

Roll No: CS23E001

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Collaborators (if any):

References/sources (if any):

- Use \LaTeX to write-up your solutions (in the solution blocks of the source \LaTeX file of this assignment), submit the resulting rollno.asst2.answers.pdf file at Crowdmark by the due date, and properly drag that pdf's answer pages to the corresponding question in Crowdmark (do this properly, otherwise we won't be able to grade!). (Note: **No late submissions** will be allowed, other than one-day late submission with 10% penalty or four-day late submission with 30% penalty.)
 - Please upload to moodle a rollno.zip file containing three files: rollno.asst2.answers.pdf file mentioned above, and two code files for the programming question (rollno.ipynb file and rollno.py file). Do not forget to upload to Crowdmark your results/answers (including Jupyter notebook **with output**) for the programming question.
 - Collaboration is encouraged, but all write-ups must be done individually and independently, and mention your collaborator(s) if any. Same rules apply for codes written for any programming assignments (i.e., write your own code; we will run plagiarism checks on codes).
 - If you have referred a book or any other online material or LLMs (Large Language Models like ChatGPT) for obtaining a solution, please cite the source. Again don't copy the source *as is* - you may use the source to understand the solution, but write-up the solution in your own words (this also means that you cannot copy-paste the solution from LLMs!). Please be advised that *the lesser your reliance on online materials or LLMs for answering the questions, the more your understanding of the concepts will be and the more prepared you will be for the course exams.*
 - Points will be awarded based on how clear, concise and rigorous your solutions are, and how correct your answer is. The weightage of this assignment is 12% towards the overall course grade.
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1. (8 points) [PRINCIPAL COMPONENT ANALYSIS - NUMERICAL] Consider the following dataset D of 8 datapoints:

You need to reduce the data into a single-dimension representation. You are given the first principal component: $PC1 = (-0.694, -0.720)$.

- (a) (2 points) What is the second principal component of the dataset D? How will you represent data #2 as a linear combination of the two principal components? What is the reconstruction error of this $(PC1, PC2)$ -based representation of data #2?

data #	x	y
1	5.51	5.35
2	20.82	24.03
3	-0.77	-0.57
4	19.30	19.38
5	14.24	12.77
6	9.74	9.68
7	11.59	12.06
8	-6.08	-5.22

Solution: The second principal component is $(-0.720, 0.694)$.

The representation of data #2 as the linear combination as:

$$\begin{bmatrix} -0.69 & -0.72 \\ -0.72 & 0.69 \end{bmatrix} \begin{bmatrix} 20.82 \\ 24.03 \end{bmatrix} = [-31.7499053 \quad 1.69]$$

The point after reconstruction is: $(-31.74, 1.69)$ The reconstruction error is: 37.45