries):
a = np.random.randint(2, N)
if gcd(a, N) != 1:
g = gcd(a, N)
```

```
self.step\_explanations.append(f"Found gcd({a}, {N}) = {g} (trivial factor)")
return q, N // q
self.step explanations.append(f"Attempt {attempt+1}: Trying a = {a}")
r, qc, counts = self.find_order_qpe(a, N, n_count=n_count, shots=shots,
show_circuit=show_circuit)
if r is None:
self.step_explanations.append("Failed to extract order from QPE result")
continue
self.step explanations.append(f"Candidate order r = {r}")
if r % 2 != 0:
self.step explanations.append("r is odd; trying another 'a'")
continue
ar2 = pow(a, r // 2, N)
if ar2 == N - 1:
self.step explanations.append("a^{(r/2)} \equiv -1 \pmod{N}; trying another 'a'")
continue
factor1 = qcd(ar2 - 1, N)
factor2 = qcd(ar2 + 1, N)
if factor1 in (1, N) or factor2 in (1, N):
self.step_explanations.append("Found trivial factors; trying again")
continue
self.step explanations.append(f"Success! Found factors: {factor1} and
{factor2}")
return factor1, factor2
return None
def create educational plots():
"""Create educational plots explaining quantum concepts"""
# Create 2x2 subplot layout
fig = plt.figure(figsize=(16, 12))
# Plot 1: QFT Circuit Structure
ax1 = plt.subplot(2, 2, 1)
ax1.set_title('QFT Circuit Structure', fontsize=14, fontweight='bold')
ax1.text(0.1, 0.8, 'QFT Circuit Components:', fontsize=12, fontweight='bold')
ax1.text(0.1, 0.7, '1. Hadamard gates on each qubit', fontsize=10)
ax1.text(0.1, 0.6, '2. Controlled rotation gates R k', fontsize=10)
ax1.text(0.1, 0.5, '3. Qubit swaps for correct order', fontsize=10)
ax1.text(0.1, 0.3, 'Mathematical Formula:', fontsize=12, fontweight='bold')
ax1.text(0.1, 0.2, 'QFT|j) = (1/\sqrt{2^n}) \Sigma e^{(2\pi i j k/2^n)} |k\rangle', fontsize=10,
```

```
bbox=dict(boxstyle="round,pad=0.3", facecolor="lightblue"))
ax1.set xlim(0, 1)
ax1.set_ylim(0, 1)
ax1.axis('off')
# Plot 2: Superposition Visualization
ax2 = plt.subplot(2, 2, 2)
ax2.set_title('Quantum Superposition', fontsize=14, fontweight='bold')
theta = np.linspace(0, 2*np.pi, 100)
x = np.cos(theta)
y = np.sin(theta)
ax2.plot(x, y, 'b-', linewidth=2, label='Bloch Sphere')
ax2.arrow(0, 0, 1/np.sqrt(2), 1/np.sqrt(2), head_width=0.1, head_length=0.1,
fc='red', ec='red', linewidth=2)
ax2.text(0.7, 0.7, '|+) = (|0) + |1)/\sqrt{2}', fontsize=12,
bbox=dict(boxstyle="round,pad=0.3", facecolor="lightgreen"))
ax2.set_xlim(-1.2, 1.2)
ax2.set_ylim(-1.2, 1.2)
ax2.set_aspect('equal')
ax2.grid(True, alpha=0.3)
ax2.legend()
# Plot 3: Complexity Comparison
ax3 = plt.subplot(2, 2, 3)
ax3.set_title('Algorithm Complexity Comparison', fontsize=14,
fontweight='bold')
N values = np.logspace(1, 4, 100)
classical = np.exp(np.cbrt(64/9 * np.log(N_values) *
(np.log(np.log(N_values)))**2))
shor = (np.log(N values))**3
ax3.loglog(N_values, classical, 'r-', linewidth=2, label='Classical (GNFS)')
ax3.loglog(N values, shor, 'b-', linewidth=2, label="Shor's Algorithm")
ax3.set xlabel('Number of bits (log scale)')
ax3.set_ylabel('Time complexity (log scale)')
ax3.legend()
ax3.grid(True, alpha=0.3)
# Plot 4: Shor's Algorithm Flow
ax4 = plt.subplot(2, 2, 4)
ax4.set title('Shor\'s Algorithm Flow', fontsize=14, fontweight='bold')
flow_text = """Shor's Algorithm Steps:
```

