

## Chapter - 1

# Goals in Problem Solving

### Goal

- Target / Desired result / Accomplishment  
(what is to be achieved?)

### Planning

- Set / sequence of tasks to achieve a goal.

### Types of planning

- 1) Linear planning
- 2) Non-linear planning



#### Linear

- Planning algorithm that works on one goal until completely finished before moving on to next goal.

#### Non-Linear

- |  |   |
|--|---|
| - Doesn't prioritize task.                       | - Considers priority                          |
| - Non-preemptive (doesn't switch)                | - Preemptive                                  |
| - Uses <u>stack</u> for goal achievement. (FIFO) | - Uses set for goal achievement.              |
| - Requires less storage / reduced search space.  | - Requires more storage / larger search space |

- Simple Algo.
- May not produce optimal sol
- Incomplete
- Complex Algo.
- May produce optimal sol
- Complete

## \*MEA (Means-End Analysis)

- Algorithm that works based on 3 parameters;
  - 1) Initial state / Current
  - 2) Final state / Goal
  - 3) Goal difference ( $\Delta$ )
- Reducing goal difference between initial state & final state, until goal difference ( $\Delta$ ) is 0
- When,  $\Delta = 0$ , goal is achieved.
- Algorithm:
  - 1) Define initial state, goal state & calculate goal difference ( $\Delta$ ),  
and, ~~state~~
  - 2) Define actions
  - 3) Choose action / procedure with least goal difference that will ultimately reach to goal.
  - 3) When goal difference ( $\Delta$ ) = 0, goal is reached.

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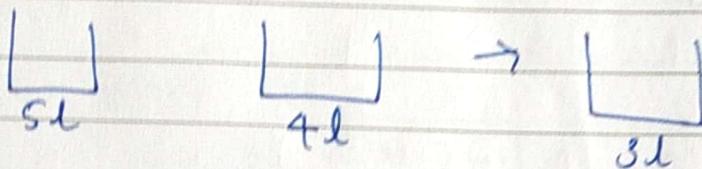
## Production Rule System

↓ eg.

$A \rightarrow B$   
if A, then B

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## Water Jug Problem



5l      4l

0	0
0	4
4	0
4	4
5	3

5l      4l

0	0
5	0
1	4
1	0
0	1
5	1

Path cost = 9

3      4  
Path cost = 10

## farmer fox Goose Grain Problem

L = Left side of River

R = Right side of River

Possible actions:

fa

fa fo

fa go

fa gr

L: fa fo go gr o → Boat

R:

fa go

L: fo gr

R: fa go o

| fa

L: fa fo gr o

R: go

fa fo

fa gr

L: gr

R: fa fo go o

| fa go

L: fa go gr o

R: fo

| fa gr

L: go

R: fo fa gr o

| fa

L: fa go o

R: gr fo

| fa go

L:

R: fa fo go gr

L: fo

R: fa gr go o

| fa go

L: fo fa go o

R: gr

fa fo

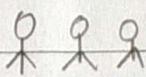
L: go

R: go fa fo o

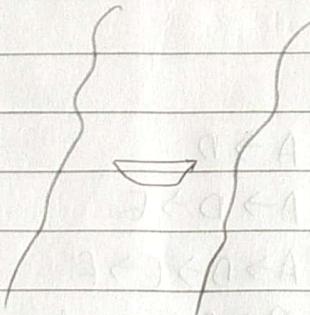
Path Cost = 7  
Total no. of states = 8

## M-C problem (Missionary Cannibal Problem)

3 Missionary



3 Cannibal



Possible Actions

1) 1M

2) 1C

3) 2M

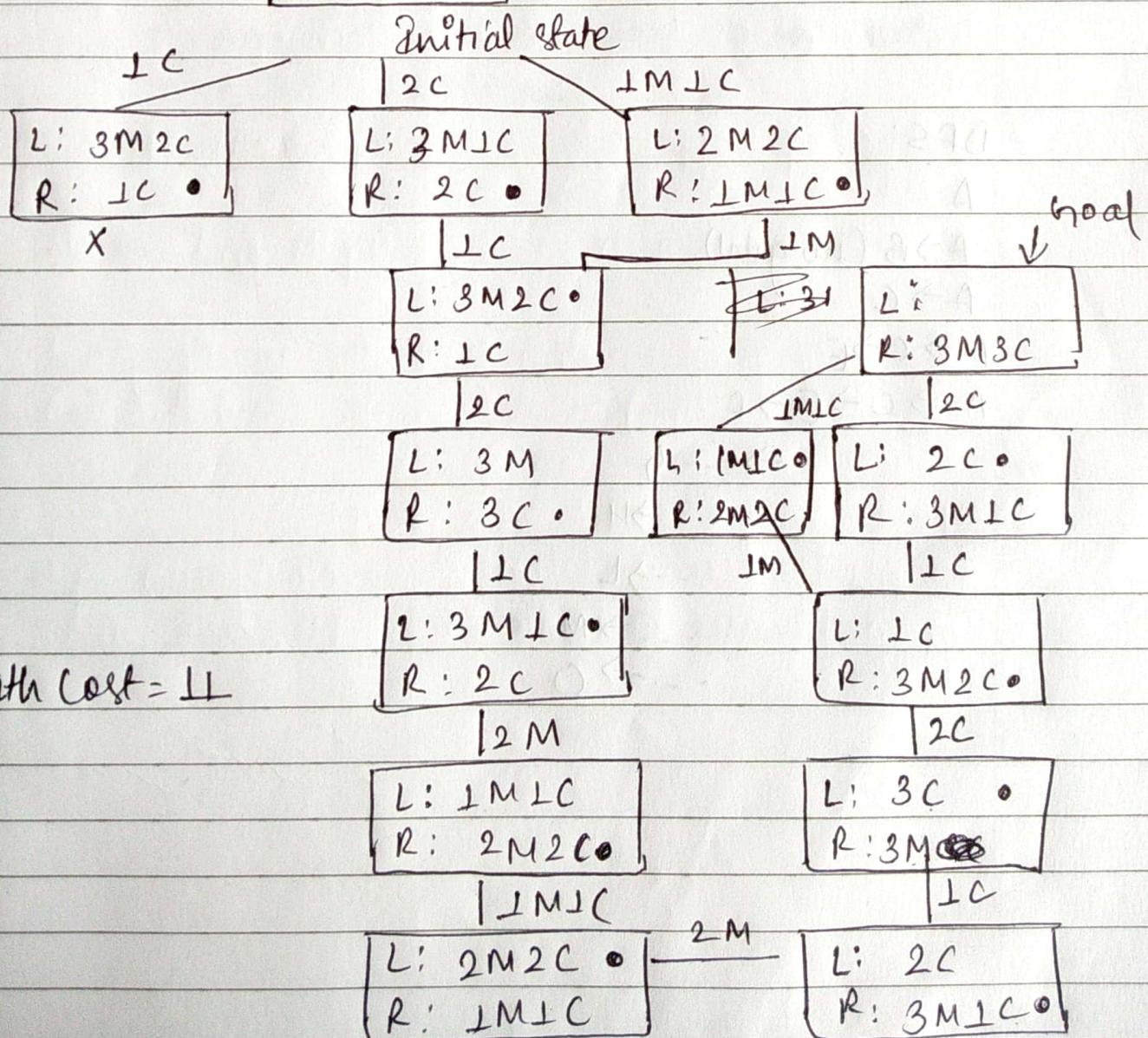
4) 2C

5) 1M1C

a) Draw Space Tree

L: 3M 3C  
R:

(State Space Tree)



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b) solve using BFS // DFS

BFS:

A

$A \rightarrow B$      $A \rightarrow C$      $A \rightarrow D$

(no goal)     $A \rightarrow C \rightarrow E$      $A \rightarrow D \rightarrow E$

$A \rightarrow C \rightarrow E \rightarrow F$      $A \rightarrow D \rightarrow E \rightarrow F$

$A \rightarrow C \dots \rightarrow G$      $A \rightarrow D \dots \rightarrow G$

$A \rightarrow C \dots \rightarrow L$      $A \rightarrow D \dots \rightarrow L$

$A \rightarrow C \dots \rightarrow M$      $A \rightarrow D \dots \rightarrow M$

$A \rightarrow C \dots \rightarrow N$      $A \rightarrow D \dots \rightarrow N$

DFS:

A

$A \rightarrow B$  (no goal)

$A \rightarrow C$

$A \rightarrow C \rightarrow E$

$A \rightarrow C \rightarrow E \rightarrow F$

$\rightarrow \dots G$

$\rightarrow H$

$\rightarrow L$

$\dots \rightarrow M$

$\dots \rightarrow O$

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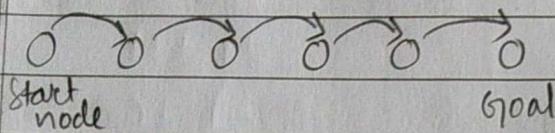
## Learning by Analogy (Analogical reasoning / learning)

- ↳ Tumor Problem
- ↳ Castle Problem
- ↳ Comparison of problems and applying solution from known problem to the new problem.
- ↳ 4 Re's.
  - Retrieve : Accessing from database
  - Reuse : Mapping same solution
  - Revise : Modification to the soln
  - Retain : Store

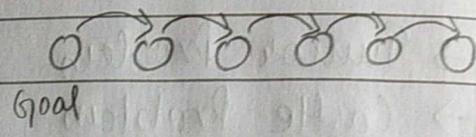
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## forward Chaining



## backward Chaining

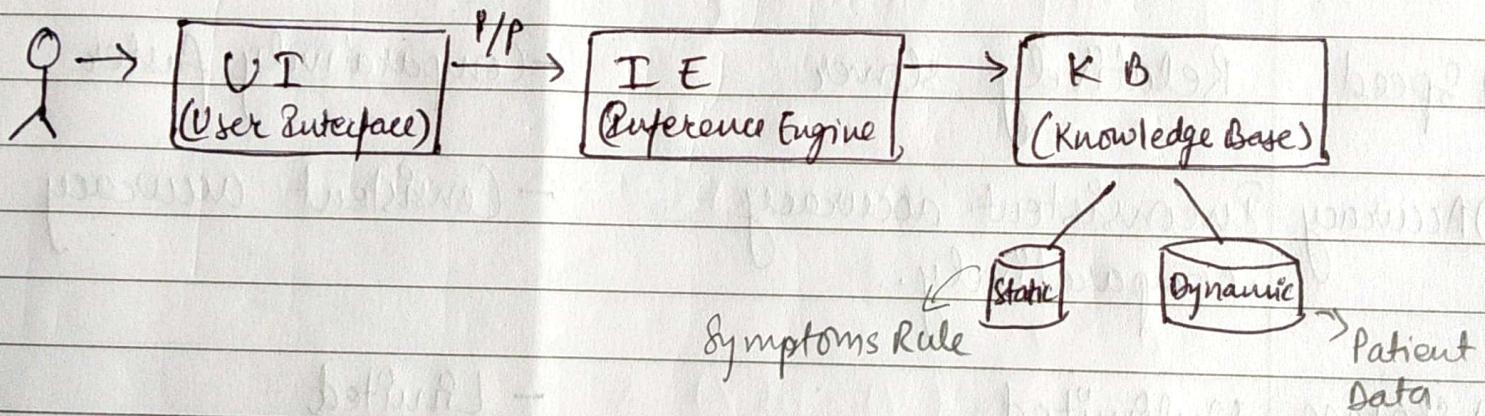


- Starts from initial state and aims for conclusion
- data driven inference technique
- Bottom-up approach
- Breadth first search
- The no. of final solution is infinite. (multiple)
- eg:  
Diagnosis Recommendation  
in a Disease Prediction  
bots
- starts from goal and backward search to necessary conclusion.
- goal driven inference technique
- Top-down approach
- Depth first search
- The no. of final solution is limited. (one)
- eg:  
Navigation system in  
Driverless car.

