

What is a sandwich?

A data analysis in  $\mathbb{R}^{43}$

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### **Abstract**

In this paper we set out to examine the sandwich views of students and teachers at William Lyon Mackenzie C.I.

Our study consisted of a survey conducted in person with 140 participants. We asked participants basic demographic information about where they fit into the William Lyon Mackenzie Collegiate Institute community, and examined correlations between sandwich views and demographics.

We propose the creation of a two-dimensional sandwich alignment chart, inspired by two-dimensional political axes. The sandwich alignment chart has a dimension for “sandwich purity”, and “sandwich orthodoxy”.

We hypothesize that:

1. Sandwich purity and sandwich orthodoxy will be positively correlated.
2. Students in the MaCS or Gifted program are more likely to have a low orthodoxy score.

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# Part I

## Introduction

# Chapter 1

## Terminology and notation

As this paper is dealing with sandwich mathematics, which is a developing field, we will define the terms we have coined in this chapter.

**Food question** A food question is any question asked about sandwiches or their ingredients. We asked 43 food questions as a part of this study. Participants answered each question on a 0 to 10 scale. We purposely started the scale at 0 so as to make 5 exactly in the middle of the range of possible responses.

**Demographic question** A demographic question is any of the non-food questions asked in our survey. These questions asked about participants demographics, in order to examine any correlations between demographics and sandwich views.

# Chapter 2

## Methodology

### 2.1 Survey type

We conducted our survey as mix of a stratified, voluntary, and random sample. We surveyed roughly 10% of the William Lyon Mackenzie population.

Unfortunately, we failed to collect a perfectly stratified sample. However, an analysis of the data shows that to be inconsequential.

We made manual corrections to categorical to correct for similar, blank, and inappropriate responses. As part of this, we grouped ethnicity into the following 11 categories: Caucasian, Chinese, East Asian, Filipino, Jewish, Korean, Middle Eastern, Mixed, Other, South Asian, and Vietnamese.



# Chapter 3

## Metrics

### 3.1 Axes metrics

We have two metrics used in our calculations: purity and orthodoxy.

Purity is how pure a respondent's definition of a sandwich is. The less things a respondent considers a sandwich, the greater their purity score will be. Similarly, the more things a respondent considers a sandwich, the lower their purity score will be.

Orthodoxy is a measure of how much a respondent differs from the mean set of responses. The less a respondent's answers differ from the mean set of answers, the greater their orthodoxy score will be. Similarly, the more a respondent's answers differ from the mean set of answers, the lower their orthodoxy score will be.

Both purity and orthodoxy are bound in the range  $[-1, 1]$ .

We describe the general scoring system in subsection 3.1.1 on the following page. This scoring system is used to calculate the purity metric described in subsection 3.1.2 on the next page and the orthodoxy metric described in subsection 3.1.3 on page 6.

### 3.1.1 Scoring

While participants answered each food question on a 0 to 10 scale, it is more convenient to perform calculations using a  $-5$  to  $5$  scale. We converted responses from the 0 to 10 scale to the  $-5$  to  $5$  scale by subtracting each response from 5.

Formally, for each response to a food question, we calculate the score for the response by the passing the response through the sandwich spectrum function, defined in 1.

**Definition 1** (Sandwich spectrum function). The sandwich spectrum function is defined as:

$$s : \{x \in \mathbb{R} \mid 0 \leq x \leq 10\} \rightarrow \{x \in \mathbb{R} \mid -5 \leq x \leq 5\} \text{ by } s(x) = 5 - x \quad (3.1)$$

Due to the format of our survey, all responses are integers, and are mapped to another integer by the sandwich spectrum function. Although, in principle, the sandwich spectrum function works for real numbers as well.

We can create a table for  $s$ :

$x$	0	1	2	3	4	5	6	7	8	9	10
$s(x)$	5	4	3	2	1	0	-1	-2	-3	-4	-5

One will note that this gives responses that were originally high a lower score. This is intentional. Subsection 3.1.2 will show it to be useful for calculating the purity metric, and subsection 3.1.3 on the next page will show it to be irrelevant for calculating the orthodoxy metric.

### 3.1.2 Purity

The purity score for a respondent is defined as the sum of a respondent's scores divided by the maximum possible score.

The maximum score for a question is 5, and there are 43 food questions. This means that the maximum possible score is  $43 \times 5 = 215$ .

**Definition 2** (Sadwich purity function). For a given response with a set of 43 food answers,  $A$ , we define the sandwich purity function as:

$$p : \mathbb{R}^{43} \rightarrow \mathbb{R} \text{ by } p(A) = \frac{\sum_{i=1}^{43} A_i}{215} \quad (3.2)$$

This definition illustrates why we subtract each response from 5 to get the score. The sandwich spectrum function will assign higher purity values for lower responses. Since a lower response to a question implies a more pure definition of a sandwich, 1 on the preceding page is a valid metric.

### 3.1.3 Orthodoxy

To calculate orthodoxy for each respondent, we take the score for each question as a dimension of a vector, which creates a vector in 43-dimensional Euclidean space.

We also calculate the mean response for each question, and create an additional  $\mathbb{R}^{43}$  vector from that. This vector is referred to as the mean vector, and denoted as  $\vec{m}$ .

The orthodoxy score for a respondent is defined as the cosine similarity between the respondent's  $\mathbb{R}^{43}$  vector and  $\vec{m}$ .

**Definition 3** (Mean vector). To calculate the value of the mean vector,  $\vec{m}$ :

Let  $A \in \mathbb{R}^{43}$  be the set of response vectors. Then,  $n(A)$  is the cardinality of the set  $A$ .

Then:

$$\vec{m} = \frac{\sum_{i=1}^{n(A)} A_i}{n(A)} \quad (3.3)$$

**Definition 4** (Sandwich orthodoxy function). To calculate the orthodoxy score for a respondent:

Let  $\vec{r}$  be a vector in  $\mathbb{R}^{43}$  defined as having its each of its components equal to the score for each food question.

$$o : \mathbb{R}^{43} \rightarrow \mathbb{R} \text{ by } o(\vec{r}) = \frac{\vec{r} \cdot \vec{m}}{\|\vec{r}\| \|\vec{m}\|} \quad (3.4)$$

Since we are calculating orthodoxy as the cosine of the angle between two vectors, it is useful to have some vector components be negative, as that allows respondents to have a negative orthodoxy score if they answer opposite to the mean response. It does not matter what direction the vectors are in, as we are only looking at the angle between them. This means that the

sandwich spectrum function could have been defined as subtracting 5 instead of subtracting from 5 for the purposes of the orthodoxy function. Since both definitions would have worked for orthodoxy, we stick with 1 on page 5 for the sake of consistency with the purity metric.

## Part II

### Results Summary

# Chapter 4

## Results summary

### 4.1 Data with outliers

Table 4.1: The results of all respondents with outliers included. Teachers had their stream set to “Teacher”.

#	Purity	Orthodoxy	Grade	Background	Stream
1	-0.26047	0.78743	Grade 12	Mixed	Gifted
2	0.04186	0.90389	Grade 12	Filipino	Academic
3	-0.70233	0.415	Grade 11	Chinese	MaCS
4	-0.66512	0.46478	Grade 11	Caucasian	MaCS
5	0.04651	0.87398	Grade 12	Chinese	MaCS
6	0.12558	0.76755	Grade 12	East Asian	MaCS
7	-0.29767	0.04865	Grade 12	Chinese	MaCS
8	-0.16279	0.89784	Grade 12	Jewish	MaCS
9	-0.17674	0.62968	Grade 12	Middle Eastern	Academic
10	-0.50233	0.67579	Grade 12	Filipino	MaCS
11	-0.05581	0.92452	Grade 12	Mixed	MaCS
12	0.18605	0.83489	Teacher	Jewish	Teacher
13	0.13488	0.8108	Grade 12	Middle Eastern	Gifted
14	-0.67442	0.3936	Grade 12	South Asian	MaCS
15	0.11628	0.78018	Grade 12	Chinese	MaCS
16	0.12093	0.83977	Grade 11	Korean	MaCS
17	-0.55814	0.54878	Grade 11	Chinese	MaCS

