

# Neural Scene Flow Fields for Space-Time View Synthesis of Dynamic Scenes

## Related Work

view synthesis nerf (static) { kernels btw two images  
 novel time synthesis { optical flow, warping features  
 ? layered  
 space-time view synthesis scene change with time  
 { illumination changes; previous relighting work only assume static  
 { 3D scene motion: previous require multi-view, time synchronised as input

## Approach

Neural scene flow fields for dynamic scenes (NSFF, the dynamic version of nerf)

recall:  $C(x, d) = F_{\theta}(x, d)$  # nerf takes a position, a direction, outputs a rgb, a density.

now:  $(C_i, f_i, W_i) = F_{\theta}^{dyn}(x, d, i)$  # nsff<sup>dyn</sup> takes additionally a time  $i$ , outputs additionally:

$f_i = (f_{i \rightarrow i+1}, f_{i \rightarrow i-1})$  # 3D scene flow, offset of location  $x$  @  $i-1, i+1$   
 $W_i = (w_{i \rightarrow i+1}, w_{i \rightarrow i-1})$  # 1D disocclusion weights  $W_i$ , details below

Optimization core of nsff. to understand this paper from THE NEW LOSS

temporal photometric consistency scene @  $i$  should be consistent with scene @  $j \in \mathcal{N}(i)$ , if neighbor scene got from nsff.

$\hat{C}_{j \rightarrow i}(r; i) = \int_{t_w}^t T(t) g(r; i, j, t) C_j(r; i, j, t) dt$  where  $r; i, j, t = r(t) + f_{i \rightarrow j}(r; i, t)$  noticing  $t$  is distance (consider as a position is good) # color for  $r$  is from time neighbors  
 roughly:  $L_{pho} = \sum_{r_i} \sum_{j \in \mathcal{N}(i)} \|\hat{C}_{j \rightarrow i}(r; i) - C_i(r; i)\|_2^2$  # ray-wise, all neighbors should render same as ground truth for a single pixel

However, this is not always correct for neighboring, # motion causes 3D disocclusion regions, this is ambiguity. Or to say:

So, results from neighbors should be weighted (not always average)

you cannot ask neighbors render exact same! what if there is occlusion/disocclusion?

Weights for each neighbor:  $\hat{W}_{j \rightarrow i}(r; i) = \int_{t_w}^t T(t) g(r; i, j, t) W_j(r; i, j, t) dt$  # you should be noticing rgb is function of direction, but this weight is not  
 [0,1] to 1 # for all pixels, your render results should be weighted neighbor-consistent.

the final:  $L_{pho} = \sum_{r_i} \sum_{j \in \mathcal{N}(i)} \hat{W}_{j \rightarrow i}(r; i) \|\hat{C}_{j \rightarrow i}(r; i) - C_i(r; i)\|_2^2 + \beta_w \sum_{r_i} \|\hat{W}_{j \rightarrow i}(r; i) - 1\|_1$  # for all rays, your render points should have everywhere close-to-1 weights  
 for all pixels each ray for all rays each position #  $\beta_w$ : reg weight (=0.1),  $\mathcal{N}(i) = 5$  (i.e. chained)  
 #  $j=i$ : self case,  $\hat{W}_{i \rightarrow i}(r; i) = 1, f_{i \rightarrow i} = 0, \hat{C}_{i \rightarrow i}(r; i) = \hat{C}_i(r; i)$ , original case.

Scene flow priors points back & forth with nsff should be consistent with each other

$x_i$  have forward scene flow  $f_{i \rightarrow j}$ , gives point  $x_{i \rightarrow j} = x_i + f_{i \rightarrow j}$

$x_i \xrightarrow{f_{i \rightarrow j}} x_j (=x_{i \rightarrow j})$  this has to be true  $f_{i \rightarrow j}(x_i) + f_{j \rightarrow i}(x_j) = f_{i \rightarrow j}(x_i) + f_{j \rightarrow i}(x_{i \rightarrow j}) = 0$   
 no need to really bother  $j$  now

you are predicting next  $x$  position with forward flow, then take the new next position. Naturally, should the new position take one step back at exactly  $x$ .

$L_{cyc} = \sum_{r_i} \sum_{j \in \mathcal{N}(i)} w_{ij} \|f_{i \rightarrow j}(x_i) + f_{j \rightarrow i}(x_{i \rightarrow j})\|_1$  # for each position, this should be true always, only closest neighbors 2

data-driven priors results better consistent with other methods w.r.t. positions

geometric consistency 2D optical flow guides 3D scene flow fields

optical flow methods give a next-time 2D position, nsff gives a 3D position but we do projection. They should be same.

2D optical flow  $P_{i \rightarrow j} = P_i + u_{i \rightarrow j}$  (Given By OF methods)

3D nsff for one ray  $r_i$ , we volume render the  $f_{i \rightarrow j}$  and  $x_i$

# recall how we compute depth? recall volume render seems apply everything

$\hat{F}_{i \rightarrow j}(r; i) = \int_{t_w}^t T(t) g(r; i, j, t) f_{i \rightarrow j}(r; i, t) dt$  } next world position:  $\hat{X}_i(r; i) + \hat{F}_{i \rightarrow j}(r; i)$ , then, do projection to frame at time  $j$ .  
 $\hat{X}_i(r; i) = \int_{t_w}^t T(t) g(r; i, j, t) x_i(r; i, t) dt$  }  $\hat{P}_{i \rightarrow j}(r; i) = \mathcal{P}(K(R^j, t^j) (\hat{X}_i(r; i) + \hat{F}_{i \rightarrow j}(r; i)) + t^j)$  {  $[R^j, t^j]$ : extrinsic at time  $j$  # world position (trained from nerf/nsff)  
 $K$ : intrinsic shared to camera position.

$L_{geo} = \sum_{r_i} \sum_{j \in \mathcal{N}(i)} \|\hat{P}_{i \rightarrow j}(r; i) - P_{i \rightarrow j}(r; i)\|_1$  # for all pixels/each ray result, it should be same.

single-view depth monodepth prediction guides

$L_z = \sum_{r_i} \|\hat{Z}_i^*(r; i) - Z_i^*(r; i)\|_1$  # check the supp for real implementation here.

**Integrating a static scene representation** differentiate background static and foreground dynamic then combine

static background scene:  $(c, G, V) = F_{\theta}^{st}(x, d)$  # static/dyn balance:  $V$  (fyi, this is not a necessarily trained param)

dynamic foreground scene:  $(c_i, G_i, F_i, W_i) = F_{\theta}^{dy}(x, d, i)$  # blending weight  $V$  is actually  $V = f(c, G_i)$

Combined rendering equation:  $\hat{C}_i^{cb}(r_i) = \int_{t_{in}}^{t_f} T_i^{cb}(ct) \underbrace{G_i^{cb}(cb) c_i^{cb}(ct)}_{\text{a weighted render}} dt$

$$L_{cb} = \sum_i \| \hat{C}_i^{cb}(r_i) - C_i(r_i) \|_2^2$$

# this is a PURE color render, basically has a PURE nerf for background, and a nsff for foreground.  
we don't render with neighbor information!

**Regularisation**

**Spatial smoothness** points along ray should have neighboring similar scene flow

$$L_{sp} = \sum_i \sum_{y_i \in M(x_i)} \sum_{j \in \mathcal{N}_i} \exp(-\lambda \|x_i, y_i\|_2) \exp(-\lambda \|f_{i \rightarrow j}(x_i) - f_{i \rightarrow j}(y_i)\|_1)$$

# for each ray, considering each point

**Temporal smoothness** backward and forward should equal # for some reason

$$L_{temp} = \frac{1}{2} \sum_i \| f_{i \rightarrow i+1}(x_i) + f_{i+1 \rightarrow i}(x_i) \|_2^2$$

# for each point

**Sf minimal** encourage sf to be low # cause frames are continuous

$$L_{min} = \sum_i \sum_{j \in \mathcal{N}_i} \| f_{i \rightarrow j}(x_i) \|_1$$

FINALLY

$$L = L_{cb} + L_{pno} + \beta^1 L_{cyc} + \beta^2 L_{data} + \beta^3 L_{reg}$$

$$\text{where } \begin{cases} L_{data} = L_{geo} + \beta_2 L_2 \\ L_{reg} = L_{sp} + L_{temp} + L_{min} \end{cases}$$

**rendering** the splatting-based plane-sweep volume rendering approach # render with changing time, not view

to render intermediate time  $i + \delta_i, \delta_i \in (0, 1)$ , sweep over every step  $t$  (a location along the ray)

for one point  $\begin{cases} \text{query } i \text{ and get: } (c_i, G_i)(F_i) \\ \text{query } i+1 \text{ and get: } (c_{i+1}, G_{i+1})(F_{i+1}) \end{cases}$

at time  $i + \delta_i$ , points will be NEW and BUFFERED.

$(c, G)$  given by queried results already.  $\begin{cases} x_i + \delta_i f_{i \rightarrow i+1}(x_i) \\ \text{position given by new as, } x_{i+1} + (1 - \delta_i) f_{i+1 \rightarrow i} \end{cases}$

two parts will be linearly blended, # for a buffer

**Implementation Details**

refer to supp.

How to understand this algo?

basically we don't know the color @  $i + \delta_i$  and how color flows, so we query @  $i$  and @  $i+1$ . the result includes  $(c, G)$  and  $(f, w)$ . so now,  $f$  is indicating where these points in nsff are going to, for time  $i + \delta_i$ , the querying results come from a BUFFER, this BUFFER has the points warped by  $f$  from time  $i$  and  $i+1$ , along with their original queried  $(c, G)$ . By this way, we don't query directly from nsff for  $(c, G)$  at intermediate time. we only query a correct 'NEFF' result and correct 'NSFF' flow to get what we want finally