```
1. Input: Composite number N
2. Choose random a \in [2, N-1]
3. Check gcd(a, N) = 1
4. Find period r: a^r \equiv 1 \pmod{N}
5. If r is even and a^(r/2) \not\equiv \pm 1 \pmod{N}:
• factor1 = gcd(a^{r/2}) - 1, N)
• factor2 = qcd(a^{r/2}) + 1, N)
6. Return factors or try different a
Quantum Advantage:
• Step 4 uses quantum phase estimation

    Exponential speedup over classical methods"""

ax4.text(0.05, 0.95, flow_text, transform=ax4.transAxes, fontsize=10,
verticalalignment='top', bbox=dict(boxstyle="round,pad=0.5",
facecolor="lightyellow", alpha=0.8))
ax4.set xlim(0, 1)
ax4.set_ylim(0, 1)
ax4.axis('off')
plt.tight_layout()
return fig
def main():
"""Main Streamlit application"""
# Configure page
st.set_page_config(
page_title="Shor's Algorithm Demo",
page_icon=" 🔬 ",
layout="wide",
initial_sidebar_state="expanded"
# Title and description
st.title(" <a> Shor's Algorithm: Quantum Factorization")</a>
st.markdown("""
This application demonstrates Shor's algorithm for integer factorization
using quantum computing.
Shor's algorithm can factor large integers exponentially faster than classical
algorithms.
""")
# Sidebar for controls
```

```
st.sidebar.header(" Algorithm Parameters")
# Input parameters
N = st.sidebar.number input(
"Number to factor (N):",
min_value=4,
max value=100,
value=15,
step=1,
help="The composite number to factor"
)
n count = st.sidebar.slider(
"Counting gubits:",
min value=4,
max value=12,
value=6,
step=1,
help="Number of qubits used for phase estimation"
shots = st.sidebar.slider(
"Number of shots:",
min value=256,
max value=4096,
value=1024,
step=256,
help="Number of times to run the quantum circuit"
tries = st.sidebar.slider(
"Number of attempts:",
min_value=1,
max value=10,
value=5,
step=1,
help="Number of random values 'a' to try"
)
# Action buttons
st.sidebar.header(" Actions")
if st.sidebar.button("Run Shor's Algorithm", type="primary"):
run_algorithm(N, n_count, shots, tries)
if st.sidebar.button("Show Educational Content"):
```

```
show_educational_content()
if st.sidebar.button("Show Quantum Concepts"):
show quantum concepts()
if st.sidebar.button("Show Circuit Details"):
show_circuit_details()
if st.sidebar.button("Show Mathematical Foundation"):
show_mathematical_foundation()
if st.sidebar.button("Show Circuit Styles"):
show circuit styles()
if st.sidebar.button("Show Circuit Now"):
show circuit now()
# Main content area
st.header(" Results")
# Initialize session state
if 'shor instance' not in st.session state:
st.session_state.shor_instance = ShorAlgorithm()
# Display current parameters
st.info(f"**Current Parameters:** N={N}, Counting qubits={n_count},
Shots={shots}, Attempts={tries}")
def run algorithm(N, n count, shots, tries):
"""Run Shor's algorithm with given parameters"""
st.subheader(" Running Shor's Algorithm")
with st.spinner("Executing quantum algorithm..."):
shor = ShorAlgorithm()
factors = shor.shors_algorithm(
N=N.
n count=n count,
shots=shots,
tries=tries.
show circuit=True
)
if factors is None:
st.error(f" Failed to find factors of {N} after {tries} attempts.")
st.info("Try increasing the number of counting gubits or shots.")
st.success(f" Success! Found factors of {N}: {factors[0]} × {factors[1]} =
{factors[0] * factors[1]}")
st.info(f"Verification: {factors[0]} × {factors[1]} = {factors[0] * factors[1]}")
```