18	-0.44186	0.6077	Grade 11	Chinese	MaCS
19	0.13023	0.82374	Grade 12	East Asian	MaCS
20	-0.25581	0.79897	Grade 12	Chinese	MaCS
21	-0.11628	0.85328	Grade 12	Vietnamese	Academic
22	-0.03256	0.90503	Grade 12	Jewish	Academic
23	-0.03256	0.81788	Grade 12	South Asian	Academic
24	-0.2	0.72832	Grade 11	Vietnamese	Other
25	0.15814	0.8595	Grade 12	Filipino	Academic
26	-0.09767	0.75217	Grade 12	Jewish	Gifted
27	0.13953	0.8086	Teacher	Other	Teacher
28	0.22791	0.62137	Grade 12	Chinese	MaCS
29	-0.28837	0.84233	Grade 12	East Asian	MaCS
30	-0.2093	0.89615	Grade 12	Caucasian	MaCS
31	0.08372	0.8059	Grade 12	Jewish	MaCS
32	-0.42791	0.72797	Grade 12	Chinese	MaCS
33	-0.14419	0.87928	Grade 12	Caucasian	MaCS
34	0.09302	0.82863	Grade 12	Vietnamese	MaCS
35	-0.58605	0.56467	Grade 11	Caucasian	MaCS
36	-0.02791	0.79334	Grade 12	South Asian	MaCS
37	0.00465	0.85846	Teacher	Other	Teacher
38	-0.16279	0.69499	Grade 12	Caucasian	MaCS
39	-0.06047	0.91415	Grade 12	Caucasian	MaCS
40	-0.24186	0.76056	Grade 12	Jewish	MaCS
41	-0.53023	0.54403	Grade 11	Other	MaCS
42	-0.06047	0.77035	Grade 12	South Asian	Applied
43	0.08837	0.67952	Grade 12	Mixed	Academic
44	0.05116	0.87279	Grade 12	Filipino	Academic
45	-0.14419	0.64695	Grade 9	Caucasian	Academic
46	-0.24186	0.64867	Grade 12	Caucasian	Academic
47	-0.13953	0.73419	Grade 9	East Asian	Academic
48	0.27907	0.80968	Grade 12	Jewish	Academic
49	-0.04651	0.81095	Grade 12	Jewish	Academic
50	-0.30698	0.67331	Grade 12	East Asian	Academic
51	0.21395	0.30716	Grade 12	Caucasian	Academic
52	-0.8	0.23213	Grade 12	Caucasian	Academic
53	0.38605	0.46599	Grade 12	Vietnamese	Academic
54	0.25581	0.52316	Grade 12	Other	Other
55	-0.14419	0.77929	Grade 9	Jewish	Academic

56	0.17674	0.82393	Grade 12	Mixed	Academic
57	0.24651	0.75861	Grade 12	Caucasian	Applied
58	0.40465	0.56366	Grade 12	Mixed	Academic
59	0.17674	0.13833	Grade 11	Other	Academic
60	-0.29767	0.78865	Teacher	Caucasian	Teacher
61	-0.01395	0.5918	Grade 11	Other	Applied
62	-0.04651	0.44875	Grade 12	Korean	Academic
63	0.00465	0.79811	Grade 12	Filipino	Academic
64	-0.66512	-0.13785	Grade 12	Korean	Gifted
65	-0.15349	0.52585	Grade 12	Filipino	Academic
66	-0.0093	0.86197	Grade 12	Caucasian	Academic
67	-0.07907	0.55806	Grade 12	South Asian	MaCS
68	-0.57674	0.52544	Grade 11	Caucasian	Academic
69	0.10698	0.49637	Grade 12	Jewish	Academic
70	-0.04186	0.84955	Grade 12	Caucasian	Gifted
71	-0.81395	0.29688	Grade 12	Chinese	MaCS
72	0.07907	0.77065	Grade 12	Caucasian	Gifted
73	0.25116	0.81689	Grade 11	Korean	MaCS
74	0.22791	0.79962	Grade 11	South Asian	MaCS
75	-0.03721	0.83146	Grade 12	East Asian	Gifted
76	0.12558	0.81047	Grade 11	Other	Academic
77	-0.24651	0.87283	Grade 11	Caucasian	MaCS
78	-0.4186	0.52009	Grade 11	Jewish	Gifted
79	-0.42791	0.52045	Grade 11	Other	Gifted
80	-0.37209	0.44516	Grade 11	Vietnamese	Gifted
81	-0.01395	-0.20124	Grade 11	Caucasian	Other
82	0.33023	0.38251	Grade 9	Other	Other
83	0.16279	0.01988	Grade 9	Caucasian	Other
84	0.26047	0.801	Grade 9	Mixed	MaCS
85	0.07907	0.63674	Grade 12	Middle Eastern	Academic
86	-0.17209	0.72197	Grade 12	Other	Academic
87	0.09767	0.66355	Grade 12	Chinese	Academic
88	-0.0186	0.83655	Teacher	Other	Teacher
89	-0.12558	0.83448	Grade 11	Caucasian	Applied
90	0.08837	0.76628	Grade 10	Other	Academic
91	0.10698	0.70924	Grade 9	Mixed	Academic
92	-0.17674	0.82363	Grade 11	Mixed	MaCS
93	-0.33488	0.66008	Grade 11	Chinese	MaCS



94	-0.51163	0.54699	Grade 11	Mixed	MaCS
95	-0.23721	0.82223	Grade 12	East Asian	Academic
96	0.03256	0.87361	Grade 9	South Asian	MaCS
97	-0.05581	0.82581	Grade 12	Caucasian	Academic
98	0.39535	0.61396	Grade 10	Jewish	MaCS
99	0.15349	0.833	Grade 10	Caucasian	MaCS
100	0.33488	0.75085	Grade 11	Korean	Gifted
101	0.04186	0.84494	Grade 11	South Asian	Gifted
102	0.03721	0.88977	Grade 12	Jewish	MaCS
103	-0.03721	-0.03783	Grade 11	Filipino	Academic
104	-0.28372	0.82859	Grade 11	Mixed	Academic
105	0.17674	0.85856	Grade 12	Other	Academic
106	0.15814	0.70685	Grade 12	Middle Eastern	Academic
107	0.04186	0.812	Grade 12	Caucasian	Academic
108	-0.22791	0.6251	Grade 10	Middle Eastern	MaCS
109	0.0093	0.8927	Grade 9	East Asian	MaCS
110	0.23721	0.79064	Grade 9	Jewish	MaCS
111	0.85581	-0.02167	Grade 11	South Asian	Academic
112	-0.25581	0.88868	Grade 12	Chinese	MaCS
113	0.14419	0.33265	Grade 11	Other	MaCS
114	0.27442	0.74374	Grade 9	Other	MaCS
115	-0.33488	0.65545	Other	Other	Other
116	-0.34419	0.80198	Grade 10	Jewish	MaCS
117	0.13023	0.8297	Grade 11	Mixed	MaCS
118	-0.53488	0.63103	Grade 9	Chinese	Gifted
119	0.4	0.62724	Grade 11	Middle Eastern	Academic
120	0.14884	0.22078	Grade 12	Caucasian	MaCS
121	-0.17209	0.83039	Grade 10	Mixed	MaCS
122	0.32093	0.77196	Grade 12	Filipino	Academic
123	-0.04186	0.81574	Grade 10	East Asian	MaCS
124	0.2093	0.79373	Grade 12	Other	MaCS
125	-0.06047	0.404	Grade 9	Other	MaCS
126	0.21395	0.80349	Grade 11	Caucasian	MaCS
127	-0.01395	0.81005	Grade 12	Mixed	MaCS
128	-0.0186	0.89398	Grade 10	South Asian	MaCS
129	0.25581	0.4521	Grade 10	Korean	MaCS
130	0.23256	0.31299	Grade 10	South Asian	MaCS
131	0.1907	0.825	Grade 11	Other	Academic

132	0.4093	0.7017	Grade 10	Filipino	Academic
133	-0.16279	0.73321	Grade 9	East Asian	Gifted
134	0.11163	0.72394	Grade 11	Caucasian	MaCS
135	-0.03721	0.77001	Grade 12	Other	Other
136	-0.07442	0.85982	Grade 10	Korean	Gifted
137	0.26047	0.83633	Grade 11	Caucasian	MaCS
138	0.44651	0.56466	Grade 11	South Asian	MaCS
139	0.22791	0.56602	Grade 11	Vietnamese	Gifted
140	0.0186	0.78616	Grade 12	South Asian	MaCS

## 4.2 Data without outliers

See chapter 5 on page 19 for an explanation of how we identified and removed outliers. The numbers given for removed outliers match with those in table 4.1 on page 9.

Table 4.2: The results of all respondents with outliers removed. Teachers had their stream set to “Teacher”.