# Mycn

- ↳ Expert system to identify bacterial infections and recommend antibiotics.
- ↳ 500 production rules
  - If symptoms, then this disease
  - If disease, then this antibiotics

e.g.: If <sup>is strain</sup> <sub>of</sub> <sup>its negative and morphology</sup> organism is rod, then, suggest enterobacteriaceae.



## Chapter-2

## Intelligence

~~Vive~~  
HI Vs MIHuman Intelligence  
(Natural)

1) Operational Ability Performance declines overtime.

2) Speed Relatively slower

3) Accuracy Inconsistent accuracy comparatively.

4) Storage Capacity Unlimited

5) Decision making/  
Reasoning  
" might be  
Based on multiple emotions  
(Good abstract decisions)

6) Perception Perceives by pattern

Machine Intelligence  
(Artificial)

- Multitasking with consistent performance.

- Comparatively faster

- Consistent accuracy

- Limited

- Unbiased &amp; Rational

- Perceives in terms of datasets

## Chapter - 4

## Inference &amp; Reasoning

## Search Techniques:

- 1) Blind search or Uninformed search
- 2) Heuristic search or Informed search

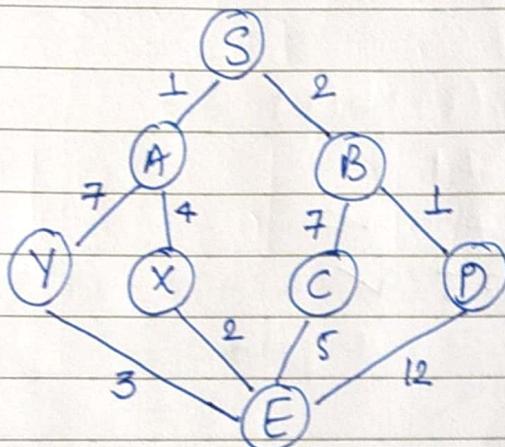
BFS

DFS

Greedy

A\*

Q

Values for  $h$  (heuristic):

A	5
B	6
C	4
D	15
X	5
Y	8
E	0

①

Greedy search :

$$f(n) = h(n)$$

Where,  $f(n)$  = evaluation function $h(n)$  = heuristic value of node 'n'

= estimated path cost from 'n' to goal

- Start node : S

S → A

$$f(n) = h(n)$$

$$f(A) = h(A) = 5 \checkmark$$

S → B

$$f(B) = h(B) = 6$$

- Expanding S → A

S → A → X

$$f(X) = h(X) = 5 \checkmark$$

S → A → Y

$$f(Y) = h(Y) = 8$$

- Expanding S → A → X

S → A → X → E

$$f(E) = h(E) = 0 \checkmark$$

~~S → A → X → E~~

∴ S → A → X → E is the best path.  
(Path cost = 7)

(ii) A\* Search :

$$f(n) = g(n) + h(n)$$

Where,

$g(n)$  = Path cost to reach node ' $n$ '

$S \rightarrow A$

$$\begin{aligned} f(A) &= g(A) + h(A) \\ &= 1 + 5 \\ &= 6 \quad \checkmark \end{aligned}$$

$S \rightarrow B$

$$\begin{aligned} f(B) &= g(B) + h(B) \\ &= 2 + 6 \\ &= 8 \quad \checkmark \end{aligned}$$

• Expanding  $S \rightarrow A$

$S \rightarrow A \rightarrow X$

$$\begin{aligned} f(X) &= g(X) + h(X) \\ &= 5 + 5 \\ &= 10 \quad \checkmark \end{aligned}$$

$S \rightarrow A \rightarrow Y$

$$\begin{aligned} f(Y) &= g(Y) + h(Y) \\ &= 8 + 8 \\ &= 16 \end{aligned}$$

• Expanding  $S \rightarrow B$

$S \rightarrow B \rightarrow C$

$$\begin{aligned} \therefore f(C) &= g(C) + h(C) \\ &= 9 + 4 = 13 \end{aligned}$$

S → B → D

$$\begin{aligned}f(D) &= g(D) + h(D) \\&= 3 + 15 \\&= 18\end{aligned}$$

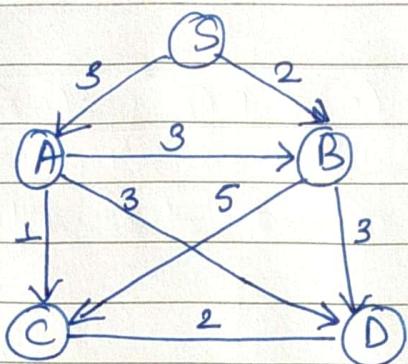
• Expanding S → A → X

S → A → X → E

$$\begin{aligned}f(E) &= g(E) + h(E) \\&= 7 + 0 \\&= 7 \quad \text{tc}\end{aligned}$$

∴ S → A → X → E is the best path  
(path cost = 7)

Q



$h(S)$	$h(A)$	$h(B)$	$h(C)$	$h(D)$
1	3	3	0	0

①

Greedy search:

$$f(n) = h(n)$$

- Start node: S

 $S \rightarrow A$ 

$$f(A) = h(A) = 3 \quad \checkmark$$

 $S \rightarrow B$ 

$$f(B) = h(B) = 3$$

- Expanding  $S \rightarrow A$

 $S \rightarrow A \rightarrow B$ 

$$f(B) = h(B) = 3$$

~~$S \rightarrow A \rightarrow D$~~

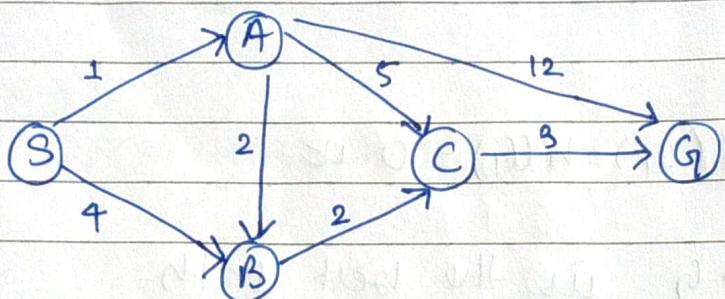
$$f(D) = h(D) = 0$$
 $S \rightarrow A \rightarrow C$ 

$$f(C) = h(C) = 0$$

 $S \rightarrow A \rightarrow D$ 

$$f(D) = h(D) = 0$$

9



<u>State</u>	<u><math>h</math></u>
S	7
A	6
B	2
C	1
G	0

Q)

Greedy Search:

$$f(n) = h(n)$$

Start node: S

Expanding S,

$$S \rightarrow A$$

$$f(A) = h(A) = 6$$

$$S \rightarrow B$$

$$f(B) = h(B) = 2 \quad \checkmark$$

Expanding  $S \rightarrow B$ ,

$$S \rightarrow B \rightarrow C$$

$$f(C) = h(C) = 1$$

- Expanding  $S \rightarrow B \rightarrow C$ ,

$S \rightarrow B \rightarrow C \rightarrow G$

$$f(G) = h(G) = 0 \text{ w}$$

$\therefore S \rightarrow B \rightarrow C \rightarrow G$  is the best path  
(path cost = 9)

(ii)

### A\* Search:

$$f(n) = g(n) + h(n)$$

- Start node:  $S$

- Expanding  $S$ ,

$S \rightarrow A$

$$f(A) = g(A) + h(A) = 1 + 6 \\ = 7$$

$S \rightarrow B$

$$f(B) = g(B) + h(B) \\ = 4 + 2 \\ = 6 \quad \checkmark$$

- Expanding  $S \rightarrow B$ ,

$S \rightarrow B \rightarrow C$ ,

$$f(C) = g(C) + h(C) \\ = 6 + 1 \\ = 7$$

- Expanding  $S \rightarrow A$ , & Expanding  $S \rightarrow B \rightarrow C$ ,

$S \rightarrow A \rightarrow B$

$$\begin{aligned}f(B) &= g(B) + h(B) \\&= 3 + 2 \\&= 5 \quad \checkmark\end{aligned}$$

$S \rightarrow B \rightarrow C \rightarrow G$ ,

$$\begin{aligned}f(G) &= g(G) + h(G) \\&= 9 + 0 \\&= 9\end{aligned}$$

$S \rightarrow A \rightarrow C$

$$\begin{aligned}f(C) &= g(C) + h(C) \\&= 6 + 1 \\&= 7\end{aligned}$$

$S \rightarrow A \rightarrow G$

$$\begin{aligned}f(G) &= g(G) + h(G) \\&= 13 + 0 \\&= 13\end{aligned}$$

- Expanding  $S \rightarrow A \rightarrow B$ ,

$S \rightarrow A \rightarrow B \rightarrow C$ ,

$$\begin{aligned}f(C) &= g(C) + h(C) \\&= 5 + 1 \\&= 6 \quad \checkmark\end{aligned}$$

- Expanding  $S \rightarrow A \rightarrow B \rightarrow C$ ,

$S \rightarrow A \rightarrow B \rightarrow C \rightarrow G$ ,

$$\begin{aligned}f(G) &= g(G) + h(G) \\&= 8 + 0 \\&= 8 \quad \checkmark\end{aligned}$$

- Expanding  $S \rightarrow A \rightarrow C$ ,

$S \rightarrow A \rightarrow C \rightarrow G$

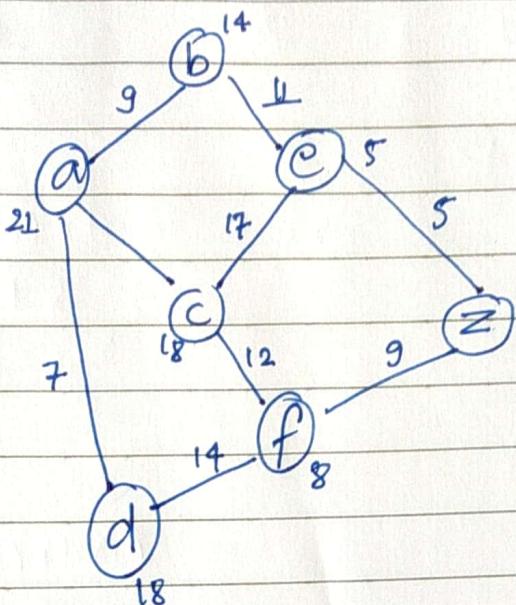
$$\begin{aligned}f(G) &= g(G) + h(G) \\&= 9 + 0 \\&= 9\end{aligned}$$

$\therefore S \rightarrow A \rightarrow B \rightarrow C \rightarrow G$  is the best path,  
(path cost = 8)

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Q



<u>State</u>	<u>h</u>
a	21
b	14
c	18
d	18
e	5
f	8

Next,

i) Greedy Method:

## Greedy

1)  $f(n) = h(n)$

A\*

-  $f(n) = g(n) + h(n)$

2) Heuristic value

- May consider paths

3) Not required

- Backtracking

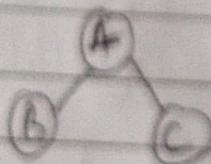
4) Simple & faster

- comparatively lower

5) Comparatively lower

- Time complexity & space complexity higher.

cg :

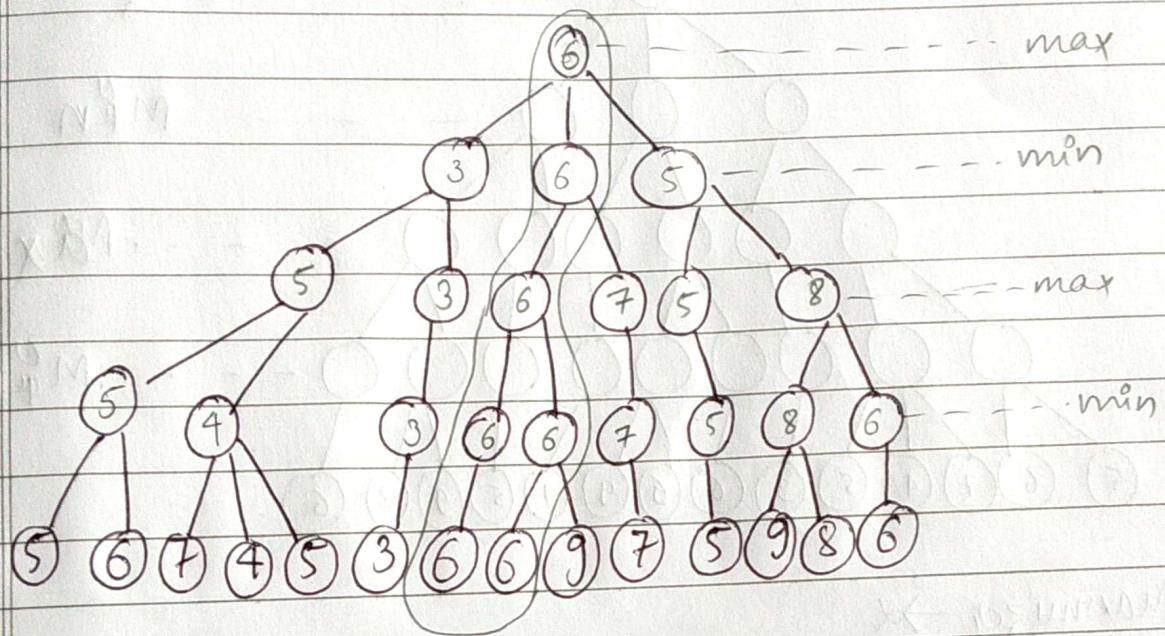


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## Minmax Algorithm

2-player games (Tic-Tac-Toe, Chess, Checkers)



Minimizer: selects min. value

Maximizer: selects max. value

↳ Game playing algorithm used in 2 player games.  
(Tic-Tac-Toe, Chess, Checkers)

↳ Two-players : Minimizer  
: Maximizer

↳ Limitations:

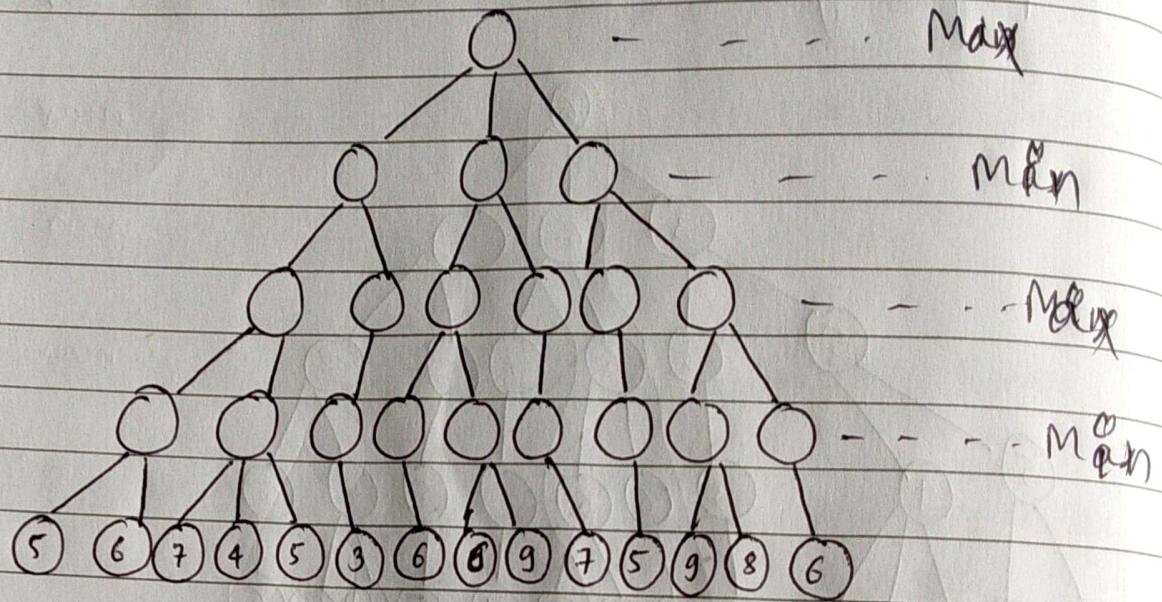
- Time & space complexity higher

- Alpha - beta pruning overcomes these limitations.

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## $\alpha$ - $\beta$ Pruning (Alpha-Beta Pruning)



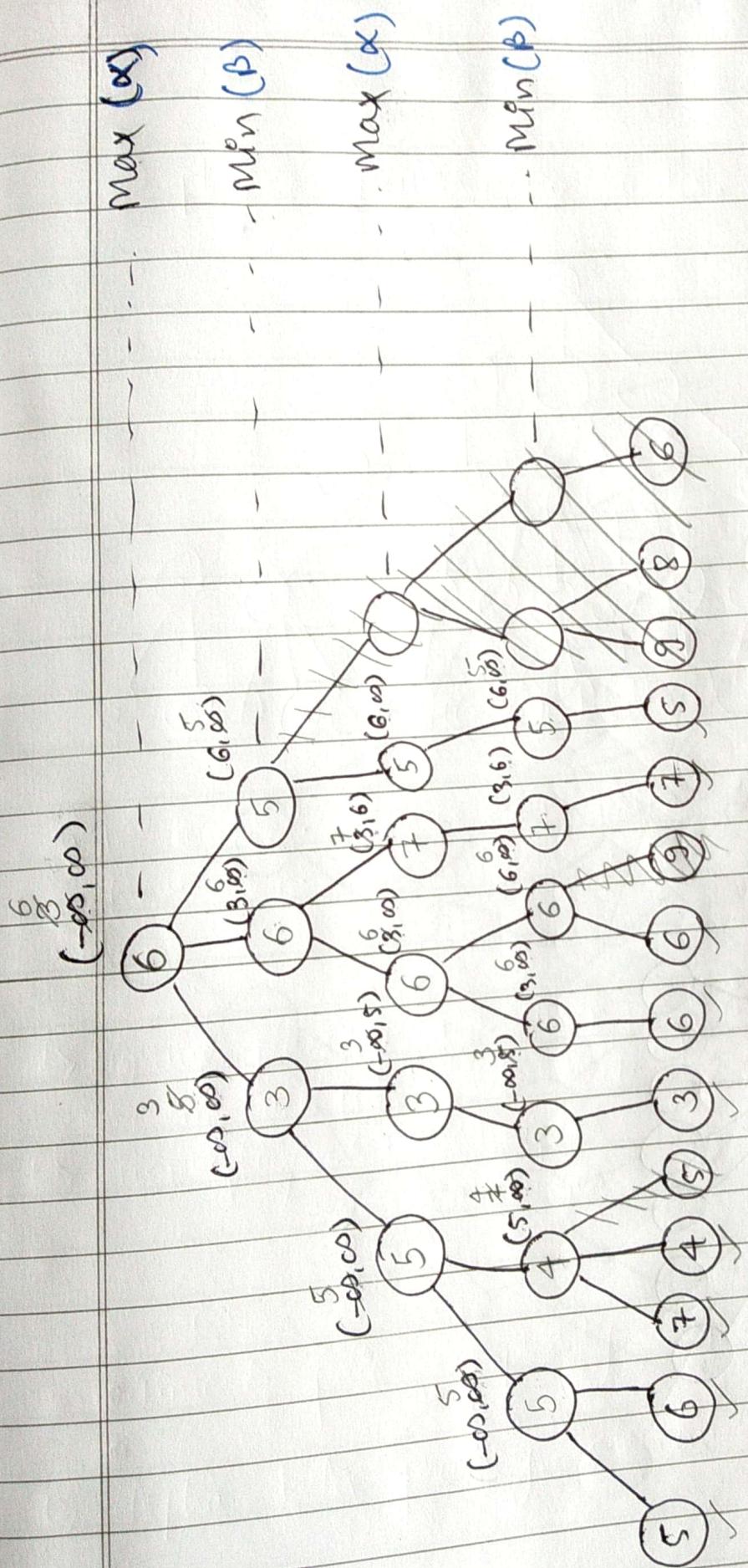
- Maximizer  $\rightarrow \alpha$
- Minimizer  $\rightarrow \beta$

→ Initial value  $(-\infty, \infty)$

- 1) Check min, max level  $(\beta)$  or  $(\alpha)$
- 2) Update  $\alpha$ - $\beta$  values
- 3) Push min max values