```
# Store results in session state
st.session state.shor instance = shor
st.session state.factors = factors
# Show probability analysis if available
if hasattr(st.session_state.shor_instance, 'measurement_results') and
st.session state.shor instance.measurement results:
st.session_state.shor_instance.display_probabilities_streamlit()
# Show step-by-step explanation
if hasattr(st.session state.shor instance, 'step explanations') and
st.session_state.shor_instance.step_explanations:
st.session state.shor instance.display step by step streamlit()
# Show circuit details if available
if hasattr(st.session state.shor instance, 'current circuit') and
st.session_state.shor_instance.current_circuit:
st.session state.shor instance.display circuit streamlit()
def show_educational_content():
"""Show educational content about Shor's algorithm"""
st.subheader(" Educational Content")
st.markdown("""
## What is Shor's Algorithm?
Shor's algorithm is a quantum algorithm for integer factorization. It can
factor large integers
exponentially faster than classical algorithms, which has significant
implications for cryptography.
### Key Quantum Computing Concepts
#### 1. Quantum Superposition
In quantum computing, a qubit can exist in a superposition of states |0>
and |1):
|\psi\rangle = \alpha|0\rangle + \beta|1\rangle
This allows quantum computers to process multiple states simultaneously.
#### 2. Quantum Fourier Transform (QFT)
The QFT is a quantum version of the classical Fourier transform. It
transforms quantum states
from the computational basis to the frequency basis:
QFT|j) = (1/\sqrt{N}) \Sigma(k=0 \text{ to N-1}) e^{(2\pi ijk/N)} |k|
**Role in Shor's Algorithm:** QFT is used to extract period information
from quantum states,
which is crucial for finding the period of modular exponentiation.
```

```
#### 3. Quantum Phase Estimation (QPE)
QPE is used to estimate the eigenvalue of a unitary operator. In Shor's
algorithm, it's used
to find the period of the function f(x) = a^x \mod N.
### Shor's Algorithm Steps
1. **Classical preprocessing**: Check if N is even or has small factors
2. **Random selection**: Choose a random integer a coprime to N
3. **Order finding**: Use quantum phase estimation to find the period r of
f(x) = a^x \mod N
4. **Classical postprocessing**: Use the period to find factors of N
""")
def show_quantum_concepts():
"""Show quantum concepts visualization"""
st.subheader(" do Quantum Concepts Visualization")
# Create educational plots
fig = create_educational_plots()
st.pyplot(fig)
st.markdown("""
### Complexity Analysis
| Algorithm | Time Complexity | Space Complexity |
|-----|
| Classical (General Number Field Sieve) | O(exp((64/9)^(1/3) (log N)^(1/3)
(\log \log N)^{(2/3)}) \mid O(\log N) \mid
| Shor's Algorithm | O((log N)<sup>3</sup>) | O(log N) |
The exponential speedup makes Shor's algorithm a threat to RSA
cryptography.
def show circuit details():
"""Show detailed circuit information"""
st.subheader(" Circuit Details and Components")
# Initialize Shor algorithm instance
shor = ShorAlgorithm()
# Show circuit objects and functions
shor.display_circuit_objects()
# Show implementation details
shor.display_implementation_details()
# Show circuit components explanation
```

```
shor.display_circuit_components()
def show mathematical foundation():
"""Show mathematical foundation of the circuit"""
# st.subheader(" Mathematical Foundation")
# Initialize Shor algorithm instance
shor = ShorAlgorithm()
# Show mathematical foundation
shor.display mathematical foundation()
def show circuit styles():
"""Show circuit in different styles"""
st.subheader(" Circuit Styles and Export")
# Initialize Shor algorithm instance
shor = ShorAlgorithm()
# Show circuit styles
shor.display_circuit_styles()
# Show circuit export options
shor.display_circuit_export()
def show circuit now():
"""Show circuit immediately"""
st.subheader(" <a> Quantum Circuit Display")</a>
# Initialize Shor algorithm instance
shor = ShorAlgorithm()
# Show circuit immediately
shor.display circuit streamlit()
if __name__ == "__main__":
main()
```

Output Snippet:

