What is a sandwich? A data analysis in \mathbb{R}^{43}

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Abstract

In this paper we set out to examine the sandwich views of students and teachers at William Lyon Mackenzie C.I.

Our study consisted of a survey conducted in person with 140 participants. We asked participants basic demographic information about where they fit into the William Lyon Mackenzie Collegiate Institute community, and examined correlations between sandwich views and demographics.

We propose the creation of a two-dimensional sandwich alignment chart, inspired by two-dimensional political axes. The sandwich alignment chart has a dimension for "sandwich purity", and "sandwich orthodoxy".

We hypothesize that:

- 1. Sandwich purity and sandwich orthodoxy will be positively correlated.
- 2. Students in the MaCS or Gifted program are more likely to have a low orthodoxy score.

We believe the first hypothesis to be true because we believe those with a pure definition of a sandwich will also have an orthodoxy definition. We believe the second hypothesis to be true because we believe that students in those programs tend to challenge societal norms more so than most.

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Part I Introduction

Purpose

1.1 The failure of the dictionary

We find dictionary definitions to be insufficient, as they are either too restrictive, or too vague.

The Oxford English Dictionary [10] restrictively defines a sandwich as:

An item of food consisting of two pieces of bread with a filling between them, eaten as a light meal.

Whereas The Free Dictionary [31] more broadly defines a sandwich as:

- a. Two or more slices of bread with a filling such as meat or cheese placed between them.
- b. A partly split long or round roll containing a filling.
- c. One slice of bread covered with a filling.

Since the Oxford English Dictionary definition requires two pieces of bread, this excludes sub sandwiches, which most would consider a sandwich. This makes the Oxford definition too restrictive.

Also, both definitions fail to adequately define "filling". The Free Dictionary gives meat and cheese as examples, but many people put lettuce and tomato in their sandwiches, neither of which are meat or cheese.

So, dictionary definitions of "sandwich" are insufficient to determine what a sandwich is.

1.2 Legal background

The question of what is a sandwich has been the centre of several legal publications. We believe that these publications have failed to provide a strong definition of what a sandwich is, and they contradict each other.

For tax purposes, the New York State Department of Taxation and Finance [28] says:

Sandwiches include cold and hot sandwiches of every kind that are prepared and ready to be eaten, whether made on bread, on bagels, on rolls, in pitas, in wraps, or otherwise, and regardless of the filling or number of layers. A sandwich can be as simple as a buttered bagel or roll, or as elaborate as a six-foot, toasted submarine sandwich.

Some examples of taxable sandwiches include:

- common sandwiches, such as:
 - BLTs (bacon, lettuce, and tomato sandwiches);
 - club sandwiches;
 - o cold cut sandwiches;
 - o grilled cheese sandwiches;
 - peanut butter and jelly sandwiches
 - o salad-type sandwiches (e.g., chicken, egg, ham, and tuna);
- bagel sandwiches (served buttered or with spreads, or otherwise as a sandwich);
- burritos
- cheese-steak sandwiches;
- croissant sandwiches;
- fish fry sandwiches;
- flatbread sandwiches;

- breakfast sandwiches;
- gyros;
- hamburgers on buns, rolls, etc.;
- heroes, hoagies, torpedoes, grinders, submarines, and other such sandwiches;
- hot dogs and sausages on buns, rolls, etc.;
- melt sandwiches;
- open-faced sandwiches;
- panini sandwiches;
- Reuben sandwiches; and
- wraps and pita sandwiches.

This is a very broad definition, but it is also quite comprehensive and informative. It is important to note that [28] defines burritos as sandwiches. However, other legal cases contradict this definition.

A case in the Commonwealth of Massachusetts Superior Court entitled White City Shopping Center, LP v. PR Restaurants, LLC dba Bread Panera [45] involved two companies in a dispute over whether or not burritos are sandwiches. In this case, the court ruled that burritos are not sandwiches. This contradicts the definition in New York State tax law. So, we can clearly see that there is no legal consensus on this matter.

Furthermore, the legal scholar Marjorie Florestal argues that the decision of the White City case is rooted in classist and racial views of sandwich cuisine [15]:

The burrito meets resistance not just because of its class but also because of its race—and the way the two play off each other.

So, we have established that the definition of a sandwich is inconclusive among both the linguist and legal communities [10, 31, 28, 45]. The question is also of importance for better understanding class systems and race in our society [15].

Terminology and definitions

This chapter will explain any terminology and definitions we use throughout this paper.

2.1 Question types

Demographic question A demographic question is any of the non-food questions asked in our survey. These questions asked about participants demographics, in order to examine any correlations between demographics and sandwich views.

Food question A food question is any question asked about sandwiches or their ingredients. We asked 43 food questions as a part of this study. Participants answered each question on a 0 to 10 scale. We purposely started the scale at 0 so as to make 5 exactly in the middle of the range of possible responses.

2.2 Variables

The demographic questions are our independent variables. We mainly look at academic stream, grade, and race as our independent variables.

The food questions are used to calculate orthodoxy and purity, which are our dependent variables.

We also consider the correlation between our two dependent variables to gain a deeper understanding of how they relate.

2.3 Population of interest

Our population of interest is the population of both students and teachers at William Lyon Mackenzie C.I.

Methodology

3.1 Survey type

We conducted our survey as mix of a stratified, voluntary, and random sample. We surveyed roughly 10% of the William Lyon Mackenzie population. With a sample size this large, most bias should be eliminated.

Unfortunately, we failed to collect a perfectly stratified sample. However, an analysis of the data shows that to be inconsequential.

We made manual changes to categorical to correct for similar, blank, and inappropriate responses. As part of this, we grouped ethnicity into the following 11 categories: Caucasian, Chinese, East Asian, Filipino, Jewish, Korean, Middle Eastern, Mixed, Other, South Asian, and Vietnamese.

Demographic questions

For demographic information, we asked participants for their grade (with teacher as an option), favourite subjects, and ethnic background. We asked students for their academic stream, and teachers for their department.

Since the number of teachers surveyed was small, we do not do any analysis on teachers departments, and instead treat them as a separate grade and academic stream. We also do not analyze the data on favourite subjects since it is very noisy.

Food questions

We asked respondents 43 questions related to sandwiches and their ingredients. We use all of this data.

Metrics

4.1 Axes metrics

We have two metrics used in our calculations: purity and orthodoxy.

Purity is how pure a respondent's definition of a sandwich is. The less things a respondent considers a sandwich, the greater their purity score will be. Similarly, the more things a respondent considers a sandwich, the lower their purity score will be.

Orthodoxy is a measure of how much a respondent differs from the mean set of responses. The less a respondent's answers differ from the mean set of answers, the greater their orthodoxy score will be. Similarly, the more a respondent's answers differ from the mean set of answers, the lower their orthodoxy score will be.

Both purity and orthodoxy are bound in the range [-1, 1].

We describe the general scoring system in subsection 4.1.1. This scoring system is used to calculate the purity metric described in subsection 4.1.2 on the next page and the orthodoxy metric described in subsection 4.1.3 on page 10.

4.1.1 Scoring

While participants answered each food question on a 0 to 10 scale, it is more convenient to perform calculations using a -5 to 5 scale. We converted responses from the 0 to 10 scale to the -5 to 5 scale by subtracting each response from 5.

Formally, for each response to a food question, we calculate the score for the response by the passing the response through the sandwich spectrum function, defined in 1 on the next page.

Definition 1 (Sandwich spectrum function). The sandwich spectrum function is defined as:

$$s: \{x \in \mathbb{R} \mid 0 \le x \le 10\} \to \{x \in \mathbb{R} \mid -5 \le x \le 5\} \text{ by } s(x) = 5 - x \quad (4.1)$$

Due to the format of our survey, all responses are integers, and are mapped to another integer by the sandwich spectrum function. Although, in principle, the sandwich spectrum function works for real numbers as well.

We can create a table for s:

One will note that this gives responses that were originally high a lower score. This is intentional. Subsection 4.1.2 will show it to be useful for calculating the purity metric, and subsection 4.1.3 on the next page will show it to be irrelevant for calculating the orthodoxy metric.

4.1.2 Purity

The purity score for a respondent is defined as the sum of a respondent's scores divided by the maximum possible score.

The maximum score for a question is 5, and there are 43 food questions. This means that the maximum possible score is $43 \times 5 = 215$.

Definition 2 (Sadwich purity function). For a given response with a set of 43 food answers, A, we define the sandwich purity function as:

$$p: \mathbb{R}^{43} \to \mathbb{R} \text{ by } p(A) = \frac{\sum_{i=1}^{43} A_i}{215}$$
 (4.2)

This definition illustrates why we subtract each response from 5 to get the score. The sandwich spectrum function will assign higher purity values for lower responses. Since a lower response to a question implies a more pure definition of a sandwich, 1 is a valid metric.

4.1.3 Orthodoxy

To calculate orthodoxy for each respondent, we take the score for each question as a dimension of a vector, which creates a vector in 43-dimensional Euclidean space.

We also calculate the mean response for each question, and create an additional \mathbb{R}^{43} vector from that. This vector is referred to as the mean vector, and denoted as \overrightarrow{m} .

The orthodoxy score for a respondent is defined as the cosine similarity between the respondent's \mathbb{R}^{43} vector and \overrightarrow{m} .

Definition 3 (Mean vector). To calculate the value of the mean vector, \vec{m} :

Let $A \in \mathbb{R}^{43}$ be the set of response vectors. Then, n(A) is the cardinality of the set A.

Then:

$$\vec{m} = \frac{\sum_{i=1}^{n(A)} A_i}{n(A)} \tag{4.3}$$

Definition 4 (Sandwich orthodoxy function). To calculate the orthodoxy score for a respondent:

Let \vec{r} be a vector in \mathbb{R}^{43} defined as having its each of its components equal to the score for each food question.

$$o: \mathbb{R}^{43} \to \mathbb{R} \text{ by } o(\overrightarrow{r}) = \frac{\overrightarrow{r} \cdot \overrightarrow{m}}{\|\overrightarrow{r}\| \|\overrightarrow{m}\|}$$
 (4.4)

Since we are calculating orthodoxy as the cosine of the angle between two vectors, it is useful to have some vector components be negative, as that allows respondents to have a negative orthodoxy score if they answer opposite to the mean response. It does not matter what direction the vectors are in, as we are only looking at the angle between them. This means that the sandwich spectrum function could have been defined as subtracting 5 instead of subtracting from 5 for the purposes of the orthodoxy function. Since both definitions would have worked for orthodoxy, we stick with 1 on the previous page for the sake of consistency with the purity metric.

Part II Results Summary

Results summary

All numbers in this chapter have been rounded to 5 digits after the decimal point.

5.1 Data with outliers

Table 5.1: The results of all respondents with outliers included. Teachers had their stream set to "Teacher".

| # | Purity | Orthodoxy | Grade | Background | Stream |
|----|----------|-----------|----------|----------------|----------|
| 1 | -0.26047 | 0.78743 | Grade 12 | Mixed | Gifted |
| 2 | 0.04186 | 0.90389 | Grade 12 | Filipino | Academic |
| 3 | -0.70233 | 0.41500 | Grade 11 | Chinese | MaCS |
| 4 | -0.66512 | 0.46478 | Grade 11 | Caucasian | MaCS |
| 5 | 0.04651 | 0.87398 | Grade 12 | Chinese | MaCS |
| 6 | 0.12558 | 0.76755 | Grade 12 | East Asian | MaCS |
| 7 | -0.29767 | 0.04865 | Grade 12 | Chinese | MaCS |
| 8 | -0.16279 | 0.89784 | Grade 12 | Jewish | MaCS |
| 9 | -0.17674 | 0.62968 | Grade 12 | Middle Eastern | Academic |
| 10 | -0.50233 | 0.67579 | Grade 12 | Filipino | MaCS |
| 11 | -0.05581 | 0.92452 | Grade 12 | Mixed | MaCS |
| 12 | 0.18605 | 0.83489 | Teacher | Jewish | Teacher |
| 13 | 0.13488 | 0.81080 | Grade 12 | Middle Eastern | Gifted |
| 14 | -0.67442 | 0.39360 | Grade 12 | South Asian | MaCS |
| 15 | 0.11628 | 0.78018 | Grade 12 | Chinese | MaCS |
| 16 | 0.12093 | 0.83977 | Grade 11 | Korean | MaCS |
| 17 | -0.55814 | 0.54878 | Grade 11 | Chinese | MaCS |
| 18 | -0.44186 | 0.60770 | Grade 11 | Chinese | MaCS |
| 19 | 0.13023 | 0.82374 | Grade 12 | East Asian | MaCS |
| 20 | -0.25581 | 0.79897 | Grade 12 | Chinese | MaCS |
| | | | | | |

| 21 | -0.11628 | 0.85328 | Grade 12 | Vietnamese | Academic |
|----|----------|---------|----------|-------------|----------|
| 22 | -0.03256 | 0.90503 | Grade 12 | Jewish | Academic |
| 23 | -0.03256 | 0.81788 | Grade 12 | South Asian | Academic |
| 24 | -0.20000 | 0.72832 | Grade 11 | Vietnamese | Other |
| 25 | 0.15814 | 0.85950 | Grade 12 | Filipino | Academic |
| 26 | -0.09767 | 0.75217 | Grade 12 | Jewish | Gifted |
| 27 | 0.13953 | 0.80860 | Teacher | Other | Teacher |
| 28 | 0.22791 | 0.62137 | Grade 12 | Chinese | MaCS |
| 29 | -0.28837 | 0.84233 | Grade 12 | East Asian | MaCS |
| 30 | -0.20930 | 0.89615 | Grade 12 | Caucasian | MaCS |
| 31 | 0.08372 | 0.80590 | Grade 12 | Jewish | MaCS |
| 32 | -0.42791 | 0.72797 | Grade 12 | Chinese | MaCS |
| 33 | -0.14419 | 0.87928 | Grade 12 | Caucasian | MaCS |
| 34 | 0.09302 | 0.82863 | Grade 12 | Vietnamese | MaCS |
| 35 | -0.58605 | 0.56467 | Grade 11 | Caucasian | MaCS |
| 36 | -0.02791 | 0.79334 | Grade 12 | South Asian | MaCS |
| 37 | 0.00465 | 0.85846 | Teacher | Other | Teacher |
| 38 | -0.16279 | 0.69499 | Grade 12 | Caucasian | MaCS |
| 39 | -0.06047 | 0.91415 | Grade 12 | Caucasian | MaCS |
| 40 | -0.24186 | 0.76056 | Grade 12 | Jewish | MaCS |
| 41 | -0.53023 | 0.54403 | Grade 11 | Other | MaCS |
| 42 | -0.06047 | 0.77035 | Grade 12 | South Asian | Applied |
| 43 | 0.08837 | 0.67952 | Grade 12 | Mixed | Academic |
| 44 | 0.05116 | 0.87279 | Grade 12 | Filipino | Academic |
| 45 | -0.14419 | 0.64695 | Grade 9 | Caucasian | Academic |
| 46 | -0.24186 | 0.64867 | Grade 12 | Caucasian | Academic |
| 47 | -0.13953 | 0.73419 | Grade 9 | East Asian | Academic |
| 48 | 0.27907 | 0.80968 | Grade 12 | Jewish | Academic |
| 49 | -0.04651 | 0.81095 | Grade 12 | Jewish | Academic |
| 50 | -0.30698 | 0.67331 | Grade 12 | East Asian | Academic |
| 51 | 0.21395 | 0.30716 | Grade 12 | Caucasian | Academic |
| 52 | -0.80000 | 0.23213 | Grade 12 | Caucasian | Academic |
| 53 | 0.38605 | 0.46599 | Grade 12 | Vietnamese | Academic |
| 54 | 0.25581 | 0.52316 | Grade 12 | Other | Other |
| 55 | -0.14419 | 0.77929 | Grade 9 | Jewish | Academic |
| 56 | 0.17674 | 0.82393 | Grade 12 | Mixed | Academic |
| 57 | 0.24651 | 0.75861 | Grade 12 | Caucasian | Applied |
| 58 | 0.40465 | 0.56366 | Grade 12 | Mixed | Academic |

| 59 | 0.17674 | 0.13833 | Grade 11 | Other | Academic |
|----|----------|----------|----------|----------------|----------|
| 60 | -0.29767 | 0.78865 | Teacher | Caucasian | Teacher |
| 61 | -0.01395 | 0.59180 | Grade 11 | Other | Applied |
| 62 | -0.04651 | 0.44875 | Grade 12 | Korean | Academic |
| 63 | 0.00465 | 0.79811 | Grade 12 | Filipino | Academic |
| 64 | -0.66512 | -0.13785 | Grade 12 | Korean | Gifted |
| 65 | -0.15349 | 0.52585 | Grade 12 | Filipino | Academic |
| 66 | -0.00930 | 0.86197 | Grade 12 | Caucasian | Academic |
| 67 | -0.07907 | 0.55806 | Grade 12 | South Asian | MaCS |
| 68 | -0.57674 | 0.52544 | Grade 11 | Caucasian | Academic |
| 69 | 0.10698 | 0.49637 | Grade 12 | Jewish | Academic |
| 70 | -0.04186 | 0.84955 | Grade 12 | Caucasian | Gifted |
| 71 | -0.81395 | 0.29688 | Grade 12 | Chinese | MaCS |
| 72 | 0.07907 | 0.77065 | Grade 12 | Caucasian | Gifted |
| 73 | 0.25116 | 0.81689 | Grade 11 | Korean | MaCS |
| 74 | 0.22791 | 0.79962 | Grade 11 | South Asian | MaCS |
| 75 | -0.03721 | 0.83146 | Grade 12 | East Asian | Gifted |
| 76 | 0.12558 | 0.81047 | Grade 11 | Other | Academic |
| 77 | -0.24651 | 0.87283 | Grade 11 | Caucasian | MaCS |
| 78 | -0.41860 | 0.52009 | Grade 11 | Jewish | Gifted |
| 79 | -0.42791 | 0.52045 | Grade 11 | Other | Gifted |
| 80 | -0.37209 | 0.44516 | Grade 11 | Vietnamese | Gifted |
| 81 | -0.01395 | -0.20124 | Grade 11 | Caucasian | Other |
| 82 | 0.33023 | 0.38251 | Grade 9 | Other | Other |
| 83 | 0.16279 | 0.01988 | Grade 9 | Caucasian | Other |
| 84 | 0.26047 | 0.80100 | Grade 9 | Mixed | MaCS |
| 85 | 0.07907 | 0.63674 | Grade 12 | Middle Eastern | Academic |
| 86 | -0.17209 | 0.72197 | Grade 12 | Other | Academic |
| 87 | 0.09767 | 0.66355 | Grade 12 | Chinese | Academic |
| 88 | -0.01860 | 0.83655 | Teacher | Other | Teacher |
| 89 | -0.12558 | 0.83448 | Grade 11 | Caucasian | Applied |
| 90 | 0.08837 | 0.76628 | Grade 10 | Other | Academic |
| 91 | 0.10698 | 0.70924 | Grade 9 | Mixed | Academic |
| 92 | -0.17674 | 0.82363 | Grade 11 | Mixed | MaCS |
| 93 | -0.33488 | 0.66008 | Grade 11 | Chinese | MaCS |
| 94 | -0.51163 | 0.54699 | Grade 11 | Mixed | MaCS |
| 95 | -0.23721 | 0.82223 | Grade 12 | East Asian | Academic |
| 96 | 0.03256 | 0.87361 | Grade 9 | South Asian | MaCS |

| 97 | -0.05581 | 0.82581 | Grade 12 | Caucasian | Academic |
|-----|----------|----------|----------|----------------|----------|
| 98 | 0.39535 | 0.61396 | Grade 10 | Jewish | MaCS |
| 99 | 0.15349 | 0.83300 | Grade 10 | Caucasian | MaCS |
| 100 | 0.33488 | 0.75085 | Grade 11 | Korean | Gifted |
| 101 | 0.04186 | 0.84494 | Grade 11 | South Asian | Gifted |
| 102 | 0.03721 | 0.88977 | Grade 12 | Jewish | MaCS |
| 103 | -0.03721 | -0.03783 | Grade 11 | Filipino | Academic |
| 104 | -0.28372 | 0.82859 | Grade 11 | Mixed | Academic |
| 105 | 0.17674 | 0.85856 | Grade 12 | Other | Academic |
| 106 | 0.15814 | 0.70685 | Grade 12 | Middle Eastern | Academic |
| 107 | 0.04186 | 0.81200 | Grade 12 | Caucasian | Academic |
| 108 | -0.22791 | 0.62510 | Grade 10 | Middle Eastern | MaCS |
| 109 | 0.00930 | 0.89270 | Grade 9 | East Asian | MaCS |
| 110 | 0.23721 | 0.79064 | Grade 9 | Jewish | MaCS |
| 111 | 0.85581 | -0.02167 | Grade 11 | South Asian | Academic |
| 112 | -0.25581 | 0.88868 | Grade 12 | Chinese | MaCS |
| 113 | 0.14419 | 0.33265 | Grade 11 | Other | MaCS |
| 114 | 0.27442 | 0.74374 | Grade 9 | Other | MaCS |
| 115 | -0.33488 | 0.65545 | Other | Other | Other |
| 116 | -0.34419 | 0.80198 | Grade 10 | Jewish | MaCS |
| 117 | 0.13023 | 0.82970 | Grade 11 | Mixed | MaCS |
| 118 | -0.53488 | 0.63103 | Grade 9 | Chinese | Gifted |
| 119 | 0.40000 | 0.62724 | Grade 11 | Middle Eastern | Academic |
| 120 | 0.14884 | 0.22078 | Grade 12 | Caucasian | MaCS |
| 121 | -0.17209 | 0.83039 | Grade 10 | Mixed | MaCS |
| 122 | 0.32093 | 0.77196 | Grade 12 | Filipino | Academic |
| 123 | -0.04186 | 0.81574 | Grade 10 | East Asian | MaCS |
| 124 | 0.20930 | 0.79373 | Grade 12 | Other | MaCS |
| 125 | -0.06047 | 0.40400 | Grade 9 | Other | MaCS |
| 126 | 0.21395 | 0.80349 | Grade 11 | Caucasian | MaCS |
| 127 | -0.01395 | 0.81005 | Grade 12 | Mixed | MaCS |
| 128 | -0.01860 | 0.89398 | Grade 10 | South Asian | MaCS |
| 129 | 0.25581 | 0.45210 | Grade 10 | Korean | MaCS |
| 130 | 0.23256 | 0.31299 | Grade 10 | South Asian | MaCS |
| 131 | 0.19070 | 0.82500 | Grade 11 | Other | Academic |
| 132 | 0.40930 | 0.70170 | Grade 10 | Filipino | Academic |
| 133 | -0.16279 | 0.73321 | Grade 9 | East Asian | Gifted |
| 134 | 0.11163 | 0.72394 | Grade 11 | Caucasian | MaCS |

| 135 | -0.03721 | 0.77001 | Grade 12 | Other | Other |
|-----|----------|---------|----------|-------------|--------|
| 136 | -0.07442 | 0.85982 | Grade 10 | Korean | Gifted |
| 137 | 0.26047 | 0.83633 | Grade 11 | Caucasian | MaCS |
| 138 | 0.44651 | 0.56466 | Grade 11 | South Asian | MaCS |
| 139 | 0.22791 | 0.56602 | Grade 11 | Vietnamese | Gifted |
| 140 | 0.01860 | 0.78616 | Grade 12 | South Asian | MaCS |

5.2 Data without outliers

See chapter 6 on page 22 for an explanation of how we identified and removed outliers. The numbers given for removed outliers match with those in table 5.1 on page 12.

Table 5.2: The results of all respondents with outliers removed. Teachers had their stream set to "Teacher".

| # | Purity | Orthodoxy | Grade | Background | Stream |
|----|----------|-----------|----------|----------------|----------|
| 1 | -0.26047 | 0.78968 | Grade 12 | Mixed | Gifted |
| 2 | 0.04186 | 0.90595 | Grade 12 | Filipino | Academic |
| 3 | -0.70233 | 0.42474 | Grade 11 | Chinese | MaCS |
| 4 | -0.66512 | 0.47101 | Grade 11 | Caucasian | MaCS |
| 5 | 0.04651 | 0.87742 | Grade 12 | Chinese | MaCS |
| 6 | 0.12558 | 0.77250 | Grade 12 | East Asian | MaCS |
| 8 | -0.16279 | 0.90018 | Grade 12 | Jewish | MaCS |
| 9 | -0.17674 | 0.63965 | Grade 12 | Middle Eastern | Academic |
| 10 | -0.50233 | 0.67820 | Grade 12 | Filipino | MaCS |
| 11 | -0.05581 | 0.92256 | Grade 12 | Mixed | MaCS |
| 12 | 0.18605 | 0.84173 | Teacher | Jewish | Teacher |
| 13 | 0.13488 | 0.81892 | Grade 12 | Middle Eastern | Gifted |
| 14 | -0.67442 | 0.40191 | Grade 12 | South Asian | MaCS |
| 15 | 0.11628 | 0.78026 | Grade 12 | Chinese | MaCS |
| 16 | 0.12093 | 0.85531 | Grade 11 | Korean | MaCS |
| 17 | -0.55814 | 0.55359 | Grade 11 | Chinese | MaCS |
| 18 | -0.44186 | 0.61922 | Grade 11 | Chinese | MaCS |
| 19 | 0.13023 | 0.81850 | Grade 12 | East Asian | MaCS |
| 20 | -0.25581 | 0.80421 | Grade 12 | Chinese | MaCS |

| 21 | -0.11628 | 0.84608 | Grade 12 | Vietnamese | Academic |
|----|----------|---------|----------|-------------|----------|
| 22 | -0.03256 | 0.91319 | Grade 12 | Jewish | Academic |
| 23 | -0.03256 | 0.81780 | Grade 12 | South Asian | Academic |
| 24 | -0.20000 | 0.73308 | Grade 11 | Vietnamese | Other |
| 25 | 0.15814 | 0.86354 | Grade 12 | Filipino | Academic |
| 26 | -0.09767 | 0.77076 | Grade 12 | Jewish | Gifted |
| 27 | 0.13953 | 0.82063 | Teacher | Other | Teacher |
| 28 | 0.22791 | 0.60112 | Grade 12 | Chinese | MaCS |
| 29 | -0.28837 | 0.84816 | Grade 12 | East Asian | MaCS |
| 30 | -0.20930 | 0.89411 | Grade 12 | Caucasian | MaCS |
| 31 | 0.08372 | 0.79274 | Grade 12 | Jewish | MaCS |
| 32 | -0.42791 | 0.73105 | Grade 12 | Chinese | MaCS |
| 33 | -0.14419 | 0.88462 | Grade 12 | Caucasian | MaCS |
| 34 | 0.09302 | 0.83049 | Grade 12 | Vietnamese | MaCS |
| 35 | -0.58605 | 0.56729 | Grade 11 | Caucasian | MaCS |
| 36 | -0.02791 | 0.79916 | Grade 12 | South Asian | MaCS |
| 37 | 0.00465 | 0.86234 | Teacher | Other | Teacher |
| 38 | -0.16279 | 0.69419 | Grade 12 | Caucasian | MaCS |
| 39 | -0.06047 | 0.92165 | Grade 12 | Caucasian | MaCS |
| 40 | -0.24186 | 0.75200 | Grade 12 | Jewish | MaCS |
| 41 | -0.53023 | 0.55661 | Grade 11 | Other | MaCS |
| 42 | -0.06047 | 0.77395 | Grade 12 | South Asian | Applied |
| 43 | 0.08837 | 0.67583 | Grade 12 | Mixed | Academic |
| 44 | 0.05116 | 0.88368 | Grade 12 | Filipino | Academic |
| 45 | -0.14419 | 0.66187 | Grade 9 | Caucasian | Academic |
| 46 | -0.24186 | 0.63411 | Grade 12 | Caucasian | Academic |
| 47 | -0.13953 | 0.73373 | Grade 9 | East Asian | Academic |
| 48 | 0.27907 | 0.81327 | Grade 12 | Jewish | Academic |
| 49 | -0.04651 | 0.82498 | Grade 12 | Jewish | Academic |
| 50 | -0.30698 | 0.66416 | Grade 12 | East Asian | Academic |
| 52 | -0.80000 | 0.23584 | Grade 12 | Caucasian | Academic |
| 53 | 0.38605 | 0.45733 | Grade 12 | Vietnamese | Academic |
| 54 | 0.25581 | 0.52042 | Grade 12 | Other | Other |
| 55 | -0.14419 | 0.76742 | Grade 9 | Jewish | Academic |
| 56 | 0.17674 | 0.82218 | Grade 12 | Mixed | Academic |
| 57 | 0.24651 | 0.75231 | Grade 12 | Caucasian | Applied |
| 58 | 0.40465 | 0.55844 | Grade 12 | Mixed | Academic |
| 60 | -0.29767 | 0.78683 | Teacher | Caucasian | Teacher |

| 61 | -0.01395 | 0.57851 | Grade 11 | Other | Applied |
|-----|----------|---------|----------|----------------|----------|
| 63 | 0.00465 | 0.80447 | Grade 12 | Filipino | Academic |
| 65 | -0.15349 | 0.54823 | Grade 12 | Filipino | Academic |
| 66 | -0.00930 | 0.87140 | Grade 12 | Caucasian | Academic |
| 67 | -0.07907 | 0.55018 | Grade 12 | South Asian | MaCS |
| 68 | -0.57674 | 0.53140 | Grade 11 | Caucasian | Academic |
| 70 | -0.04186 | 0.86196 | Grade 12 | Caucasian | Gifted |
| 71 | -0.81395 | 0.30360 | Grade 12 | Chinese | MaCS |
| 72 | 0.07907 | 0.75029 | Grade 12 | Caucasian | Gifted |
| 73 | 0.25116 | 0.82084 | Grade 11 | Korean | MaCS |
| 74 | 0.22791 | 0.79648 | Grade 11 | South Asian | MaCS |
| 75 | -0.03721 | 0.84123 | Grade 12 | East Asian | Gifted |
| 76 | 0.12558 | 0.81990 | Grade 11 | Other | Academic |
| 77 | -0.24651 | 0.87925 | Grade 11 | Caucasian | MaCS |
| 78 | -0.41860 | 0.53666 | Grade 11 | Jewish | Gifted |
| 79 | -0.42791 | 0.53284 | Grade 11 | Other | Gifted |
| 80 | -0.37209 | 0.45348 | Grade 11 | Vietnamese | Gifted |
| 84 | 0.26047 | 0.79445 | Grade 9 | Mixed | MaCS |
| 85 | 0.07907 | 0.64001 | Grade 12 | Middle Eastern | Academic |
| 86 | -0.17209 | 0.70523 | Grade 12 | Other | Academic |
| 87 | 0.09767 | 0.68654 | Grade 12 | Chinese | Academic |
| 88 | -0.01860 | 0.83619 | Teacher | Other | Teacher |
| 89 | -0.12558 | 0.82854 | Grade 11 | Caucasian | Applied |
| 90 | 0.08837 | 0.77318 | Grade 10 | Other | Academic |
| 91 | 0.10698 | 0.70861 | Grade 9 | Mixed | Academic |
| 92 | -0.17674 | 0.82523 | Grade 11 | Mixed | MaCS |
| 93 | -0.33488 | 0.65441 | Grade 11 | Chinese | MaCS |
| 94 | -0.51163 | 0.55424 | Grade 11 | Mixed | MaCS |
| 95 | -0.23721 | 0.82289 | Grade 12 | East Asian | Academic |
| 96 | 0.03256 | 0.87637 | Grade 9 | South Asian | MaCS |
| 97 | -0.05581 | 0.83830 | Grade 12 | Caucasian | Academic |
| 98 | 0.39535 | 0.59620 | Grade 10 | Jewish | MaCS |
| 99 | 0.15349 | 0.83942 | Grade 10 | Caucasian | MaCS |
| 100 | 0.33488 | 0.74844 | Grade 11 | Korean | Gifted |
| 101 | 0.04186 | 0.84523 | Grade 11 | South Asian | Gifted |
| 102 | 0.03721 | 0.88892 | Grade 12 | Jewish | MaCS |
| 104 | -0.28372 | 0.83573 | Grade 11 | Mixed | Academic |
| 105 | 0.17674 | 0.86396 | Grade 12 | Other | Academic |