#	Purity	Orthodoxy	Grade	Background	Stream
1	-0.26047	0.78815	Grade 12	Mixed	Gifted
2	0.04186	0.90326	Grade 12	Filipino	Academic
3	-0.70233	0.42266	Grade 11	Chinese	MaCS
4	-0.66512	0.47168	Grade 11	Caucasian	MaCS
5	0.04651	0.8733	Grade 12	Chinese	MaCS
6	0.12558	0.76728	Grade 12	East Asian	MaCS
7	-0.29767	0.0506	Grade 12	Chinese	MaCS
8	-0.16279	0.89988	Grade 12	Jewish	MaCS
9	-0.17674	0.63362	Grade 12	Middle Eastern	Academic
10	-0.50233	0.68039	Grade 12	Filipino	MaCS
11	-0.05581	0.92441	Grade 12	Mixed	MaCS
12	0.18605	0.83312	Teacher	Jewish	Teacher
13	0.13488	0.81043	Grade 12	Middle Eastern	Gifted
14	-0.67442	0.39959	Grade 12	South Asian	MaCS
15	0.11628	0.77803	Grade 12	Chinese	MaCS
16	0.12093	0.83883	Grade 11	Korean	MaCS
17	-0.55814	0.55405	Grade 11	Chinese	MaCS

18	-0.44186	0.61217	Grade 11	Chinese	MaCS
19	0.13023	0.82177	Grade 12	East Asian	MaCS
20	-0.25581	0.80138	Grade 12	Chinese	MaCS
21	-0.11628	0.85365	Grade 12	Vietnamese	Academic
22	-0.03256	0.90589	Grade 12	Jewish	Academic
23	-0.03256	0.81831	Grade 12	South Asian	Academic
24	-0.2	0.72945	Grade 11	Vietnamese	Other
25	0.15814	0.85655	Grade 12	Filipino	Academic
26	-0.09767	0.75429	Grade 12	Jewish	Gifted
27	0.13953	0.80702	Teacher	Other	Teacher
28	0.22791	0.61649	Grade 12	Chinese	MaCS
29	-0.28837	0.84506	Grade 12	East Asian	MaCS
30	-0.2093	0.89862	Grade 12	Caucasian	MaCS
31	0.08372	0.80452	Grade 12	Jewish	MaCS
32	-0.42791	0.73191	Grade 12	Chinese	MaCS
33	-0.14419	0.87949	Grade 12	Caucasian	MaCS
34	0.09302	0.8266	Grade 12	Vietnamese	MaCS
35	-0.58605	0.56963	Grade 11	Caucasian	MaCS
36	-0.02791	0.79424	Grade 12	South Asian	MaCS
37	0.00465	0.85834	Teacher	Other	Teacher
38	-0.16279	0.69682	Grade 12	Caucasian	MaCS
39	-0.06047	0.91568	Grade 12	Caucasian	MaCS
40	-0.24186	0.76238	Grade 12	Jewish	MaCS
41	-0.53023	0.55032	Grade 11	Other	MaCS
42	-0.06047	0.76982	Grade 12	South Asian	Applied
43	0.08837	0.67731	Grade 12	Mixed	Academic
44	0.05116	0.87281	Grade 12	Filipino	Academic
45	-0.14419	0.6505	Grade 9	Caucasian	Academic
46	-0.24186	0.64962	Grade 12	Caucasian	Academic
47	-0.13953	0.73656	Grade 9	East Asian	Academic
48	0.27907	0.8067	Grade 12	Jewish	Academic
49	-0.04651	0.81201	Grade 12	Jewish	Academic
50	-0.30698	0.6755	Grade 12	East Asian	Academic
51	0.21395	0.3018	Grade 12	Caucasian	Academic
52	-0.8	0.24014	Grade 12	Caucasian	Academic
53	0.38605	0.45965	Grade 12	Vietnamese	Academic
54	0.25581	0.52025	Grade 12	Other	Other
55	-0.14419	0.77982	Grade 9	Jewish	Academic

56	0.17674	0.8213	Grade 12	Mixed	Academic
57	0.24651	0.75488	Grade 12	Caucasian	Applied
58	0.40465	0.55973	Grade 12	Mixed	Academic
59	0.17674	0.13431	Grade 11	Other	Academic
60	-0.29767	0.79173	Teacher	Caucasian	Teacher
61	-0.01395	0.59031	Grade 11	Other	Applied
62	-0.04651	0.44906	Grade 12	Korean	Academic
63	0.00465	0.79806	Grade 12	Filipino	Academic
64	-0.66512	-0.12974	Grade 12	Korean	Gifted
65	-0.15349	0.53067	Grade 12	Filipino	Academic
66	-0.0093	0.86244	Grade 12	Caucasian	Academic
67	-0.07907	0.55812	Grade 12	South Asian	MaCS
68	-0.57674	0.53104	Grade 11	Caucasian	Academic
69	0.10698	0.49374	Grade 12	Jewish	Academic
70	-0.04186	0.85092	Grade 12	Caucasian	Gifted
71	-0.81395	0.30472	Grade 12	Chinese	MaCS
72	0.07907	0.76819	Grade 12	Caucasian	Gifted
73	0.25116	0.81383	Grade 11	Korean	MaCS
74	0.22791	0.79754	Grade 11	South Asian	MaCS
75	-0.03721	0.83171	Grade 12	East Asian	Gifted
76	0.12558	0.80812	Grade 11	Other	Academic
77	-0.24651	0.87637	Grade 11	Caucasian	MaCS
78	-0.4186	0.5233	Grade 11	Jewish	Gifted
79	-0.42791	0.52325	Grade 11	Other	Gifted
80	-0.37209	0.44752	Grade 11	Vietnamese	Gifted
81	0.33023	0.37562	Grade 9	Other	Other
82	0.16279	0.01816	Grade 9	Caucasian	Other
83	0.26047	0.79635	Grade 9	Mixed	MaCS
84	0.07907	0.63522	Grade 12	Middle Eastern	Academic
85	-0.17209	0.72342	Grade 12	Other	Academic
86	0.09767	0.66397	Grade 12	Chinese	Academic
87	-0.0186	0.83643	Teacher	Other	Teacher
88	-0.12558	0.83503	Grade 11	Caucasian	Applied
89	0.08837	0.76433	Grade 10	Other	Academic
90	0.10698	0.7068	Grade 9	Mixed	Academic
91	-0.17674	0.82482	Grade 11	Mixed	MaCS
92	-0.33488	0.66197	Grade 11	Chinese	MaCS
93	-0.51163	0.55082	Grade 11	Mixed	MaCS

94	-0.23721	0.82381	Grade 12	East Asian	Academic
95	0.03256	0.87259	Grade 9	South Asian	MaCS
96	-0.05581	0.82647	Grade 12	Caucasian	Academic
97	0.39535	0.60729	Grade 10	Jewish	MaCS
98	0.15349	0.83218	Grade 10	Caucasian	MaCS
99	0.33488	0.74636	Grade 11	Korean	Gifted
100	0.04186	0.84329	Grade 11	South Asian	Gifted
101	0.03721	0.88879	Grade 12	Jewish	MaCS
102	-0.03721	-0.03835	Grade 11	Filipino	Academic
103	-0.28372	0.83128	Grade 11	Mixed	Academic
104	0.17674	0.85693	Grade 12	Other	Academic
105	0.15814	0.70517	Grade 12	Middle Eastern	Academic
106	0.04186	0.81177	Grade 12	Caucasian	Academic
107	-0.22791	0.62601	Grade 10	Middle Eastern	MaCS
108	0.0093	0.89322	Grade 9	East Asian	MaCS
109	0.23721	0.78687	Grade 9	Jewish	MaCS
110	-0.25581	0.89106	Grade 12	Chinese	MaCS
111	0.14419	0.33119	Grade 11	Other	MaCS
112	0.27442	0.74006	Grade 9	Other	MaCS
113	-0.33488	0.65934	Other	Other	Other
114	-0.34419	0.8054	Grade 10	Jewish	MaCS
115	0.13023	0.8282	Grade 11	Mixed	MaCS
116	-0.53488	0.63568	Grade 9	Chinese	Gifted
117	0.4	0.62004	Grade 11	Middle Eastern	Academic
118	0.14884	0.21818	Grade 12	Caucasian	MaCS
119	-0.17209	0.83282	Grade 10	Mixed	MaCS
120	0.32093	0.76796	Grade 12	Filipino	Academic
121	-0.04186	0.81481	Grade 10	East Asian	MaCS
122	0.2093	0.79192	Grade 12	Other	MaCS
123	-0.06047	0.40232	Grade 9	Other	MaCS
124	0.21395	0.80023	Grade 11	Caucasian	MaCS
125	-0.01395	0.81109	Grade 12	Mixed	MaCS
126	-0.0186	0.89308	Grade 10	South Asian	MaCS
127	0.25581	0.44946	Grade 10	Korean	MaCS
128	0.23256	0.30747	Grade 10	South Asian	MaCS
129	0.1907	0.82166	Grade 11	Other	Academic
130	0.4093	0.69627	Grade 10	Filipino	Academic
131	-0.16279	0.73301	Grade 9	East Asian	Gifted

132	0.11163	0.72323	Grade 11	Caucasian	MaCS
133	-0.03721	0.76895	Grade 12	Other	Other
134	-0.07442	0.86083	Grade 10	Korean	Gifted
135	0.26047	0.83348	Grade 11	Caucasian	MaCS
136	0.44651	0.55779	Grade 11	South Asian	MaCS
137	0.22791	0.56078	Grade 11	Vietnamese	Gifted
138	0.0186	0.78707	Grade 12	South Asian	MaCS

### 4.3 Summary with outliers

Table 4.3: A summary of all respondents with outliers included.

Purity	Orthodoxy
Min. : -0.81395	Min. : -0.2012
1st Qu.: -0.20233	1st Qu.: 0.5657
Median : -0.01628	Median : 0.7688
Mean : -0.04259	Mean : 0.6758
3rd Qu.: 0.15000	3rd Qu.: 0.8265
Max. : 0.85581	Max. : 0.9245

### 4.4 Summary without outliers

Table 4.4: A summary of all respondents with outliers removed.

Purity	Orthodoxy
Min. : -0.81395	Min. : -0.1297
1st Qu.: -0.20697	1st Qu.: 0.5946
Median : -0.01860	Median : 0.7681
Mean : -0.04931	Mean : 0.6872
3rd Qu.: 0.14768	3rd Qu.: 0.8266
Max. : 0.44651	Max. : 0.9244

## Part III

## Analysis

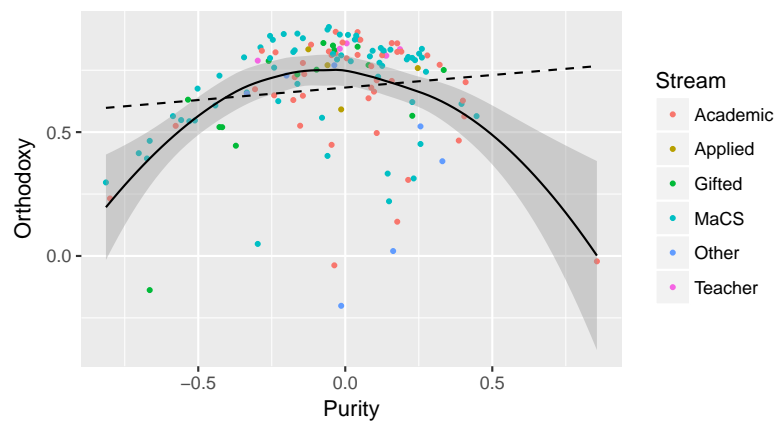
# Chapter 5

## Outliers

We begin our analysis by plotting the purity vs orthodoxy and performing both a linear and locally weighted regression analysis in figure 5.1.

### 5.1 With outliers

Figure 5.1: A plot of purity vs orthodoxy with data points coloured based on stream.



Here, the solid curve is the result of the locally weighted regression analysis, and the shaded area is the 95% confidence interval for that analysis. The dashed line is the result of the linear regression.

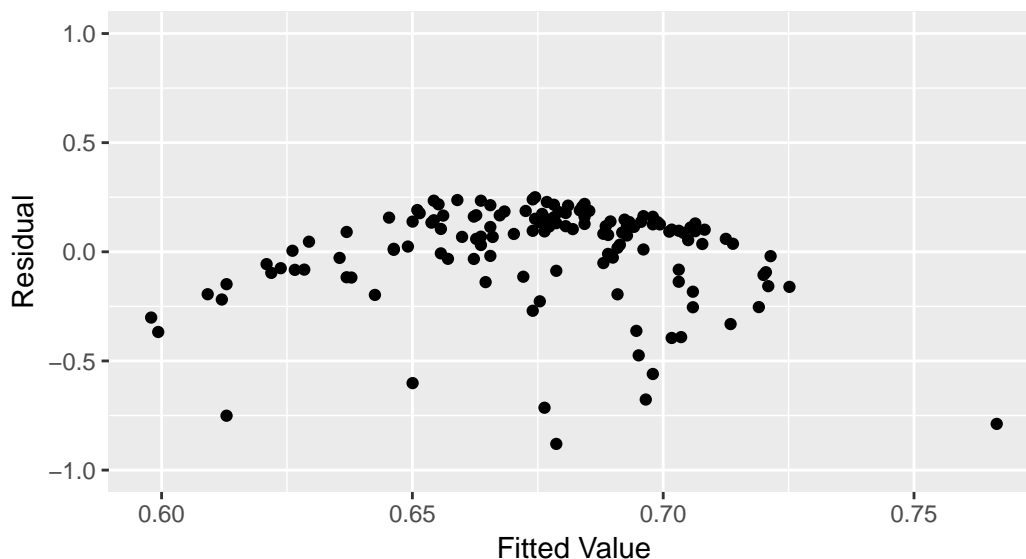


The linear regression has a positive slope, which proves the first hypothesis that purity and orthodoxy are positively correlated.

## 5.2 Identifying outliers

From the locally weighted regression analysis, it is clear that some points are extremely deviate. We next create residual plots using the linear model in figure 5.2.

Figure 5.2: A residual plot using the linear regression analysis method.



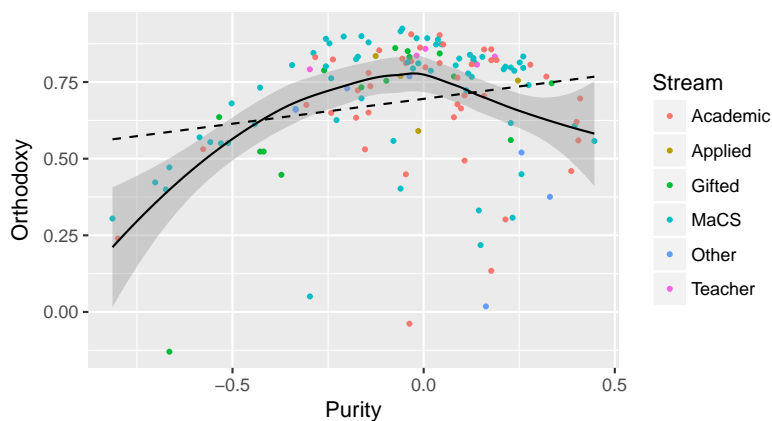
We will eliminate any points with an absolute residual exceeding a certain value.

For the linear analysis, we exclude any points with an absolute residual above 0.76. These are respondents #81, and #111. We will continue the rest of the analysis as if they did not do the survey at all.

## 5.3 Outliers removed

We once again plot orthodoxy vs purity by stream in figure 5.3, this time with the outliers removed.

Figure 5.3: A plot of purity vs orthodoxy with data points coloured based on stream. Outliers have been removed.



Here, the solid curve is the result of the locally weighted regression analysis, and the shaded area is the 95% confidence interval for that analysis. The dashed line is the result of the linear regression.

From this, we can clearly see that the two outliers removed were significantly affecting the correlation, especially for the locally weighted regression analysis.

# Part IV

## Appendices

# Appendix A

## Questions

### A.1 Sandwich Survey

What defines a sandwich?

### A.2 Demographic Information

We need to study correlations and demographics.

#### A.2.1 What grade are you in?

*Respondents were asked to select only one option.*

☐ Grade 9    ☐ Grade 10    ☐ Grade 11    ☐ Grade 12    ☐ Teacher

### A.2.2 What is/are your favourite subjects?

Answer based on what department teaches the subject at Mackenzie.

*Respondents were asked to check all that apply.*

- |  |  |   |
|--|--|---|
| <input type="checkbox"/> Arts                | <input type="checkbox"/> Business        | <input type="checkbox"/> Computer Science<br>and Technology |
| <input type="checkbox"/> Co-op<br>Leadership | <input type="checkbox"/> English         | <input type="checkbox"/> Languages                          |
| <input type="checkbox"/> Library             | <input type="checkbox"/> Math            | <input type="checkbox"/> Physical Education                 |
| <input type="checkbox"/> Science             | <input type="checkbox"/> Social Sciences | <input type="checkbox"/> Special Education                  |
| <input type="checkbox"/> Other: _____        |  |   |

### A.2.3 What is your ethnic background?

*Respondents were asked to provide a free response.*

---

## A.3 Student Questions

*Questions in this section were asked only of respondents who identified as being in grade 9, 10, 11, or 12. It was not asked of respondents who identified as a teacher.*

### A.3.1 What is your academic stream?

Select whatever option you most closely identify with.

*Respondents were asked to select only one option.*

- ☐ Applied    ☐ Academic    ☐ MaCS    ☐ Gifted    ☐ Other: \_\_\_\_\_

## A.4 Teacher Questions

*Questions in this section were asked only of respondents who identified as being a teacher. It was not asked of respondents who identified as being in grade 9, 10, 11, or 12.*

### A.4.1 What departments do you work in at Mackenzie?

Answer based on what department teaches the subject at Mackenzie.

*Respondents were asked to check all that apply.*

- |  |  |   |
|--|--|---|
| <input type="checkbox"/> Arts                | <input type="checkbox"/> Business        | <input type="checkbox"/> Computer Science<br>and Technology |
| <input type="checkbox"/> Co-op<br>Leadership | and <input type="checkbox"/> English     | <input type="checkbox"/> Languages                          |
| <input type="checkbox"/> Library             | <input type="checkbox"/> Math            | <input type="checkbox"/> Physical Education                 |
| <input type="checkbox"/> Science             | <input type="checkbox"/> Social Sciences | <input type="checkbox"/> Special Education                  |
| <input type="checkbox"/> Student Services    | <input type="checkbox"/> Other: _____    |   |

## A.5 Sandwich Questions

For each of the following, answer on a scale from 0 to 10, where 0 is not at all a sandwich, and 10 is definitely a sandwich.