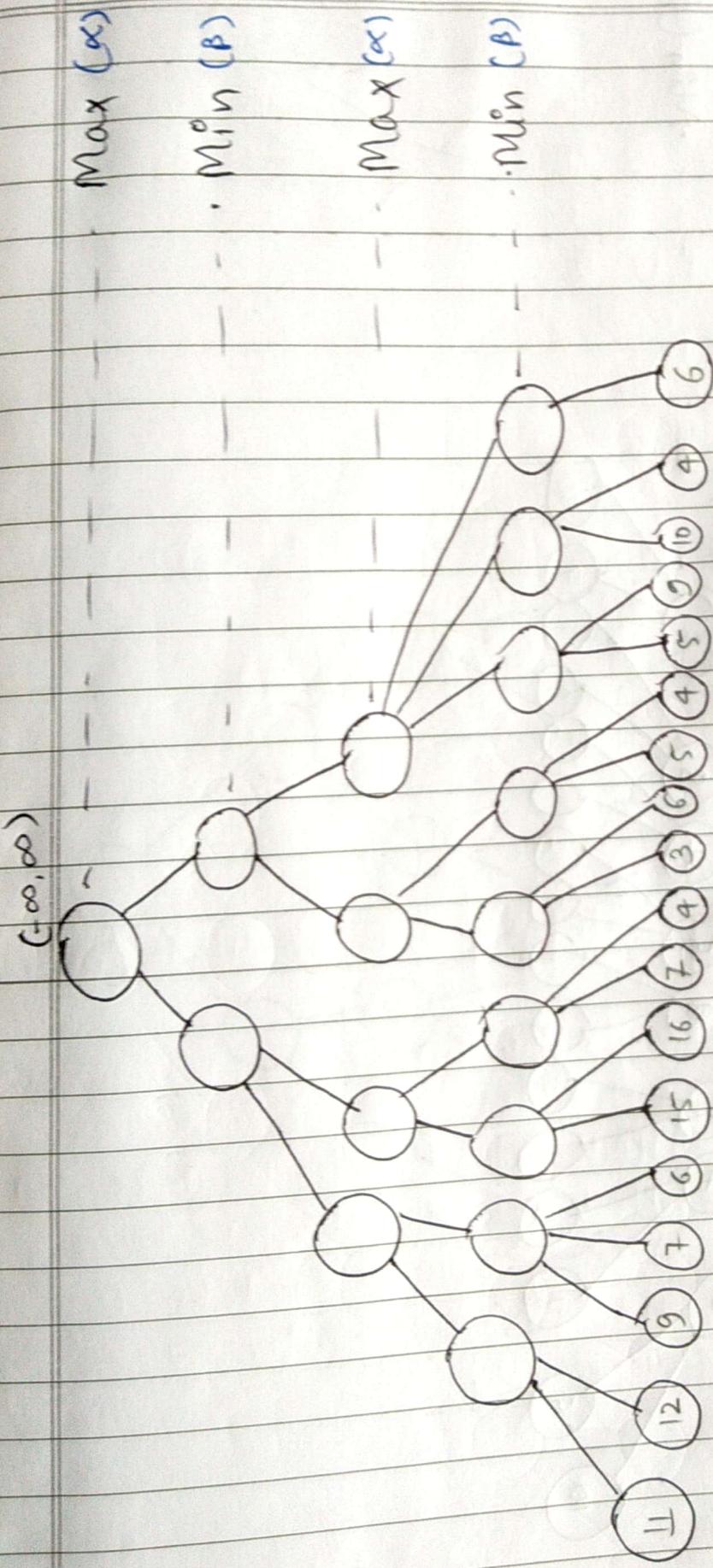
### Working Condition

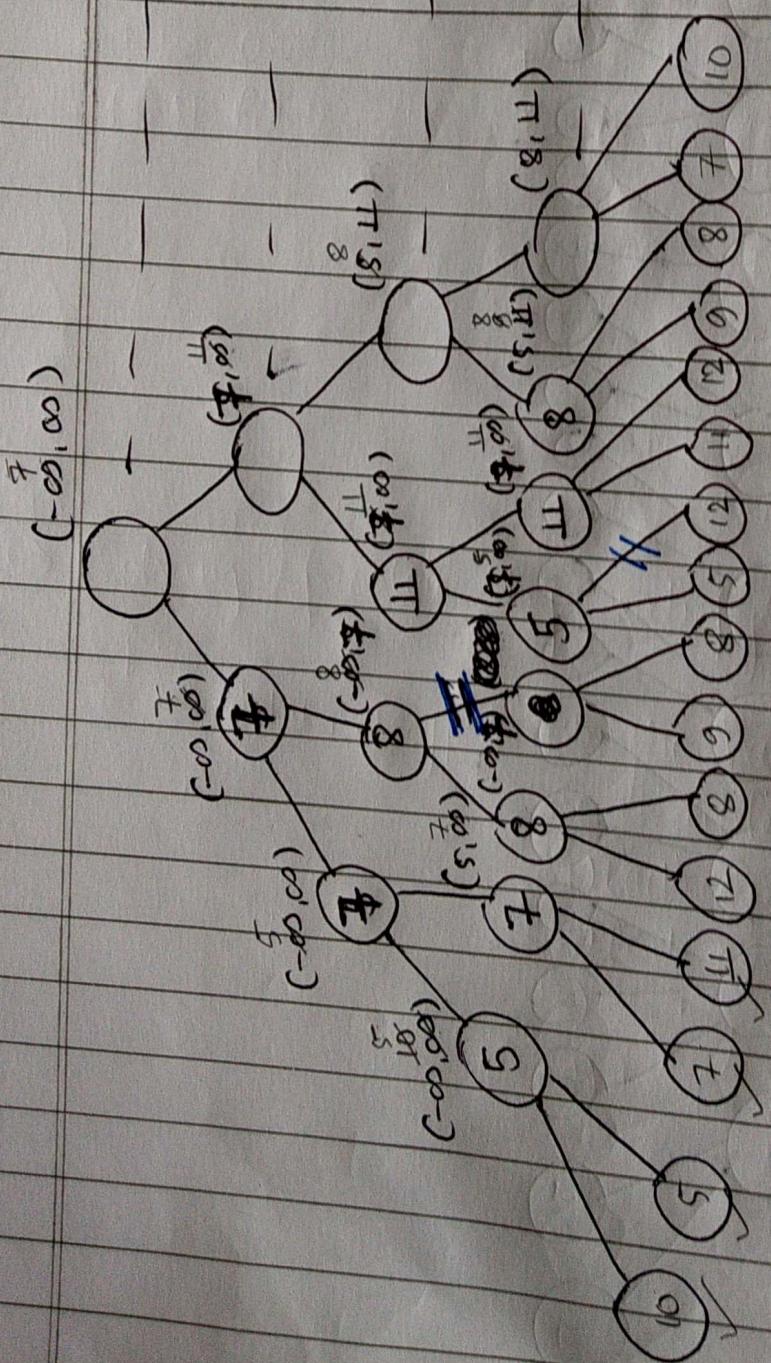
$\alpha > \beta$ ,  
prune the branches  
(cut-off)

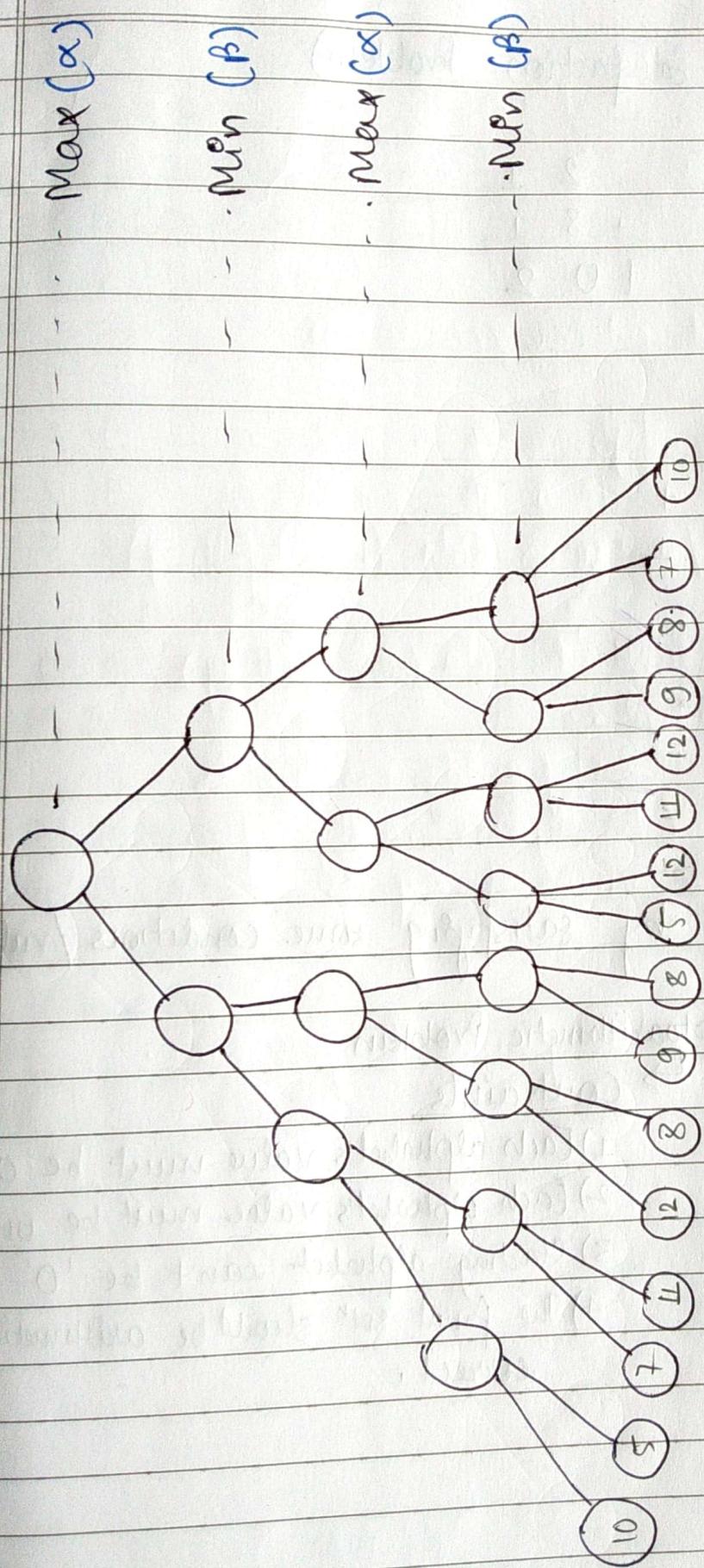


$$\begin{aligned} \alpha - \text{cutoff} &= 0 \\ \beta - \text{cutoff} &= 3 \end{aligned}$$

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## CSP (Constraint Satisfaction Problem)

$$\begin{array}{r}
 \text{TO} \quad \rightarrow \\
 + \text{GO} \\
 \hline
 \text{OUT}
 \end{array}
 \quad
 \begin{array}{r}
 2 \ 1 \\
 + 8 \ 1 \\
 \hline
 102
 \end{array}$$

$$\begin{array}{r}
 \text{TWO} \quad \Rightarrow \\
 + \text{TW O} \\
 \hline
 \text{FOUR}
 \end{array}
 \quad
 \begin{array}{r}
 7 \ 3 \ 4 \quad 8 \ 3'6 \quad 9 \ 2 \ 8 \\
 + 7 \ 3 \ 4 \quad + 8 \ 3 \ 6 \quad 9 \ 2 \ 8 \\
 \hline
 1468 \quad 1672 \quad 1856
 \end{array}$$

$$\begin{array}{r}
 9 \ 3'8 \\
 + 9 \ 38 \\
 \hline
 1876
 \end{array}$$

↳ Solving problem by satisfying some conditions / rules.  
 eg:

Sudoku, Cryptarithmic Problem

↳ Constraints

- 1) Each alphabet's value must be 0-9
- 2) Each alphabet's value must be unique
- 3) Starting alphabet can't be '0'
- 4) The final sol<sup>n</sup> should be arithmetically correct.