| 106 | 0.15814 | 0.69246 | Grade 12 | Middle Eastern | Academic |
|-----|----------|----------|----------|----------------|----------|
| 107 | 0.04186 | 0.80980 | Grade 12 | Caucasian | Academic |
| 108 | -0.22791 | 0.62789 | Grade 10 | Middle Eastern | MaCS |
| 109 | 0.00930 | 0.88855 | Grade 9 | East Asian | MaCS |
| 110 | 0.23721 | 0.78608 | Grade 9 | Jewish | MaCS |
| 111 | 0.85581 | -0.03661 | Grade 11 | South Asian | Academic |
| 112 | -0.25581 | 0.88833 | Grade 12 | Chinese | MaCS |
| 114 | 0.27442 | 0.75634 | Grade 9 | Other | MaCS |
| 115 | -0.33488 | 0.66072 | Other | Other | Other |
| 116 | -0.34419 | 0.80379 | Grade 10 | Jewish | MaCS |
| 117 | 0.13023 | 0.83008 | Grade 11 | Mixed | MaCS |
| 118 | -0.53488 | 0.62596 | Grade 9 | Chinese | Gifted |
| 119 | 0.40000 | 0.61374 | Grade 11 | Middle Eastern | Academic |
| 121 | -0.17209 | 0.83336 | Grade 10 | Mixed | MaCS |
| 122 | 0.32093 | 0.77667 | Grade 12 | Filipino | Academic |
| 123 | -0.04186 | 0.80179 | Grade 10 | East Asian | MaCS |
| 124 | 0.20930 | 0.78943 | Grade 12 | Other | MaCS |
| 126 | 0.21395 | 0.80077 | Grade 11 | Caucasian | MaCS |
| 127 | -0.01395 | 0.80887 | Grade 12 | Mixed | MaCS |
| 128 | -0.01860 | 0.90132 | Grade 10 | South Asian | MaCS |
| 129 | 0.25581 | 0.43961 | Grade 10 | Korean | MaCS |
| 131 | 0.19070 | 0.81749 | Grade 11 | Other | Academic |
| 132 | 0.40930 | 0.69923 | Grade 10 | Filipino | Academic |
| 133 | -0.16279 | 0.73236 | Grade 9 | East Asian | Gifted |
| 134 | 0.11163 | 0.72956 | Grade 11 | Caucasian | MaCS |
| 135 | -0.03721 | 0.76334 | Grade 12 | Other | Other |
| 136 | -0.07442 | 0.86029 | Grade 10 | Korean | Gifted |
| 137 | 0.26047 | 0.83846 | Grade 11 | Caucasian | MaCS |
| 138 | 0.44651 | 0.54854 | Grade 11 | South Asian | MaCS |
| 139 | 0.22791 | 0.55018 | Grade 11 | Vietnamese | Gifted |
| 140 | 0.01860 | 0.79616 | Grade 12 | South Asian | MaCS |

5.3 Summary with outliers

Table 5.3: A summary of all respondents with outliers included.

| Purity | Orthodoxy |
|------------------|-----------------|
| Min.:-0.81395 | Min.:-0.20120 |
| 1st Qu.:-0.20233 | 1st Qu.:0.56570 |
| Median: -0.01628 | Median:0.76880 |
| Mean:-0.04259 | Mean: 0.67580 |
| 3rd Qu.:0.15000 | 3rd Qu.:0.82650 |
| Max.:0.85581 | Max.:0.92450 |

5.4 Summary without outliers

Table 5.4: A summary of all respondents with outliers removed.

| Purity | Orthodoxy |
|-----------------------------------|----------------------------------|
| Min.:-0.81395 1st Qu.:-0.22326 | Min.:-0.03661 1st Qu.:0.64361 |
| Median: -0.02326 | Median: 0.78646 |
| Mean:-0.05046 3rd Qu.:0.13372 | Mean:0.73032 3rd Qu.:0.83514 |
| Max.:0.85581 | Max.:0.92256 |

Part III Hypothesis 1

Outliers

We begin our analysis by plotting the purity vs orthodoxy and performing a linear, quadratic, and locally weighted analysis in figure 6.1.

The solid red curve is the result of the locally weighted analysis, and the shaded area is the 99% confidence interval for that analysis. The dashed black line is the result of the linear line of best fit. The dotted blue line is the result of the quadratic curve of best fit.

6.1 With outliers

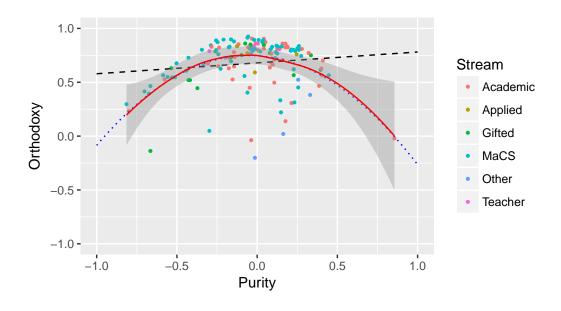


Figure 6.1: A plot of purity vs orthodoxy with data points coloured based on stream.

The linear regression has a positive slope, which proves the first hypothesis that purity and orthodoxy are positively correlated. We will investigate the significance of the correlation in chapter 7 on page 27.

6.1.1 Correlation calculations including outliers

We use the program in section B.8 on page 48 to calculate the numbers in this subsection.

6.1.1.1 Linear model

6.1.1.1.1 Equation of the linear model

 $y \approx 0.1009528x + 0.6800947$

6.1.1.1.2 r values of the linear model

 $r \approx 0.125253454074209$

 $r^2 \approx 0.01568842775752$

6.1.1.2 Quadratic model

6.1.1.2.1 Equation of the quadratic model

$$y \approx -1.3025366x^2 + 0.3363544x + 0.6757950$$

6.1.1.2.2 r^2 value of the quadratic model

 $r^2 \approx 0.25095758979336$

6.2 Identifying outliers

From the this analysis, it is clear that some points are extremely deviate. We next create a residual plot using the quadratic model in figure 6.2.

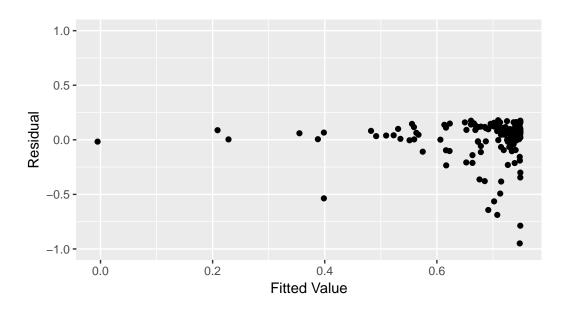


Figure 6.2: A residual plot using the quadratic regression analysis method.

We calculate the interquartile range of the residuals and remove any data that are 1.5 times the ICQ above the third quartile or 1.5 times the ICQ below the first quartile. This is done using the program in section B.8 on page 48. This program then creates a new file for analyzing with the following respondents removed: 7, 51, 59, 62, 64, 69, 81, 82, 83, 103, 113, 120, 125, and 130.

6.3 Outliers removed

We once again plot orthodoxy vs purity by stream in figure 6.3 on the next page, this time with the outliers removed.

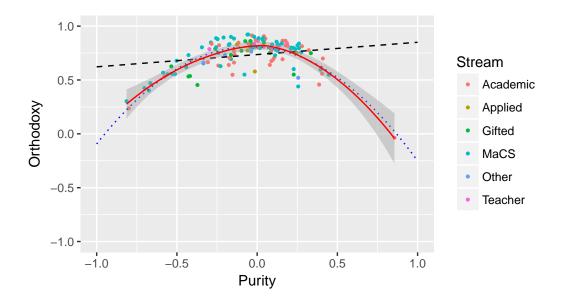


Figure 6.3: A plot of purity vs orthodoxy with data points coloured based on stream. Outliers have been removed.

The solid red curve is the result of the locally weighted analysis, and the shaded area is the 99% confidence interval for that analysis. The dashed black line is the result of the linear line of best fit. The dotted blue line is the result of the quadratic curve of best fit.

6.3.1 Correlation calculations with outliers removed

We use the program in section B.8 on page 48 to calculate the numbers in this subsection.

6.3.1.1 Linear model

6.3.1.1.1 Equation of the linear model

$$y \approx 0.1138999x + 0.7360640$$

6.3.1.1.2 r values of the linear model

 $r \approx 0.209\,580\,523\,324\,373$

 $r^2 \approx 0.043\,923\,995\,756\,918$

6.3.1.2 Quadratic model

6.3.1.2.1 Equation of the quadratic model

$$y \approx -1.3512289x^2 + 0.3633135x + 0.7303165$$

6.3.1.2.2 r^2 value of the quadratic model

 $r^2 \approx 0.651494497892727$

6.4 Effect of outliers on the data

Removing the outliers does not significantly effect the curves due to the high sample size. However, it does greatly increase the accuracy of the model and only a handful of points were removed. This is especially notable in the r^2 value for the quadratic model, which more than doubles.

Unless otherwise specified, the rest of this paper will be excluding outliers from calculations.

Chapter 7 Significance

Part IV Appendices

Appendix A

Questions

A.1 Sandwich Survey

What defines a sandwich?

A.2 Demographic Information

We need to study correlations and demographics.

A.2.1What grade are you in? Respondents were asked to select only one option. O Grade 10 O Grade 11 O Grade 12 O Teacher What is/are your favourite subjects? A.2.2Answer based on what department teaches the subject at Mackenzie. Respondents were asked to check all that apply. □ Business \square Arts □ Computer Science and Technology □ Co-op \Box English □ Languages and Leadership □ Library \square Math □ Physical Education □ Science □ Social Sciences □ Special Education □ Other: _____

A.2.3 What is your ethnic background?

Respondents were asked to provide a free response.

A.3 Student Questions

Questions in this section were asked only of respondents who identified as being in grade 9, 10, 11, or 12. It was not asked of respondents who identified as a teacher.

A.3.1 What is your academic stream?

| Select whatever option you most closely identify with. | | | | | | | | | |
|--------------------------------------------------------|------------|--------|-------------------|--------|--|--|--|--|--|
| Respondents were asked to select only one option. | | | | | | | | | |
| Applied | O Academic | O MaCS | \bigcirc Gifted | Other: | | | | | |
| | | | | | | | | | |

A.4 Teacher Questions

Questions in this section were asked only of respondents who identified as being a teacher. It was not asked of respondents who identified as being in grade 9, 10, 11, or 12.

A.4.1 What departments do you work in at Mackenzie?

| Answer based on what department teaches the subject at Mackenzie. | | |
|-------------------------------------------------------------------|-----------------------|-----------------------------------|
| Respondents were asked to | check all that apply. | |
| □ Arts | □ Business | ☐ Computer Science and Technology |
| □ Co-op and Leadership | □ English | □ Languages |
| □ Library | \square Math | □ Physical Education |
| □ Science | □ Social Sciences | □ Special Education |
| □ Student Services | □ Other: | |

A.5 Sandwich Questions

For each of the following, answer on a scale from 0 to 10, where 0 is not at all a sandwich, and 10 is definitely a sandwich.

A.5.1 Ham between two slices of bread

Respondents were asked to select only one option, with 0 being "Not at all a sandwich" and 10 being "Definitely a sandwich".

Image from [14].

A.5.2 Bacon, lettuce, and tomato between two slices of bread

Respondents were asked to select only one option, with 0 being "Not at all a sandwich" and 10 being "Definitely a sandwich".

Image from [36].

A.5.3 Grilled cheese

Respondents were asked to select only one option, with 0 being "Not at all a sandwich" and 10 being "Definitely a sandwich".

Image from [4].

A.5.4 Panini

Respondents were asked to select only one option, with 0 being "Not at all a sandwich" and 10 being "Definitely a sandwich".

Image from [41].



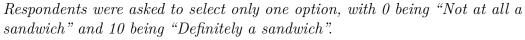


Image cropped from [9].

A.5.6 Hamburger

Respondents were asked to select only one option, with 0 being "Not at all a sandwich" and 10 being "Definitely a sandwich".

Image from [6].

A.5.7 Hotdog

Respondents were asked to select only one option, with 0 being "Not at all a sandwich" and 10 being "Definitely a sandwich".

Image from [38].

A.5.8 Ice cream between two cookies

Respondents were asked to select only one option, with 0 being "Not at all a sandwich" and 10 being "Definitely a sandwich".

Image from [8].

A.5.9 Burrito

Respondents were asked to select only one option, with 0 being "Not at all a sandwich" and 10 being "Definitely a sandwich".

 \bigcirc \bigcirc \bigcirc \bigcirc \bigcirc 0 0 \circ \bigcirc 2 3 0 1 4 5 6 7 9 10

Image from [43].

A.5.10 Taco

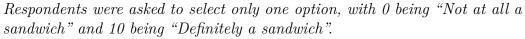


Image from [7].

A.5.11 Calzone

Respondents were asked to select only one option, with 0 being "Not at all a sandwich" and 10 being "Definitely a sandwich".

Image from [22].

A.5.12 Quesadilla

Respondents were asked to select only one option, with 0 being "Not at all a sandwich" and 10 being "Definitely a sandwich".

Image from [18].

A.5.13 Open-faced sandwich

Respondents were asked to select only one option, with 0 being "Not at all a sandwich" and 10 being "Definitely a sandwich".

Image from [34].

A.5.14 Pizza

Respondents were asked to select only one option, with 0 being "Not at all a sandwich" and 10 being "Definitely a sandwich".

 \bigcirc \bigcirc \bigcirc \bigcirc \bigcirc 0 0 \circ \bigcirc 2 3 0 1 4 5 6 7 9 10

Image from [35].

A.5.15 Two slices of pizza, face down, on top of each other

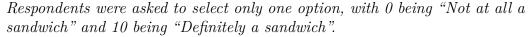


Image from [44].

A.5.16 Slice of bread between two more slices of bread

Respondents were asked to select only one option, with 0 being "Not at all a sandwich" and 10 being "Definitely a sandwich".

Image from [30].

A.5.17 Oreo cookie

Respondents were asked to select only one option, with 0 being "Not at all a sandwich" and 10 being "Definitely a sandwich".

Image from [13].

A.5.18 Ritz cracker

Respondents were asked to select only one option, with 0 being "Not at all a sandwich" and 10 being "Definitely a sandwich".

 $egin{pmatrix} egin{pmatrix} egi$

Image from [24].

A.5.19 Sushi burrito

Respondents were asked to select only one option, with 0 being "Not at all a sandwich" and 10 being "Definitely a sandwich".

 \circ 0 0 0 0 \bigcirc \circ \bigcirc \bigcirc 0 1 2 3 4 5 6 7 8 9 10

Image from [17].

A.5.20 Nigiri sushi

Respondents were asked to select only one option, with 0 being "Not at all a sandwich" and 10 being "Definitely a sandwich".

Image from [46].

A.5.21 Slice of cheese

Respondents were asked to select only one option, with 0 being "Not at all a sandwich" and 10 being "Definitely a sandwich".

Image cropped from [27].

A.5.22 Salad with croutons

Respondents were asked to select only one option, with 0 being "Not at all a sandwich" and 10 being "Definitely a sandwich".

Image from [16].

A.5.23 Brick between two slices of bread

Respondents were asked to select only one option, with 0 being "Not at all a sandwich" and 10 being "Definitely a sandwich".

Image created in GIMP using [47] and [25].

A.6 Ingredient Questions

For each of the following, answer on a scale from 0 to 10, where 0 is not at all a sandwich ingredient, and 10 is definitely a sandwich ingredient.

A.6.1 Cold cuts

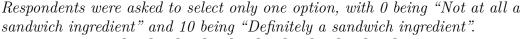


Image from [37].

A.6.2 Tomato

Respondents were asked to select only one option, with 0 being "Not at all a sandwich ingredient" and 10 being "Definitely a sandwich ingredient".

Image from [1].

A.6.3 Cheese

Respondents were asked to select only one option, with 0 being "Not at all a sandwich ingredient" and 10 being "Definitely a sandwich ingredient".

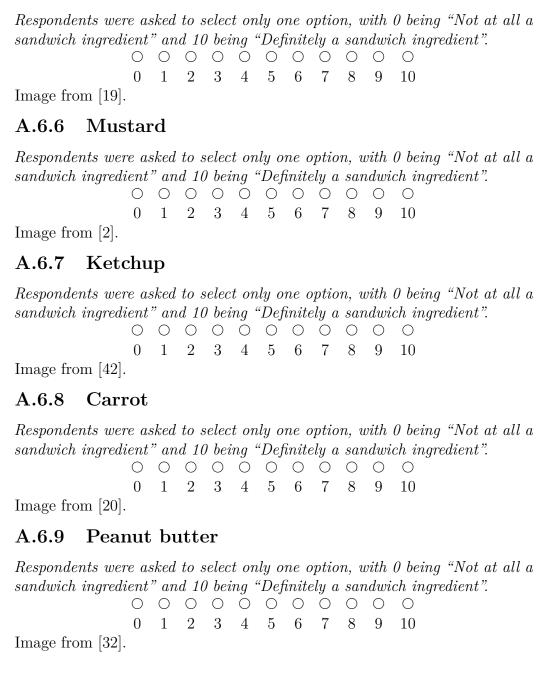
Image cropped from [27].

A.6.4 Lettuce

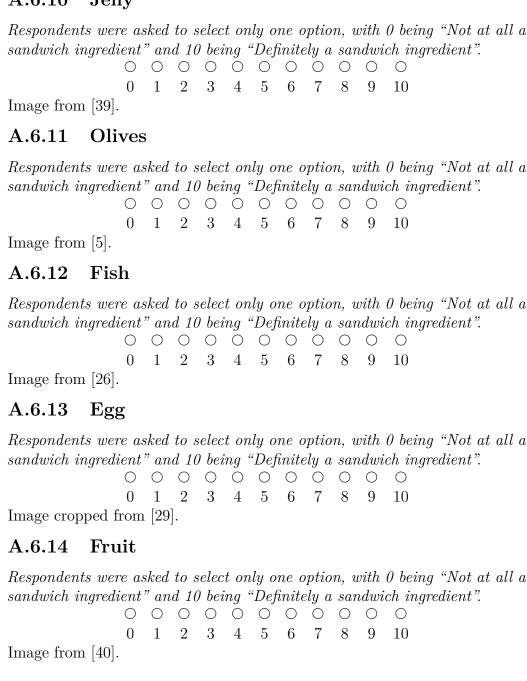
Respondents were asked to select only one option, with 0 being "Not at all a sandwich ingredient" and 10 being "Definitely a sandwich ingredient".

Image from [48].

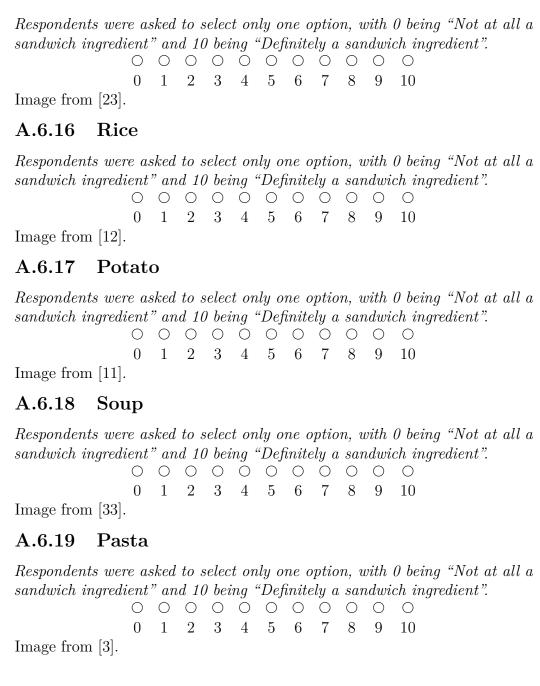
A.6.5 Mayonnaise



A.6.10 Jelly



A.6.15 Chicken foot



A.6.20 Grass

Respondents were asked to select only one option, with 0 being "Not at all a sandwich ingredient" and 10 being "Definitely a sandwich ingredient".

Image from [21].

Appendix B

Source Code

B.1 Functions.R

```
# Calculate the cosine similarity between two vectors.
cosineSimilarity <- function(a, b) {
    return (sum(a * b) / (sqrt(sum(a^2)) * sqrt(sum(b^2))
    ))
4 }</pre>
```

B.2 Calculate.R.

```
# This is a program to calculate the orthodoxy and purity
     scores on the sandwich spectrum for all respondents.
3
  source("Functions.R")
  # Define the constants for what columns data is in inside the
      CSV file.
6| GRADE_COLUMN <- 1 # What column the grade data is in.
  SUBJECTS_COLUMN <- 2 # What column the favourite subjects
      data is in.
8 BACKGROUND_COLUMN <- 3 # What column the ethnic background
     data is in.
9 STREAM_COLUMN <- 4 # What column the stream data is in.
10 QUESTIONS_START <- 6 # What column the food questions start
11 QUESTIONS_END <- 48 # What column the food questions end at.
12 lockBinding("GRADE_COLUMN", globalenv())
13 lockBinding("SUBJECTS_COLUMN", globalenv())
14 lockBinding("BACKGROUND_COLUMN", globalenv())
15 lockBinding("STREAM_COLUMN", globalenv())
16 lockBinding("QUESTIONS_START", globalenv())
17 lockBinding("QUESTIONS_END", globalenv())
18
```

```
19 | #respondents <- read.csv("CleanedData.csv", check.names =
      FALSE) # Read in the CSV with outliers.
20 respondents <- read.csv("NoOutliers.csv", check.names = FALSE
     ) # Read in the CSV without outliers.
21 NUM_RESPONDENTS <- nrow(respondents)
22 lockBinding("NUM_RESPONDENTS", globalenv())
24 foodResponses <- as.matrix(respondents)[,QUESTIONS_START:
     QUESTIONS_END] # Convert responses to a matrix.
25 foodResponses <- apply(foodResponses, 1, as.numeric) # Make
      the matrix numeric.
26 foodResponses <- 5 - foodResponses
27
28| NUM_QUESTIONS <- nrow(foodResponses) # The number of sandwich
       questions.
29 lockBinding("NUM_QUESTIONS", globalenv())
31 totalResponse <- numeric(NUM_QUESTIONS)
32 averageResponse <- numeric(NUM_QUESTIONS)
33
34 \mid # Sum up the total score for each question by respondent.
35 for (i in 1 : NUM_RESPONDENTS) {
36
          totalResponse <- totalResponse + (foodResponses[,i])</pre>
37|}
38 averageResponse <- totalResponse / NUM_RESPONDENTS # Divide
     by the number of respondents to find the mean.
39
40 orthodoxyScores <- numeric(NUM_RESPONDENTS)
  purityScores <- numeric(NUM_RESPONDENTS)</pre>
42
43 for (i in 1 : NUM_RESPONDENTS) {
44
          orthodoxyScores[i] <- cosineSimilarity(foodResponses</pre>
      [,i], averageResponse)
          purityScores[i] <- sum(foodResponses[,i])</pre>
45
46|}
47 purityScores <- purityScores / (5 * NUM_QUESTIONS)
48
49 # Put data into frame.
50 data <- data.frame(purity = purityScores, orthodoxy =
     orthodoxyScores, grade = respondents[,GRADE_COLUMN],
     subjects = respondents[,SUBJECTS_COLUMN], background =
     respondents[,BACKGROUND_COLUMN], stream = respondents[,
     STREAM COLUMN])
```

B.3 BoxPlots.R.

```
1 # This program creates box plots of the respondents.
3
  library(ggplot2)
  source("Calculate.R")
6
  makeBoxPlot <- function(categoryData, categoryName,</pre>
      categoryTitle) {
7
           boxPlotData <- data[categoryData %in% names(table(</pre>
      categoryData))[table(categoryData) > 1],] # Remove all
      categorical data points only occurring once, as these data
       are not helpful for a box plot.
8
9
           # Create the purity plot.
10
           dataPlot <- ggplot(boxPlotData, aes_string(x =</pre>
      categoryName, y = "purity", fill=categoryName)) # Setup
      the plot.
           dataPlot <- dataPlot + coord_cartesian(ylim = c(-1,</pre>
11
      1)) # Set the graph limits.
           dataPlot <- dataPlot + geom boxplot() # Add the data
12
      points.
           dataPlot <- dataPlot + labs(x = categoryTitle, y = "</pre>
13
      Purity") # Give axes proper labels.
           dataPlot <- dataPlot + theme(legend.position = "none"
      ) # Remove the legend.
15
           ggsave(paste(categoryTitle, "Purity.pdf"), plot=
      dataPlot, width=9, height=8)
16
17
           # Create the orthodoxy plot.
18
           dataPlot <- ggplot(boxPlotData, aes_string(x =</pre>
      categoryName, y = "orthodoxy", fill=categoryName)) # Setup
       the plot.
19
           dataPlot <- dataPlot + coord_cartesian(ylim = c(-1,</pre>
      1)) # Set the graph limits.
20
           dataPlot <- dataPlot + geom_boxplot() # Add the data</pre>
      points.
           dataPlot <- dataPlot + labs(x = categoryTitle, y = "</pre>
      Orthodoxy") # Give axes proper labels.
22
           dataPlot <- dataPlot + theme(legend.position = "none"
      ) # Remove the legend.
23
           ggsave(paste(categoryTitle, "Orthodoxy.pdf"), plot=
      dataPlot, width=9, height=8)
24| \}
25
```

```
26 makeBoxPlot(data$grade, "grade", "Grade")
27|\,makeBoxPlot(	exttt{data}$background, "background", "Ethnic Background
28 makeBoxPlot(data$stream, "stream", "Stream")
30 boxPlotData <- data
31
32 # Create the purity plot.
33 dataPlot <- ggplot(boxPlotData, aes(x = 1, y = purity)) #
      Setup the plot.
34 dataPlot <- dataPlot + coord_cartesian(ylim = c(-1, 1)) # Set
       the graph limits.
35|\operatorname{dataPlot} <- \operatorname{dataPlot} + \operatorname{geom\_boxplot}() # Add the data points.
36 dataPlot <- dataPlot + labs(x = "All respondents", y = "
      Purity") # Give axes proper labels.
37 dataPlot <- dataPlot + theme(axis.text.x = element_blank(),</pre>
      axis.ticks.x = element_blank()) # Remove the x axis.
38|ggsave("PurityBoxPlot.pdf", plot=dataPlot, width=2, height=8)
40 # Create the orthodoxy plot.
41 dataPlot <- ggplot(boxPlotData, aes(x = 1, y = orthodoxy)) #
      Setup the plot.
42 dataPlot <- dataPlot + coord_cartesian(ylim = c(-1, 1)) # Set
       the graph limits.
43 dataPlot <- dataPlot + geom_boxplot() # Add the data points.
44 dataPlot <- dataPlot + labs(x = "All respondents", y = "
      Orthodoxy") # Give axes proper labels.
45 dataPlot <- dataPlot + theme(axis.text.x = element_blank(),
      axis.ticks.x = element blank()) # Remove the x axis.
46|ggsave("OrthodoxyBoxPlot.pdf", plot=dataPlot, width=2, height
```

B.4 PurityOrthodoxyPlot.R

```
8
           dataPlot <- ggplot(data, aes(purity, orthodoxy)) #</pre>
      Setup the plot.
9
           dataPlot <- dataPlot + xlim(-1, 1) + ylim(-1, 1) #
      Set the graph limits.
10
           dataPlot <- dataPlot + geom_point(aes_string(colour =</pre>
       categoryName), size = 0.75) # Add the data points.
11
           dataPlot <- dataPlot + geom_smooth(method = lm,</pre>
      formula = y ~ x, fullrange = TRUE, se = FALSE, colour = "
      black", size = 0.5, linetype="dashed") # Add the line of
      best fit.
12
           dataPlot <- dataPlot + geom_smooth(method = lm,</pre>
      formula = y ~ poly(x, 2), fullrange = TRUE, se = FALSE,
      colour = "blue", size = 0.5, linetype="dotted") # Add the
      curve of best fit.
13
           dataPlot <- dataPlot + geom_smooth(method = loess,</pre>
      level = 0.99, colour = "red", size = 0.5) # Add the
      confidence curve.
14
           dataPlot <- dataPlot + labs(x = "Purity", y = "</pre>
      Orthodoxy", colour = categoryTitle) # Give axes and legend
      proper labels.
           \#dataPlot \leftarrow dataPlot + geom_text(x = -0.25, y =
15
      0.75, label = lm_eqn(data), parse = TRUE)
          ggsave(paste(categoryTitle, "PurityVsOrthodoxy.pdf",
16
      sep = ""), plot=dataPlot, width=5.5, height=3)
17 }
18
19 makeScatterPlot("stream", "Stream")
20 makeScatterPlot("grade", "Grade")
21 makeScatterPlot("background", "Ethnic Background")
```

B.5 Residuals.R

```
# This program creates a residual plot of the respondents
    using the quadratic method.

library(ggplot2)
library(broom)

source("Calculate.R")

residualPlotData <- data</pre>
```

B.6 Levels.R.

```
# Output the levels for certain columns of interest in the
     input.
  # Define the constants for what columns data is in inside the
      CSV file.
4| GRADE_COLUMN <- 1 # What column the grade data is in.
5 SUBJECTS_COLUMN <- 2 # What column the favourite subjects
      data is in.
6 BACKGROUND_COLUMN <- 3 # What column the ethnic background
     data is in.
7 STREAM_COLUMN <- 4 # What column the stream data is in.
8 QUESTIONS_START <- 6 # What column the food questions start
     at.
9 QUESTIONS_END <- 48 # What column the food questions end at.
10 lockBinding("GRADE_COLUMN", globalenv())
11 lockBinding("SUBJECTS_COLUMN", globalenv())
12 lockBinding("BACKGROUND_COLUMN", globalenv())
13 lockBinding("STREAM_COLUMN", globalenv())
14 lockBinding("QUESTIONS_START", globalenv())
15 lockBinding("QUESTIONS_END", globalenv())
17 respondents <- read.csv("CleanedData.csv") # Read in the CSV.
19 print (paste (nrow (respondents), "respondents"))
21 summary (respondents [, GRADE_COLUMN])
```

B.7 Tables.R

```
# This program creates a CSV file with the data on each
    respondent's metrics.

source("Calculate.R")

data$purity <- round(data$purity, digits=5)
data$orthodoxy <- round(data$orthodoxy, digits=5)

data <- data[,-4]
write.csv(data, file = "Results.csv")
write.csv(summary(data), file = "Summary.csv")</pre>
```

B.8 Outliers.R

```
# This program removes outliers.

source("Calculate.R")

outlierData <- data

function of the district model.
mod <- lm(orthodoxy ~ poly(purity, 2), data = outlierData)
resid <- unname(mod$residuals)</pre>
```

```
10
11 # Compute the cutoffs.
12 q1 <- unname(quantile(resid)[2])
13 q3 <- unname(quantile(resid)[4])
14 icq = q3 - q1
15 lowCutoff = q1 - 1.5 * icq
16 highCutoff = q3 + 1.5 * icq
17
18 remove <- -which(resid < lowCutoff | resid > highCutoff)
19 removed <- respondents[remove,]
20 print(remove)
21
22 write.csv(removed, file = "NoOutliers.csv", row.names = FALSE
    )
```

B.9 Significance.R

```
# This program creates a residual plot of the respondents
     using the quadratic method.
3
  library(ggplot2)
  source("Calculate.R")
  significanceData <- data
9 # Create the linear model.
10 linearModel <- lm(orthodoxy \tilde{} purity, data = significanceData
11 quadraticModel <- lm(orthodoxy ~ poly(purity, 2), data =
     significanceData)
13 print ("Linear model")
14 print ("
15 print ("Coefficients")
16 coef(linearModel)
17 print ("Correlations")
18 paste("r =", cor(significanceData$purity, y =
     significanceData$orthodoxy))
19 paste("r^2 =", summary(linearModel)$r.squared)
```

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