

An Investigation into Machine Learning and Neural Networks through the Simulation of Human Survival

Computer Science NEA

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2. Analysis

1. Statement of Investigation

I plan to investigate Machine Learning by developing a survival simulation environment in which a character will be controlled by a Machine Learning algorithm. The survival simulation will present multiple challenges such as dynamic threats towards the agent in order to provide a complex problem for it to solve. The key question I aim to answer with this investigation is:

Can you train a Machine Learning algorithm to survive in a pseudo random, open-world environment?

I find this question to be quite interesting because there is multiple layers of complexity to it, with several different problems to solve. Answering the question will require me to dive headfirst into Machine Learning picking things up as fast as possible.

2. Background

I am investigating this area of Computer Science because I've been interesting in attempting a form of Machine Learning for a while now but haven't had a reason to dive into it. Machine Learning is an evolving field, with mere infinite applications such as Image Recognition, Chat Bots, Self Driving Cars, etc. I feel as though my project will be sufficiently advanced enough to expand my knowledge of the subject. It will require lots of research, planning, and design work in order to successfully fulfil my Technical Solution.

3. Expert

For my expert I approached one of my friends, Shaun, who has prior experience with Machine Learning. He has created his own Hand Written Digit Recognition Network before, along with using Python Libraries such as *PyTorch* to train an agent to play the game *Flappy Bird*, among other ML projects. He has a much better understanding of Machine Learning than me currently, so hopefully he will be a good resource as I develop my project.

He has agreed to answer some questions for my Interview once I have completed my Initial Investigation.

4. Initial Research

(a) Existing Investigations

i. Crafter

In my research on the Internet I discovered a project called *Crafter*.

<https://github.com/danijar/crafter>

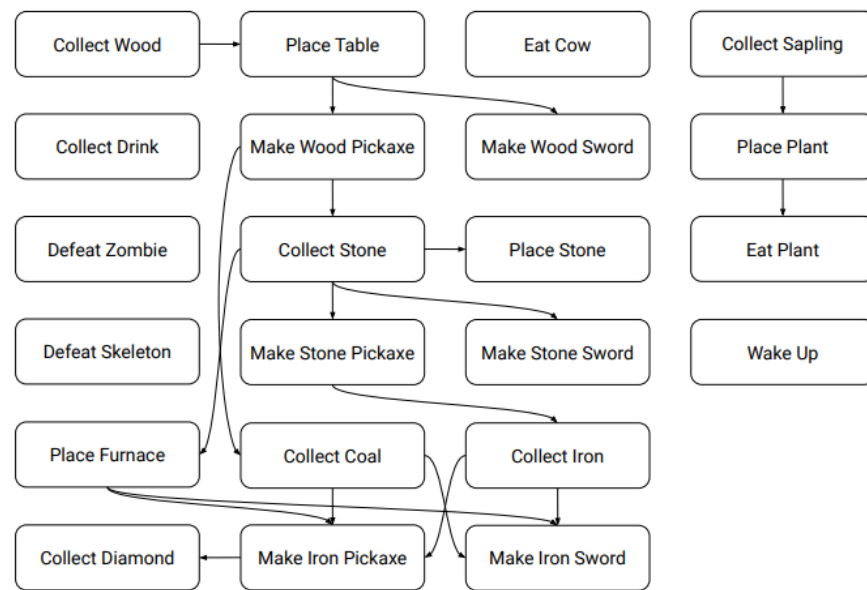
Crafter is described to be "*Benchmarking the Spectrum of Agent Capabilities*", and is utilised in conjunction with Machine Learning Algorithms such as

DreamerV2, *PPO* and *Rainbow*. Crafter poses significant challenge towards its Player, requiring high levels of generalisation, long-term reasoning, and complex problem solving. If the machine Learning algorithm in question fails to achieve one of these aspects it will struggle to full "Solve" the simulation.

High levels of generalisation are required when training a Machine Learning algorithm, if this is not achieved then your network will only lend itself to a single Dataset/Problem. An example of this would be training a network used to recognise hand written digits on only one way of writing 4's, if presented with an input for a different type of 4 it may not recognise it and identify it incorrectly.

Long-Term reasoning is a complex problem to solve in the context of Machine Learning, current Machine Learning models struggle to deal with this problem. This is dealt with by using algorithms built to mimic "memory". A common implementation of this is Experience Replay which stores states in a queue, and relearns from it after every N ammount of steps.

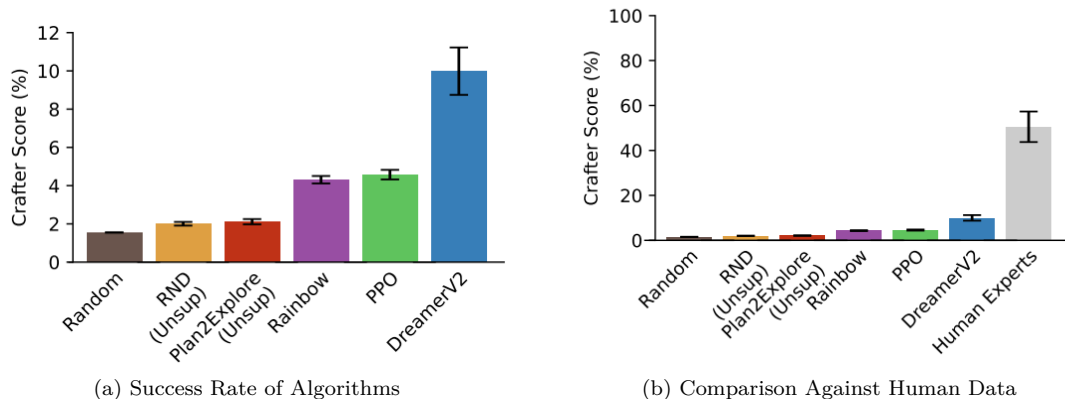
A complex reward and action system may take time for an algorithm to learn but it certainly is possible with current Machine Learning Models. Crafter utilises a complex action system with a flow chart determining which Action can be taken given the current state of the simulation. Below is shown the Complex Flow Chart of Actions:



Complex action system as shown in the Paper "Benchmarking the Spectrum of Agent Capabilities"

Crafter manages to achieve quite high success rates with various Algorithms, but they still fail to overcome, or even match human standards. This is likely due to the complexity of the problem, and in theory will be solvable within the near future as Machine Learning advances over the next few years. This is why I plan to create a simpler simulation which the Agent will be more likely to be able to solve. Below is shown the Success Rate Data for both Algorithms and Human Experts.

While I would love to create a simulation similar to crafter, it is very complex and would take a long time to develop. Yet would not net many marks in the process. Overall I feel like Crafter is a good example that my project is possible, but will require a complex Machine Learning Model in order to achieve reliable



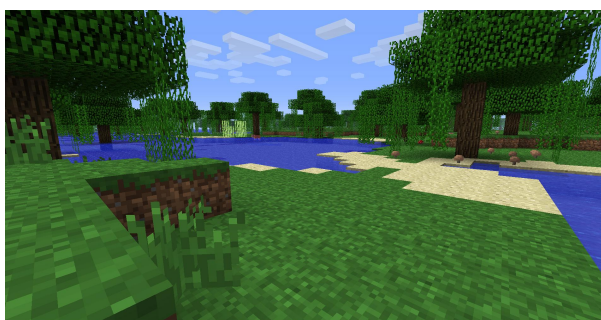
results from my Investigation.

ii. Minecraft

Minecraft is a *very* popular Game. It's a sandbox game, meaning that the player can do almost anything they want. The game is formed from blocks which can be broken or placed, along with a plethora of items, enemies, passive animals and more. It has infinite terrain generation, and explicitly uses Perlin Noise, and is generated from a seed. The seed determines all the terrain generation, loot tables, random structures, caves, etc.

First it starts off on a very broad level, painting a basic topographical map of the world. It uses Perlin Noise to sample a height value for each chunk, where chunks are 16x16 areas of blocks. Then within these chunks the game uses the Diamond Square algorithm to interpolate between it and the chunks around it, creating blocks where the terrain should be. This produces an entirely deterministic results based upon the seed.

Secondly, the Caves are generated using Perlin Worms, which travel in deterministic directions based on their starting position. These worms dig through the terrain carving out caves which can then be traversed by the player. Within these Caves spawn water sources, pools of lava, useful ores. All of these are deterministically generated by the original seed.



Example of Minecraft's terrain generation in a Swamp Biome



Example of a Sunken Pirate Ship Structure

Minecraft itself is too complex and dynamic to be solved by current Machine Learning algorithms, along with there is no quantifiable metric for performance due to its sandbox nature. There exist data sets for Minecraft, in the form of captured gameplay footage, but there has been little to no success of quantifiably good solutions to solving Machine Learning problems within Minecraft.

Overall I feel like it would be good to borrow elements from Minecraft's terrain generation, such as its utilisation of Perlin Noise. But the majority of the games systems are way too complex for a Machine Learning algorithm to solve.

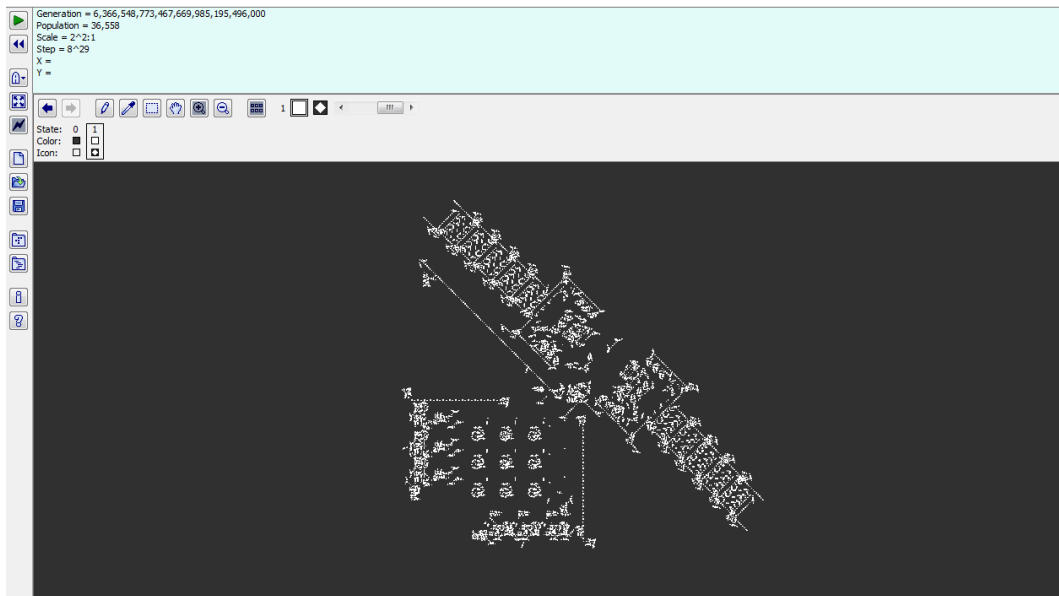
iii. **Conway's Game of Life**

Conway's Game of Life is what's called a Cellular Automaton, which is a discrete computation model formed from a grid of cells along with a ruleset. Conway's is commonly referred to a Zero Player Game, where the input for the Automaton is defined at the start, with no further adjustment needed for it to run. The game is fully Turing complete and can simulate a Universal Constructor.

The rules of Conway's are such that:

1. Any live cell with fewer than two live neighbours dies, as if by underpopulation.
2. Any live cell with two or three live neighbours lives on to the next generation.
3. Any live cell with more than three live neighbours dies, as if by overpopulation.
4. Any dead cell with exactly three live neighbours becomes a live cell.

It is rather interesting that such complicated Machines can be formed from such a simple ruleset, as an example here is a Turing Machine formed from 34 Thousand Cells:



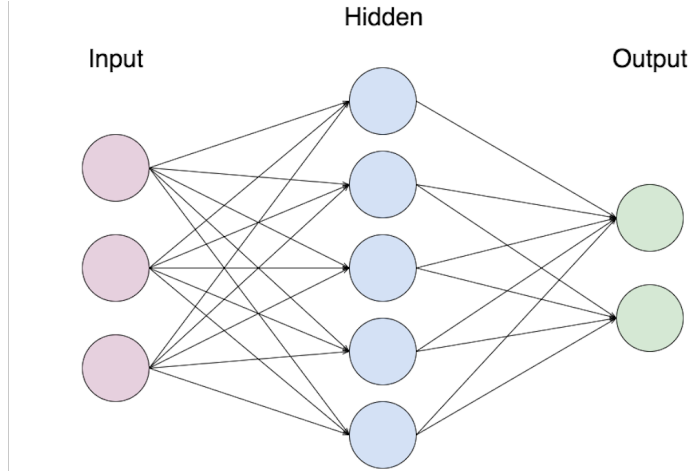
Overall, I think this shows that my simulation doesn't need to have complex rules in order to achieve interesting results. Conway's is formed from 4 simple rules, and yet is Turing complete.

(b) Algorithms and Potential Data Types

Neural Network and Matrices

As part of developing a Machine Learning Algorithm, I will need to implement a Matrix class in order to implement a neural network. Matrices are commonly used to represent individual layers of a network. Along with making calculations much easier, condensing them into performing operations on matrices, rather than nested using nested for loops and lists. As part of my Initial Research I have taken the time to understand how a Neural Network functions, it turns out I have already learned most of the Maths needed to understand how it works in my A Level Maths and Further Maths courses.

A Neural Network functions as a series of mathematical equations used to recognise relationships between inputs and desired outputs. They take in a Vector of Input Data, and output a Vector of Output Data. They can be in simple terms as a function: $N(x)$ where: $\{x \in V, N(x) \in V\}$. The function's name in this case is Forward Propagation. We form a Neural Network with multiple layers of Nodes, the layers being referred to as the Input Layer, Hidden Layer/s and Output Layer. In this case each Node is connected to every Node in the previous layer and the following layer. In the below image is represented a Neural Network with a layer structure of [3, 5, 2].

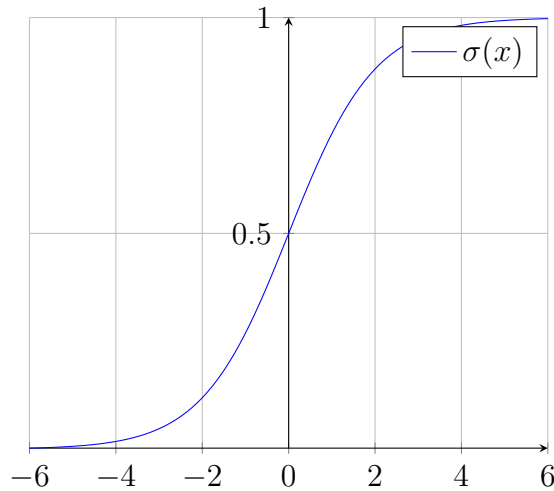


Each connection, otherwise known as an Arc or Edge, has an associated weight. Along with every output of a layer having an associated Bias. These are used to compute the outcome of a network. Forward Propagation is used to compute the outcome of a network, it has a general form and uses Matrix Multiplication and Addition to achieve this.

$$S^{(L)} = \begin{bmatrix} s_0^{(L)} \\ s_1^{(L)} \\ \vdots \\ s_n^{(L)} \end{bmatrix} = \begin{bmatrix} w_{0,0}^{(L-1)} & w_{0,1}^{(L-1)} & \dots & w_{0,m}^{(L-1)} \\ w_{1,0}^{(L-1)} & w_{1,1}^{(L-1)} & \dots & w_{1,m}^{(L-1)} \\ \vdots & \vdots & \ddots & \vdots \\ w_{n,0}^{(L-1)} & w_{n,1}^{(L-1)} & \dots & w_{n,m}^{(L-1)} \end{bmatrix} \begin{bmatrix} a_0^{(L-1)} \\ a_1^{(L-1)} \\ \vdots \\ a_n^{(L-1)} \end{bmatrix} + \begin{bmatrix} b_0^{(L)} \\ b_1^{(L)} \\ \vdots \\ b_n^{(L)} \end{bmatrix}$$

$$\sigma(S^{(L)}) = \sigma \left(\begin{bmatrix} s_0^{(L)} \\ s_1^{(L)} \\ \vdots \\ s_n^{(L)} \end{bmatrix} \right) = \begin{bmatrix} \sigma(s_0^{(L)}) \\ \sigma(s_1^{(L)}) \\ \vdots \\ \sigma(s_n^{(L)}) \end{bmatrix}$$

We then apply an activation function as shown above, in this case we will apply the Sigmoid function: $\sigma(x)$ to $S^{(L)}$. The Sigmoid function is a Mathematical Function which *squishes* values between 0 and 1. Shown Below:



Matrices can be used for all parts of a Neural Network implementation, and will prove very useful in my Technical Solution.

Procedural Generation

For my project I am going to have to procedurally generate 2d terrain, while researching this I came across a few algorithms which seemed to be able to do this pretty well. I will compare two algorithms I discovered below.

Post-Processing Algorithms	Perlin Noise
<p>I discovered two post processing algorithms often used for simple 2d terrain generation. 1 Averages squares around the selected square, and the other pulls it up or down the gradient its currently on. I find these interesting because they're relatively simple, and I'm not quite sure whether they will produce good results or not. So it would be interesting to test out implementing these in my prototype.</p>	<p>Perlin Noise is an algorithm developed by Ken Perlin for use in the digital generation of noise. This noise can be combined to create <i>realistic</i> looking height maps for world generation. Perlin Noise retains continuity and is seeded so the generation can be entirely controlled. By "retains continuity" I mean that you can sample the same point and retrieve the same value.</p> <p>If I was to implement Perlin noise it would take longer, but also might end up with a better result due to it being more widely used. It's a trade-off between time to implement and desired result.</p>

I also discovered an algorithm called Poisson Disc Sampling, this can be used to sample random points in N dimensional space. It takes in 2 values, the R and K value, these values determine the output of the function. The R values is the minimum distance a point has to be from another, randomly placed point which hasn't been selected yet. If the distance between any existing points is less than R, the point will be rejected and another will be selected. The K value determines how many rejected are needed before the algorithm will stop attempting to choose a new point.

Proposed Programming Language and Associated Libraries

When selecting a Programming Language and associated Graphical Libraries I took into consideration a few options. Below I have weighed up 3 options for Programming Language, along with 2 graphical libraries per language

Proposed Solution	Benefits and Downsides of Proposed Solution
Python	Python is the first thought which comes to mind when I think about programming, it is my favourite language and I'm yet to find anything which I prefer. Its very versatile and great for rapid prototyping, the dynamic typing makes It great for coding quickly without worrying too much about whether you're using a <i>float32</i> or <i>float64</i> . It also has hundreds of libraries and is very well supported by its developers and the community.

Python Graphical Libraries	Pygame	Pygame is a highly customizable and well developed binding of <i>Simple DirectMedia Layer</i> (SDL) Library. It has a full set of 2d drawing tools, along with keyboard and audio capabilities. I have lots of experience with Pygame so I already have code which I can take from, which will speed up development when dealing with the Pygame library.
	Tkinter	Tkinter provides an interface to the standard <i>Tcl/Tk GUI Toolkit</i> , which is available for most platforms, this makes it highly versatile. Though as my project is not intended as a software package I dont see this as being an incredibly big selling point. Tkinter will serve mostly the same purpose as Pygame but give me easier options for Graphical Input, I dont currently plan to add GUI so this feature isnt neccesary.
C#	C# is my second favourite language, I have plenty of experience with it from developing games with Unity. Its faster than Python and is less abstracted, but this speed isn't necessarily required for my project. With C# I could utilise the <i>Unity Game Engine</i> for my project, but then I might end-up relying on builtin types and functions rather than developing my own.	

Proposed Solution	Benefits and Downsides of Proposed Solution	
C# Graphical Libraries	Windows Forms	Windows Forms is a relatively simple drag drop interface for designing your own applications. I've never used it before but I could utilise it with C# to create my project. I believe it might be a bit overkill for my needs though, as it includes many, many UI features which I will have no use for.
	WPF	WPF or <i>Windows Presentation Foundation</i> is a versatile development platform for desktop applications. It is relatively versatile in its uses and utilises XAML and is the UI Language of Windows Platforms. XAML would be a new language for me to learn but I have experience with HTML so I don't believe it would be too difficult. The platform would provide a stable base to my project.
Rust	Rust is low level language designed for speed and efficiency, I started using it recently as a side hobby and would like to use it more in future projects of mine. Though I feel like it may be a bit overkill for a Computer Science NEA, with it often being used for server side applications rather than general purpose applications.	
Rust Graphical Libraries	Piston2d	Piston2d is a feature complete 2d graphics library which utilises OpenGL, I've worked with it briefly before and I believe it would be a good option over Pixels if I needed more complex drawing methods.
	Pixels	Pixels is a lightweight 2d graphics library designed to simply push pixels to the screen, Its relatively simple and ive used it for making a simple <i>Falling Sand Game</i> before, could be a good little option if I wanted to develop a lightweight solution.

(c) Interview

5. Prototype

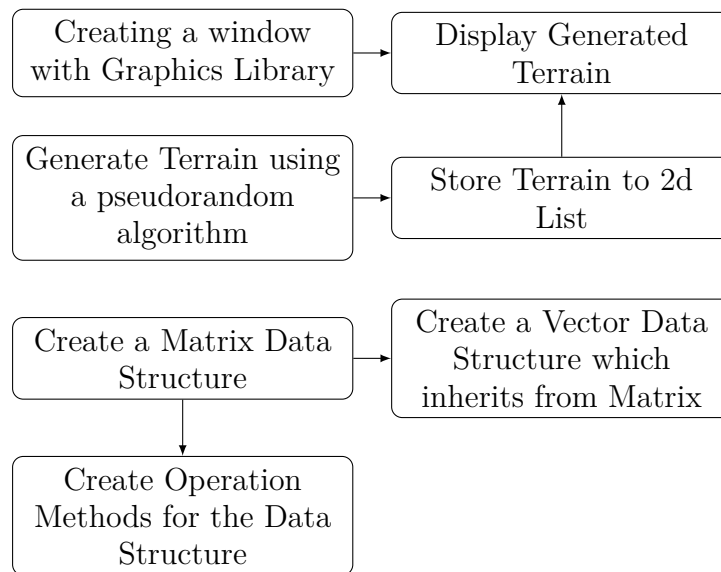
Before starting my Prototype I had to decide upon a short list of objectives I wanted to complete/investigate as part of it. These boiled down to a few things:

- (a) Terrain Generation
- (b) Displaying the Generated Terrain using a Graphics Library
- (c) Matrix and Vector implementation

For my Prototype, I first created a GitHub Repository, available here:

<https://github.com/TheTacBanana/CompSciNEAPrototype>

I had created a hierarchy of importance for development in my head, visualized using this flow diagram:



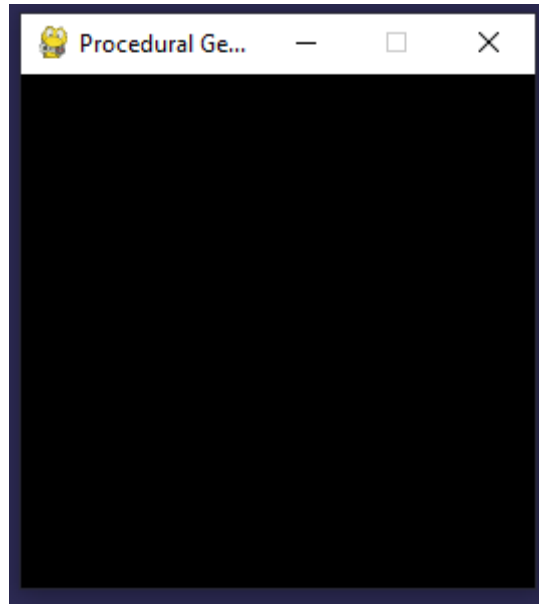
I decided to use Python for developing my Prototype, this seemed like a good fit due to me having lots of experience with the language. Python is a Dynamically Typed and Interpretted language which makes it versatile for prototyping and fast, iterative development.

Terrain Generation and Displaying

Starting from the begining of my hierarchy I installed Pygame using *pip* and started creating a window. This was a relatively simple task only taking a few lines:

```
1  import pygame
2
3  simSize = 128
4  gridSize = 2
5
6  window = pygame.display.set_mode((simSize*gridSize, simSize*gridSize))
7  pygame.display.set_caption("Procedural Generation")
8
9  running = True
10 while running == True:
11     for event in pygame.event.get():
12         if event.type == pygame.QUIT:
13             running = False
```

This creates a window like this:



Following the hierarchy I then added noise generation by generating random numbers and assigning them to a 2d List. Shown here:

```
1 def GenerateMap(self, seed):
2     random.seed(seed)
3     for y in range(0, self.arraySize):
4         for x in range(0, self.arraySize):
5             self.heightArray[x][y] = round(random.random(),2)
```

After creating some code to draw squares based upon the random value, I ended up with this random array of Black-White squares:



This was a good start, but didnt really look like terrain yet. As part of my research I came across simple algorithms to turn random noise into usable 2d terrain. I decided to implement these algorithms. They are relatively short and didnt take too much time to implement. I've named the two algorithms UpDownNeutralGen and Average.

UpDownNeutralGen Method

The UpDownNeutralGen method takes a tile, and considers every tile around it. It sums the tile which are greater than, less than, or within a certain range of the tile height. And then pulls the selected tile in the direction which has the highest precedence. As an example, here are some randomly generated values:

0.71	0.19	0.3
0.46	0.26	0.82
0.63	0.35	0.05

If we count the surrounding values into corresponding Higher, Lower and Neutral we get:

Higher	Lower	Neutral
4	1	3

This leads us to calculating the *pullValue*, respectively for each case:

$$\begin{aligned} Up- &> pullValue = upTiles * 0.09 \\ Down- &> pullValue = upTiles * -0.08 \\ Neutral- &> pullValue = 0 \end{aligned}$$

$$Value[x][y] += pullValue$$

We then add the pullValue to the original square value, leaving us with the updated value. The code for this shown under the Prototype Code Header.

Average Method

The Average method takes a tile and considers every tile around it, this time instead of looking at the differences, it creates an average from the 8 surrounding tiles. It then sets the selected tile to this average value. As an example, here are some randomly generated values:

0.83	0.93	0.64
0.07	0.38	0.21
0.33	0.94	0.95

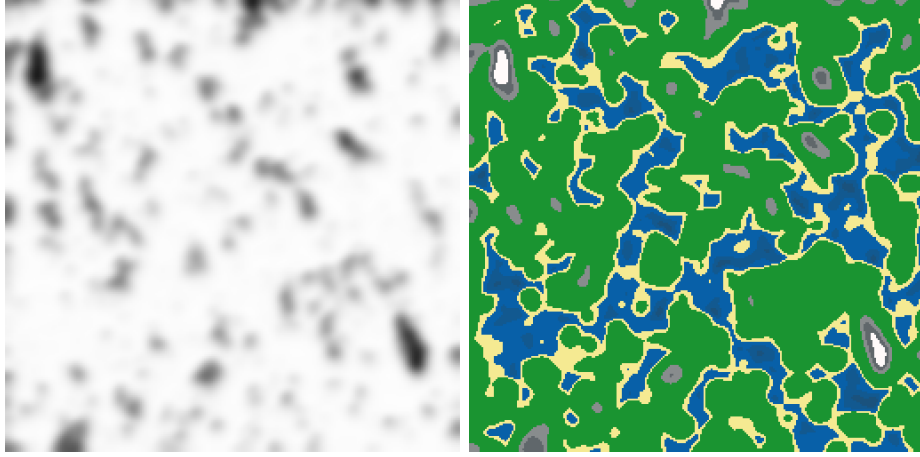
Summing these and dividing by the total grants us the average:

$$\frac{0.83 + 0.93 + 0.64 + 0.07 + 0.38 + 0.21 + 0.95 + 0.33 + 0.94}{9} = 0.586$$
$$Value[x][y] = 0.586$$

The code for this shown under the Prototype Code Header.

Finished Terrain Generation

Overall I am happy with the Terrain generation, though I feel as if it could be improved to look more realistic. The difference between the original random noise and the Colour Mapped Terrain looks so much better.



Matrix Data Structure

As part of my Matrix Class I made a list of operations which would be key to a Matrix Class, along with being useful for Machine Learning. A Matrix is an abstract data type, commonly used in Maths, but has practical uses in the world of Computer Science. It holds a 2d array of values such as:

$$\begin{pmatrix} a & b \\ c & d \end{pmatrix} \begin{pmatrix} a & b & c \\ d & e & f \\ g & h & i \end{pmatrix} \begin{pmatrix} a \\ b \\ c \end{pmatrix} \begin{pmatrix} a & b & c & d \\ e & f & g & h \end{pmatrix}$$

The values in a Matrix can be manipulated using common operations such as $+$ $-$ $*$ as long as the orders of the 2 Matrices match up. Along with other, non-standard operations which have other purposes.

As part of my Matrix Class, I implemented the following operators:

(a) Addition/Subtraction

Implementing Addition didnt take too long, I utilised a nested for loop to iterate over every value in both Matrices. Adding the two values together into a temporary Matrix which the method then returned.

$$\begin{pmatrix} a & b \\ c & d \end{pmatrix} + \begin{pmatrix} e & f \\ g & h \end{pmatrix} = \begin{pmatrix} a+e & b+f \\ c+g & d+h \end{pmatrix}$$

(b) Multiplication

Multiplication of Matrices is slightly more complicated, it is of $O(n^3)$ complexity, utilising a triple nested for loop. It multiplies the row of a $M1$, by the column in $M2$. Summing the calculation into the element in the new Matrix $M3$.

$$\begin{pmatrix} a & b \\ c & d \end{pmatrix} * \begin{pmatrix} e & f \\ g & h \end{pmatrix} = \begin{pmatrix} a * e + b * g & a * f + b * h \\ c * e + d * g & c * f + d * h \end{pmatrix}$$

There is also Scalar Multiplication which multiplies each value of a Matrix by the Scalar.

$$k * \begin{pmatrix} a & b \\ c & d \end{pmatrix} = \begin{pmatrix} ka & kb \\ kc & kd \end{pmatrix}$$

(c) Determinant

Calculating the Determinant of an NxN Matrix is a recursive algorithm. With the base case being the Determinant of a 2x2 Matrix. When calculating the Determinant of a 3x3 Matrix you create a Matrix of Cofactors, and multiply each value by the corresponding value in the Sin Matrix (*Formed from repeating 1's and -1's*). Summing the values from a singular Row or Column will then give you the Determinant. For a 4x4 you simply calculate the Determinant of the corresponding 3x3's to get the Cofactors.

$$\begin{vmatrix} a & b \\ c & d \end{vmatrix} = a * d - b * c$$

$$\begin{vmatrix} a & b & c \\ d & e & f \\ g & h & i \end{vmatrix} = a * \begin{vmatrix} e & f \\ h & i \end{vmatrix} - b * \begin{vmatrix} d & f \\ g & i \end{vmatrix} + c * \begin{vmatrix} d & e \\ g & h \end{vmatrix}$$

(d) Dot Product

The Dot Product occurs between two vectors, and can be used to calculate the angle between them. Its a relatively simple operation only taking a few lines of code.

$$\begin{pmatrix} a \\ b \\ c \end{pmatrix} \cdot \begin{pmatrix} d \\ e \\ f \end{pmatrix} = a * d + b * e + c * f$$

All code is available under the Prototype Code Header.

Prototype Evaluation

Overall I am happy with my prototype, though I feel like some parts need to be improved. I did meet my objectives for my prototype but there were improvements which can be made when I create my Technical Solution. Namely the Terrain Generation along with the Matrix class. I feel that Perlin noise would be a better alternative to the two algorithms I used. In theory it should produce better results, and also provide more marks for complexity. My Matrix class could be rewritten to be more efficient, along with using operator overloading, which I didn't know Python could do at the time. I also feel like having vector inherit from matrix is relatively pointless, there is no need for it when I could just use 1 wide Matrices.

6. Interview

As part of my Investigation I approached my friend Shaun, who has Machine Learning Experience, to give me feedback on my research. Along with any suggestions for my investigation. I formed a list of questions to ask him, the responses are paraphrased for clarity.

(a)

7. Objectives

Taking into account my Prototype and Interview, I have formed a list of objectives I feel to be most appropriate for my Investigation. If all completed they will form a complete solution which will answer my Investigations question. Below is the list of objectives split into 6 key sections:

(a) User Input

- i. Read Parameters from a Json formatted file
- ii. Check Parameters fall within a certain range to prevent errors
- iii. Give user option to load Neural Network Training progress

(b) Simulation

- i. Utilise Perlin Noise to generate a 2d List of terrain heights
- ii. Store Terrain Heights in a Tile Data Type
- iii. Utilise Threading to generate Terrain Faster
- iv. Display terrain to a pygame window
- v. Map ranges of terrain heights to specific colour bands
- vi. Utilise Poisson Disc Sampling to generate objects for the Agent to interact with
- vii. Implement enemies which use basic pathfinding to traverse towards the player
- viii. Generate multiple enemies upon starting the simulation
- ix. Allow the enemies to attack the Agent

(c) Agent

- i. Implement Movement options for the Agent
- ii. Implement the ability to pick up the generated Objects
- iii. Implement the ability to attack the generated enemies
- iv. Create methods to sample the terrain around the Agent
- v. Create methods to convert the sampled Tiles into a grayscale input vector for a neural network
- vi. Create reward methods to reward the agent given the terrain samples and action

(d) Matrix Class

- i. Implement a Dynamic Matrix Class with appropriate Operations such as:
 - A. Multiplication
 - B. Addition
 - C. Subtraction
 - D. Transpose
 - E. Sum
 - F. Select Row/Column
- ii. Create appropriate errors to throw when utilising methods the incorrect way

(e) Deep Q Learning

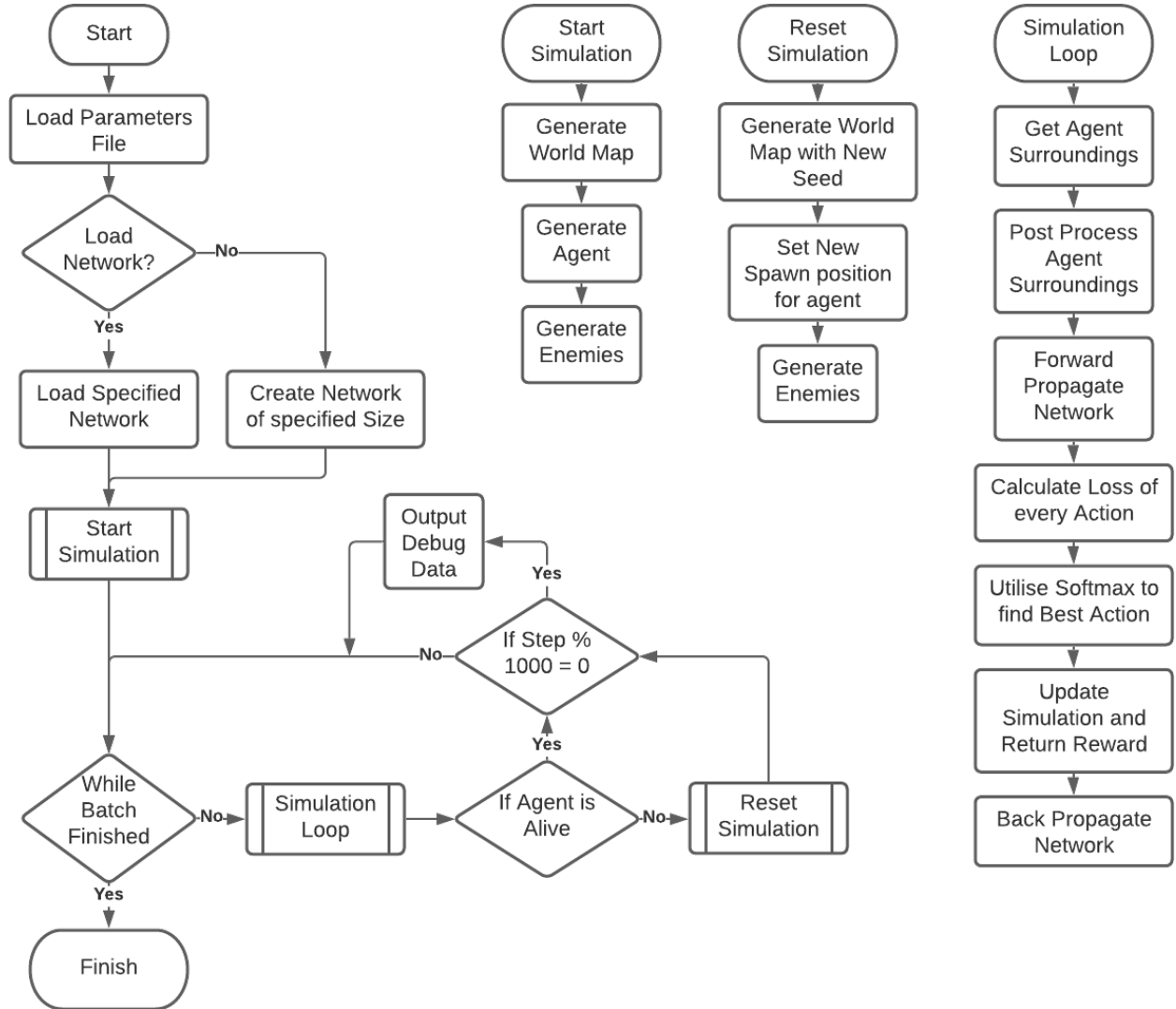
- i. Dynamically create a Dual Neural Network model based upon loaded parameters
- ii. Implement an Abstract Class for Activation Functions
- iii. Implement Activation Functions inheriting from the Abstract Class such as:
 - A. ReLu
 - B. Sigmoid
 - C. SoftMax
- iv. Create methods to Forward Propagate the neural network
- v. Create methods to calculate the loss of the network using the Bellman Equation

- vi. Create methods to Back Propagate calculated error through the neural network
 - vii. Create methods to update weights and biases within the network to converge on a well trained network
 - viii. Utilise the outlined Matrix class to perform the mathematical operations in the specified methods
 - ix. Implement Load and Save Methods to save progress in training
 - x. Implement a Double Ended Queue/Deque Data Type
 - xi. Implement Experience Replay utilising the Deque Data Type to increase training accuracy
- (f) Data Logger
- i. Be able to create a Data Logger class to log data points across training
 - ii. Be able to create a Data Structure for the Data Logger
 - iii. Allow multiple types specified types for a single parameter
 - iv. When adding a new Data Point the Logger will check it to make sure it matches the given Data Structure
 - v. Implement a Heap Data Type
 - vi. Implement a Heap sort using the Heap Data Type
 - vii. Be able to sort by a parameter in the Data Structure
 - viii. Be able to select a single parameter from the data points
 - ix. Implement Load and Save Functions to save progress during training

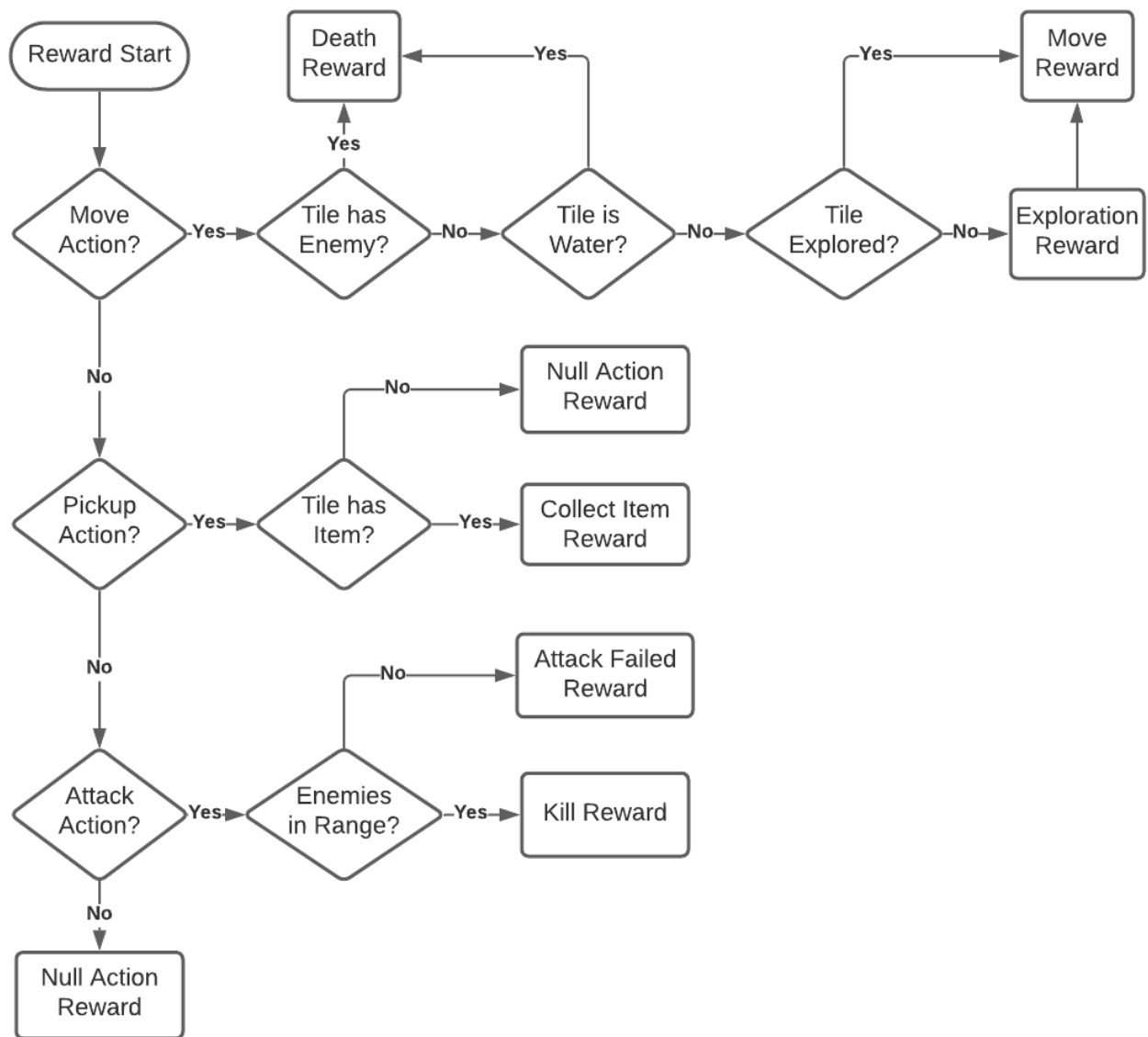
3. Design

1. System Flow Charts

Below is shown the Flow Chart Overview of my Entire Project. This flowchart is very abstracted without going into the fine detail of each Process.



Below is shown the Action and Reward Tree for the Agent. Any Reward is added to a Total Reward Buffer and returned as part of the Function.



2. Class Diagrams Below is shown the Class Diagram of the entire Technical Solution. The Data Logger is listed separately for clarity, as in practice multiple sections of the Program will aggregate with it.

This algorithm is a Mathematical Operation to add 2 Matrices together. To Add together 2 Matrices their Orders must be the same. To perform the Operation you must Sum each element in Matrix A with the corresponding element in Matrix B, placing the result of each Sum in the resultant Matrix.

```

1  SUBROUTINE MatrixAddition(Matrix1, Matrix2)
2      temporaryMatrix ← NEW Matrix(Matrix1.Order)
3      FOR Row ← 0 TO Matrix1.Order[0]
4          FOR Column ← 0 TO Matrix1.Order[1]
5              temporaryMatrix[Row, Column] ← Matrix1[Row, Column] + Matrix2[Row, Column]
6          END FOR
7      END FOR
8      RETURN temporaryMatrix
9  ENDSUBROUTINE

```

2) Matrix Subtraction

This algorithm is a Mathematical Operation to subtract 2 Matrices. To Subtract 2 Matrices their Orders must be the same. To perform the Operation you must Sum each element in Matrix A with the negative of the corresponding element in Matrix B, placing the result of each Sum in the resultant Matrix.

```

1  SUBROUTINE MatrixSubtraction(Matrix1, Matrix2)
2      temporaryMatrix ← NEW Matrix(Matrix1.Order)
3      FOR Row ← 0 TO Matrix1.Order[0]
4          FOR Column ← 0 TO Matrix1.Order[1]
5              temporaryMatrix[Row, Column] ← Matrix1[Row, Column] - Matrix2[Row, Column]
6          END FOR
7      END FOR
8      RETURN temporaryMatrix
9  ENDSUBROUTINE

```

3) Matrix Multiplication

This algorithm is a Mathematical Operation to find the product of 2 Matrices. To Multiply 2 Matrices the number of Columns in the Matrix A must be equal to the number of Rows in Matrix B. Where Matrix A has dimensions of $m \times n$ and Matrix B has dimensions of $j \times k$, the resultant Matrix will have dimensions of $n \times j$. To Multiply two Matrices, the algorithm performs the Dot Product between the Row in Matrix A and the corresponding Column in Matrix B. The Dot Product is the Sum of the Products of corresponding elements.

```

1  SUBROUTINE MatrixMultiplication(Matrix1, Matrix2)
2      tempMatrix ← NEW Matrix((Matrix1.Order[0], Matrix2.Order[1]))
3      FOR i ← 0 TO Matrix1.Order[0]
4          FOR j ← 0 TO Matrix2.Order[1]
5              FOR l ← 0 TO Matrix1.Order[1]
6                  tempMatrix[i, j] ← tempMatrix[i, j] + Matrix1[i, l] * Matrix2[l, j]
7              END FOR
8          END FOR
9      END FOR
10     RETURN tempMatrix
11  ENDSUBROUTINE

```

4) Matrix Scalar Multiplication

This algorithm is a Mathematical Operation to find the product between a Matrix and a Scalar. The result can be found by Multiplying each element of the Matrix by the Scalar Value to form the Resultant Matrix.

```

1 | SUBROUTINE MatrixScalarMultiplication(Scalar, Matrix)
2 |     temporaryMatrix ← NEW Matrix(Matrix.Order)
3 |     FOR Row ← 0 TO Matrix.Order[0]
4 |         FOR Column ← 0 TO Matrix.Order[1]
5 |             temporaryMatrix[Row, Column] ← Scalar * Matrix[Row, Column]
6 |         END FOR
7 |     END FOR
8 |     RETURN temporaryMatrix
9 | ENDSUBROUTINE

```

5) Matrix Hadamard Product

This algorithm is a Mathematical Operation to another way to find the product between 2 Matrices. Instead of applying the Dot Product between Rows and Columns, you find the product between each element in Matrix A with the corresponding element in Matrix B, placing the result in the resultant Matrix.

```

1 | SUBROUTINE MatrixHadamardProduct(Matrix1, Matrix2)
2 |     temporaryMatrix ← NEW Matrix(Matrix1.Order)
3 |     FOR Row ← 0 TO Matrix1.Order[0]
4 |         FOR Column ← 0 TO Matrix1.Order[1]
5 |             temporaryMatrix[Row, Column] ← Matrix1[Row, Column] * Matrix2[Row, Column]
6 |         END FOR
7 |     END FOR
8 |     RETURN temporaryMatrix
9 | ENDSUBROUTINE

```

6) Matrix Power

This algorithm is a Mathematical Operation to find the power of a Matrix. The given Matrix needs to have square dimensions. The result can be found by multiplying the given Matrix by itself n ammount of times where n is the given power.

7) Matrix Transpose

This algorithm is a Mathematical Operation used to Flip a Matrix across its Diagonal. The Transpose of any Matrix can be found by converting each Row of the Matrix into a Column. An $m \times n$ Matrix will turn into an $n \times m$ Matrix.

```

1 | SUBROUTINE MatrixTranspose(Matrix)
2 |     temporaryMatrix ← NEW Matrix(Matrix.Order)
3 |     FOR Row ← 0 TO Matrix.Order[0]
4 |         FOR Column ← 0 TO Matrix.Order[1]
5 |             temporaryMatrix[Row, Column] ← Matrix[Column, Row]
6 |         END FOR
7 |     END FOR
8 |     RETURN temporaryMatrix
9 | ENDSUBROUTINE

```

8) Activation Function SoftMax

This algorithm is a logistic function that creates a probability distribution from a set of points. This probability distribution sums to 1. It applies the standard Exponential Function to each element, then normalises this value by dividing by the sum of all these Exponentials.

```

1 | SUBROUTINE Softmax(Input)
2 |     OutVector ← NEW Matrix(Input.Order)
3 |     ExpSum ← 0
4 |     FOR Row ← 0 TO Input.Order[0]

```

```

5      ExpSum  $\leftarrow$  ExpSum + Math.exp(Input[Row, 0])
6  END FOR
7  FOR Row  $\leftarrow$  0 TO Input.Order[0]
8      OutVector[Row]  $\leftarrow$  Input[Row, 0] / ExpSum
9  END FOR
10 RETURN OutVector
11 ENDSUBROUTINE

```

9) Neural Network Forward Propagation

This algorithm is used to obtain the outputs of a Neural Network. It uses Matrix Multiplication to propagate the inputs of the network from Layer to Layer, eventually reaching the Output Layer. My Multiplying the Weight Matrix and the outputs of the previous Layer, and then adding the Bias. We can obtain the output of the layer.

10) Neural Network Loss Function

The algorithm for to calculate the Loss of a Dual Neural Network can be calculated by using a variation of the Bellman Equation. The Bellman Equation is necessary for Mathematically Optimising in this case. It determines the Value of a decision at a certain point in time, in terms of the Payoff from the Initial Action and the Value of the Potential Payoff after taking that Initial Action.

11) Neural Network Backwards Propagation

This algorithm is used within a Neural Network to adjust its Weights and Biases, allowing it to more accurately predict the best outcome. In Reinforcement Learning, the Network is trained using an estimate for what is the best action given a situation. Using this estimate, we can train the Network to predict this outcome by converging the series of Weights and Biases towards a local minimum. This is done by calculating partial derivatives for every weight and bias value with respect to the cost function. This derivative is then subtracted from the existing weight or bias, eventually converging on the best possible value.

12) Agent Get Tile Vector

This algorithm takes the current World Data of the simulation, and produces a Vector of Tile Data surrounding the Agent. This can be done using a nested For Loop rather simply.

```

1  SUBROUTINE GetTileVector(WorldMap)
2      Offset  $\leftarrow$  LoadFromParameters("DQLOffset")
3      SideLength  $\leftarrow$  2 * Offset + 1
4      TileVector  $\leftarrow$  NEW Matrix((Math.pow(sideLength, 2), 1))
5      Num  $\leftarrow$  0
6      FOR i  $\leftarrow$  Agent.Pos[1] - Offset TO Agent.Pos[1] + offset + 1
7          FOR j  $\leftarrow$  Agent.Pos[0] - offset TO Agent.Pos[1] + offset + 1
8              TileVector[Num, 0]  $\leftarrow$  WorldMap[j, i]
9              Num  $\leftarrow$  Num + 1
10         END FOR
11     END FOR
12     RETURN TileVector
13 ENDSUBROUTINE

```

13) Agent Convert to Grayscale

This algorithm converts a given RGB Colour Value to the corresponding Gray Scale Value. The Red, Green and Blue elements of the colour value are multiplied by the

specific values 0.299, 0.587 and 0.114. You then sum the results, and divide by 255.

```

1 SUBROUTINE RGBToGrayscale(GBVal)
2   GrayscaleValue ← 0
3   GrayscaleValue ← GrayscaleValue + (0.299 * RGBVal[0])
4   GrayscaleValue ← GrayscaleValue + (0.587 * RGBVal[1])
5   GrayscaleValue ← GrayscaleValue + (0.114 * RGBVal[2])
6   RETURN GrayscaleValue / 255
7 ENDSUBROUTINE

```

14) Agent Post Process Tile Vector

This algorithm will convert the Tile Vector into a Vector of Grayscale values, which can be used as the input for the Neural Network.

```

1 SUBROUTINE GetTileVector(TileVector)
2   ProcessedVector ← NEW Matrix(TileVector.Order)
3   FOR Row ← 0 TO TileVector.Order[0]
4     ProcessedVector[Row, 0] ← RGBToGrayscale(TileVector[Row, 0].RGBValue)
5   END FOR
6   RETURN ProcessedVector
7 ENDSUBROUTINE

```

15) Agent Spawn Position

This algorithm will create a list of spawnable tiles for which the Agent could spawn on, and then randomly select a specific tile as its spawn position.

16) Enemy Spawn Position

This algorithm will create a list of spawnable tiles for which Enemies can spawn on, then select tiles randomly, if they don't already contain an enemy or the agent it will create an Enemy Object with that position. It will do this n amount of times where n is the limit to how many enemies can spawn.

17) Enemy Move

The algorithm I have designed for the Enemy Pathfinding is rather simple, and won't take up much runtime in my solution. First it calculates the distance between itself and the Agent in both Axis. The Enemy will then converge upon the Agent's position by moving in the direction with the greatest distance, effectively finding the nearest diagonal and following it.

```

1 SUBROUTINE EnemyMove(Agent, WorldMap)
2   XDifference ← Agent.Pos[0] - This.Pos[0]
3   YDifference ← Agent.Pos[1] - This.Pos[0]
4
5   IF XDifference == 0 AND YDifference == 0
6     Agent.Alive = False
7     RETURN
8   END IF
9
10  IF abs(XDifference) > abs(YDifference)
11    IF XDifference > 0
12      This.Pos[0] ← This.Pos[0] + 1
13    ELSE
14      This.Pos[0] ← This.Pos[0] - 1
15    END IF
16  ELSE IF abs(XDifference) < abs(YDifference)
17    IF YDifference > 0

```

```

18         This.Pos[1] ← This.Pos[1] + 1
19     ELSE
20         This.Pos[1] ← This.Pos[1] - 1
21     END IF
22 END IF
23 ENDSUBROUTINE

```

18) Poisson Disc Sampling

Poisson Disc Sampling is used to sample a set of points in N Dimensional Space. It takes two parameters, r and k , where r is the minimum distance a specified point must be from every other point, and k is the limit of samples to choose before rejection. It starts by creating an N Dimensional Grid which accelerates spacial searches. An initial sample is then chosen and inserted into the grid. It then chooses a random point, and determines if it is greater than r range from every other point in the grid. This can easily be accomplished using the previously defined Grid. If after k attempts, no point is found then the search is concluded.

19) Perlin Noise

Perlin Noise is a method of generating a procedural texture depending upon input parameters. It defines an n-dimensional grid of Vectors, each grid intersection contains a fixed, random unit vector. To sample Perlin Noise, the grid cell which the point lies in must be found. The Vectors between the sampled point, and the corners of the cell. We then take the Dot Product between these new Vectors, and the Vectors applied to the intersections. In 2d Space this leaves us with 4 Values. We then use an Interpolation function to Interpolate between the 4 Values.

```

1 PermTable ← [1 → 255].Shuffle() * 2
2
3 SUBROUTINE PerlinNoise(X, Y)
4     XFloor ← Math.floor(X)
5     YFloor ← Math.floor(Y)
6
7     G1 ← PermTable[PermTable[XFloor] + YFloor]
8     G2 ← PermTable[PermTable[XFloor + 1] + YFloor]
9     G3 ← PermTable[PermTable[XFloor] + YFloor + 1]
10    G4 ← PermTable[PermTable[XFloor + 1] + YFloor + 1]
11
12    XExact ← X - XFloor
13    YExact ← Y - YFloor
14
15    D1 ← Grad(G1, XFloor, YFloor)
16    D2 ← Grad(G2, XFloor - 1, YFloor)
17    D3 ← Grad(G3, XFloor, YFloor - 1)
18    D4 ← Grad(G4, XFloor - 1, YFloor - 1)
19
20    U ← Fade(XFloor)
21    V ← Fade(YFloor)
22
23    XInterpolated ← Lerp(U, D1, D2)
24    YInterpolated ← Lerp(U, D3, D4)
25
26    RETURN Lerp(V, XInterpolated, YInterpolated)
27 ENDSUBROUTINE
28
29 SUBROUTINE Grad(Hash, X, Y)
30     Temp ← Hash BITWISEAND 3
31     IF Temp == 0

```

```

32         RETURN X + Y
33     ELSE IF Temp == 1
34         RETURN -X + Y
35     ELSE IF Temp == 2
36         RETURN X - Y
37     ELSE IF Temp == 3
38         RETURN -X - Y
39     ELSE
40         RETURN 0
41 ENDSUBROUTINE
42
43 SUBROUTINE Lerp(Ammount, Left, Right)
44     RETURN ((1 - Ammount) * Left + Ammount * Right)
45 ENDSUBROUTINE
46
47 SUBROUTINE Fade(T)
48     RETURN T * T * T * (T * (T * 6 - 15) + 10)
49 ENDSUBROUTINE

```

20) Octave Perlin Noise

Octave Perlin Noise takes the existing Perlin Noise algorithm, but adds rescaled clones of itself into itself, to create what is known as Fractal Noise. Creating this Fractal Noise is common practice because it reduces the sharp edges encountered with just the regular Perlin Noise Algorithm.

```

1  SUBROUTINE OctaveNoise(X, Y, Octaves, Persistence)
2      Total ← 0
3      Frequency ← 1
4      Amplitude ← 1
5      MaxValue ← 0
6
7      FOR i ← 0 TO Octaves
8          Total ← Total + (PerlinNoise(X * Frequency, Y * Frequency) * Amplitude
9
10         MaxValue ← MaxValue + Amplitude
11
12         Amplitude ← Amplitude * Persistence
13         Frequency ← Frequency * 2
14     END FOR
15
16     RETURN Total / MaxValue
17 ENDSUBROUTINE

```

4. Description of Data Structures

(a) Matrices

As part of developing a Neural Network, I will extensively use Matrices, as they are an integral part of the algorithms used for Machine Learning. After creating a prototype Matrix class as part of my prototype, I will represent it in the same format. In my prototype I created a Class, and then represented the values of the Matrix with a 2d List (List of Lists). As part of my Matrix Class I will have multiple constructors, to help avoid repeating code.

4. Testing

4.1 Testing Table

As part of testing my NEA, I identified the key areas of my project which needed testing. My testing targets these areas from different angles to ensure they work correctly. These areas are:

1. User Input and Program Output
 - (a) Parameter Loading
 - (b) Neural Network Loading
 - (c) Graphical Output
 - (d) Console Output
2. Matrix Implementation
 - (a) Constructor Cases
 - (b) Matrix Operations
 - (c) Thrown Exceptions
3. Deep Q Learning Algorithm
 - (a) Forward Propagation
 - (b) Loss Function
 - (c) Back Propagation
 - (d) Double Ended Queue Data Type
4. Data Logger
 - (a) Data Structure Matching
 - (b) Heap Data Structure
 - (c) Heap Sort Implementation
5. Simulation
 - (a) Generation of 2d Terrain
 - (b) Continuity of Generation
 - (c) ML Agent
 - (d) Reward Methods

Below is included an NEA Testing video used for some parts of Testing Evidence

[*https://thisisalink.com/youtotallybelieve/*](https://thisisalink.com/youtotallybelieve/)

1. User Input and Program Output

Test No.	Test Name	Input Data / Description	Expected Output	Pass / Fail	Testing Evidence
1	Loading Parameters File	Input "Default.json" file which contains the loadable values	Loads parameters into the Parameters Dictionary variable	Pass	1.1
2	Parameters within range	Input Loaded Parameters Dictionary	Prints to console "Parameters within Specified Ranges"	Pass	1.2
3	Below Range Parameter	Input "Default.json" file with a below range parameters	Raises an exception detailing the Parameter, Value of Parameters, and the given Range Required	Pass	1.3
4	Above Range Parameter	Input "Default.json" file with an above range parameters	Raises an exception detailing the Parameter, Value of Parameters, and the given Range Required	Pass	1.4
5	Network Saved Data Loading	When Prompted to load network data type "Y", and type the file name of network data to load	Network Data is loaded successfully, training position stored	Pass	1.5
6	Window Opening	Run Program, enter setup info as normal	Window opens and is of the correct size/resolution	Pass	1.6
7	Window Displays correct debug information	Run Program, enter setup info as normal, with "Debug" = 1 in parameters file	Debug Layer output info displayed on Right side of Window	Pass	1.7
8	Agent is displayed	Run Program, enter setup info as normal	Orange square displayed on screen	Pass	1.8
9	Enemies are displayed	Run Program, enter setup info as normal, with "StartEnemyCount" >= 1	Red Square/s are displayed on Screen	Pass	1.9
10	Console Messages Output	Run Program, enter setup info as normal	Console Messages Outputted per 100 Steps	Pass	1.10

2. Matrix Implementation

Test No.	Test Name	Input Data / Description	Expected Output	Pass / Fail	Testing Evidence
11	Create Matrix with Tuple	A Tuple for the order of the Matrix	Matrix is created with an order the same as the Tuple	-	-
12	Create Matrix with 2d List	A 2d List, where the parent list holds a list for every row, each "row list" is of the same length	Matrix is created with the same values as the 2d List	-	-

13	Create Vector with List	A 1d List of any Values	Vector is created with the same values as the List	-	-
14	Print Matrix to Console	A valid Matrix of any size	Matrix Prints to the console with the correct formatting	-	-
15	Create Randomised Matrix	A Tuple for the order of the Matrix, and the the keyargument random=True	Matrix is created with randomised values between -0.5 and 0.5	-	-
16	Create Identity Matrix	A Tuple for the order of the Matrix, and the the keyargument identity=True	Matrix is created with all 0's and 1's down the diagonal	-	-
17	Matrix Addition Calculation	Two Matrices of the same order	Matrix Addition is performed to create a new Matrix with the added values	-	-
18	Matrix Subtraction Calculation	Two Matrices of the same order	Matrix Subtraction is performed to create a new Matrix with the subtracted values	-	-
19	Matrix Multiplication Calculation	Two Matrices where Width of M1 is equal to the height of M2	Matrix Multiplication is performed to create a new Matrix with the multiplied values	-	-
20	Matrix Scalar Multiplication Calculation	A <i>float/int</i> as the scalar and any size Matrix	Matrix Scalar Multiplication is performed to create a new Matrix with the multiplied values	-	-
21	Vector Hadamard Product Calculation	Two Vectors with the same Order	Vector Hadamard Product is performed to create a new Vector with the multiplied values	-	-
22	Matrix Power Calculation	A Square Matrix with values stored in it	Matrix to the Power of is performed to create a new Matrix with the correct values	-	-
23	Matrix Transpose Calculation	A Matrix with values stored in it	New Matrix is created with values flipped across the diagonal	-	-
24	Matrix Select Column	A Matrix with values stored in it	Selects the indexed Column from the Matrix, returning as a list	-	-
25	Matrix Select Row	A Matrix with values stored in it	Selects the indexed Row from the Matrix, returning as a list	-	-
26	Vector Max in Vector	A Vector	Returns Largest value in Vector	-	-
27	Matrix Clear	A Matrix with values stored in it	Clears Matrix of any values	-	-
28	Combine Vectors	List of Vectors of the same Order	Combines the list of Vectors into a Matrix	-	-
29	Matrix Sum	-	Sums all values in the Matrix returning a <i>float/int</i>	-	-
30	Randomised Matrix Constructor Tests	Generator Constructor Parameters randomly for 10000 Tests	All Tests Should produce a valid Matrix	Pass	2.16
31	Randomised Constructor Exception Tests	Generate Random Data to cause Exceptions within the Constructor for 10000 Tests	All Tests should trigger the Targetted Exception for that test	Pass	2.17
32	Randomised Operator Tests	Generator Random Data to test the Operator Methods for 10000 Tests	All Tests should produce the correct result	Pass	2.18

33	Randomised Operator Exception Tests	Generate Random Data to cause Exceptions within the Operators for 10000 Tests	All Tests should trigger the Targetted Exception for that test	Pass	2.19
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3. Deep Q Learning Algorithm

Test No.	Test Name	Input Data / Description	Expected Output	Pass / Fail	Test-ing Evi-dence
34	Networks are Created	Run Program, enter setup info, denying the loading of weights	A Dual Neural Network is created after Program Start	-	-
35	Networks conforms to Parameters	Run Program, enter setup info, denying the loading of weights	The created Dual Neural Network conforms to the specified structure in the parameter "DeepQLearningLayers"	-	-
36	Forward Propagation Test	Where L is the Current Layer, Forward Propagation requires: $OutputVector^{L-1}, WeightMatrix^{L-1}, BiasVector^L$	The output of the Layer	-	-
37	Forward Propagation Multi Layer Test	Same as Entry Above	-	-	-
38	Loss Function Bellman Equation	-	-	-	-
39	Back Propagation Unit Test	-	-	-	-
40	Back Propagation Multi Layer Unit Test	-	-	-	-
41	Deque Push Front	A value to push to the Deque	Item is pushed to front of Deque	-	3.8
42	Deque First/Last	Call the .First() or .Last() Method for a Deque Object	Returns item at Front/Last index of Deque	-	-
43	Deque Sample N Ammount of Items	Call the .Sample(int N) Method, with a parameter of N items, for a Deque Object	Returns N number of random samples from Deque	-	-
44	Experience Replay Sampling	-	Back Propagation is performed on the sampled Deque Items	-	-
45	Activation Outputs Unit Test	Input Value Vector to the Activation Function	Returns a Vector of values, where the Activation has been applied to them	-	-
46	Activation Derivatives Output Unit Test	Input Value Vector to the Activation Derivative Function	Returns a Vector of values, where the Activation Deivative has been applied to them	-	-

4. Data Logger

Test No.	Test Name	Input Data / Description	Expected Output	Pass / Fail	Test-ing Evi-dence
----------	-----------	--------------------------	-----------------	-------------	--------------------

47	Heap Sort Descending	A randomly generated input list	Sorts the list of items into Descending order	Pass	4.1
48	Add Point	A Data Point matching the data structure of the DataCollector	Point is added to Data Points list	Pass	4.2
49	Match Data Struture with Single	Data Structure contrains an index with a Single-Typed definition	No error thrown	Pass	4.3
50	Match Data Struture with Multi-Typed	Data Structure contrains an index with a Multi-Typed definition	No error thrown	Pass	4.4
51	Match Data Struture with List-Typed	Data Structure contrains an index with a List-Typed definition	No error thrown	Pass	4.5
52	Match Data Structure Error	Try match point with structure which does not match	Error is thrown with correct info	Pass	4.6
53	Select Query	Select from DataLogger with an Index and Search Contents	Returns a list of the selected column where the Search Contents Matches	Pass	4.7
54	Save Data Points	Invoke Save method on DataLogger Object	Saves Data Points to specified File	Pass	4.8
55	Load Data Points	Invoke Load method on DataLogger Object	Loads Data Points from specified File	Pass	4.9

5. Simulation

Test No.	Test Name	Input Data / Description	Expected Output	Pass / Fail	Test- ing Evi- dence
56	Creation of Agent	Run progam as normal	Agent is created as an instance of the Agent Class	-	-
57	Creation of Enemies	Run program as normal with the "StartEnemyCount" Parameter ≥ 1	Up to the ammount of specified Enemies are created	-	-
58	Enemies Pathfind towards Agent	Run program as normal with "StartEnemyCount" Parameter ≥ 1	The spawned enemies pathfind towards the agnet using the defined pathfinding algorithm	-	-
59	Getting Tile Data	Call .GetTileVec- tor(worldMap, enemyList[]) with arguments for worldMap and the list of current Enemies	Returns a Vector of the surrounding tile objects	-	-
60	Convert Tile Data	Call .TileVectorPostPro- cess(tileVec) with argument of the result from the Test Above	Converts Tile Data into two vectors, Grayscale Colour and Tile Type	-	-
61	Reward System Test Basic Reward	-	Expected reward is given to agent	-	-
62	Reward System Test Complex Reward	-	Expected reward is given to agent	-	-

63	World Generates to an Acceptable Standard	Run program as normal	Generates 2d Terrain which roughly looks realistic	-	-
64	World Generation Conforms to Parameters	Utilise inputted parameters to identify the effect they have on the world Generation	Terrain changes depending on inputting Parameters	-	-
65	Perlin Noise retains Continuity	Generate two worlds with the same seed	Perlin Noise returns same value when using the same seed twice	-	-

4.2 Testing Evidence

Evidence 1.1

The .json file which is being loaded

```
"EnterValues": 1,
"GenerateThreaded": 0,
"EnableEnemies": 1,
"SaveWeights": 1,
"StepDelay": 0,
"Debug": 0,
"DebugScale": 1,

"WorldSize": 64,
"TileWidth": 8,
"TileBorder": 0,

"OctavesTerrain": 7,
"PersistenceTerrain": 0.6,
"WorldScale": 3.2,

"OctavesTrees": 4,
"PersistenceTrees": 0.95,
"PoissonKVal": 20,
"TreeSeedOffset": 1000,
"TreeHeight": 0.15,
"InteractableTileBorder": 0,
"TreeBeachOffset": 0.05,

"Grayscale": 0,
"Water": 0.43,
"Coast": 0.48,
"Grass": 0.63,
"Mountain": 1.0,

"TreeType": "Wood",

"StartEnemyCount": -13,
"AgentAttackRange": 1,

"ColourWater": [18, 89, 144],
"ColourCoast": [245, 234, 146],
"ColourGrass": [26, 148, 49],
"ColourMountain": [136, 140, 141],
"ColourTree": [13, 92, 28],
"ColourPlayer": [233, 182, 14],
"ColourEnemy": [207, 2, 2],

"MoveReward": 0,
"CollectItemReward": 0.1,
"DeathReward": -0.1,
"ExploreReward": 0.01,
"AttackReward": 0.5,
"AttackFailedReward": -0.1,
"NoopReward": 0,

"TargetReplaceRate": 5,
"EREnabled": 1,
"ERBuffer": 1000,
"ERSampleRate": 100,
"ERSampleSize": 10,

"DeepQLearningLayers": [49, 64, 32, 16, 7],
"DQLEpoch": 100,
"DQLearningMaxSteps": 10000,
"DQLOffset": 3,
"DQLEpsilon": 0.5,
"DQLEpisonRegression": 0.99998,
"DQLearningRate": 0.75,
"DQLGamma": 0.8
```

Printing the loaded Json File to console to Console to check the values match

```
{'EnterValues': 1, 'GenerateThreaded': 0, 'EnableEnemies': 1, 'SaveWeights': 1, 'StepDelay': 0, 'Debug': 0, 'DebugScale': 1, 'WorldSize': 64, 'TileWidth': 8, 'TileBorder': 0, 'OctavesTerrain': 7, 'PersistenceTerrain': 0.6, 'WorldScale': 3.2, 'OctavesTrees': 4, 'PersistenceTrees': 0.95, 'PoissonKVal': 20, 'TreeSeedOffset': 1000, 'TreeHeight': 0.15, 'InteractableTileBorder': 0, 'TreeBeachOffset': 0.05, 'Grayscale': 0, 'Water': 0.43, 'Coast': 0.48, 'Grass': 0.63, 'Mountain': 1.0, 'TreeType': 'Wood', 'StartEnemyCount': -13, 'AgentAttackRange': 1, 'ColourWater': [18, 89, 144], 'ColourCoast': [245, 234, 146], 'ColourGrass': [26, 148, 49], 'ColourMountain': [136, 140, 141], 'ColourTree': [13, 92, 28], 'ColourPlayer': [233, 182, 14], 'ColourEnemy': [207, 2, 2], 'MoveReward': 0, 'CollectItemReward': 0.1, 'DeathReward': -0.1, 'ExploreReward': 0.01, 'AttackReward': 0.5, 'AttackFailedReward': -0.1, 'NoopReward': 0, 'TargetReplaceRate': 5, 'EREnabled': 1, 'ERBuffer': 1000, 'ERSampleRate': 100, 'ERSampleSize': 10, 'DeepQLearningLayers': [49, 64, 32, 16, 7], 'DQLEpoch': 100, 'DQLearningMaxSteps': 10000, 'DQLOffset': 3, 'DQLEpsilon': 0.5, 'DQLEpisonRegression': 0.99998, 'DQLearningRate': 0.75, 'DQLGamma': 0.8}
```

Evidence 1.2

Console Output when parameters are within specified ranges

Parameters within Specified Ranges
Created New World: Seeds: 285407

A Screenshot of the .json file where the Ranges are defined

```
Parameters > Range.param
1  {
2    "StepDelay": [0,null],
3
4    "WorldSize": [8,1024],
5    "TileWidth": [1,8],
6    "TileBorder": [0,3],
7
8    "OctavesTerrain": [0,20],
9    "PersistenceTerrain": [0,1],
10   "WorldScale": [0.1,null],
11
12   "OctavesTrees": [0,20],
13   "PersistenceTrees": [0,1],
14   "PoissonRVal": [0,null],
15   "PoissonKVal": [0,null],
16   "TreeHeight": [0,1],
17   "InteractableTileBorder": [0,10],
18   "TreeBeachOffset": [0,1],
19
20   "Grayscale": [0,1],
21   "Water": [0,1],
22   "Coast": [0,1],
23   "Grass": [0,1],
24   "Mountain": [0,1],
25
26   "StartEnemyCount": [0, 100],
27
28   "TargetReplaceRate": [5,300],
29   "ERBuffer": [1000, 10000],
30   "ERSampleRate": [1,100],
31   "ERSampleSize": [10, 1000],
32
33   "DQLearningMaxSteps": [0,null],
34   "DQLOffset": [0,20],
35   "DQLEpsilon": [0,1],
36   "DQLEpisonRegression": [0,1],
37   "DQLearningRate": [0,1],
38   "DQLGamma": [0,1]
39 }
```

Evidence 1.3

The given out of range parameter - subceeding

```
"StartEnemyCount": -13,
```

The specified range it should be within

```
"StartEnemyCount": [0, 100],
```

The Exception thrown when the program is run

```
range
Exception: 'StartEnemyCount' of value -13, has subceeded the range: 0-100
PS E:\GithubRepos\CompSciNEA>
```

Evidence 1.4

The given out of range parameter - exceeding

```
"TreeBeachOffset": 1.2,
```

The specified range it should be within

```
InteractableFileObject : [
  "TreeBeachOffset": [0,1],
```

The Exception thrown when the program is run

```
cd range
Exception: 'TreeBeachOffset' of value 1.2, has exceeded the range: 0-1
PS C:\Github\Paper\CompSci5FA>
```

Evidence 1.5

The Console prompt if the user wants to load Network Weights

```
Load weights (Y/N): Y
State file name: DQNetwork
```

The file the program is loading

```
▼ DQLearningData ●
  DQNetwork.dqn M
```

The testing step resumes at 400, underlined in Red

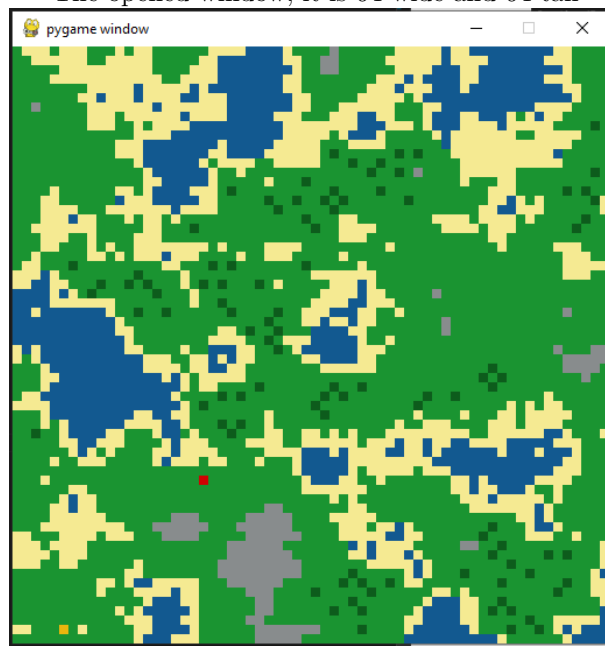
```
Created New World, Seed: 373203
Load weights (Y/N): Y
State file name: DQNetwork
Created New World, Seed: 765802
Created New World, Seed: 274263
Created New World, Seed: 142187
Created New World, Seed: 613313
Created New World, Seed: 961492
Created New World, Seed: 493768
Created New World, Seed: 551641
Created New World, Seed: 133180
400 2.049999999999966 0.49601591773672193
Created New World, Seed: 310069
PS C:\Github\Paper\CompSci5FA>
```

Evidence 1.6

The width/height of the window

```
"WorldSize": 64,
```

The opened window, it is 64 wide and 64 tall

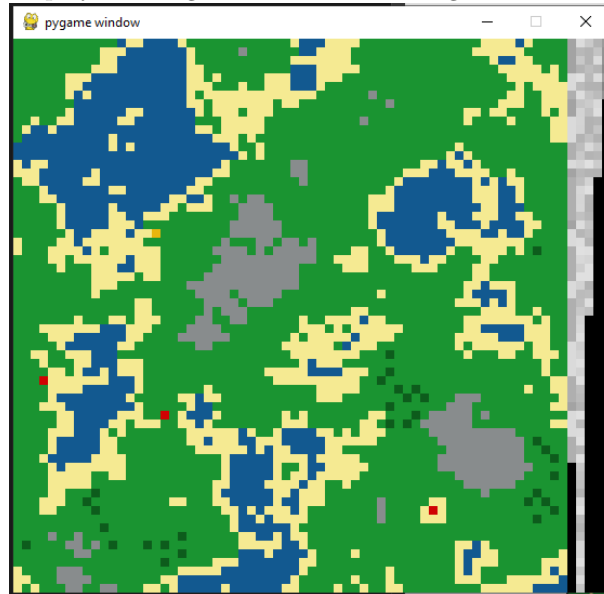


Evidence 1.7

Debug being set to 1 in the parameters file

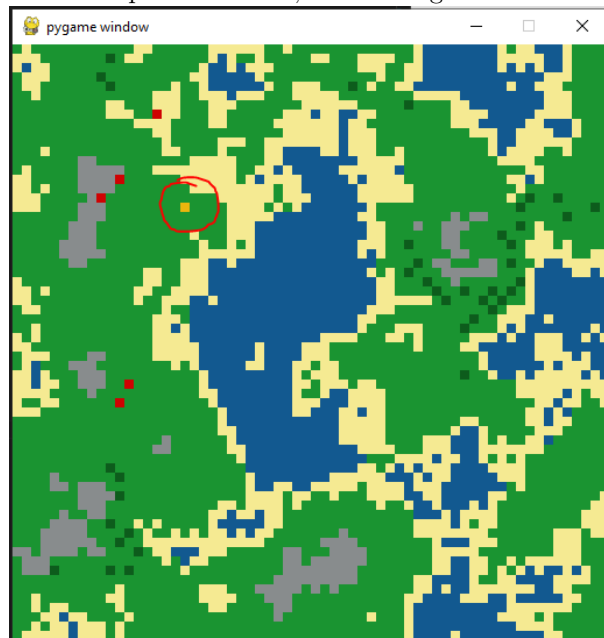
```
"Debug": 1,
```

The displayed debug information to the right of the Window



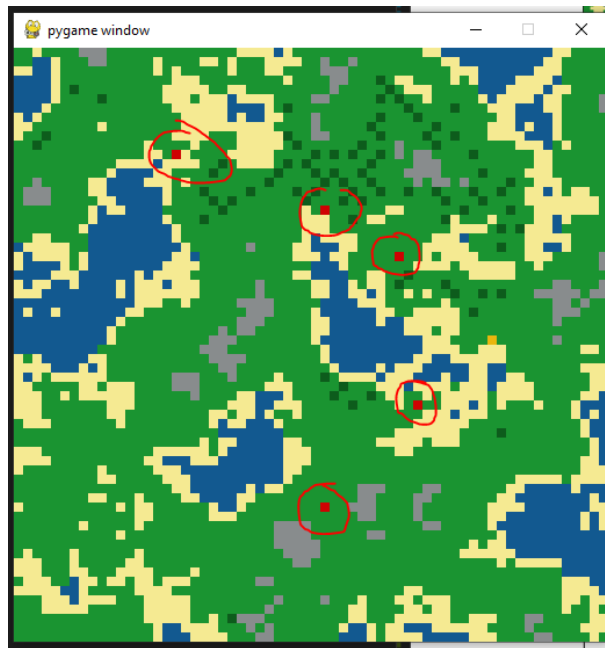
Evidence 1.8

The opened window, with the agent circled



Evidence 1.9

The opened window, with the enemies circled



Evidence 1.10

The correctly displayed console outputs

```
1200 2.089999999999997 0.4881427377231092
Created New World, Seed: 299891
Created New World, Seed: 551234
Created New World, Seed: 419121
Created New World, Seed: 241104
1300 3.5799999999999934 0.4871674181391277
Created New World, Seed: 251077
Created New World, Seed: 479658
Created New World, Seed: 213276
Created New World, Seed: 976354
Created New World, Seed: 774313
Created New World, Seed: 237960
1400 3.539999999999999 0.4861940472644421
Created New World, Seed: 344052
Created New World, Seed: 607949
Created New World, Seed: 102154
Created New World, Seed: 171940
Created New World, Seed: 356413
Created New World, Seed: 50990
Created New World, Seed: 225113
Created New World, Seed: 981988
1500 3.399999999999986 0.4852226212054902
Created New World, Seed: 61676
Created New World, Seed: 9403
Created New World, Seed: 368695
Created New World, Seed: 466339
Created New World, Seed: 851475
Created New World, Seed: 721476
Created New World, Seed: 629285
Created New World, Seed: 664084
Created New World, Seed: 589992
1600 3.1099999999999812 0.4842531360764887
```

Evidence 2.1

Console Output, all Tests have passed with no failures

```
10000/10000 | CreateVectorFrom1DList
10000/10000 | CreateMatrixFrom2DList
10000/10000 | CreateMatrixFromTuple
10000/10000 | CreateIdentityMatrix
```

Evidence 2.2

Console Output, all Tests have passed with no failures

```
10000/10000 | NoMatchingInitCase
10000/10000 | UnableToCreateIdentityMat
```

Evidence 2.3

Console Output, all Tests have passed with no failures

```
10000/10000 | AdditionMatrix
10000/10000 | AdditionInteger
10000/10000 | SubtractionMatrix
10000/10000 | SubtractionInteger
10000/10000 | MultiplicationInteger
10000/10000 | MultiplicationHadamardVector
10000/10000 | MultiplicationMatrix
10000/10000 | Power
10000/10000 | Transpose
10000/10000 | SelectColumn
10000/10000 | SelectRow
10000/10000 | CombineVectorHorizontal
10000/10000 | Sum
10000/10000 | MaxInVector
10000/10000 | Clear
```

Evidence 2.4

Console Output, all Tests have passed with no failures

```
10000/10000 | NotOfTypeVector
10000/10000 | VectorsNotOfSameLength
10000/10000 | NoMatchingMultiplyCase
10000/10000 | NoMatchingAdditionCase
10000/10000 | NoMatchingSubtractionCase
10000/10000 | NoMatchingPowerCase
10000/10000 | MismatchOrdersAdd
10000/10000 | MismatchOrdersSub
10000/10000 | MismatchOrdersMul
10000/10000 | SumOfMatrixReqNumericalVals
10000/10000 | ColumnOutOfRange
10000/10000 | ColumnMustBeInteger
10000/10000 | RowOutOfRange
10000/10000 | RowMustBeInteger
```

Evidence 3.1

Evidence 3.2

Evidence 3.3

Evidence 3.4

Evidence 3.5

Evidence 3.6

Evidence 3.7

Evidence 3.8

Pushing items to the front of the Double Ended Queue

```
1 deque = Deque(10)
2 deque.PushFront(3)
3 print("Added 3:", deque.queue)
4 deque.PushFront(-5)
5 print("Added -1:", deque.queue)
6 deque.PushFront(9)
7 print("Added 9:", deque.queue)
```

The output of the above code:

```
Added 3: [3, None, None, None, None, None, None, None, None, None]
Added -1: [3, -5, None, None, None, None, None, None, None, None]
Added 9: [3, -5, 9, None, None, None, None, None, None, None]
```

Evidence 3.9

Creating a Double Ended Queue with a length of 4, add Push Items to it, and get the Items in First and Last

```
1 deque = Deque(4)
2 deque.PushFront(3)
3 deque.PushFront(-5)
4 deque.PushFront(9)
5 deque.PushFront(4)
6 deque.PushFront(-4)
7
8 print("First:", deque.First())
9 print("Last:", deque.Last())
10 print("Queue:", deque.queue)
```

The output of the above code:

```
First: -4
Last: -5
Queue: [-4, -5, 9, 4]
```

Evidence 3.10

Create a Double Ended Queue and Sample items from the Queue

```
1 deque = Deque(4)
2 deque.PushFront(3)
3 deque.PushFront(-5)
4 deque.PushFront(9)
5 deque.PushFront(4)
6 deque.PushFront(-4)
7
8 print("Sample 1:", deque.Sample(2))
9 print("Sample 2:", deque.Sample(2))
10 print(deque.queue)
```


The output of the above code:

```
Sample 1: [-5, 4]
Sample 2: [-5, 9]
[-4, -5, 9, 4]
```

Evidence 4.1

Evidence 5.1

Randomly Generated Unsorted List, sorted by the 1st Element to form the Sorted List

```
1 inputList = [[random.randint(-10,10), random.randint(-10,10)] for i in range(5)]
2 print("Unsorted List:")
3 for item in inputList:
4     print(item)
5
6 dl = DataCollector("SortingTest", [int, int], False)
7
8 dl.LogDataPointBatch(inputList)
9
10 sortedList = dl.HeapSort(0)
11
12 print("Sorted List:")
13 for item in sortedList:
14     print(item)
```

The output of the above code:

```
Unsorted List:
[0, 6]
[-6, -4]
[-3, -2]
[-2, 1]
[7, -1]
Sorted List:
[7, -1]
[0, 6]
[-2, 1]
[-3, -2]
[-6, -4]
```

Evidence 5.2

Adding a single point: [5, 2] to DataLogger

```
1 dl = DataCollector("AddPointTest", [int, int], False)
2 print("Before: ", dl.dataPoints)
3
4 dl.LogDataPoint([5, 2])
5
6 print("After: ", dl.dataPoints)
```

The output of the above code:

```
Before: []
After: [[5, 2]]
```

Evidence 5.3

Test Data Point matches struture

```
1 | dl = DataCollector("Match Single Types", [int, float], False)
2 |
3 | print("Matches Structure: ", dl.CheckMatchStructure([-3, 2.2]))
```

The output of the above code:

```
Matches Structure: True
```

Evidence 5.4

Test Data Point matches structure

```
1 | dl = DataCollector("Match Multi Typed", [bool, [float, int]], False)
2 |
3 | print("Matches Structure: ", dl.CheckMatchStructure([False, 4.5]))
4 | print("Matches Structure: ", dl.CheckMatchStructure([True, -9]))
```

The output of the above code:

```
Matches Structure: True
Matches Structure: True
```

Evidence 5.5

Test Data Point matches structure

```
1 | dl = DataCollector("Match List Type", [bool, str], False)
2 |
3 | print("Matches Structure: ", dl.CheckMatchStructure([True, ["Matt", "Isabel", "Tristan", "Chris"]]))
```

The output of the above code:

```
Matches Structure: True
```

Evidence 5.6

Test error thrown when Data Point doesnt match the given structure

```
1 | try:
2 |     dl = DataCollector("Match Data Structure Error", [str, int], False)
3 |
4 |     print("Matches Structure: ", dl.CheckMatchStructure(["Steve Preston", True]))
5 | except Exception as x:
6 |     print(x)
```

The output of the above code:

```
Type: <class 'bool'> != Data Structure Type: <class 'int'>
[<class 'str'>, <class 'int'>]
```

Evidence 5.7

Select Prime numbers in 1st index

```
1 | inputList = [[random.randint(-10,10), random.randint(-10,10)] for i in range(5)]
2 | print("Random List:")
```

```

3   for item in inputList:
4       print(item)
5
6   dl = DataCollector("Select List", [int, int], False)
7
8   dl.LogDataPointBatch(inputList)
9
10  sortedList = dl.Select(0, [1,2,3,5,7])
11
12  print("Selected List:")
13  for item in sortedList:
14      print(item)

```

The output of the above code:

```

Random List:
[9, -5]
[8, 3]
[1, -8]
[-1, 4]
[4, -10]
Selected List:
[1, -8]

```

Evidence 5.8

Test for saving a file

```

1   inputList = [[random.randint(-10,10), random.randint(-10,10)] for i in range(5)]
2   print("Saved List:")
3   for item in inputList:
4       print(item)
5
6   dl = DataCollector("Save-Load Test", [int, int], False)
7
8   dl.LogDataPointBatch(inputList)
9
10  dl.SaveDataPoints()

```

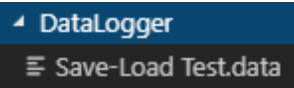
The saved Data Points

```

Saved List:
[8, 10]
[-7, -1]
[-1, -7]
[4, 1]
[5, -6]

```

The saved file "Save-Load Test.data"



Evidence 5.9

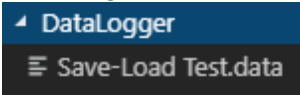
Test for loading a file

```

1   dl = DataCollector("Save-Load Test", [int, int], True)
2
3   print("Loaded List:")
4   for item in dl.dataPoints:
5       print(item)

```

The File we're loading from "Save-Load Test.data"



The loaded Data Points

```
Loaded List:  
[8, 10]  
[-7, -1]  
[-1, -7]  
[4, 1]  
[5, -6]  
55 Mi 61
```

5. Evaluation

6. Prototype Code

Below is the code I created while developing my Prototype.
The 3 Scripts listed in order are:

1. main.py
2. worldClass.py
3. mathLib.py

-
1. main.py

```
#Imports
import pygame, random, json, os, time
from datetime import datetime
import worldClass, agentClass, mathLib

#Variables
simSize = 64
gridSize = 4
simSeed = 420

#World Functions
def DrawWorld():
    if world.grayscale == False:
        for y in range(0, simSize):
            for x in range(0, simSize):
                colour = world.colourArray[x][y]
                pygame.draw.rect(window, (colour), ((x * gridSize), (y * gridSize), gridSize,
            else:
                for y in range(0, simSize):
                    for x in range(0, simSize):
                        value = world.heightArray[x][y]
                        pygame.draw.rect(window, (255 * value, 255 * value, 255 * value), ((x * gridSize),

#World Gen Functions
def RandomWorld():
    SetWorld(random.randint(0, 10000))
def SetWorld(seed):
    world.GenMap(seed)
    DrawWorld()

#Setup
window = pygame.display.set_mode((simSize * gridSize, simSize * gridSize))
pygame.display.set_caption("Procedural Generation")

world = worldClass.WorldMap(simSize)
RandomWorld()

#Main loop
running = True
while running == True:
    for event in pygame.event.get():
        if event.type == pygame.QUIT:
            running = False
        elif event.type == pygame.KEYDOWN:
            if event.key == pygame.K_RETURN:
                RandomWorld()
            elif event.key == pygame.K_F2:
```

```
pygame.image.save(window, "DevelopmentScreenshots\\screenshot {}.png".format(len
```

```
pygame.display.update()
```

2. worldClass.py

```
import random, json
```

```
class WorldMap():
```

```
    def __init__(self, size):
        self.arraySize = size
        self.heightArray = [[-1 for i in range(size)] for j in range(size)]
        self.colourArray = [[(0, 0, 0) for i in range(size)] for j in range(size)]
        self.typeArray = [[-1 for i in range(size)] for j in range(size)]
```

```
        self.inverted = False
        self.grayscale = False
        self.upNeutralDown = 0
        self.averaging = 0
        self.params = []
        self.thresholds = []
        self.LoadParameters("DefaultParameters.json")
```

```
    def LoadParameters(self, fname):
        file = open("Presets\\{}".format(fname), "r")
        self.params = json.loads(file.read())
        file.close()
```

```
    for key in self.params:
        if key == "Inverted":
            if self.params[key] == 1:
                self.inverted = True
        elif key == "UpNeutralDown":
            self.upNeutralDown = self.params[key]
        elif key == "Averaging":
            self.averaging = self.params[key]
        elif key == "Grayscale":
            if self.params[key] == 1:
                self.grayscale = True
        else:
            self.thresholds.append((float(key), (self.params[key][0], self.params[k
```

```
    def ConvertTypes(self):
        for y in range(0, self.arraySize):
            for x in range(0, self.arraySize):
                for i in range(len(self.thresholds)):
                    value = self.heightArray[x][y]
                    if self.inverted:
                        value = 1 - value
                    if value <= self.thresholds[i][0]:
                        #print(thresholds[i][0])
                        self.colourArray[x][y] = self.thresholds[i][1]
                        self.typeArray[x][y] = i
                        break
```

```
    def GenMap(self, seed):
        random.seed(seed)
        for y in range(0, self.arraySize):
            for x in range(0, self.arraySize):
                self.heightArray[x][y] = round(random.random(), 2)
```

```

    for i in range(self.upNeutralDown):
        self.UpNeutralDownGen()
        #print("UNDGen")
    for i in range(self.averaging):
        self.AverageGen()
        #print("averaging ")

    self.ConvertTypes()

def UpNeutralDownGen(self):
    dupMap = self.heightArray
    for y in range(0, self.arraySize):
        for x in range(0, self.arraySize):
            up = 0
            down = 0
            neutral = 0
            pointArr = []

            if x != 0 and y != 0:
                pointArr.append(self.heightArray[x - 1][y - 1])
            if x != 0 and y != self.arraySize - 1:
                pointArr.append(self.heightArray[x - 1][y + 1])
            if x != self.arraySize - 1 and y != self.arraySize - 1:
                pointArr.append(self.heightArray[x + 1][y + 1])
            if x != self.arraySize - 1 and y != 0:
                pointArr.append(self.heightArray[x + 1][y - 1])
            if x != 0:
                pointArr.append(self.heightArray[x - 1][y])
            if y != 0:
                pointArr.append(self.heightArray[x][y - 1])
            if x != self.arraySize - 1:
                pointArr.append(self.heightArray[x + 1][y])
            if y != self.arraySize - 1:
                pointArr.append(self.heightArray[x][y + 1])

            for i in range(len(pointArr)):
                if pointArr[i] >= self.heightArray[x][y] + 0.1:
                    up += 1
                elif pointArr[i] <= self.heightArray[x][y] - 0.1:
                    down += 1
                else:
                    neutral += 1

            if (up > down) and (up > neutral): # Up
                value = 0.09 * up
            elif (down > up) and (down > neutral): # Down
                value = -0.08 * down
            else: # Neutral
                value = 0

            dupMap[x][y] += value
            dupMap[x][y] = self.Clamp(dupMap[x][y], 0, 1)

    self.heightArray = dupMap

def AverageGen(self):
    dupMap = self.heightArray
    for y in range(0, self.arraySize):
        for x in range(0, self.arraySize):
            total = 0

```



```

count = 0
if x != 0 and y != 0:
    total += self.heightArray[x - 1][y - 1]
    count += 1
if x != 0 and y != self.arraySize - 1:
    total += self.heightArray[x - 1][y + 1]
    count += 1
if x != self.arraySize - 1 and y != self.arraySize - 1:
    total += self.heightArray[x + 1][y + 1]
    count += 1
if x != self.arraySize - 1 and y != 0:
    total += self.heightArray[x + 1][y - 1]
    count += 1
if x != 0:
    total += self.heightArray[x - 1][y]
    count += 1
if y != 0:
    total += self.heightArray[x][y - 1]
    count += 1
if x != self.arraySize - 1:
    total += self.heightArray[x + 1][y]
    count += 1
if y != self.arraySize - 1:
    total += self.heightArray[x][y + 1]
    count += 1

dupMap[x][y] = total / count
self.heightArray = dupMap

def Clamp(self, val, low, high):
    return low if val < low else high if val > high else val

```

3. mathLib.py

```

import math, random
class Matrix():
    def __init__(self, Values, cols = 0, identity = False):
        if type(Values) == list: # Predefined Values
            self.matrixArr = Values

        elif identity == True: # Identity Matrix
            if Values != cols:
                raise Exception("Cant create Identity Matrix of different orders")
            else:
                self.matrixArr = [[0 for i in range(cols)] for j in range(Values)]
                for y in range(0, Values):
                    self.matrixArr[y][y] = 1

        elif Values > 0 and cols > 0: # Blank Matrix of size x by y
            self.matrixArr = [[0 for i in range(cols)] for j in range(Values)]

        else: # Error Creating Matrix
            raise Exception("Error Creating Matrix")

    def Val(self):
        return self.matrixArr

    def Dimensions(self):
        return [len(self.matrixArr), len(self.matrixArr[0])] # Rows - Columns

    def ScalarMultiply(self, multiplier):

```

```

    for y in range(0, len(self.matrixArr)):
        for x in range(0, len(self.matrixArr[0])):
            self.matrixArr[y][x] = self.matrixArr[y][x] * multiplier

def SubMatrixList(self, rowList, colList):
    newMat = Matrix(self.Dimensions()[0] - len(rowList), self.Dimensions()[1] - len(
    xoffset = 0
    yoffset = 0
    yRowList = []

    for y in range(0, self.Dimensions()[0]):
        for x in range(0, self.Dimensions()[1]):
            if x in colList and y in rowList:
                xoffset += 1
                yoffset += 1
                continue
            elif x in colList:
                xoffset += 1
                continue
            elif y in rowList and y not in yRowList:
                yoffset += 1
                yRowList.append(y)
                continue
            else:
                newMat.matrixArr[y - yoffset][x - xoffset] = self.matrixArr[y][x]
            xoffset = 0
    return newMat

def SubMatrixRange(self, y1, y2, x1, x2):
    subMat = Matrix(y2 - y1 + 1, x2 - x1 + 1)
    for y in range(y1, y2 + 1):
        for x in range(x1, x2 + 1):
            subMat.matrixArr[y][x] = self.matrixArr[y][x]
    return subMat

def RandomVal(self):
    self.matrixArr = [[random.randint(1, 100) for i in range(self.Dimensions()[1])]

def ConvertToVector(self):
    return Vector(self.matrixArr)

@staticmethod
def Determinant(m):
    dims = m.Dimensions()
    if dims[1] <= 2:
        det = (m.matrixArr[0][0] * m.matrixArr[1][1]) - (m.matrixArr[0][1] * m.ma
        return det
    elif dims[1] != 2:
        det = 0
        subtract = False
        tempMat = m.SubMatrixList([0], [])
        for i in range(0, dims[1]):
            subMat = None
            subMat = m.SubMatrixList([0], [i])
            if subtract == False:
                det += m.matrixArr[0][i] * Matrix.Determinant(subMat)
                subtract = True
            elif subtract == True:
                det -= m.matrixArr[0][i] * Matrix.Determinant(subMat)
                subtract = False

```

```

        return det

def det(m):
    top_length = len(m[0])
    height = top_length - 1
    submats = []

    for i in range(0, top_length):
        submat = [[] for i in range(height)]
        for j in range(0, top_length):
            if i != j:
                for k in range(height):
                    submat[k].append(m[k+1][j])
        submats.append(submat)
    return submats

# Static Methods
@staticmethod
def MatrixAddSubtract(m1, m2, subtract = False): # Dont know how else i would make
    m1Dims = m1.Dimensions()
    m2Dims = m2.Dimensions()
    if m1Dims[0] != m2Dims[0]:
        raise Exception("Matrices_Row_Order_does_not_match")
    elif m1Dims[1] != m2Dims[1]:
        raise Exception("Matrices_Column_Order_does_not_match")
    elif type(m1) != type(m2):
        raise Exception("Types_do_not_match, Convert_Vector_to_Matrix_or_vice_vers")
    else:
        newMat = Matrix(m1Dims[0], m1Dims[1])
        for y in range(0, m1Dims[0]):
            for x in range(0, m1Dims[1]):
                if subtract:
                    newMat.matrixArr[y][x] = m1.Val()[y][x] - m2.Val()[y][x]
                else:
                    newMat.matrixArr[y][x] = m1.Val()[y][x] + m2.Val()[y][x]
        return newMat

@staticmethod
def MatrixMultiply(m1, m2): # Not that efficient, needs optimisation
    m1Dims = m1.Dimensions()
    m2Dims = m2.Dimensions()
    if m1Dims[1] != m2Dims[0]:
        raise Exception("Matrices_Multiplication_Error")
    else:
        if (type(m2) == Vector):
            newMat = Matrix(m1Dims[0], m2Dims[1])
        else:
            newMat = Matrix(m1Dims[0], m2Dims[1])
        for row in range(0, m1Dims[1]):
            subRow = m1.Val()[row][0:m1Dims[1]]
            for col in range(0, m2Dims[1]):
                subCol = []
                for i in range(0, m1Dims[0]):
                    print(i)
                    subCol.append(m2.Val()[i][col])
                total = 0
                for x in range(0, len(subRow)):
                    total += subRow[x] * subCol[x]
                newMat.matrixArr[row][col] = total
        return newMat

```

```

class Vector(Matrix):
    def __init__(self, val):
        if type(val) == list:
            if len(val[0]) != 1:
                raise Exception("Invalid Vector, use Matrix Instead")
            else:
                self.matrixArr = val
        else:
            self.matrixArr = [[0 for i in range(1)] for j in range(val)]

    def ConvertToMatrix(self):
        return Matrix(self.matrixArr)

    @staticmethod
    def DotProduct(v1, v2):
        if type(v1) != Vector or type(v2) != Vector:
            raise Exception("Wront Types: {}, {} passed into Dot Product".format(type(v1), type(v2)))
        else:
            total = 0
            for i in range(v1.Dimensions()[0]):
                total += v1.Val()[i][0] * v2.Val()[i][0]
            return total

```

7. Technical Solution