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$$\begin{array}{r}
 \text{LOGIC} \\
 + \text{LOGIC} \\
 \hline
 \text{PROLOG}
 \end{array}
 \quad
 \begin{array}{r}
 + \quad \boxed{9} \quad \boxed{0} \quad \boxed{4} \quad \boxed{5} \quad \boxed{2} \\
 + \quad \boxed{9} \quad \boxed{0} \quad \boxed{4} \quad \boxed{5} \quad \boxed{2} \\
 \hline
 \boxed{1} \quad \boxed{8} \quad \boxed{0} \quad \boxed{9} \quad \boxed{0} \quad \boxed{4}
 \end{array}$$

$$\begin{array}{r}
 \times \quad \boxed{7} \quad \boxed{9} \quad \boxed{6} \quad \boxed{4} \quad \boxed{8} \\
 + \quad \boxed{7} \quad \boxed{9} \quad \boxed{6} \quad \boxed{4} \quad \boxed{8} \\
 \hline
 \boxed{1} \quad \boxed{5} \quad \boxed{9} \quad \boxed{2} \quad \boxed{9} \quad \boxed{6}
 \end{array}$$

$$\begin{array}{r}
 \text{SEND} \\
 + \text{MORE} \\
 \hline
 \text{MONEY}
 \end{array}
 \quad
 \begin{array}{r}
 \text{C}_2=1 \quad \text{C}_1=1 \quad \text{C}_0=1 \\
 + \quad \boxed{9} \quad \boxed{5} \quad \boxed{6} \quad \boxed{7} \\
 + \quad \boxed{1} \quad \boxed{0} \quad \boxed{8} \quad \boxed{5} \\
 \hline
 \boxed{1} \quad \boxed{0} \quad \boxed{6} \quad \boxed{5} \quad \boxed{2}
 \end{array}$$

↓

$$\begin{aligned}
 1) \quad & E + 1 = N \\
 2) \quad & N + R + C_0 = 10 + E \\
 & R + 1 + R + C_0 = 10 + E \\
 & R + C_0 = 9
 \end{aligned}$$

E	N
0	1
1	2
2	3
3	4
4	5
5	6
6	7
7	8
8	9

## Uncertainty with Baye's Rule

Q) What is uncertainty? Sources? How to overcome? Baye's Rule? Eg.?

↳ Unable to predict outcome / conclusion

↳ Sources of Uncertainty

1) Incomplete data / Unknown data (Under fitting)  
(Insufficient)

2) Vague data / Redundant Data (Over fitting) / Weak implication

3) Imprecise Language:

    Use of ambiguous words  
    (hardly ever, rarely, often, sometimes)

4) Combining / Multiple views of experts

★ To overcome uncertainty, use Baye's Rule.

# Bayes' Rule / Bayesian Network / BBN (Bayes' Belief Network)

- ↳ Handles uncertainty / uncertain data
- ↳ deals with conditional probability, probability of an event 'A' ( $P(A|B)$ ) given that 'B' has occurred prior.

$$P(A|B) = \frac{P(A \cap B)}{P(B)} \quad \longrightarrow \quad (1) \quad P(A \cap B) = P(A|B) \cdot P(B)$$

$$P(B|A) = \frac{P(B \cap A)}{P(A)} \quad \longrightarrow \quad (2) \quad P(A \cap B) = P(B|A) \cdot P(A)$$

$$P(A|B) = \frac{P(B|A) \cdot P(A)}{P(B)} \quad \longrightarrow \quad (3)$$

## Numerical

1) While watching a game of champion League of football in a cafe, you observe someone who is clearly supporting Manchester United in the game. What is the prob. that they were born within 25 miles of Manchester.  
Assume that:

- Prob. that a randomly selected person in that bar is born within 25 miles of Manchester is  $\frac{1}{20}$ .
- The chance that a person born within 25 miles of manchester actually supports Manchester United is  $\frac{7}{10}$ .
- Prob. that the a person not born within 25 miles of Manchester supports Manchester United is  $\frac{1}{10}$ .

Sol",

$S$  = Supports Man U

$B$  = Born within 25 miles of Manchester

Given,

$$P(B) = \frac{1}{20}$$

$$P(S/B) = \frac{7}{10}$$

$$P(B/S) = ?$$

$$P(S/\bar{B}) = \frac{1}{10}$$

um,

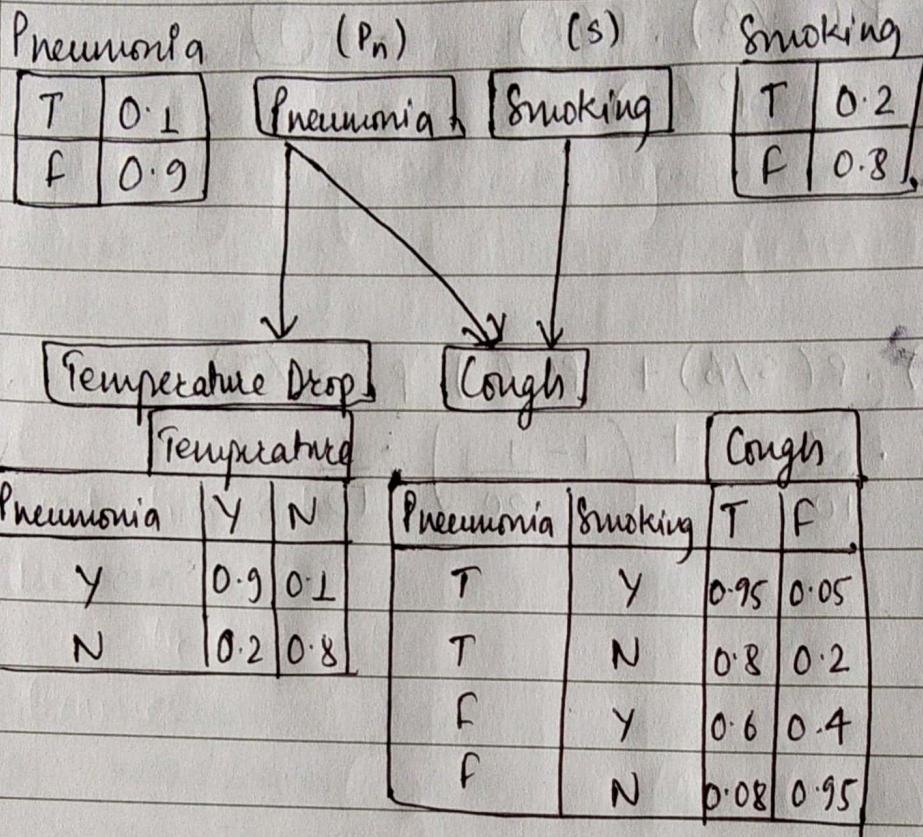
$$P(B/S) = \frac{P(S/B) \cdot P(B)}{P(S)} \rightarrow ①$$

here,

$$\begin{aligned} P(S) &= P(B) \cdot P(S/B) + P(\bar{B}) \cdot P(S/\bar{B}) \\ &= \frac{1}{20} \cdot \frac{7}{10} + \left(1 - \frac{1}{20}\right) \cdot \frac{1}{10} \\ &= \underline{\underline{0}} \end{aligned}$$

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## Bayesian Network



Conditional Probability Table (CPT)

- 1)  $P(C/S \cap P_n) = 0.95$  (Prob. of cough due to Pneumonia & Smoking)
- 2)  $P(C) = \text{Prob. of } C$
- 3)  $P(C/s) = \text{Prob. of } C \text{ due to smoking.}$

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2)  $P(C) = \text{prob. of Cough}$

$$= P(P_n) \cdot P(S) \cdot P(C/P_n \cap S) + P(P_n) \cdot P(\bar{S}) \cdot P(C/P_n \cap \bar{S}) \\ + P(\bar{P}_n) \cdot P(S) \cdot P(C/\bar{P}_n \cap S) + P(\bar{P}_n) \cdot P(\bar{S}) \cdot P(C/\bar{P}_n \cap \bar{S})$$

3)  $P(C/S) = \text{Prob. of cough due to smoking}$

$$= P(P_n) \cdot P(S) \cdot P(C/P_n \cap S) + P(\bar{P}_n) \cdot P(S) \cdot P(C/\bar{P}_n \cap S)$$

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2)  $P(C) = \text{prob. of Cough}$

$$= P(P_n) \cdot P(S) \cdot P(C/P_n \cap S) + P(P_n) \cdot P(\bar{S}) \cdot P(C/P_n \cap \bar{S}) \\ + P(\bar{P}_n) \cdot P(S) \cdot P(C/\bar{P}_n \cap S) + P(\bar{P}_n) \cdot P(\bar{S}) \cdot P(C/\bar{P}_n \cap \bar{S})$$

3)  $P(C/S) = \text{Prob. of cough due to smoking}$

$$= P(P_n) \cdot P(S) \cdot P(C/P_n \cap S) + P(\bar{P}_n) \cdot P(S) \cdot P(C/\bar{P}_n \cap S)$$

## Chapter - 3

### Knowledge Representation

↪ The branch of AI that deals with storing or representing knowledge / datasets in Database / KB (Knowledge Base) for inference or reasoning.

