

# **An Investigation into Machine Learning and Neural Networks through the Simulation of Human Survival**

Computer Science NEA

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## 2. Analysis

### 1. Statement of Investigation

I plan to investigate Machine Learning by developing a survival simulation environment in which an Agent will be controlled by a Machine Learning algorithm. The survival simulation will present multiple challenges towards the agent in order to provide a complex problem for it to solve. The key question I aim to answer with this investigation is:

**Can you train a Machine Learning algorithm to survive in a pseudo random, open-world environment?**

I find this question to be quite interesting because there is multiple layers of complexity to it, with several different problems to solve. Answering the question will require me to dive headfirst into Machine Learning picking things up as fast as possible.

2. Background
3. Expert
4. Initial Research

## 5. Prototype

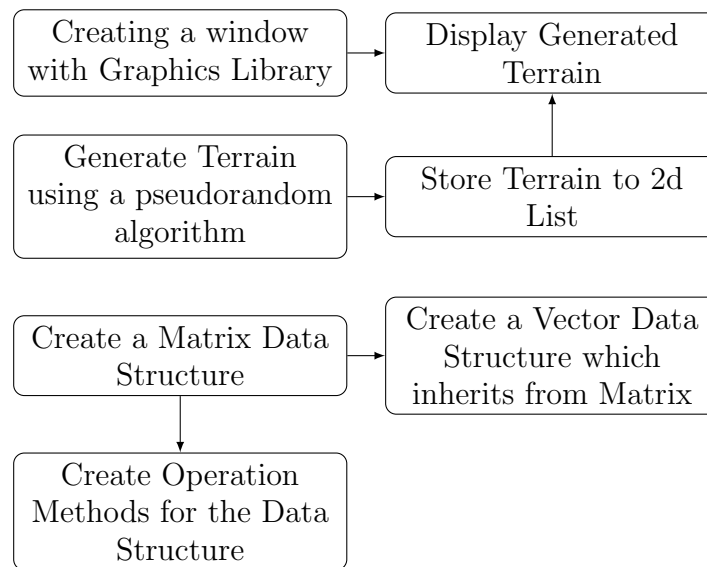
Before starting my Prototype I had to decide upon a short list of objectives I wanted to complete/investigate as part of it. These boiled down to a few things:

- (a) Terrain Generation
- (b) Displaying the Generated Terrain using a Graphics Library
- (c) Matrix and Vector implementation

For my Prototype, I first created a GitHub Repository, available here:

<https://github.com/TheTacBanana/CompSciNEAPrototype>

I had created a hierarchy of importance for development in my head, visualized using this flow diagram:



I decided to use Python for developing my Prototype, this seemed like a good fit due to me having lots of experience with the language. Python is a Dynamically Typed and Interpretted language which makes it versatile for prototyping and fast, iterative development.

### Terrain Generation and Displaying

Starting from the begining of my hierarchy I installed Pygame using *pip* and started creating a window. This was a relatively simple task only taking a few lines:

```

import pygame

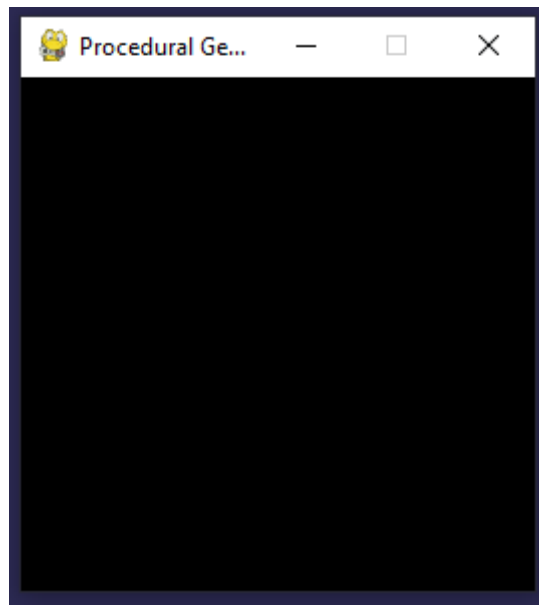
simSize = 128
gridSize = 2

window = pygame.display.set_mode((simSize*gridSize, simSize*gridSize))
pygame.display.set_caption("Procedural_Generation")

running = True
while running == True:
    for event in pygame.event.get():
        if event.type == pygame.QUIT:
            running = False

```

This creates a window like this:



Following the hierarchy I then added noise generation by generating random numbers and assigning them to a 2d List. Shown here:

```

def GenerateMap(self, seed):
    random.seed(seed)
    for y in range(0, self.arraySize):
        for x in range(0, self.arraySize):
            self.heightArray[x][y] = round(random.random(), 2)

```

After creating some code to draw squares based upon the random value, I ended up with this random array of Black-White squares:



This was a good start, but didnt really look like terrain yet. As part of my research I came across simple algorithms to turn random noise into usable 2d terrain. I decided to implement these algorithms. They are relatively short and didnt take too much time to implement. I've named the two algorithms UpDownNeutralGen and Average.

#### UpDownNeutralGen Method

The UpDownNeutralGen method takes a tile, and considers every tile around it. It sums the tile which are greater than, less than, or within a certain range of the tile height. And then pulls the selected tile in the direction which has the highest precedence. As an example, here are some randomly generated values:

0.71	0.19	0.3
0.46	0.26	0.82
0.63	0.35	0.05

If we count the surrounding values into corresponding Higher, Lower and Neutral we get:

Higher	Lower	Neutral
4	1	3

This leads us to calculating the *pullValue*, respectively for each case:

$$\begin{aligned}
 Up- & \rightarrow pullValue = upTiles * 0.09 \\
 Down- & \rightarrow pullValue = upTiles * -0.08 \\
 Neutral- & \rightarrow pullValue = 0
 \end{aligned}$$

$$Value[x][y] += pullValue$$

We then add the pullValue to the original square value, leaving us with the updated value. The code for this shown under the Prototype Code Header.

#### Average Method

The Average method takes a tile and considers every tile around it, this time instead of looking at the differences, it creates an average from the 8 surrounding tiles. It then sets the selected tile to this average value. As an example, here are some randomly generated values:

0.83	0.93	0.64
0.07	0.38	0.21
0.33	0.94	0.95

Summing these and dividing by the total grants us the average:

$$\frac{0.83 + 0.93 + 0.64 + 0.07 + 0.38 + 0.21 + 0.95 + 0.33 + 0.94}{9} = 0.586$$

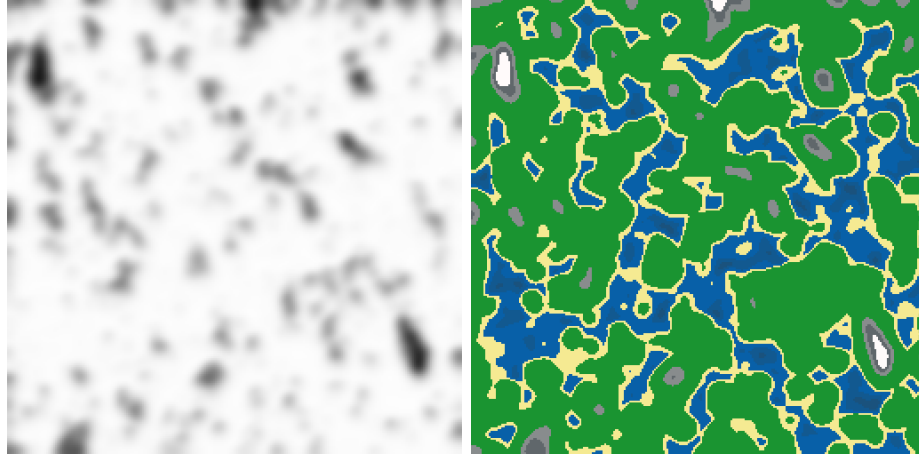
$$Value[x][y] = 0.586$$

The code for this shown under the Prototype Code Header.

#### Finished Terrain Generation



Overall I am happy with the Terrain generation, though I feel as if it could be improved to look more realistic. The difference between the original random noise and the Colour Mapped Terrain looks so much better.



## Matrix Data Structure

As part of my Matrix Class I made a list of operations which would be key to a Matrix Class, along with being useful for Machine Learning. A Matrix is an abstract data type, commonly used in Maths, but has practical uses in the world of Computer Science. It holds a 2d array of values such as:

$$\begin{pmatrix} a & b \\ c & d \end{pmatrix} \begin{pmatrix} a & b & c \\ d & e & f \\ g & h & i \end{pmatrix} \begin{pmatrix} a \\ b \\ c \end{pmatrix} \begin{pmatrix} a & b & c & d \\ e & f & g & h \end{pmatrix}$$

The values in a Matrix can be manipulated using common operations such as  $+$   $-$   $*$  as long as the orders of the 2 Matrices match up. Along with other, non-standard operations which have other purposes.

As part of my Matrix Class, I implemented the following operators:

### (a) Addition/Subtraction

Implementing Addition didnt take too long, I utilised a nested for loop to iterate over every value in both Matrices. Adding the two values together into a temporary Matrix which the method then returned.

$$\begin{pmatrix} a & b \\ c & d \end{pmatrix} + \begin{pmatrix} e & f \\ g & h \end{pmatrix} = \begin{pmatrix} a+e & b+f \\ c+g & d+h \end{pmatrix}$$

(b) Multiplication

Multiplication of Matrices is slightly more complicated, it is of  $O(n^3)$  complexity, utilising a triple nested for loop. It multiplies the row of a  $M1$ , by the column in  $M2$ . Summing the calculation into the element in the new Matrix  $M3$ .

$$\begin{pmatrix} a & b \\ c & d \end{pmatrix} * \begin{pmatrix} e & f \\ g & h \end{pmatrix} = \begin{pmatrix} a * e + b * g & a * f + b * h \\ c * e + d * g & c * f + d * h \end{pmatrix}$$

There is also Scalar Multiplication which multiples each value of a Matrix by the Scalar.

$$k * \begin{pmatrix} a & b \\ c & d \end{pmatrix} = \begin{pmatrix} ka & kb \\ kc & kd \end{pmatrix}$$

(c) Determinant

Calculating the Determinant of an NxN Matrix is a recursive algorithm. With the base case being the Determinant of a 2x2 Matrix. When calculating the Determinant of a 3x3 Matrix you create a Matrix of Cofactors, and multiply each value by the corresponding value in the Sin Matrix (*Formed from repeating 1's and -1's*). Summing the values from a singular Row or Column will then give you the Determinant. For a 4x4 you simply calculate the Determinant of the corresponding 3x3's to get the Cofactors.

$$\begin{vmatrix} a & b \\ c & d \end{vmatrix} = a * d - b * c$$

$$\begin{vmatrix} a & b & c \\ d & e & f \\ g & h & i \end{vmatrix} = a * \begin{vmatrix} e & f \\ h & i \end{vmatrix} - b * \begin{vmatrix} d & f \\ g & i \end{vmatrix} + c * \begin{vmatrix} d & e \\ g & h \end{vmatrix}$$

(d) Dot Product

The Dot Product occurs between two vectors, and can be used to calculate the angle between them. Its a relatively simple operation only taking a few lines of code.

$$\begin{pmatrix} a \\ b \\ c \end{pmatrix} \cdot \begin{pmatrix} d \\ e \\ f \end{pmatrix} = a * d + b * e + c * f$$

All code is available under the Prototype Code Header.

## Prototype Evaluation

Overall I am happy with my prototype, though I feel like some parts need to be improved. I did meet my objectives for my prototype but there were improvements which can be made when I create my Technical Solution. Namely the Terrain Generation along with the Matrix class. I feel that Perlin noise would be a better alternative to the two algorithms I used. In theory it should produce better results, and also provide more marks for complexity. My Matrix class could be rewritten to be more efficient, along with using operator overloading, which I didn't know Python could do at the time. I also feel like having vector inherit from matrix is relatively pointless, there is no need for it when I could just use 1 wide Matrices.

## 6. Objectives

Taking into account my Prototype and Interview, I have formed a list of objectives I feel to be most appropriate for my Investigation. If all completed they will form a complete solution which will answer my Investigations question. Below is the list of objectives split into 6 key sections:

### (a) User Input

- i. Read Parameters from a Json formatted file
- ii. Check Parameters fall within a certain range to prevent errors
- iii. Give user option to load Neural Network Training progress

### (b) Simulation

- i. Utilise Perlin Noise to generate a 2d List of terrain heights
- ii. Store Terrain Heights in a Tile Data Type
- iii. Utilise Threading to generate Terrain Faster
- iv. Display terrain to a pygame window
- v. Map ranges of terrain heights to specific colour bands
- vi. Utilise Poisson Disc Sampling to generate objects for the Agent to interact with
- vii. Implement enemies which use basic pathfinding to traverse towards the player
- viii. Generate multiple enemies upon starting the simulation
- ix. Allow the enemies to attack the Agent

### (c) Agent

- i. Implement Movement options for the Agent
- ii. Implement the ability to pick up the generated Objects
- iii. Implement the ability to attack the generated enemies
- iv. Create methods to sample the terrain around the Agent
- v. Create methods to convert the sampled Tiles into a grayscale input vector for a neural network
- vi. Create reward methods to reward the agent given the terrain samples and action

### (d) Matrix Class

- i. Implement a Dynamic Matrix Class with appropriate Operations such as:
  - A. Multiplication
  - B. Addition
  - C. Subtraction

- D. Transpose
- E. Sum
- F. Select Row/Column
- ii. Create appropriate errors to throw when utilising methods the incorrect way
- (e) Deep Q Learning
  - i. Dynamically create a Dual Neural Network model based upon loaded parameters
  - ii. Implement an Abstract Class for Activation Functions
  - iii. Implement Activation Functions inheriting from the Abstract Class such as:
    - A. ReLu
    - B. Sigmoid
    - C. SoftMax
  - iv. Create methods to Forward Propagate the neural network
  - v. Create methods to calculate the loss of the network using the Bellman Equation
  - vi. Create methods to Back Propagate calculated error through the neural network
  - vii. Create methods to update weights and biases within the network to converge on a well trained network
  - viii. Utilise the outlined Matrix class to perform the mathematical operations in the specified methods
  - ix. Implement Load and Save Methods to save progress in training
  - x. Implement a Double Ended Queue/Deque Data Type
  - xi. Implement Experience Replay utilising the Deque Data Type to increase training accuracy
- (f) Data Logger
  - i. Be able to create a Data Logger class to log data points across training
  - ii. Be able to create a Data Structure for the Data Logger
  - iii. Allow multiple types specified types for a single parameter
  - iv. When adding a new Data Point the Logger will check it to make sure it matches the given Data Structure
  - v. Implement a Heap Data Type
  - vi. Implement a Heap sort using the Heap Data Type
  - vii. Be able to sort by a parameter in the Data Structure
  - viii. Be able to select a single parameter from the data points
  - ix. Implement Load and Save Functions to save progress during training

### 3. Design

## 4. Testing

As part of testing my NEA, I identified the key areas of my project which needed testing. My testing targets these areas from different angles to ensure they work correctly. These areas are:

1. User Input
  - (a) Parameter Loading
  - (b) Neural Network Loading
2. Matrix Implementation
  - (a) Constructor Cases
  - (b) Matrix Operations
  - (c) Thrown Exceptions
3. Deep Q Learning Algorithm
  - (a) Forward Propagation
  - (b) Loss Function
  - (c) Back Propagation
  - (d) Double Ended Queue Data Type
4. Data Logger
  - (a) Data Structure Matching
  - (b) Heap Data Structure
  - (c) Heap Sort Implementation
5. Simulation
  - (a) Generation of 2d Terrain
  - (b) Continuity of Generation

Below is the included NEA Testing video for testing evidence

*<https://thisisalink.com/youtotallybelieveme/>*

## 1.1 User Input

Test No.	Test Name	Input Data	Expected Output	Pass / Fail	Time Stamp
1	Loading Parameters File	"Default.json" file which contains the loadable values	Loads parameters into the Parameters Dictionary variable	Pass	00:00
2	Test Parameters within range	-	-	-	-
3	Loading of Network Weights	-	-	-	-
4	-	-	-	-	-
5	-	-	-	-	-



## 6. Prototype Code

Below is the code I created while developing my Prototype.  
The 3 Scripts listed in order are:

1. main.py
2. worldClass.py
3. mathLib.py

- 
1. main.py

```
#Imports
import pygame, random, json, os, time
from datetime import datetime
import worldClass, agentClass, mathLib

#Variables
simSize = 64
gridSize = 4
simSeed = 420

#World Functions
def DrawWorld():
    if world.grayscale == False:
        for y in range(0, simSize):
            for x in range(0, simSize):
                colour = world.colourArray[x][y]
                pygame.draw.rect(window, (colour), ((x * gridSize), (y * gridSize), gridSize, gridSize))
            else:
                for y in range(0, simSize):
                    for x in range(0, simSize):
                        value = world.heightArray[x][y]
                        pygame.draw.rect(window, (255 * value, 255 * value, 255 * value), ((x * gridSize), (y * gridSize), gridSize, gridSize))

#World Gen Functions
def RandomWorld():
    SetWorld(random.randint(0, 10000))
def SetWorld(seed):
    world.GenMap(seed)
    DrawWorld()

#Setup
window = pygame.display.set_mode((simSize * gridSize, simSize * gridSize))
pygame.display.set_caption("Procedural_Generation")

world = worldClass.WorldMap(simSize)
RandomWorld()
```

```

#Main loop
running = True
while running == True:
    for event in pygame.event.get():
        if event.type == pygame.QUIT:
            running = False
        elif event.type == pygame.KEYDOWN:
            if event.key == pygame.K_RETURN:
                RandomWorld()
            elif event.key == pygame.K_F2:
                pygame.image.save(window, "DevelopmentScreenshots\\screenshot{}.png".format(
                    counter))
            counter += 1
    pygame.display.update()

```

## 2. worldClass.py

```

import random, json

class WorldMap():
    def __init__(self, size):
        self.arraySize = size
        self.heightArray = [[-1 for i in range(size)] for j in range(size)]
        self.colourArray = [[(0, 0, 0) for i in range(size)] for j in range(size)]
        self.typeArray = [[-1 for i in range(size)] for j in range(size)]

        self.inverted = False
        self.grayscale = False
        self.upNeutralDown = 0
        self.averaging = 0
        self.params = []
        self.thresholds = []
        self.LoadParameters("DefaultParameters.json")

    def LoadParameters(self, fname):
        file = open("Presets\\{}".format(fname), "r")
        self.params = json.loads(file.read())
        file.close()

        for key in self.params:
            if key == "Inverted":
                if self.params[key] == 1:
                    self.inverted = True
            elif key == "UpNeutralDown":
                self.upNeutralDown = self.params[key]
            elif key == "Averaging":
                self.averaging = self.params[key]
            elif key == "Grayscale":
                if self.params[key] == 1:
                    self.grayscale = True

```

```

        else:
            self.thresholds.append((float(key), (self.params[key][0], self.par

def ConvertTypes(self):
    for y in range(0, self.arraySize):
        for x in range(0, self.arraySize):
            for i in range(len(self.thresholds)):
                value = self.heightArray[x][y]
                if self.inverted:
                    value = 1 - value
                if value <= self.thresholds[i][0]:
                    #print(thresholds[i][0])
                    self.colourArray[x][y] = self.thresholds[i][1]
                    self.typeArray[x][y] = i
                    break

def GenMap(self, seed):
    random.seed(seed)
    for y in range(0, self.arraySize):
        for x in range(0, self.arraySize):
            self.heightArray[x][y] = round(random.random(), 2)

    for i in range(self.upNeutralDown):
        self.UpNeutralDownGen()
        #print("UNDGen")
    for i in range(self.averaging):
        self.AverageGen()
        #print("averaging")

    self.ConvertTypes()

def UpNeutralDownGen(self):
    dupMap = self.heightArray
    for y in range(0, self.arraySize):
        for x in range(0, self.arraySize):
            up = 0
            down = 0
            neutral = 0
            pointArr = []

            if x != 0 and y != 0:
                pointArr.append(self.heightArray[x - 1][y - 1])
            if x != 0 and y != self.arraySize - 1:
                pointArr.append(self.heightArray[x - 1][y + 1])
            if x != self.arraySize - 1 and y != self.arraySize - 1:
                pointArr.append(self.heightArray[x + 1][y + 1])
            if x != self.arraySize - 1 and y != 0:
                pointArr.append(self.heightArray[x + 1][y - 1])

```

```

    if x != 0:
        pointArr.append(self.heightArray[x - 1][y])
    if y != 0:
        pointArr.append(self.heightArray[x][y - 1])
    if x != self.arraySize - 1:
        pointArr.append(self.heightArray[x + 1][y])
    if y != self.arraySize - 1:
        pointArr.append(self.heightArray[x][y + 1])

    for i in range(len(pointArr)):
        if pointArr[i] >= self.heightArray[x][y] + 0.1:
            up += 1
        elif pointArr[i] <= self.heightArray[x][y] - 0.1:
            down += 1
        else:
            neutral += 1

    if (up > down) and (up > neutral): # Up
        value = 0.09 * up
    elif (down > up) and (down > neutral): # Down
        value = -0.08 * down
    else: # Neutral
        value = 0

    dupMap[x][y] += value
    dupMap[x][y] = self.Clamp(dupMap[x][y], 0, 1)

self.heightArray = dupMap

def AverageGen(self):
    dupMap = self.heightArray
    for y in range(0, self.arraySize):
        for x in range(0, self.arraySize):
            total = 0
            count = 0
            if x != 0 and y != 0:
                total += self.heightArray[x - 1][y - 1]
                count += 1
            if x != 0 and y != self.arraySize - 1:
                total += self.heightArray[x - 1][y + 1]
                count += 1
            if x != self.arraySize - 1 and y != self.arraySize - 1:
                total += self.heightArray[x + 1][y + 1]
                count += 1
            if x != self.arraySize - 1 and y != 0:
                total += self.heightArray[x + 1][y - 1]
                count += 1
            if x != 0:
                total += self.heightArray[x - 1][y]

```

```

        count += 1
    if y != 0:
        total += self.heightArray[x][y - 1]
        count += 1
    if x != self.arraySize - 1:
        total += self.heightArray[x + 1][y]
        count += 1
    if y != self.arraySize - 1:
        total += self.heightArray[x][y + 1]
        count += 1

    dupMap[x][y] = total / count
    self.heightArray = dupMap

def Clamp(self, val, low, high):
    return low if val < low else high if val > high else val

```

### 3. mathLib.py

```

import math, random
class Matrix():
    def __init__(self, Values, cols = 0, identity = False):
        if type(Values) == list: # Predefined Values
            self.matrixArr = Values

        elif identity == True: # Identity Matrix
            if Values != cols:
                raise Exception("Cant create Identity Matrix of different orders")
            else:
                self.matrixArr = [[0 for i in range(cols)] for j in range(Values)]
                for y in range(0, Values):
                    self.matrixArr[y][y] = 1

        elif Values > 0 and cols > 0: # Blank Matrix of size x by y
            self.matrixArr = [[0 for i in range(cols)] for j in range(Values)]

        else: # Error Creating Matrix
            raise Exception("Error Creating Matrix")

    def Val(self):
        return self.matrixArr

    def Dimensions(self):
        return [len(self.matrixArr), len(self.matrixArr[0])] # Rows - Columns

    def ScalarMultiply(self, multiplier):
        for y in range(0, len(self.matrixArr)):
            for x in range(0, len(self.matrixArr[0])):
                self.matrixArr[y][x] = self.matrixArr[y][x] * multiplier

```

```

def SubMatrixList(self, rowList, colList):
    newMat = Matrix(self.Dimensions()[0] - len(rowList), self.Dimensions()[1])
    xoffset = 0
    yoffset = 0
    yRowList = []

    for y in range(0, self.Dimensions()[0]):
        for x in range(0, self.Dimensions()[1]):
            if x in colList and y in rowList:
                xoffset += 1
                yoffset += 1
                continue
            elif x in colList:
                xoffset += 1
                continue
            elif y in rowList and y not in yRowList:
                yoffset += 1
                yRowList.append(y)
                continue
            else:
                newMat.matrixArr[y - yoffset][x - xoffset] = self.matrixArr[y][x]
        xoffset = 0
    return newMat

def SubMatrixRange(self, y1, y2, x1, x2):
    subMat = Matrix(y2 - y1 + 1, x2 - x1 + 1)
    for y in range(y1, y2 + 1):
        for x in range(x1, x2 + 1):
            subMat.matrixArr[y][x] = self.matrixArr[y][x]
    return subMat

def RandomVal(self):
    self.matrixArr = [[random.randint(1, 100) for i in range(self.Dimensions[1]) for j in range(self.Dimensions[0])]

def ConvertToVector(self):
    return Vector(self.matrixArr)

@staticmethod
def Determinant(m):
    dims = m.Dimensions()
    if dims[1] <= 2:
        det = (m.matrixArr[0][0] * m.matrixArr[1][1]) - (m.matrixArr[0][1] * m.matrixArr[1][0])
        return det
    elif dims[1] != 2:
        det = 0
        subtract = False
        tempMat = m.SubMatrixList([0], [])
        for i in range(0, dims[1]):

```

```

        subMat = None
        subMat = m.SubMatrixList([0],[i])
        if subtract == False:
            det += m.matrixArr[0][i] * Matrix.Determinant(subMat)
            subtract = True
        elif subtract == True:
            det -= m.matrixArr[0][i] * Matrix.Determinant(subMat)
            subtract = False
    return det

def det(m):
    top_length = len(m[0])
    height = top_length - 1
    submats = []

    for i in range(0, top_length):
        submat = [[] for i in range(height)]
        for j in range(0, top_length):
            if i != j:
                for k in range(height):
                    submat[k].append(m[k+1][j])
        submats.append(submat)
    return submats

# Static Methods
@staticmethod
def MatrixAddSubtract(m1, m2, subtract = False): # Dont know how else i would
    m1Dims = m1.Dimensions()
    m2Dims = m2.Dimensions()
    if m1Dims[0] != m2Dims[0]:
        raise Exception("Matrices_Row_Order_does_not_match")
    elif m1Dims[1] != m2Dims[1]:
        raise Exception("Matrices_Column_Order_does_not_match")
    elif type(m1) != type():
        raise Exception("Types_do_not_match,_Convert_Vector_to_Matrix_or_vice")
    else:
        newMat = Matrix(m1Dims[0], m1Dims[1])
        for y in range(0, m1Dims[0]):
            for x in range(0, m1Dims[1]):
                if subtract:
                    newMat.matrixArr[y][x] = m1.Val()[y][x] - m2.Val()[y][x]
                else:
                    newMat.matrixArr[y][x] = m1.Val()[y][x] + m2.Val()[y][x]
        return newMat

@staticmethod
def MatrixMultiply(m1, m2): # Not that efficient, needs optimisation
    m1Dims = m1.Dimensions()
    m2Dims = m2.Dimensions()

```

```

if m1Dims[1] != m2Dims[0]:
    raise Exception("Matrices_Multiplication_Error")
else:
    if (type(m2) == Vector):
        newMat = Matrix(m1Dims[0], m2Dims[1])
    else:
        newMat = Matrix(m1Dims[0], m2Dims[1])
    for row in range(0, m1Dims[1]):
        subRow = m1.Val()[row][0:m1Dims[1]]
        for col in range(0, m2Dims[1]):
            subCol = []
            for i in range(0, m1Dims[0]):
                print(i)
                subCol.append(m2.Val()[i][col])
            total = 0
            for x in range(0, len(subRow)):
                total += subRow[x] * subCol[x]
            newMat.matrixArr[row][col] = total
    return newMat

class Vector(Matrix):
    def __init__(self, val):
        if type(val) == list:
            if len(val[0]) != 1:
                raise Exception("Invalid_Vector,_use_Matrix_Instead")
            else:
                self.matrixArr = val
        else:
            self.matrixArr = [[0 for i in range(1)] for j in range(val)]

    def ConvertToMatrix(self):
        return Matrix(self.matrixArr)

    @staticmethod
    def DotProduct(v1, v2):
        if type(v1) != Vector or type(v2) != Vector:
            raise Exception("Wront_Types:{},{} _passed_into_Dot_Product".format(type(v1), type(v2)))
        else:
            total = 0
            for i in range(v1.Dimensions()[0]):
                total += v1.Val()[i][0] * v2.Val()[i][0]
            return total

```



## 7. Technical Solution