### A.5.1 Ham between two slices of bread

*Respondents were asked to select only one option, with 0 being “Not at all a sandwich” and 10 being “Definitely a sandwich”.*

☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐  
0 1 2 3 4 5 6 7 8 9 10

Image from [13].

### A.5.2 Bacon, lettuce, and tomato between two slices of bread

*Respondents were asked to select only one option, with 0 being “Not at all a sandwich” and 10 being “Definitely a sandwich”.*

☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐  
0 1 2 3 4 5 6 7 8 9 10

Image from [32].

### A.5.3 Grilled cheese

*Respondents were asked to select only one option, with 0 being “Not at all a sandwich” and 10 being “Definitely a sandwich”.*

☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐  
0 1 2 3 4 5 6 7 8 9 10

Image from [4].

### A.5.4 Panini

*Respondents were asked to select only one option, with 0 being “Not at all a sandwich” and 10 being “Definitely a sandwich”.*

☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐  
0 1 2 3 4 5 6 7 8 9 10

Image from [37].

### A.5.5 Sub

*Respondents were asked to select only one option, with 0 being “Not at all a sandwich” and 10 being “Definitely a sandwich”.*



Image cropped from [9].

### A.5.6 Hamburger

*Respondents were asked to select only one option, with 0 being “Not at all a sandwich” and 10 being “Definitely a sandwich”.*



Image from [6].

### A.5.7 Hotdog

*Respondents were asked to select only one option, with 0 being “Not at all a sandwich” and 10 being “Definitely a sandwich”.*



Image from [34].

### A.5.8 Ice cream between two cookies

*Respondents were asked to select only one option, with 0 being “Not at all a sandwich” and 10 being “Definitely a sandwich”.*



Image from [8].

### A.5.9 Burrito

*Respondents were asked to select only one option, with 0 being “Not at all a sandwich” and 10 being “Definitely a sandwich”.*



Image from [39].



### A.5.10 Taco

*Respondents were asked to select only one option, with 0 being “Not at all a sandwich” and 10 being “Definitely a sandwich”.*

☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐  
0 1 2 3 4 5 6 7 8 9 10

Image from [7].

### A.5.11 Calzone

*Respondents were asked to select only one option, with 0 being “Not at all a sandwich” and 10 being “Definitely a sandwich”.*

☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐  
0 1 2 3 4 5 6 7 8 9 10

Image from [20].

### A.5.12 Quesadilla

*Respondents were asked to select only one option, with 0 being “Not at all a sandwich” and 10 being “Definitely a sandwich”.*

☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐  
0 1 2 3 4 5 6 7 8 9 10

Image from [16].

### A.5.13 Open-faced sandwich

*Respondents were asked to select only one option, with 0 being “Not at all a sandwich” and 10 being “Definitely a sandwich”.*

☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐  
0 1 2 3 4 5 6 7 8 9 10

Image from [30].

### A.5.14 Pizza

*Respondents were asked to select only one option, with 0 being “Not at all a sandwich” and 10 being “Definitely a sandwich”.*

☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐  
0 1 2 3 4 5 6 7 8 9 10

Image from [31].

### A.5.15 Two slices of pizza, face down, on top of each other

*Respondents were asked to select only one option, with 0 being “Not at all a sandwich” and 10 being “Definitely a sandwich”.*



Image from [40].

### A.5.16 Slice of bread between two more slices of bread

*Respondents were asked to select only one option, with 0 being “Not at all a sandwich” and 10 being “Definitely a sandwich”.*



Image from [27].

### A.5.17 Oreo cookie

*Respondents were asked to select only one option, with 0 being “Not at all a sandwich” and 10 being “Definitely a sandwich”.*



Image from [12].

### A.5.18 Ritz cracker

*Respondents were asked to select only one option, with 0 being “Not at all a sandwich” and 10 being “Definitely a sandwich”.*



Image from [22].

### A.5.19 Sushi burrito

*Respondents were asked to select only one option, with 0 being “Not at all a sandwich” and 10 being “Definitely a sandwich”.*



Image from [15].

### A.5.20 Nigiri sushi

*Respondents were asked to select only one option, with 0 being “Not at all a sandwich” and 10 being “Definitely a sandwich”.*



Image from [41].

### A.5.21 Slice of cheese

*Respondents were asked to select only one option, with 0 being “Not at all a sandwich” and 10 being “Definitely a sandwich”.*



Image cropped from [25].

### A.5.22 Salad with croutons

*Respondents were asked to select only one option, with 0 being “Not at all a sandwich” and 10 being “Definitely a sandwich”.*



Image from [14].

### A.5.23 Brick between two slices of bread

*Respondents were asked to select only one option, with 0 being “Not at all a sandwich” and 10 being “Definitely a sandwich”.*



Image created in GIMP using [42] and [23].

## A.6 Ingredient Questions

For each of the following, answer on a scale from 0 to 10, where 0 is not at all a sandwich ingredient, and 10 is definitely a sandwich ingredient.

### A.6.1 Cold cuts

*Respondents were asked to select only one option, with 0 being “Not at all a sandwich ingredient” and 10 being “Definitely a sandwich ingredient”.*

☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐  
0 1 2 3 4 5 6 7 8 9 10

Image from [33].

### A.6.2 Tomato

*Respondents were asked to select only one option, with 0 being “Not at all a sandwich ingredient” and 10 being “Definitely a sandwich ingredient”.*

☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐  
0 1 2 3 4 5 6 7 8 9 10

Image from [1].

### A.6.3 Cheese

*Respondents were asked to select only one option, with 0 being “Not at all a sandwich ingredient” and 10 being “Definitely a sandwich ingredient”.*

☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐  
0 1 2 3 4 5 6 7 8 9 10

Image cropped from [25].

### A.6.4 Lettuce

*Respondents were asked to select only one option, with 0 being “Not at all a sandwich ingredient” and 10 being “Definitely a sandwich ingredient”.*

☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐  
0 1 2 3 4 5 6 7 8 9 10

Image from [43].

### A.6.5 Mayonnaise

*Respondents were asked to select only one option, with 0 being “Not at all a sandwich ingredient” and 10 being “Definitely a sandwich ingredient”.*

☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐  
0 1 2 3 4 5 6 7 8 9 10

Image from [17].

### A.6.6 Mustard

*Respondents were asked to select only one option, with 0 being “Not at all a sandwich ingredient” and 10 being “Definitely a sandwich ingredient”.*

☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐  
0 1 2 3 4 5 6 7 8 9 10

Image from [2].

### A.6.7 Ketchup

*Respondents were asked to select only one option, with 0 being “Not at all a sandwich ingredient” and 10 being “Definitely a sandwich ingredient”.*

☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐  
0 1 2 3 4 5 6 7 8 9 10

Image from [38].

### A.6.8 Carrot

*Respondents were asked to select only one option, with 0 being “Not at all a sandwich ingredient” and 10 being “Definitely a sandwich ingredient”.*

☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐  
0 1 2 3 4 5 6 7 8 9 10

Image from [18].

### A.6.9 Peanut butter

*Respondents were asked to select only one option, with 0 being “Not at all a sandwich ingredient” and 10 being “Definitely a sandwich ingredient”.*

☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐  
0 1 2 3 4 5 6 7 8 9 10

Image from [28].

### A.6.10 Jelly

*Respondents were asked to select only one option, with 0 being “Not at all a sandwich ingredient” and 10 being “Definitely a sandwich ingredient”.*

☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐  
0 1 2 3 4 5 6 7 8 9 10

Image from [35].

### A.6.11 Olives

*Respondents were asked to select only one option, with 0 being “Not at all a sandwich ingredient” and 10 being “Definitely a sandwich ingredient”.*

☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐  
0 1 2 3 4 5 6 7 8 9 10

Image from [5].

### A.6.12 Fish

*Respondents were asked to select only one option, with 0 being “Not at all a sandwich ingredient” and 10 being “Definitely a sandwich ingredient”.*

☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐  
0 1 2 3 4 5 6 7 8 9 10

Image from [24].

### A.6.13 Egg

*Respondents were asked to select only one option, with 0 being “Not at all a sandwich ingredient” and 10 being “Definitely a sandwich ingredient”.*

☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐  
0 1 2 3 4 5 6 7 8 9 10

Image cropped from [26].

### A.6.14 Fruit

*Respondents were asked to select only one option, with 0 being “Not at all a sandwich ingredient” and 10 being “Definitely a sandwich ingredient”.*

☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐  
0 1 2 3 4 5 6 7 8 9 10

Image from [36].

### A.6.15 Chicken foot

*Respondents were asked to select only one option, with 0 being “Not at all a sandwich ingredient” and 10 being “Definitely a sandwich ingredient”.*

☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐  
0 1 2 3 4 5 6 7 8 9 10

Image from [21].

### A.6.16 Rice

*Respondents were asked to select only one option, with 0 being “Not at all a sandwich ingredient” and 10 being “Definitely a sandwich ingredient”.*

☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐  
0 1 2 3 4 5 6 7 8 9 10

Image from [11].

### A.6.17 Potato

*Respondents were asked to select only one option, with 0 being “Not at all a sandwich ingredient” and 10 being “Definitely a sandwich ingredient”.*

☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐  
0 1 2 3 4 5 6 7 8 9 10

Image from [10].

### A.6.18 Soup

*Respondents were asked to select only one option, with 0 being “Not at all a sandwich ingredient” and 10 being “Definitely a sandwich ingredient”.*

☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐  
0 1 2 3 4 5 6 7 8 9 10

Image from [29].

### A.6.19 Pasta

*Respondents were asked to select only one option, with 0 being “Not at all a sandwich ingredient” and 10 being “Definitely a sandwich ingredient”.*

☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐ ☐  
0 1 2 3 4 5 6 7 8 9 10

Image from [3].

### A.6.20 Grass

*Respondents were asked to select only one option, with 0 being “Not at all a sandwich ingredient” and 10 being “Definitely a sandwich ingredient”.*



Image from [19].



# Appendix B

## Source Code

### B.1 Functions.R

```
1 # Calculate the cosine similarity between two vectors.
2 cosineSimilarity <- function(a, b) {
3     return (sum(a * b) / (sqrt(sum(a^2)) * sqrt(sum(b^2)))
4     )
5 }
```

### B.2 Calculate.R

```
1 # This is a program to calculate the orthodoxy and purity
2   scores on the sandwich spectrum for all respondents.
3
4 source("Functions.R")
5
6 # Define the constants for what columns data is in inside the
7   CSV file.
8 GRADE_COLUMN <- 1 # What column the grade data is in.
9 SUBJECTS_COLUMN <- 2 # What column the favourite subjects
10   data is in.
11 BACKGROUND_COLUMN <- 3 # What column the ethnic background
12   data is in.
13 STREAM_COLUMN <- 4 # What column the stream data is in.
```

```

10 QUESTIONS_START <- 6 # What column the food questions start
    at.
11 QUESTIONS_END <- 48 # What column the food questions end at.
12 lockBinding("GRADE_COLUMN", globalenv())
13 lockBinding("SUBJECTS_COLUMN", globalenv())
14 lockBinding("BACKGROUND_COLUMN", globalenv())
15 lockBinding("STREAM_COLUMN", globalenv())
16 lockBinding("QUESTIONS_START", globalenv())
17 lockBinding("QUESTIONS_END", globalenv())
18
19 respondents <- read.csv("NoOutliers.csv") # Read in the CSV.
20 NUM_RESPONDENTS <- nrow(respondents)
21 lockBinding("NUM_RESPONDENTS", globalenv())
22
23 foodResponses <- as.matrix(respondents)[,QUESTIONS_START:
    QUESTIONS_END] # Convert responses to a matrix.
24 foodResponses <- apply(foodResponses, 1, as.numeric) # Make
    the matrix numeric.
25 foodResponses <- 5 - foodResponses
26
27 NUM_QUESTIONS <- nrow(foodResponses) # The number of sandwich
    questions.
28 lockBinding("NUM_QUESTIONS", globalenv())
29
30 totalResponse <- numeric(NUM_QUESTIONS)
31 averageResponse <- numeric(NUM_QUESTIONS)
32
33 # Sum up the total score for each question by respondent.
34 for (i in 1 : NUM_RESPONDENTS) {
35     totalResponse <- totalResponse + (foodResponses[,i])
36 }
37 averageResponse <- totalResponse / NUM_RESPONDENTS # Divide
    by the number of respondents to find the mean.
38
39 orthodoxyScores <- numeric(NUM_RESPONDENTS)
40 purityScores <- numeric(NUM_RESPONDENTS)
41
42 for (i in 1 : NUM_RESPONDENTS) {
43     orthodoxyScores[i] <- cosineSimilarity(foodResponses
        [,i], averageResponse)
44     purityScores[i] <- sum(foodResponses[,i])
45 }
46 purityScores <- purityScores / (5 * NUM_QUESTIONS)
47
48 # Put data into frame.

```

```

49 data <- data.frame(purity = purityScores, orthodoxy =
    orthodoxyScores, grade = respondents[,GRADE_COLUMN],
    subjects = respondents[,SUBJECTS_COLUMN], background =
    respondents[,BACKGROUND_COLUMN], stream = respondents[,
    STREAM_COLUMN])

```

## B.3 BoxPlots.R

```

1  # This program creates box plots of the respondents.
2
3  library(ggplot2)
4  source("Calculate.R")
5
6  makeBoxPlot <- function(categoryData, categoryName,
    categoryTitle) {
7      boxPlotData <- data[categoryData %in% names(table(
        categoryData))[table(categoryData) > 1],] # Remove all
        categorical data points only occurring once, as these data
        are not helpful for a box plot.
8
9      # Create the purity plot.
10     dataPlot <- ggplot(boxPlotData, aes_string(x =
        categoryName, y = "purity", fill=categoryName)) # Setup
        the plot.
11     dataPlot <- dataPlot + coord_cartesian(ylim = c(-1,
        1)) # Set the graph limits.
12     dataPlot <- dataPlot + geom_boxplot() # Add the data
        points.
13     dataPlot <- dataPlot + labs(x = categoryTitle, y = "
        Purity") # Give axes proper labels.
14     dataPlot <- dataPlot + theme(legend.position = "none"
        ) # Remove the legend.
15     ggsave(paste(categoryTitle, "Purity.pdf"), plot=
        dataPlot, width=9, height=8)
16
17     # Create the orthodoxy plot.
18     dataPlot <- ggplot(boxPlotData, aes_string(x =
        categoryName, y = "orthodoxy", fill=categoryName)) # Setup
        the plot.
19     dataPlot <- dataPlot + coord_cartesian(ylim = c(-1,
        1)) # Set the graph limits.

```

```

20     dataPlot <- dataPlot + geom_boxplot() # Add the data
      points.
21     dataPlot <- dataPlot + labs(x = categoryTitle, y = "
      Orthodoxy") # Give axes proper labels.
22     dataPlot <- dataPlot + theme(legend.position = "none"
      ) # Remove the legend.
23     ggsave(paste(categoryTitle, "Orthodoxy.pdf"), plot=
      dataPlot, width=9, height=8)
24 }
25
26 makeBoxPlot(data$grade, "grade", "Grade")
27 makeBoxPlot(data$background, "background", "Ethnic Background
      ")
28 makeBoxPlot(data$stream, "stream", "Stream")
29
30 boxPlotData <- data
31
32 # Create the purity plot.
33 dataPlot <- ggplot(boxPlotData, aes(x = 1, y = purity)) #
      Setup the plot.
34 dataPlot <- dataPlot + coord_cartesian(ylim = c(-1, 1)) # Set
      the graph limits.
35 dataPlot <- dataPlot + geom_boxplot() # Add the data points.
36 dataPlot <- dataPlot + labs(x = "All respondents", y = "
      Purity") # Give axes proper labels.
37 dataPlot <- dataPlot + theme(axis.text.x = element_blank(),
      axis.ticks.x = element_blank()) # Remove the x axis.
38 ggsave("PurityBoxPlot.pdf", plot=dataPlot, width=2, height=8)
39
40 # Create the orthodoxy plot.
41 dataPlot <- ggplot(boxPlotData, aes(x = 1, y = orthodoxy)) #
      Setup the plot.
42 dataPlot <- dataPlot + coord_cartesian(ylim = c(-1, 1)) # Set
      the graph limits.
43 dataPlot <- dataPlot + geom_boxplot() # Add the data points.
44 dataPlot <- dataPlot + labs(x = "All respondents", y = "
      Orthodoxy") # Give axes proper labels.
45 dataPlot <- dataPlot + theme(axis.text.x = element_blank(),
      axis.ticks.x = element_blank()) # Remove the x axis.
46 ggsave("OrthodoxyBoxPlot.pdf", plot=dataPlot, width=2, height
      =8)

```

## B.4 PurityOrthodoxyPlot.R

```
1 # This is a program to plot orthodoxy vs purity on the
   sandwich spectrum for all respondents.
2
3 library(ggplot2)
4 source("Calculate.R")
5
6 makeScatterPlot <- function(categoryName, categoryTitle) {
7     # Create the plot.
8     dataPlot <- ggplot(data, aes(purity, orthodoxy)) #
   Setup the plot.
9     #dataPlot <- dataPlot + coord_cartesian(xlim = c(-1,
   1), ylim = c(-1, 1)) # Set the graph limits.
10    dataPlot <- dataPlot + geom_point(aes_string(colour =
   categoryName), size = 0.75) # Add the data points.
11    dataPlot <- dataPlot + geom_smooth(method = loess,
   level = 0.95, colour = "black", size = 0.5) # Add the
   confidence curve.
12    dataPlot <- dataPlot + geom_smooth(method = lm, se =
   FALSE, colour = "black", size = 0.5, linetype="dashed") #
   Add the line of best fit.
13    dataPlot <- dataPlot + labs(x = "Purity", y = "
   Orthodoxy", colour = categoryTitle) # Give axes and legend
   proper labels.
14    ggsave(paste(categoryTitle, "PurityVsOrthodoxy.pdf",
   sep = ""), plot=dataPlot, width=5.5, height=3)
15 }
16
17 makeScatterPlot("stream", "Stream")
18 makeScatterPlot("grade", "Grade")
19 makeScatterPlot("background", "Ethnic Background")
```

## B.5 Residuals.R

```
1 # This program creates a residual plot of the respondents.
2
3 library(ggplot2)
4 library(broom)
5
6 source("Calculate.R")
7
```

```

8 residualPlotData <- data
9
10 # Create the linear model.
11 mod <- lm(orthodoxy ~ purity, data = residualPlotData)
12 df <- augment(mod)
13 #print(df[which(df$.resid < -0.76),])
14 which(df$.resid < -0.76)
15
16 # Create the residual plot.
17 dataPlot <- ggplot(df, aes(.fitted, .resid)) + geom_point()
18 dataPlot <- dataPlot + coord_cartesian(ylim = c(-1, 1)) # Set
    the graph limits.
19 dataPlot <- dataPlot + labs(x = "Fitted Value", y = "Residual
    ") # Give axes proper labels.
20 ggsave("LinearResidualPlot.pdf", plot=dataPlot, width=5.5,
    height=3)
21
22 # Create the loess model.
23 mod <- loess(orthodoxy ~ purity, data = residualPlotData)
24 df <- augment(mod)
25 #print(df[which(df$.resid < -0.8),])
26 which(df$.resid < -0.80)
27
28 # Create the residual plot.
29 dataPlot <- ggplot(df, aes(.fitted, .resid)) + geom_point()
30 dataPlot <- dataPlot + coord_cartesian(ylim = c(-1, 1)) # Set
    the graph limits.
31 dataPlot <- dataPlot + labs(x = "Fitted Value", y = "Residual
    ") # Give axes proper labels.
32 ggsave("LoessResidualPlot.pdf", plot=dataPlot, width=5.5,
    height=3)

```

## B.6 Levels.R

```

1 # Output the levels for certain columns of interest in the
    input.
2
3 # Define the constants for what columns data is in inside the
    CSV file.
4 GRADE_COLUMN <- 1 # What column the grade data is in.
5 SUBJECTS_COLUMN <- 2 # What column the favourite subjects
    data is in.

```

```

6 BACKGROUND_COLUMN <- 3 # What column the ethnic background
  data is in.
7 STREAM_COLUMN <- 4 # What column the stream data is in.
8 QUESTIONS_START <- 6 # What column the food questions start
  at.
9 QUESTIONS_END <- 48 # What column the food questions end at.
10 lockBinding("GRADE_COLUMN", globalenv())
11 lockBinding("SUBJECTS_COLUMN", globalenv())
12 lockBinding("BACKGROUND_COLUMN", globalenv())
13 lockBinding("STREAM_COLUMN", globalenv())
14 lockBinding("QUESTIONS_START", globalenv())
15 lockBinding("QUESTIONS_END", globalenv())
16
17 respondents <- read.csv("CleanedData.csv") # Read in the CSV.
18
19 print(paste(nrow(respondents), "respondents"))
20
21 summary(respondents[,GRADE_COLUMN])
22 print(paste(length(levels(respondents[,GRADE_COLUMN])), "
  grades"))
23
24 #summary(respondents[,SUBJECTS_COLUMN])
25 #print(paste(length(levels(respondents[,SUBJECTS_COLUMN])), "
  subjects."))
26
27 summary(respondents[,BACKGROUND_COLUMN])
28 print(paste(length(levels(respondents[,BACKGROUND_COLUMN])),
  "ethnic backgrounds"))
29
30 summary(respondents[,STREAM_COLUMN])
31 print(paste(length(levels(respondents[,STREAM_COLUMN])), "
  streams"))

```

## B.7 Tables.R

```

1 # This program creates a CSV file with the data on each
  respondent's metrics.
2
3 source("Calculate.R")
4
5 data$purity <- round(data$purity, digits=5)
6 data$orthodoxy <- round(data$orthodoxy, digits=5)

```

```
7 data <- data[,-4]
8 write.csv(data, file = "Results.csv")
9 write.csv(summary(data), file = "Summary.csv")
```



# Bibliography

- [1] Adityamadhav83. *Sliced Round Tomato at Madhurawada, Visakhapatnam*. Oct. 10, 2012. URL: [https://commons.wikimedia.org/wiki/File:Sliced\\_Round\\_Tomato\\_at\\_Madhurawada.JPG](https://commons.wikimedia.org/wiki/File:Sliced_Round_Tomato_at_Madhurawada.JPG) (visited on 2018-05-21).
- [2] Aeæ commonswiki. *A squeeze bottle of French's Classic Yellow Mustard*. May 21, 2006. URL: [https://commons.wikimedia.org/wiki/File:French%27s\\_classic\\_yellow\\_mustard.jpg](https://commons.wikimedia.org/wiki/File:French%27s_classic_yellow_mustard.jpg) (visited on 2018-05-21).
- [3] Tim Bartel. *Spaghetti*. Dec. 20, 2004. URL: <https://commons.wikimedia.org/wiki/File:Spaghetti.jpg> (visited on 2018-05-21).
- [4] Mack Male from Edmonton Canada AB. *Grilled Cheese Olympics*. Mar. 14, 2010. URL: [https://commons.wikimedia.org/wiki/File:Simple\\_grilled\\_cheese.jpg](https://commons.wikimedia.org/wiki/File:Simple_grilled_cheese.jpg) (visited on 2018-05-19).
- [5] Renee Comet. *green olives*. 1994. URL: [https://commons.wikimedia.org/wiki/File:NCI\\_2\\_green\\_olives.jpg](https://commons.wikimedia.org/wiki/File:NCI_2_green_olives.jpg) (visited on 2018-05-21).
- [6] Renee Comet. *Hamburger*. 1994. URL: [https://commons.wikimedia.org/wiki/File:Cheeseburger\\_\(2\).jpg](https://commons.wikimedia.org/wiki/File:Cheeseburger_(2).jpg) (visited on 2018-05-19).
- [7] Renee Comet. *Hard-shell taco with meat, cheese, lettuce, tomatoes, and onions*. 1994. URL: [https://commons.wikimedia.org/wiki/File:NCI\\_Visuals\\_Food\\_Taco.jpg](https://commons.wikimedia.org/wiki/File:NCI_Visuals_Food_Taco.jpg) (visited on 2018-05-19).

- [8] Renee Comet. *Ice Cream Sandwich*. 1994. URL: [https://commons.wikimedia.org/wiki/File:Ice\\_cream\\_sandwich\\_\(1\).jpg](https://commons.wikimedia.org/wiki/File:Ice_cream_sandwich_(1).jpg) (visited on 2018-05-19).
- [9] Crisco 1492. *A Subway pizza sub in Hong Kong (near the Grand Kowloon)*. Aug. 10, 2013. URL: [https://commons.wikimedia.org/wiki/File:Subway\\_Pizza\\_Sub,\\_Hong\\_Kong.JPG](https://commons.wikimedia.org/wiki/File:Subway_Pizza_Sub,_Hong_Kong.JPG) (visited on 2018-05-19).
- [10] Doudoulolita. *3 potatoes*. Mar. 21, 2012. URL: [https://commons.wikimedia.org/wiki/File:Pommes\\_de\\_terre.png](https://commons.wikimedia.org/wiki/File:Pommes_de_terre.png) (visited on 2018-05-21).
- [11] Earth100. *The four, main, common forms of consumed rice*. Nov. 16, 2012. URL: [https://commons.wikimedia.org/wiki/File:White,\\_Brown,\\_Red\\_%26\\_Wild\\_rice.jpg](https://commons.wikimedia.org/wiki/File:White,_Brown,_Red_%26_Wild_rice.jpg) (visited on 2018-05-21).
- [12] Evan-Amos. *Two Double Stuf Oreos, by Nabisco. Bought in a New York supermarket*. Mar. 31, 2017. URL: <https://commons.wikimedia.org/wiki/File:Nabisco-Double-Stuf-Oreos.jpg> (visited on 2018-05-20).
- [13] Fancy steve. *A plain ham sandwich*. Nov. 11, 2011. URL: [https://commons.wikimedia.org/wiki/File:Ham\\_sandwich.jpg](https://commons.wikimedia.org/wiki/File:Ham_sandwich.jpg) (visited on 2018-05-19).
- [14] jeffreyw. *Romaine lettuce salad*. Jan. 28, 2011. URL: [https://commons.wikimedia.org/wiki/File:Romaine\\_lettuce\\_salad.jpg](https://commons.wikimedia.org/wiki/File:Romaine_lettuce_salad.jpg) (visited on 2018-05-19).
- [15] jen. *sushirrito*. July 9, 2013. URL: [https://commons.wikimedia.org/wiki/File:Sushirrito\\_\(9310623804\).jpg](https://commons.wikimedia.org/wiki/File:Sushirrito_(9310623804).jpg) (visited on 2018-05-21).
- [16] Jennifer. *Lamb quesadillas made with leftover grilled lamb, cheddar cheese, red onion, and peppers from the garden*. Feb. 7, 2005. URL: [https://commons.wikimedia.org/wiki/File:Lamb\\_quesadilla.jpg](https://commons.wikimedia.org/wiki/File:Lamb_quesadilla.jpg) (visited on 2018-05-20).

- [17] Joey 424. *mayonaise on da hot afternoon [sic]*. June 1, 1933. URL: <https://commons.wikimedia.org/wiki/File:Jorgedamayo.jpg> (visited on 2018-05-21).
- [18] Kander. *Carrots on display at local greengrocer*. Oct. 27, 2007. URL: <https://commons.wikimedia.org/wiki/File:Carrots.JPG> (visited on 2018-05-21).
- [19] Ubaid kareem. *Beauty of grass*. Oct. 28, 2013. URL: [https://commons.wikimedia.org/wiki/File:Beauty\\_of\\_grass.jpg](https://commons.wikimedia.org/wiki/File:Beauty_of_grass.jpg) (visited on 2018-05-21).
- [20] Kobako. *Calzone*. Aug. 7, 2013. URL: <https://commons.wikimedia.org/wiki/File:Calzone04.jpg> (visited on 2018-05-20).
- [21] Krista. *A chicken foot*. Dec. 24, 2007. URL: [https://commons.wikimedia.org/wiki/File:A\\_chicken\\_foot.jpg](https://commons.wikimedia.org/wiki/File:A_chicken_foot.jpg) (visited on 2018-05-21).
- [22] Lance. *Lance Gluten Free Sandwich Crackers*. URL: [https://images-na.ssl-images-amazon.com/images/I/71bduHPOL9L.\\_SL1500\\_.jpg](https://images-na.ssl-images-amazon.com/images/I/71bduHPOL9L._SL1500_.jpg) (visited on 2018-05-21).
- [23] Lowes. *Bennett is brick*. Apr. 16, 2017. URL: [https://commons.wikimedia.org/wiki/File:Brick\\_Bennett.jpg](https://commons.wikimedia.org/wiki/File:Brick_Bennett.jpg) (visited on 2018-05-19).
- [24] Tiia Monto. *Cod fillet baked in oven*. Mar. 7, 2018. URL: [https://commons.wikimedia.org/wiki/File:Baked\\_cod\\_fillet.jpg](https://commons.wikimedia.org/wiki/File:Baked_cod_fillet.jpg) (visited on 2018-05-21).
- [25] Tiia Monto. *Emmental cheese slices*. Mar. 26, 2016. URL: [https://commons.wikimedia.org/wiki/File:Emmental\\_slices.jpg](https://commons.wikimedia.org/wiki/File:Emmental_slices.jpg) (visited on 2018-05-21).
- [26] Porsche997SBS. *A picture of an egg being fried*. Nov. 10, 2006. URL: [https://commons.wikimedia.org/wiki/File:Fried\\_egg,\\_sunny\\_side\\_up\\_\(black\\_background\).PNG](https://commons.wikimedia.org/wiki/File:Fried_egg,_sunny_side_up_(black_background).PNG) (visited on 2018-05-21).

- [27] Qwantz. *This is an image of a toast sandwich, shot from the side. Sandwich was made and photographed by me, Ryan. It was okay.* Mar. 26, 2014. URL: [https://commons.wikimedia.org/wiki/File:An\\_image\\_of\\_a\\_toast\\_sandwich,\\_shot\\_from\\_the\\_side.jpg](https://commons.wikimedia.org/wiki/File:An_image_of_a_toast_sandwich,_shot_from_the_side.jpg) (visited on 2018-05-20).
- [28] Susan Slater. *peanut butter.* Aug. 4, 2015. URL: [https://commons.wikimedia.org/wiki/File:96\\_-\\_IMG\\_20150804\\_111725.jpg](https://commons.wikimedia.org/wiki/File:96_-_IMG_20150804_111725.jpg) (visited on 2018-05-21).
- [29] Stu Spivack. *Creamed corn soup.* June 14, 2006. URL: [https://commons.wikimedia.org/wiki/File:Creamed\\_corn.jpg](https://commons.wikimedia.org/wiki/File:Creamed_corn.jpg) (visited on 2018-05-21).
- [30] stef yau stef. *tuna, guacamole sauce and cherry tomatoes.* Aug. 5, 2007. URL: [https://commons.wikimedia.org/wiki/File:Open\\_faced\\_tuna\\_sandwich\\_with\\_cherry\\_tomato\\_and\\_guacamole\\_spread.jpg](https://commons.wikimedia.org/wiki/File:Open_faced_tuna_sandwich_with_cherry_tomato_and_guacamole_spread.jpg) (visited on 2018-05-20).
- [31] Becky Stern. *Pizza at State of the Fruit meeting.* June 19, 2015. URL: [https://commons.wikimedia.org/wiki/File:Pizza\\_at\\_State\\_of\\_the\\_Fruit\\_meeting\\_\(18611225834\).jpg](https://commons.wikimedia.org/wiki/File:Pizza_at_State_of_the_Fruit_meeting_(18611225834).jpg) (visited on 2018-05-20).
- [32] Groves Steven. *A bacon, lettuce and tomato sandwich on toasted bread.* Feb. 14, 2011. URL: [https://commons.wikimedia.org/wiki/File:BLT\\_sandwich\\_on\\_toast.jpg](https://commons.wikimedia.org/wiki/File:BLT_sandwich_on_toast.jpg) (visited on 2018-05-19).
- [33] Stilfehler. *Pastrami.* May 8, 2009. URL: <https://commons.wikimedia.org/wiki/File:Pastrami.jpg> (visited on 2018-05-21).
- [34] Evan Swigart. *Hot Dog.* Sept. 8, 2010. URL: [https://commons.wikimedia.org/wiki/File:Hotdog\\_-\\_Evan\\_Swigart.jpg](https://commons.wikimedia.org/wiki/File:Hotdog_-_Evan_Swigart.jpg) (visited on 2018-05-19).
- [35] terri-bateman. *blackberry jelly.* July 21, 2014. URL: [https://commons.wikimedia.org/wiki/File:Blackberry\\_jelly\\_\(20248988916\).jpg](https://commons.wikimedia.org/wiki/File:Blackberry_jelly_(20248988916).jpg) (visited on 2018-05-21).

- [36] Tomwsulcer. *Fruit platter*. Mar. 30, 2013. URL: [https://commons.wikimedia.org/wiki/File:Fruit\\_platter\\_at\\_a\\_party\\_with\\_kiwi\\_melons\\_strawberries\\_etc.JPG](https://commons.wikimedia.org/wiki/File:Fruit_platter_at_a_party_with_kiwi_melons_strawberries_etc.JPG) (visited on 2018-05-21).
- [37] Tomwsulcer. *Panini sandwich at a restaurant*. Feb. 27, 2013. URL: [https://commons.wikimedia.org/wiki/File:Panini\\_sandwich\\_in\\_a\\_restaurant.JPG](https://commons.wikimedia.org/wiki/File:Panini_sandwich_in_a_restaurant.JPG) (visited on 2018-05-19).
- [38] Tt341. *Heinz Organic Ketchup*. Oct. 2, 2016. URL: [https://commons.wikimedia.org/wiki/File:Heinz\\_USDA\\_Organic\\_Tomato\\_Ketchup.jpg](https://commons.wikimedia.org/wiki/File:Heinz_USDA_Organic_Tomato_Ketchup.jpg) (visited on 2018-05-21).
- [39] Elliot Volkman. *A basic burrito*. June 24, 2009. URL: [https://commons.wikimedia.org/wiki/File:Basic\\_burrito.jpg](https://commons.wikimedia.org/wiki/File:Basic_burrito.jpg) (visited on 2018-05-19).
- [40] Gabby Wang. *Pizza sandwich*. URL: <https://s3.amazonaws.com/spoonuniversi-wpengine/spoonuniversi/wp-content/uploads/sites/71/2015/02/pizza-sandwich-1.jpg> (visited on 2018-05-20).
- [41] www.bluewaikiki.com. *Salmon Nigiri Sushi with chopsticks, 2008*. Sept. 5, 2008. URL: [https://commons.wikimedia.org/wiki/File:Salmon\\_Nigiri\\_Sushi\\_with\\_chopsticks,\\_2008.jpg](https://commons.wikimedia.org/wiki/File:Salmon_Nigiri_Sushi_with_chopsticks,_2008.jpg) (visited on 2018-05-21).
- [42] yamada taro. *Slices Of Bread Free Stock Photo - Public Domain Pictures*. URL: <https://www.publicdomainpictures.net/en/view-image.php?image=26198&picture=slices-of-bread> (visited on 2018-05-19).
- [43] Rainer Zenz. *Romaine lettuce*. 2006. URL: <https://commons.wikimedia.org/wiki/File:Romaine.jpg> (visited on 2018-05-21).