#### KR schemes:

- 1) Production Rule
- 2) Logic
- 3) Semantic Network
- 4) Frames

#### 1) Production Rule:

If A, then, B  
Condition → Action

Fill 4L jug.  
 $n \leftarrow 4 \rightarrow (4, y)$

#### 2) Logic :

- Propositional Logic
- Predicate Logic

## a) Propositional Logic:

- Declarative sentence that can be either True or False

## Logical Operators:

1) Unary Operator ( $\neg$ ): single operand

2) Binary Operator ( $\wedge, \vee, \rightarrow, \leftrightarrow$ ): Two operands

## Truth Table:

$P$	$Q$	$\neg P$	$\neg Q$	$P \vee Q$	$P \wedge Q$	$P \rightarrow Q$	$P \leftrightarrow Q$	$\neg P \vee Q$	$\neg Q \rightarrow P$	$(P \rightarrow Q) \wedge (Q \rightarrow P)$
T	T	F	F	T	T	T	T	T	T	T
T	F	F	T	T	F	F	F	F	F	F
F	T	T	F	T	F	T	F	T	T	F
F	F	T	T	F	F	T	T	T	T	T

(Or/Disjunction)      (And/Conjunction)      (Conditional/Simulation)      (Bi-conditional/Double Implication)

P: "It is raining"

Q: "I will take an umbrella"

## Prove:

$$a) P \rightarrow Q \equiv \neg P \vee Q$$

$$b) P \leftrightarrow Q \equiv (P \rightarrow Q) \wedge (Q \rightarrow P)$$

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## Propositional Logic:

### Normal forms:

- a) CNF (Conjunctive Normal Form) Conjunction of Disjunction
- b) DNF (Disjunctive Normal Form) Disjunction of Conjunction

### CNF Conversion Steps:

#### Step 1:

Eliminate Conditional and Bi-conditional / Double Implication  
(if present)

$$P \rightarrow Q \equiv \neg P \vee Q$$

P = "It is cold"

Q = "I will wear a sweater"

$$\begin{aligned} P \leftrightarrow Q &\equiv (P \rightarrow Q) \wedge (Q \rightarrow P) \\ &= (\neg P \vee Q) \wedge (\neg Q \vee P) \end{aligned}$$

#### Step 2:

De-Morgan's Law:

$$\neg(P \vee Q) \equiv \neg P \wedge \neg Q$$

$$\neg(P \wedge Q) \equiv \neg P \vee \neg Q$$

Step 3 :

Apply Distributive law:

$$P \wedge (Q \vee R) \equiv (P \wedge Q) \vee (P \wedge R)$$

$$P \vee (Q \wedge R) \equiv (P \vee Q) \wedge (P \vee R)$$

\* Convert  $P \rightarrow Q \rightarrow R$  into CNF

Step 1:

$$\begin{aligned} & (P \rightarrow Q) \rightarrow R \\ & \equiv (\neg P \vee Q) \rightarrow R \\ & \equiv \neg(\neg P \vee Q) \vee R \end{aligned}$$

Step 2:

$$\begin{aligned} & \neg(\neg P \vee Q) \vee R \\ & \equiv (P \wedge \neg Q) \vee R \end{aligned}$$

Step 3:

$$\begin{aligned} & P \wedge (\neg Q \vee R) \\ & \equiv (P \vee R) \wedge (\neg Q \vee R) \end{aligned}$$

req<sup>n</sup> CNF

Truth Table:

DFT

P	$\neg Q$	R	$P \rightarrow Q$	$(P \rightarrow Q) \rightarrow R$	$\neg Q \vee R$	$P \vee R$	$(P \vee R) \wedge (\neg Q \vee R)$
T	T	T	T	T	F	T	T
T	T	F	T	F	F	T	F
T	F	T	F	T	T	T	T
T	F	F	F	T	T	T	T
F	T	T	T	F	T	T	T
F	T	F	T	F	F	F	F
F	F	T	T	T	T	T	T
F	F	F	T	F	T	F	F

Proof by Results

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# Proof by Resolution / Resolution Refutation

If it is hot, then it is humid. If it is humid, then it will rain. It is hot. Prove that it will rain.

## Steps

Convert all statements into CNF.  
Negate the desired conclusion  
Apply resolution rule.

$$\begin{aligned} P \vee Q \\ \neg Q, V R \\ \therefore P \vee R \end{aligned}$$

When we derive contradiction, our assumption was false and given statement is proved.

Given:

- = "It is hot"
- = "It is humid"
- = "It will rain"

$$\begin{aligned} \rightarrow Q \\ \rightarrow R \end{aligned}$$

Prove: R

Step 1:

$$1) P \rightarrow Q$$

$$\equiv \neg P \vee Q$$

$$2) Q \rightarrow R$$

$$\equiv \neg Q \vee R$$

$$3) P$$

$$4) \neg R \text{ (Assumption)}$$

~~Step 2~~

Steps	Formulas	Derivations
1)	$\neg P \vee Q$	Given
2)	$\neg Q \vee R$	"
3)	P	"
4)	$\neg R$	"
5)	$\neg P \vee R$	Resolution in 1, 2
6)	R	Resolution in 3, 5

∴ We reach to a contradiction, hence "It will rain"

Q Either Heather attended the meeting or Heather was not invited. If the boss wanted Heather at the meeting, then, she was invited. Heather didn't attend the meeting. If the boss didn't want Heather there and the boss didn't invite her there, then, she is going to be fired.

Prove: Heather is going to be fired.

Given:

P = "Heather attended the meeting"

$\neg Q$  = "Heather was not invited"

R = "Boss wanted Heather at meeting"

S = "She is going to be fired"

Given:

$$1) P \vee \neg Q$$

$$2) R \rightarrow Q$$

$$3) \neg P$$

$$4) (\neg R \wedge \neg Q) \rightarrow S$$

$$5) \neg S \text{ (Assumption)}$$

prove: S

Step 1:

$$1) P \vee \neg Q$$

$$2) R \rightarrow Q \equiv \neg R \vee Q$$

3)  $\neg P$

$$\begin{aligned} 4) (\neg R \wedge Q) &\rightarrow S \\ \equiv \neg(\neg R \wedge Q) \vee S \\ \equiv (R \vee \neg Q) \vee S \end{aligned}$$

5)  $\neg S$  (Assumption)

Steps	Formulas	Derivation
1)	$P \vee \neg Q$	Given
2)	$\neg R \vee Q$	"
3)	$\neg P$	"
4)	$(R \vee Q) \vee S$	"
5)	$\neg S$	"
6)	$P \vee \neg R$	Resolution $\neg 1, 2$
7)	$\neg R$	Resolution $\neg 3, 6$
8)	$\neg Q$	Resolution $\neg 4, 3$
9)	$Q \vee S$	Resolution $\neg 5, 7$
10)	$S$	Resolution $\neg 8, 9$

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Predicate Logic : / FOL / FOPL : statement consisting of variables, constant, predicates, quantifiers & logical operators.

Limitation of Propositional logic / Strength of Predicate Logic:

- 1) Propositional logic can't express equations.  
"n is greater than 1"
- 2) It can't express logical equivalence between sentences in cases like : "Not all birds can fly" =  
Some birds can't fly"
- 3) Propositional logic can't generalize statements.

2020 Spring

First order logic → First order predicate logic

Q Convert into FOL / FOPL

- 1) Ramesh doesn't have a laptop
- 2) All purple mushroom are venomous.
- 3) Anything anyone eats and is not killed by its food.
- 4) Bryan eats mushroom and is still alive.
- 5) Ram likes all kinds of food.
- 6) Krishna eats everything Radha eats.
- 7) All marvel fans watch spiderman.
- 8) Ram likes samosa.
- 9) If Ram is rich, he has a nice house  
"Suyan" " " " " " "  
"Hari" " " " " " "
- 10) Not all birds can fly.  
Some birds can't fly.
- 11) n is greater than 1.

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2020 Spring

first order logic → first order predicate logic

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- 9) If Ram is rich, he has a nice house  
" Shyam " " " " " "  
" Hari " " " " " "
- 10) Not all birds can fly.  
Some birds can't fly.
- 11) n is greater than 1.

- 1)  $\exists x \text{Have}(x, \text{Laptop})$
- 2)  $\forall x \text{PurpleMushroom}(x) \rightarrow \text{Venomous}(x)$
- 3)  $\forall x \forall y \text{Eats}(x, y) \wedge \exists z \text{KilledBy}(x, y, z) \rightarrow \text{Food}(y)$
- 4)  $\text{Eats}(\text{Bryan}, \text{Mushroom}) \rightarrow \text{StillAlive}(\text{Bryan})$
- 5)  $\forall x \text{Food}(x) \rightarrow \text{Likes}(\text{Ram}, x)$
- 6)  $\forall x \text{Food}(x) \wedge \text{Eats}(\text{Radha}, x) \\ \forall x \text{Eats}(\text{Radha}, x) \rightarrow \text{Eats}(\text{Krishna}, x)$
- 7)  $\forall x \text{MarvelFan}(x) \rightarrow \text{watch}(x, \text{Spiderman})$
- 8)  $\text{Likes}(\text{Ram}, \text{Samosa})$
- 9)  $\forall x \text{IsRich}(x) \rightarrow \text{Has}(x, \text{NiceHouse})$
- 10)  $\exists x \text{Birds}(x) \rightarrow \text{CanFly}(x) \\ \exists x \text{Birds}(x) \rightarrow \exists y \text{CanFly}(y)$
- 11)  $\exists x \text{GreaterThan}(x, 1) \\ \exists x \text{Number}(x) \rightarrow \text{GreaterThan}(x, 1)$

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1) Ram likes all kinds of food  
 →  $\forall n \exists \text{Food}(n) \rightarrow \text{Likes}(\text{Ram}, n)$

2) Orange is a food.  
 → food(orange)

3) Rice is a food  
 → food(Rice)

4) Anything anyone eats and is not killed is food.  
 →  $\forall n$

5) Krishna eats Popcorn and is still alive.  
 → Eats(Krishna, Popcorn) ∧ Alive(Krishna)

6) Krishna eats everything Radha eats.  
 →  $\forall n \text{Eats}(\text{Radha}) \rightarrow \text{Eats}(\text{Krishna}, n)$

7) Prove that "Ram likes Popcorn" Using RRS  
 → Likes(Ram, Popcorn)

### Resolution Table:

Steps	Step# Facts	Derivation
1)	$\exists \text{Food}(n) \forall \text{Likes}(\text{Ram}, n)$	Given
2)	food(orange)	"
3)	food(Rice)	"
4)	$\forall a \exists f(a) \forall \text{Killed}(a) \forall \text{Food}(y)$	"
5)	Eats(Krishna, Alive(Popcorn))	"
6)	Alive(Krishna) $\equiv \neg \text{Killed}(\text{Krishna})$	"
7)	$\forall b \exists \text{Eats}(\text{Radha}, b) \forall \text{Eats}(\text{Krishna}, b)$	"
8)	$\exists \text{Likes}(\text{Ram}, \text{Popcorn})$	Assumption

(f(Krishna))

9)  $\exists Eats(Krishna, f(Krishna)) \vee food(f)$

$a = Krishna$

Resolution in 4, 6

$f(Krishna) = Popcorn$

Resolution in 5, 9

~~Popcorn~~

$n = Popcorn$

10)  $food(Popcorn)$

11)  $Likes(Ram, Popcorn)$

∴ Here, we reach a contradiction,  
Hence proved.

2018 Spring

- i) Anyone whom Mary loves is a football star.
- ii) Any student who doesn't pass doesn't play
- iii) John is a student.
- iv) Any student who doesn't study doesn't pass.
- v) Any one who doesn't play is ~~not~~ a football star.

Prove: "If John doesn't study, then Mary doesn't love John".

~~SOP~~ FOL:

- i)  $\forall n Loves(Mary, n) \rightarrow \text{Football Star}(n)$
- ii)  $\forall n \text{ Student}(n) \wedge \neg \text{Pass}(n) \rightarrow \neg \text{Play}(n)$
- iii)  $\text{Student(John)}$
- iv)  $\forall n \text{ Student}(n) \wedge \neg \text{Study}(n) \rightarrow \neg \text{Pass}(n)$
- v)  $\forall n \neg \text{Play}(n) \rightarrow \neg \text{Football Star}(n)$

2018/08/22

## Object Programs

~~Propositional Logic~~

Resolution Table

~~Steps~~ ~~Table~~

CNF:

- i)  $\exists \forall x \exists y \text{Loves}(\text{Mary}, x) \vee \text{FootballStar}(x)$
- ~~ii)~~  $\exists \exists y \text{Loves}(\text{Mary}, y) \vee \text{FootballStar}(y)$
- ii)  $\forall x \exists y (\text{student}(x) \wedge \exists z \text{Pass}(x)) \vee \exists y \neg \text{Play}(y)$   
 $\equiv \forall x \exists y \neg \text{student}(y) \vee \text{Pass}(y) \vee \exists y \neg \text{Play}(y)$   
 $\equiv \exists y \neg \text{student}(y) \vee \text{Pass}(y) \vee \exists y \neg \text{Play}(y)$
- iii)  $\text{student}(\text{John})$
- iv)  $\exists \forall x \exists y (\text{student}(x) \wedge \exists z \text{Study}(z)) \vee \exists y \neg \text{Pass}(y)$   
 $\equiv \forall x \exists y \neg \text{student}(y) \vee \text{Study}(y) \vee \exists y \neg \text{Pass}(y)$
- v)  $\exists \forall x \exists y (\neg \text{Play}(x) \vee \text{FootballStar}(x))$   
 $\equiv \forall y_3 \neg \text{Play}(y_3) \vee \text{FootballStar}(y_3)$   
 $\equiv \neg \text{Play}(y_3) \vee \neg \text{FootballStar}(y_3)$

Proof:

FOL:

$\neg \text{Study}(\text{John}) \rightarrow \neg \text{Loves}(\text{Mary}, \text{John})$

CNF:

- $$\equiv \neg (\neg \text{Study}(\text{John})) \vee \neg \text{Loves}(\text{Mary}, \text{John})$$
- $$\equiv \text{Study}(\text{John}) \vee \neg \text{Loves}(\text{Mary}, \text{John})$$

## Resolution Table:

Steps	Facts	Derivations
1)	$\neg \text{Loves}(\text{Mary}, n) \vee \text{FootballStar}(n)$	Given
2)	$\neg \text{student}(n_1) \vee \text{Pass}(n_1) \vee \neg \text{Play}(n_1)$	"
3)	$\text{Student}(\text{John})$	"
4)	$\neg \text{Student}(n_2) \vee \text{Study}(n_2) \vee \neg \text{Pass}(n_2)$	"
5)	$\text{Play}(n_3) \vee \text{FootballStar}(n_3)$	"
6)	$\neg \text{Student}(\text{John}) \vee \text{Pass}(\text{John}) \vee \neg \text{Play}(\text{John})$	$n_1 = \text{John}$ (Instantiation)
7)	$\text{Pass}(\text{John}) \vee \neg \text{Play}(\text{John})$	Resolution in 2, 3
8)	$\neg \text{Student}(\text{John}) \vee \text{Study}(\text{John}) \vee \neg \text{Pass}(\text{John})$	Resolution in 3, 6
9)	$\text{Study}(\text{John}) \vee \neg \text{Pass}(\text{John})$	<del>Resolution</del> $n_2 = \text{John}$
10)	$\text{Pass}(\text{John}) \vee \neg \text{FootballStar}(\text{John})$	Resolution in 5, 7 $n_3 = \text{John}$
11)	$\text{Study}(\text{John}) \vee \neg \text{FootballStar}(\text{John})$	Resolution in 9, 10
12)	$\text{Study}(\text{John}) \vee \neg \text{Loves}(\text{Mary}, \text{John})$	Resolution in 1, 11

2018 fall

2078/09/12

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Q Birendra likes easy courses.

SMP is a hard course.

All courses in Software Department are easy.

AINN is Software Development course.

Use resolution to answer

What course Birendra likes?

Ans:

FOL:

- i)  $\forall n \text{ EasyCourse}(n) \rightarrow \text{Likes}(\text{Birendra})$
- ii)  $\text{HardCourse(SMP)} \equiv \neg \text{EasyCourse(SMP)}$
- iii)  $\forall n \text{ SoftwareDeptCourse}(n) \rightarrow \text{EasyCourse}(n)$
- iv)  $\text{SoftwareDeptCourse(AINN)}$

CNF:

- i)  $\forall n \text{ EasyCourse}(n) \rightarrow \text{Likes}(\text{Birendra}, n)$   
 $\equiv \forall n \neg \text{EasyCourse}(n) \vee \text{Likes}(\text{Birendra}, n)$  [E: Elimination]  
 $\equiv \neg \text{EasyCourse}(n) \vee \text{Likes}(\text{Birendra}, n)$  [E: Drop  $\forall n$ ]
- iii)  $\forall n \text{ SoftwareDeptCourse}(n) \rightarrow \text{EasyCourse}(n)$   
 $\equiv \forall n \neg \text{SoftwareDeptCourse}(n) \vee \text{EasyCourse}(n)$   
 $\equiv \forall a \neg \text{SoftwareDeptCourse}(a) \vee \text{EasyCourse}(a)$   
 $\equiv \neg \text{SoftwareDeptCourse}(a) \vee \text{EasyCourse}(a)$

## Resolution Table :

Steps	Step facts	Derivations
1)	$\exists \text{EasyCourse}(x) \vee \text{Likes}(\text{Birendra}, x)$	Given
2)	$\exists \text{EasyCourse}(smp)$	"
3)	$\exists \text{SoftwareDeptCourse}(a) \vee \text{EasyCourse}(a)$	"
4)	$\text{SoftwareDeptCourse}(\text{AINN})$	"
5)	$\text{EasyCourse}(\text{AINN})$	$a = \text{AINN}$ (instantiation)
6)	$\text{Likes}(\text{Birendra}, \text{AINN})$	Resolution in 3, 4 $x = \text{AINN}$ R in L, 5
7)	$\text{Birendra likes AINN}$	

g) Marcus was a man.

Marcus was a Roman

All men are people.

Caesar was a Ruler.

All Romans were either loyal to Caesar or hated him.

Everyone is loyal to someone.

People only try to assassinate ruler they are not loyal to.

Marcus tried to assassinate Caesar.

Prove:

Marcus hated Caesar

FOL:

i) Man (Marcus)

ii) Roman (Marcus)

iii)  $\forall x \text{ Man}(x) \rightarrow \text{People}(x)$

iv) Ruler (Caesar)

v)  $\forall x \text{ Roman}(x) \rightarrow \text{LoyalTo}(x, \text{Caesar}) \vee \text{Hated}(x, \text{Caesar})$

vi)  $\exists x \forall y \text{ LoyalTo}(x, y)$

vii)  $\forall x \forall y (\text{People}(x) \wedge \text{Ruler}(y) \wedge \text{LoyalTo}(x, y) \rightarrow \text{TriedToAssassinate}(x, y))$

viii)  $\text{TriedToAssassinate}(\text{Marcus}, \text{Caesar})$

Prove:

Marcus Hated Caesar [Hated (Marcus, Caesar)]

CNF:

→ show all steps

iii)  $\neg \text{Man}(a) \vee \text{People}(a)$

v)  $\neg \text{Roman}(a) \vee \text{LoyalTo}(a, \text{Caesar}) \vee \text{Hated}(a, \text{Caesar})$

vi)  $\neg \text{LoyalTo}(c, f(c))$

vii)  $\neg \text{People}(b) \vee \neg \text{Ruler}(f(b)) \vee \text{LoyalTo}(b, f(b)) \vee \text{TriedToAssassinate}(b, f(b))$

2078/09/18 3

## ~~VVF~~ Semantic Networks & frames

KR scheme that represents knowledge in graphical networks. Also called "Associative network".

### \* Associative Network:

↳ shows association between nodes

↳ consists of:

1) Nodes

2) Links / Edges

3) Link Labels

#### 1) Nodes:

Represents entity (nouns) or objects represented by circle, ellipse or rectangle.

#### 2) Links / Edges:

Represents direction of relationship between nodes.

#### 3) Link Labels:

Represents the relationship between nodes.

### \* Knowledge Representation

↳ Production Rule

↳ Logic - Proposition

↳ Predicate

↳ Semantic Nets

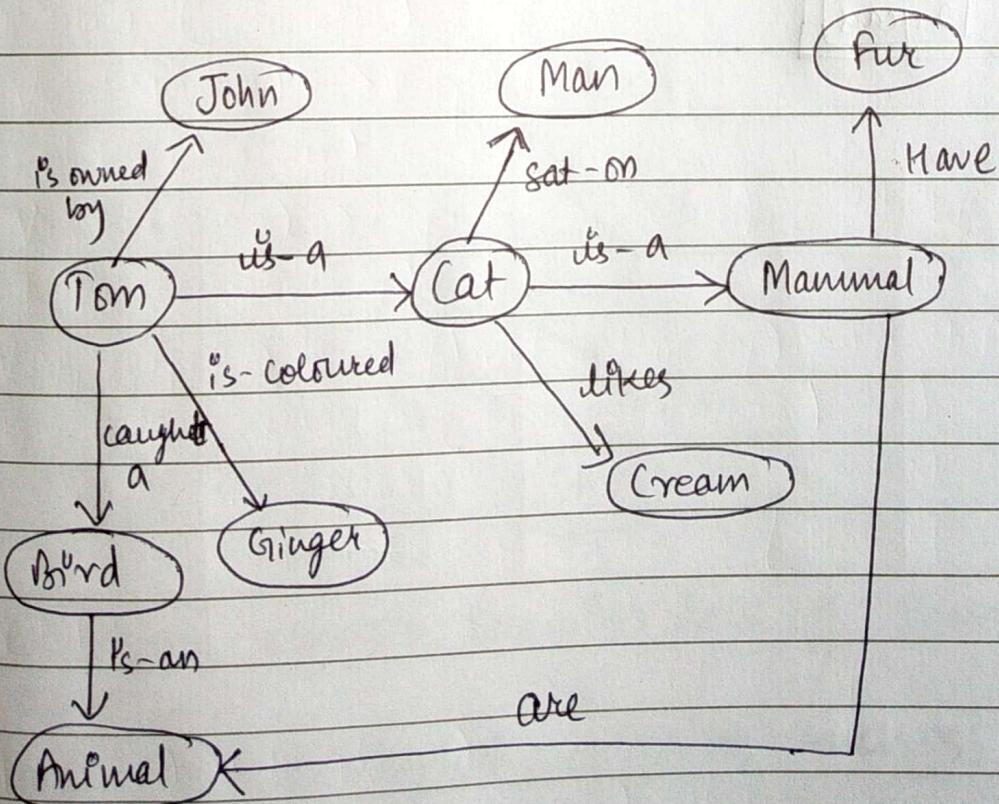
↳ Frames

VVI

## Represent following in Semantic Network

- 1) Tom is a Cat.
- 2) Tom caught a bird.
- 3) Tom is ginger in color.
- 4) Cats like cream.
- 5) Tom is owned by John
- 6) The cat sat on the mat.
- 7) A cat is a mammal.
- 8) All bird is an animal.
- 9) All mammals are animals.
- 10) Mammals have fur.

Sol"



frames:

- ↳ represent additional proper or characteristics of entity/nodes in semantic networks.
  - ↳ extension of semantic networks
  - ↳ Represent characteristics in key-value pair

eg !

Tom  
Height 100m  
Weight 20kg  
Age 2 years

Animal	
color	[Ginger]
Type	[cat]

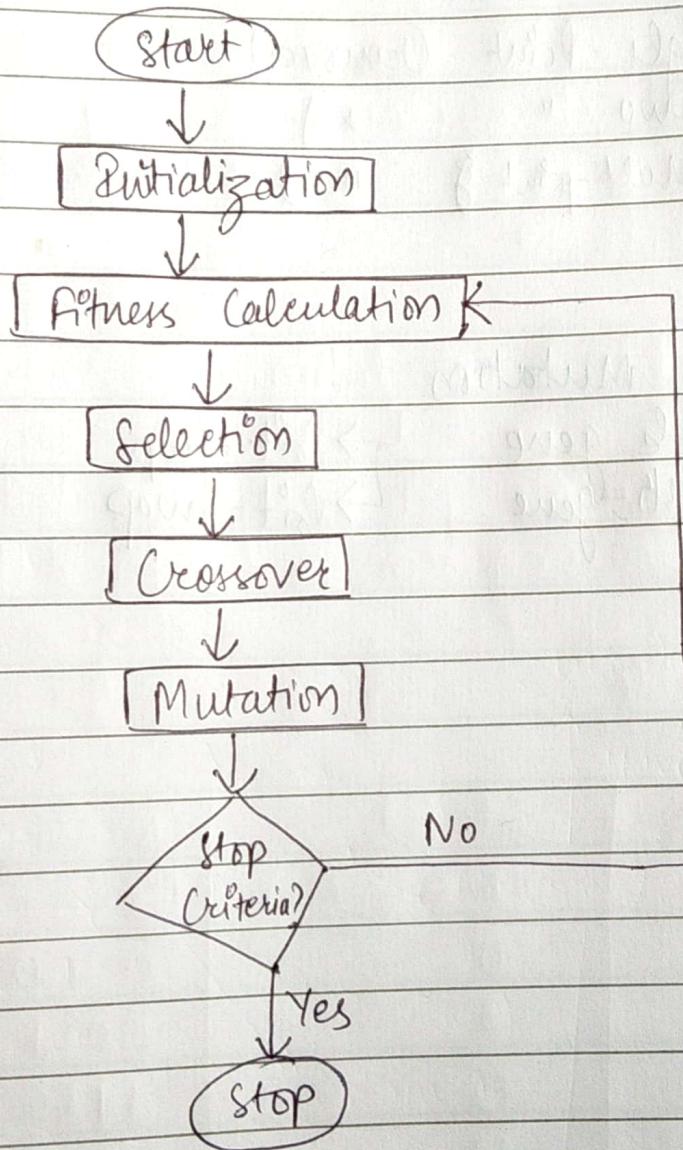
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## Chapter - 5

### Genetic Algorithm (GA)

- ↳ Maximization / Optimization Algorithm



- ↳ Based on Charles Darwin's Law of Theory of Natural Selection.
- ↳ Based on Biological operators such as;
  - Selection
  - Crossover
  - Mutation

~~2078/09/19~~

Q) Maximize  $f(n) = n^2$ ;  $0 \leq n \leq 31$ ,  $n = 4$   
 $f(x) = 15x - x^2$ ,  $0 \leq x \leq 31$

↳ Types of Crossover:

- 1) SPX (Single Point Crossover)
- 2) TPX (Two " "
- 3) MPX (Multi-point " )

↳ Types of Mutation

- ↳ Single gene
- ↳ Multi-gene
- ↳ Bit-flip
- ↳ Bit-swap

2078/09/19

2019 Fall

Use GA to find maximum value of function  
 $f(n) = 15n - n^2$ ,  $0 \leq n \leq 15$  and take population size of 4.

### Step 1: Initialization

Select chromosomes randomly where no. of chromosomes equals to population size.  
 $n = 0, 3, 12, 14$

### Step 2: fitness Calculation

Calculate fitness of selected chromosomes.  
 The fitness equation is defined by  $f(n) = 15n - n^2$

### Fitness Table

Chromosome Label	Selected Chromosome (n)	Chromosome (in Binary)	Fitness Value (f(n))
A	0	0000	0
B	3	0011	36
C	12	1100	36
D	14	1110	14

$\Sigma f(n) = 86$

### Step 3: Selection

B & C , B & D

Select parent chromosomes for crossover.

## Step 4: Crossover / Mating / Reproduction

$$B = 0|011$$

$$C = 1|100$$
  
SPX

$$b = 0|011$$

$$D = 1|110$$
  
SPX

Exchange of genes between parent chromosomes

$$B' = 0100$$

$$B'' = 0110$$

$$C' = 1011$$

$$D = 1011$$

$$A = 10|10|11$$

$$B = 01|10|10$$

TPY

$$A = 10|00|100$$

$$B = 0\boxed{1}|10|010$$

MPX

$$A' = 101011$$

$$B' = 011010$$

$$A' = 1010100$$

$$B' = 0100010$$

## Step 5: Mutation

Random change in gene of chromosome

$$C' = \boxed{1}011 = 0111$$

Bit swap

2nd Gen

PTO

Fitness Table

Chromosome Label	Selected Chromosome ( $n$ )	Chromosome (in binary)	Fitness Value ( $f(n)$ )
B'	4	0100	44
C''	7	0111	56
B''	6	0110	54
D'	11	1011	44
$\Sigma f(n) = 198$			

Conclusion:

- 1) Fitness value increased from 86 to 198
- 2) When,  $n=7$ ,  $f(n)$  its maximum

$$f(n) = 15n - n^2, \quad 0 \leq n \leq 31, \quad n=6$$

Step 1: Initialization

$$n = 0, 3, 12, 15, 5, 6, 20$$

Step 2: Fitness Calculation

1st Gen

Fitness Table

Chromosome Label	Selected Chromosomes (n)	Chromosome (In binary)	Fitness Value [f(n)]
A	0	00000	0
B	3	00011	36
C	12	01100	36
D	5	00101	50
E	6	00110	54
F	20	10100	-100
$\sum f(n) = 76$			

Step 3: Selection

E & D, E & C, B & D

### Step 4: Crossover

$$E = 00110$$

$$D = \cancel{00101}$$

$$E = 00110$$

$$C = \cancel{01100}$$

$$B = 00\cancel{0}11$$

$$D = 00101$$

$$E' = 00101$$

$$D' = \underline{00110}$$

$$E'' = 00100$$

$$C' = 01110$$

$$B' = 00101$$

$$D'' = \underline{00011}$$

Here, Mutation on

( $E'$ ) & ( $B'$ )

$$B' = \boxed{0}0101$$

$$B'' = \underline{1}0101$$

(single gene  
bit-flip)

2nd Gen

Fitness Table

Chromosome Label	Selected Chromosome (n)	Chromosome (in binary)	Fitness Value [f(n)]
E'	5	00101	50
D'	6	00110	54
E''	9	00100	44
C'	14	01110	14
B''	21	10101	-126
D''	3	00011	36
$\Sigma f(n) = 72$			

- 1) fitness value decreased from 76 to 72
- 2) When,  $n=6$ ,  $f(n)$  is maximum

2078/09/21

Q No. of bits in chromosome = 8  
 $f(x) = (a+b) - (c-d) + (e+f) - (g+h)$   
 Take pop size ( $n$ ) = 6

Soln,

→ Initialization:

1st gen:	a	b	c	d	e	f	g	h
A	5	4	3	2	1	1	2	3
B	1	2	3	4	5	6	7	8
C	9	9	9	9	9	9	9	9
D	2	4	6	8	1	3	5	7
E	0	0	0	0	0	0	0	0
F	9	8	4	1	0	4	2	6

→ Fitness Calculation:

$$\begin{aligned}
 A &= 11 & - (5) \\
 B &= 16 & - (3) \\
 C &= 36 & - (1) \\
 D &= 14 & - (4) \\
 E &= 0 & - (6) \\
 F &= 22 & - (2) \\
 &\hline
 &+ 99
 \end{aligned}$$

→ Selection:

C &amp; F, C &amp; B, C &amp; D

GA operators  
 - fitness calc  
 - selection  
 - crossover  
 - mutation

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→ Crossover :

$$C = 9999|9999$$

$$F = 9841|0426$$

SPX

$$C = 9999|9999$$

$$B = 1234|5678$$

SPX

$$C = 9999|9999$$

$$D = 2468|1357$$

SPX

$$C' = 99990426$$

$$F' = 98419999$$

$$C'' = 99995678$$

$$B = 12349999$$

$$C''' = 99991957$$

$$D' = 24689999$$

→ Mutation! No Mutation

2nd gen:

f(n)

$$C' = 26$$

$$F' = 32$$

$$C'' = 30$$

$$B' = 22$$

$$C''' = 24$$

$$D' = 26$$

# Machine Learning (ML)

- ↳ Application of AI that deals with training machines for learning and improving from experience without design being explicitly programmed.
- ↳ Types of ML
- + 1) Supervised ML : i/p + processing given / training labels given
- + 2) Unsupervised ML: i/p , self-processing / training labels not given
- + 3) Reinforcement ML: