

# CPU Performance

## About

### Title

Relative CPU Performance Data, described in terms of its cycle time, memory size, etc.

### Data Source

- Feldmesser, Jacob. (1987). Computer Hardware. UCI Machine Learning Repository.
- <https://archive-beta.ics.uci.edu/dataset/29/computer+hardware>

### Relevant Information

The estimated relative performance values were estimated by the authors using a linear regression method.

## Dataset

### Load CPU Performance dataset

Data Dictionary

Column	Description
vendor name	30 different vendor
Model Name	many unique symbols
MYCT	machine cycle time in nanoseconds (integer)
MMIN	minimum main memory in kilobytes (integer)
MMAX	maximum main memory in kilobytes (integer)
CACH	cache memory in kilobytes (integer)

Column	Description
CHMIN	minimum channels in units (integer)
CHMAX	maximum channels in units (integer)
PRP	published relative performance (integer)
ERP	estimated relative performance from the original article (integer)

Class Distribution: the class value (PRP) is continuously valued.

PRP Value Range	Number of Instances in Range
0-20	31
21-100	121
101-200	27
201-300	13
301-400	7
401-500	4
501-600	2
above 600	4

	Vendor	Model	MYCT	MMIN	MMAX	CACH	CHMIN	CHMAX	PRP	ERP
1	adviser	32/60	125	256	6000	256	16	128	198	199
2	amdahl	470v/7	29	8000	32000	32	8	32	269	253
3	amdahl	470v/7a	29	8000	32000	32	8	32	220	253
4	amdahl	470v/7b	29	8000	32000	32	8	32	172	253
5	amdahl	470v/7c	29	8000	16000	32	8	16	132	132
6	amdahl	470v/b	26	8000	32000	64	8	32	318	290

### Summary Statistics

Vendor	Model	MYCT	MMIN
Length:209	Length:209	Min. : 17.0	Min. : 64
Class :character	Class :character	1st Qu.: 50.0	1st Qu.: 768
Mode :character	Mode :character	Median : 110.0	Median : 2000
		Mean : 203.8	Mean : 2868
		3rd Qu.: 225.0	3rd Qu.: 4000
		Max. :1500.0	Max. :32000
MMAX	CACH	CHMIN	CHMAX
Min. : 64	Min. : 0.00	Min. : 0.000	Min. : 0.00
1st Qu.: 4000	1st Qu.: 0.00	1st Qu.: 1.000	1st Qu.: 5.00

Median : 8000	Median : 8.00	Median : 2.000	Median : 8.00
Mean :11796	Mean : 25.21	Mean : 4.699	Mean : 18.27
3rd Qu.:16000	3rd Qu.: 32.00	3rd Qu.: 6.000	3rd Qu.: 24.00
Max. :64000	Max. :256.00	Max. :52.000	Max. :176.00
PRP	ERP		
Min. : 6.0	Min. : 15.00		
1st Qu.: 27.0	1st Qu.: 28.00		
Median : 50.0	Median : 45.00		
Mean : 105.6	Mean : 99.33		
3rd Qu.: 113.0	3rd Qu.: 101.00		
Max. :1150.0	Max. :1238.00		

### Glimpse of Data

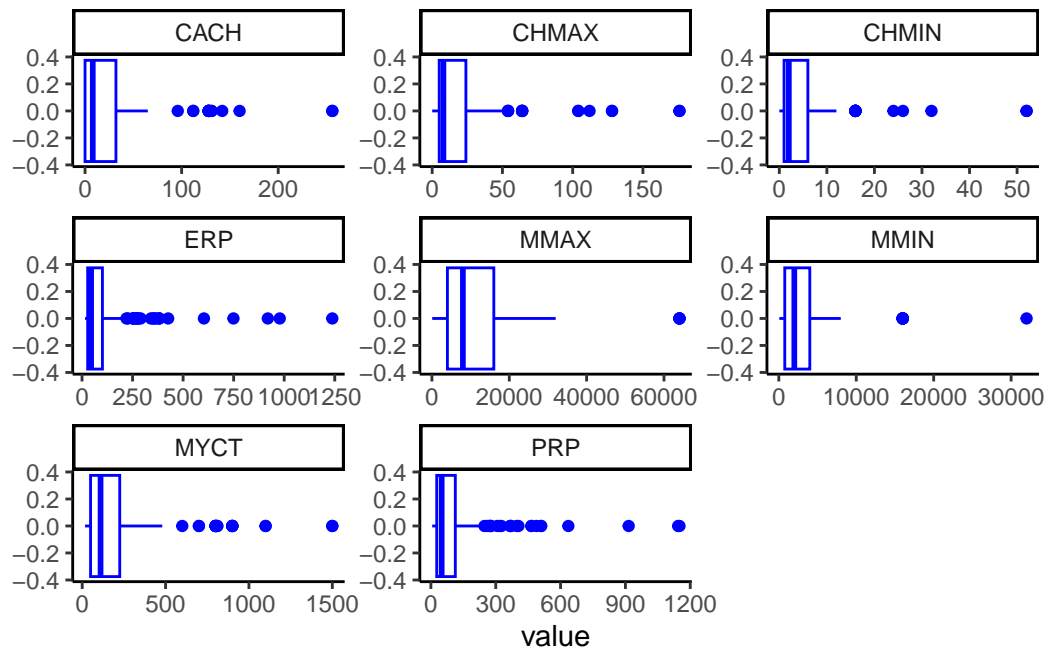
Rows: 209

Columns: 10

```
$ Vendor <chr> "adviser", "amdahl", "amdahl", "amdahl", "amdahl", "amdahl", "a~
$ Model <chr> "32/60", "470v/7", "470v/7a", "470v/7b", "470v/7c", "470v/b", "~
$ MYCT <int> 125, 29, 29, 29, 29, 26, 23, 23, 23, 23, 400, 400, 60, 50, 350,~
$ MMIN <int> 256, 8000, 8000, 8000, 8000, 8000, 16000, 16000, 16000, 32000, ~
$ MMAX <int> 6000, 32000, 32000, 32000, 16000, 32000, 32000, 32000, 64000, 6~
$ CACH <int> 256, 32, 32, 32, 32, 64, 64, 64, 64, 128, 0, 4, 65, 65, 0, 0, 8~
$ CHMIN <int> 16, 8, 8, 8, 8, 8, 16, 16, 16, 32, 1, 1, 1, 1, 1, 4, 4, 7, 5, 8~
$ CHMAX <int> 128, 32, 32, 32, 16, 32, 32, 32, 32, 64, 2, 6, 8, 8, 4, 32, 15,~
$ PRP <int> 198, 269, 220, 172, 132, 318, 367, 489, 636, 1144, 38, 40, 92, ~
$ ERP <int> 199, 253, 253, 253, 132, 290, 381, 381, 749, 1238, 23, 24, 70, ~
```

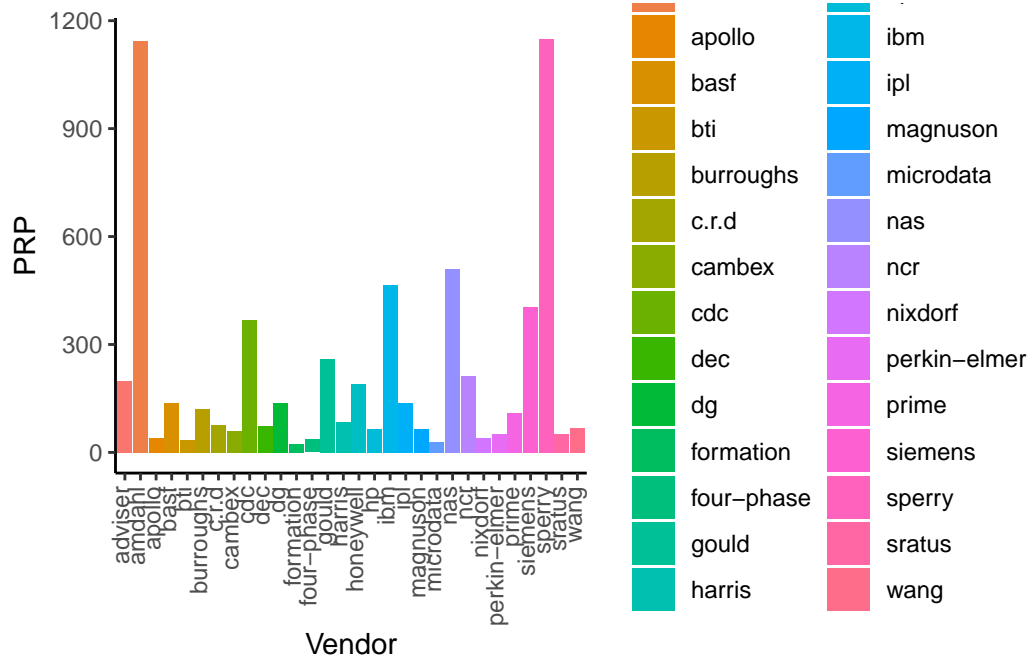
## Visual Analysis

### Histograms



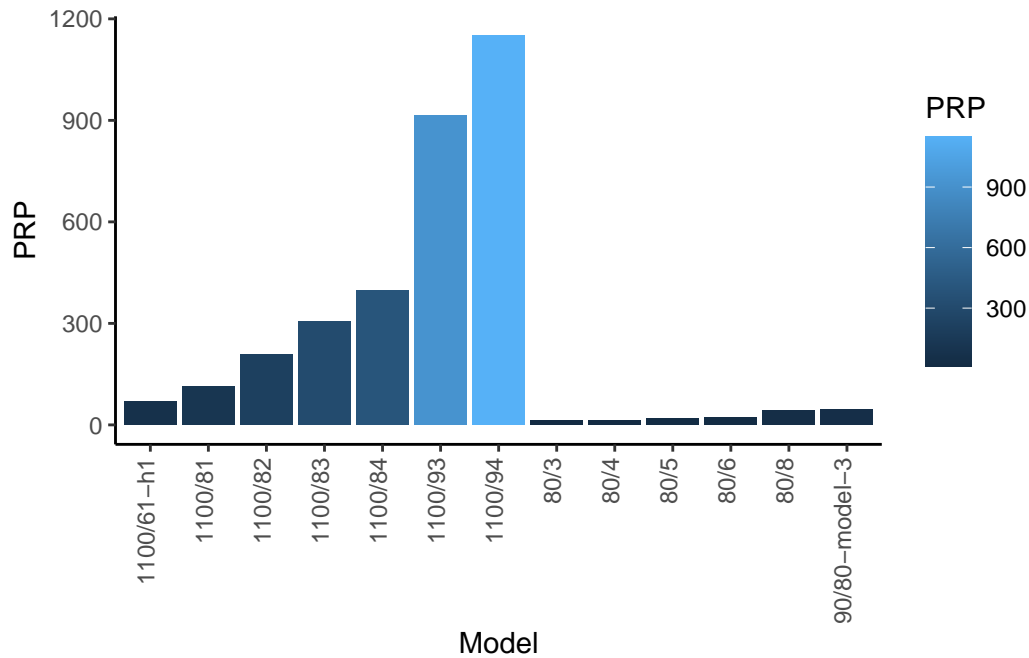
All of the features have some outliers.

## Performance per Vendor



Amdahl and Sperry have the highest performance

## Performance per Model of Sperry



The better performing Sperry is model #1100/94

## Correlations

### Drop Vendor, Model, and ERP from dataset

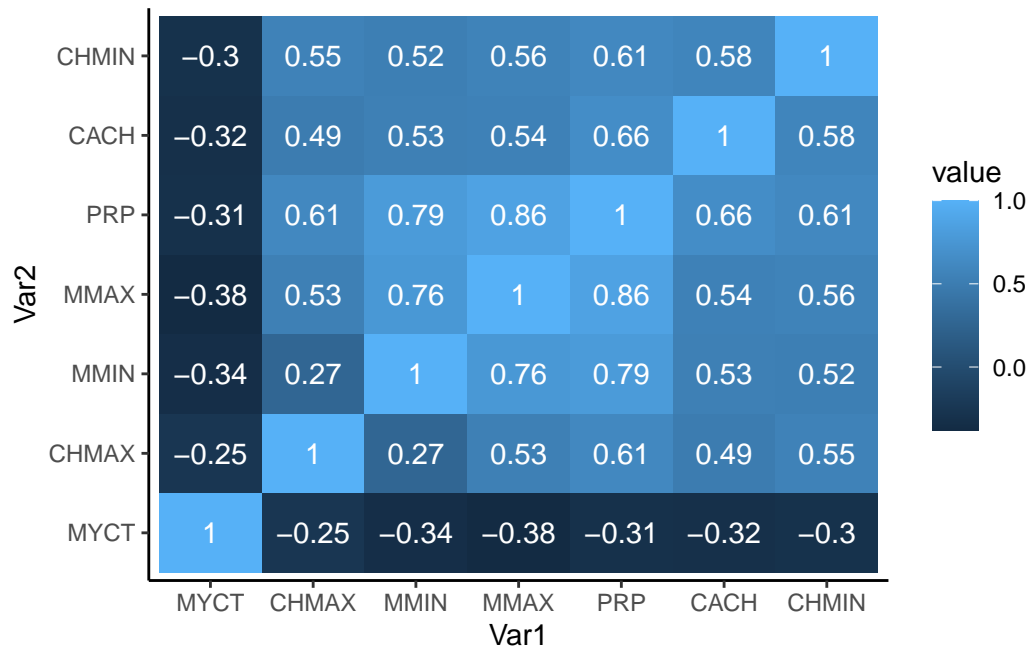
	MYCT	MMIN	MMA	CACH	CHMIN	CHMAX	PRP
1	125	256	6000	256	16	128	198
2	29	8000	32000	32	8	32	269
3	29	8000	32000	32	8	32	220
4	29	8000	32000	32	8	32	172
5	29	8000	16000	32	8	16	132
6	26	8000	32000	64	8	32	318

### Run correlation

	MYCT	MMIN	MMA	CACH	CHMIN	CHMAX	PRP
MYCT	1.00	-0.34	-0.38	-0.32	-0.30	-0.25	-0.31
MMIN	-0.34	1.00	0.76	0.53	0.52	0.27	0.79
MMA	-0.38	0.76	1.00	0.54	0.56	0.53	0.86

CACH	-0.32	0.53	0.54	1.00	0.58	0.49	0.66
CHMIN	-0.30	0.52	0.56	0.58	1.00	0.55	0.61
CHMAX	-0.25	0.27	0.53	0.49	0.55	1.00	0.61

### Correlation heatmap

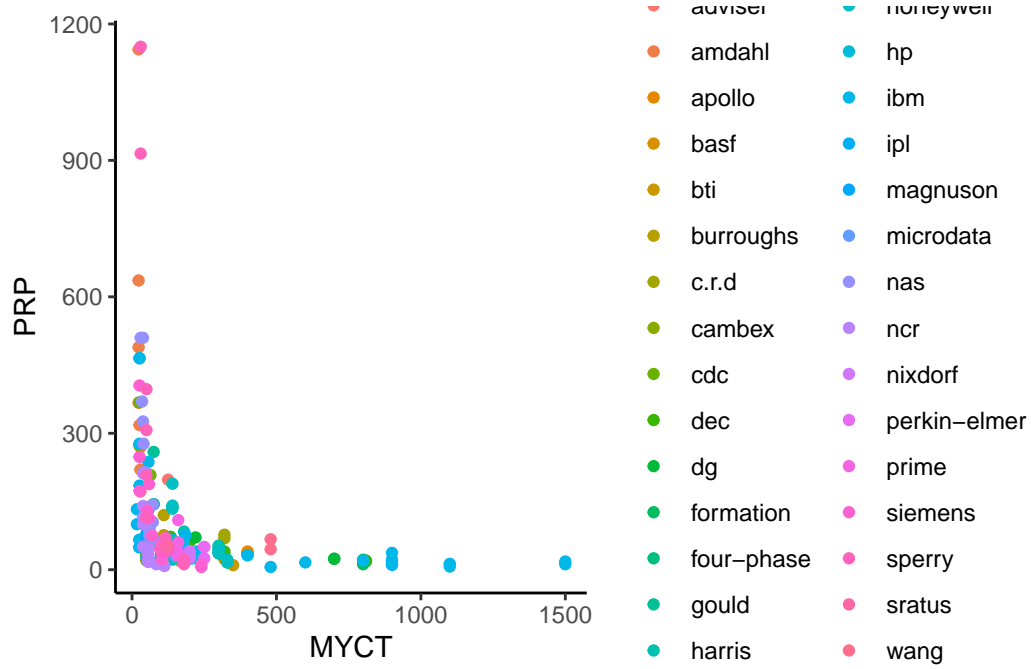


From the correlation matrix we can see:

- PRP and MMAX are highly correlated
- PRP and CACH are highly correlated
- PRP and CHMAX are highly correlated
- PRP and MMIN are highly correlated
- PRP and CHMIN are highly correlated

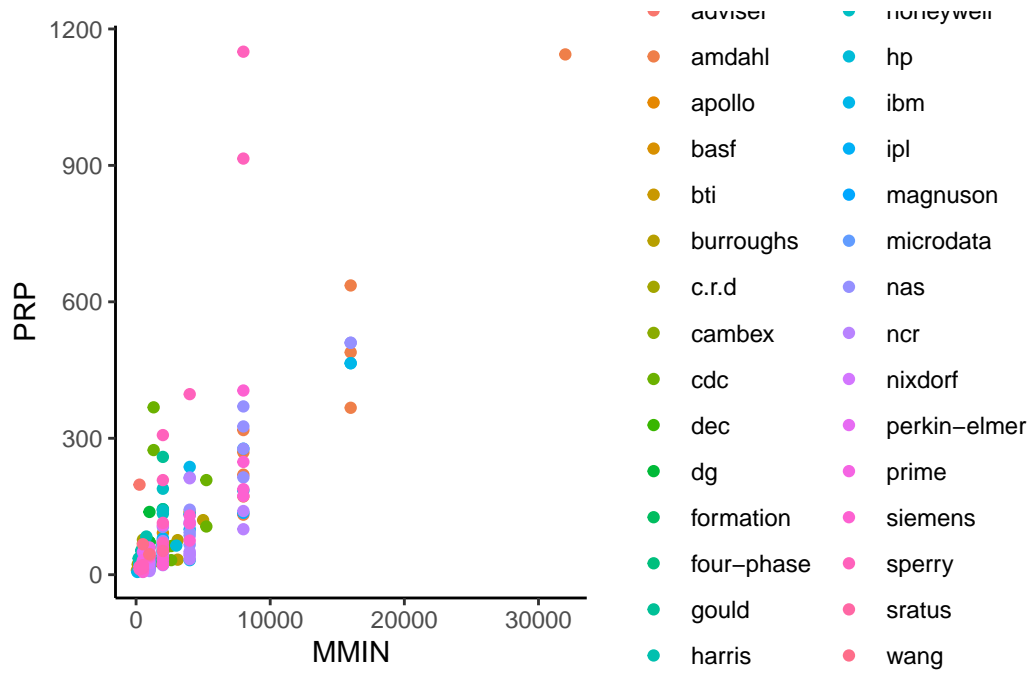
## Scatterplot of PRP vs features

### PRP vs MYCT

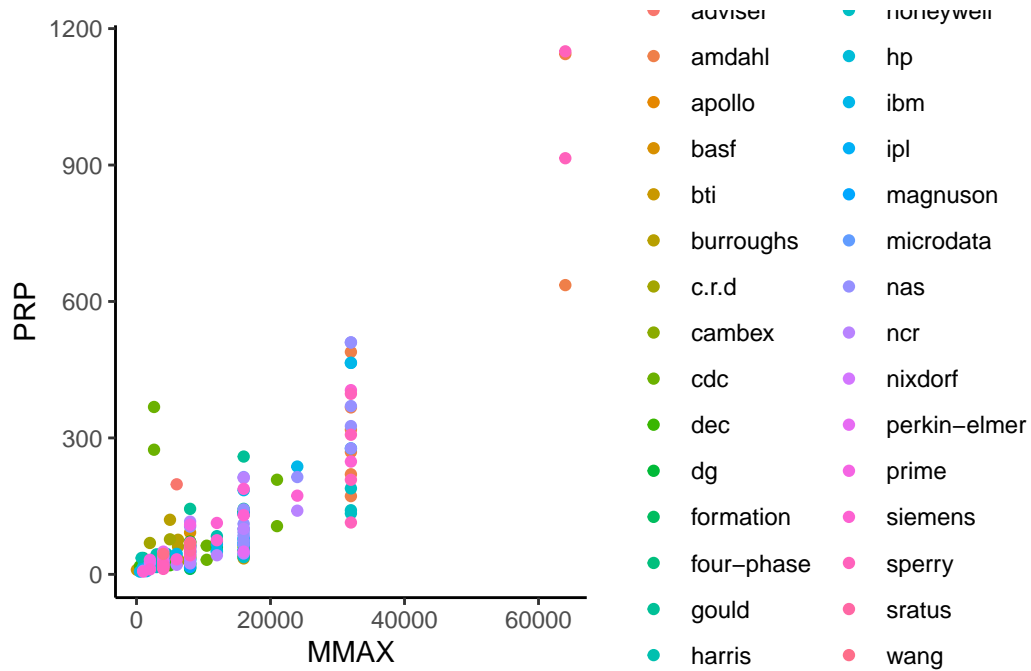




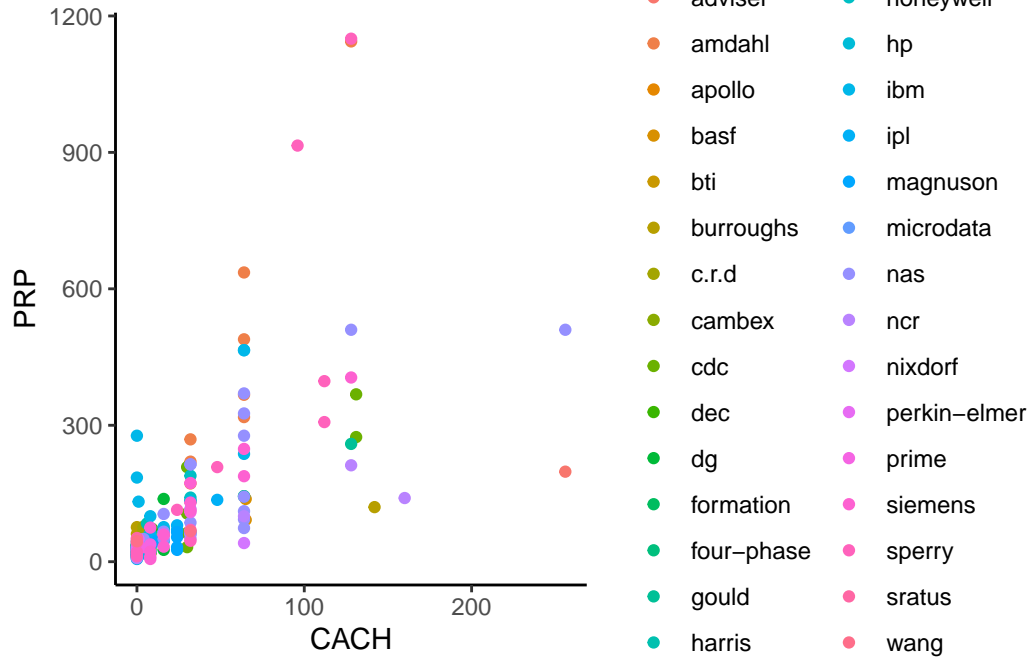
## PRP vs MYCT



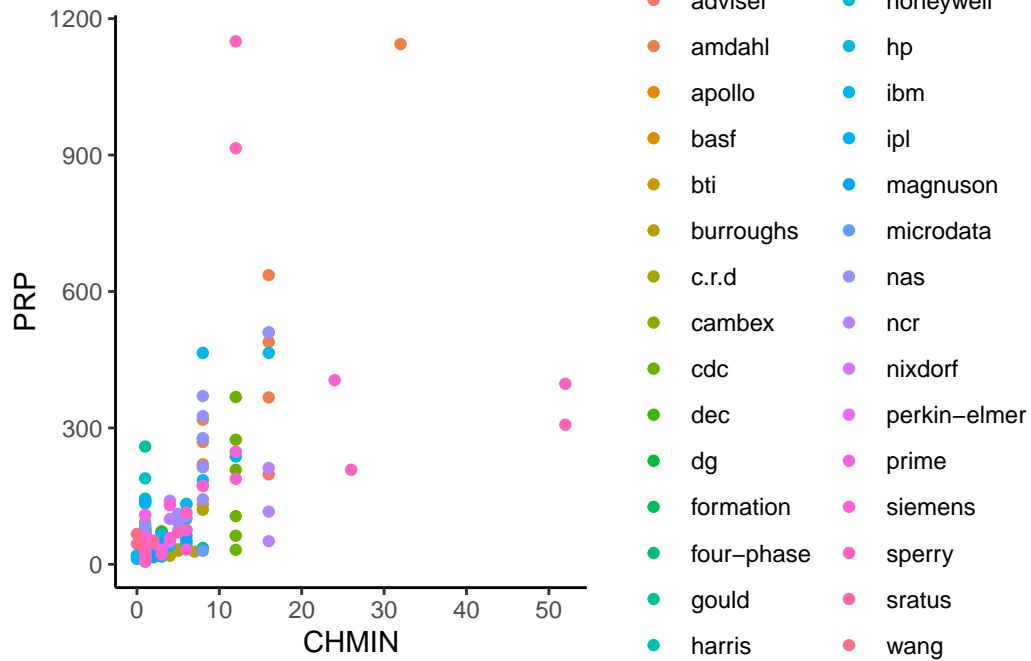
## PRP vs MMAX



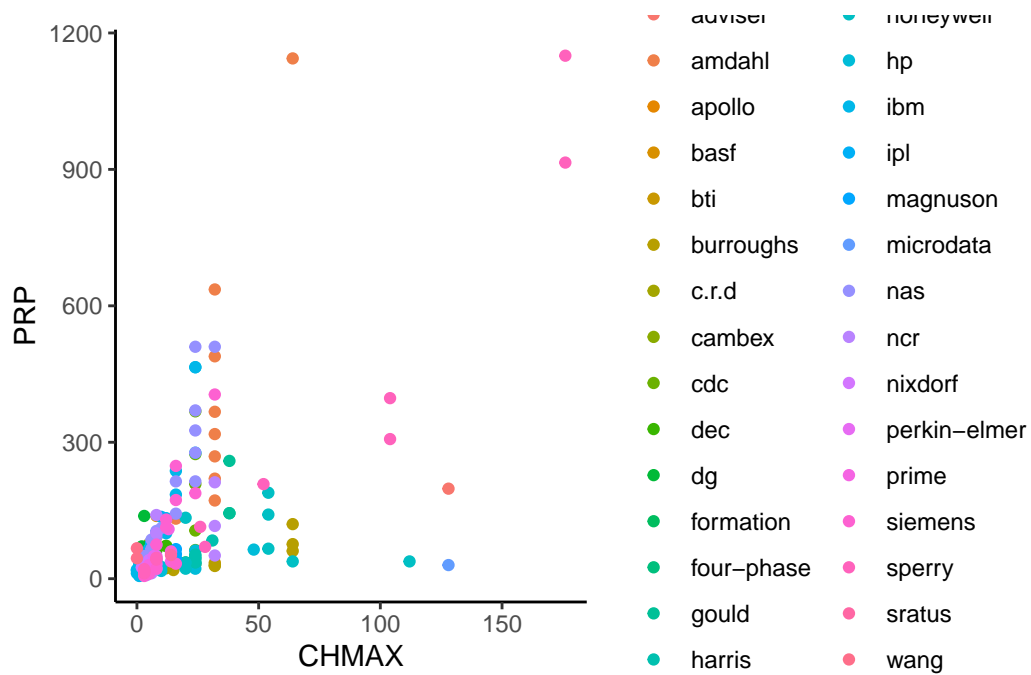
PRP vs CACH



PRP vs CHMIN



## PRP vs CHMAX



## Model

### Split data into training and test datasets

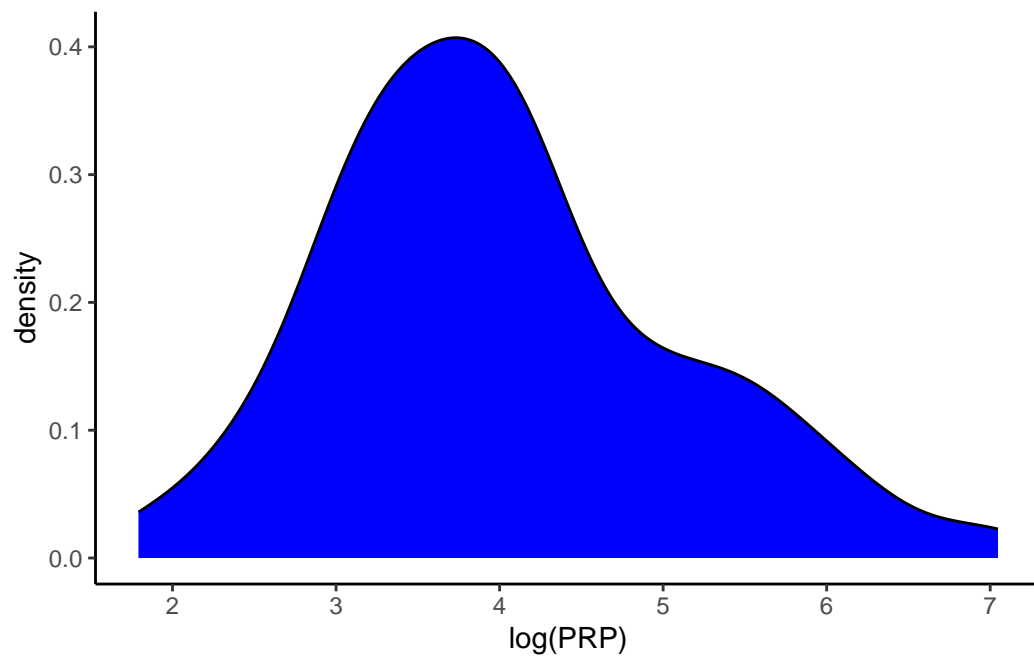
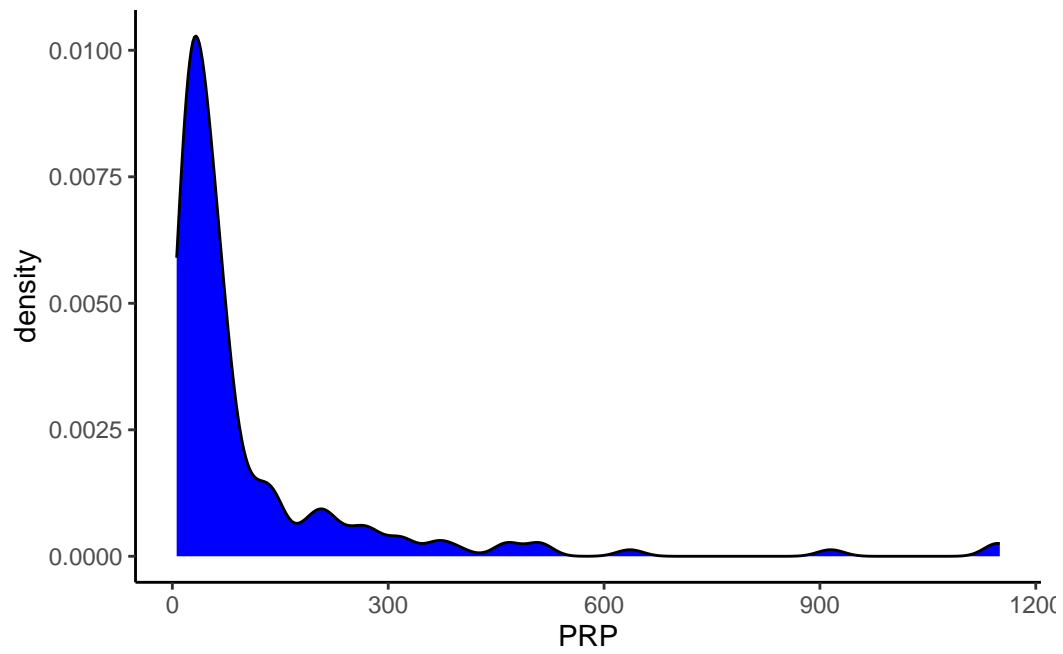
train: 167 7

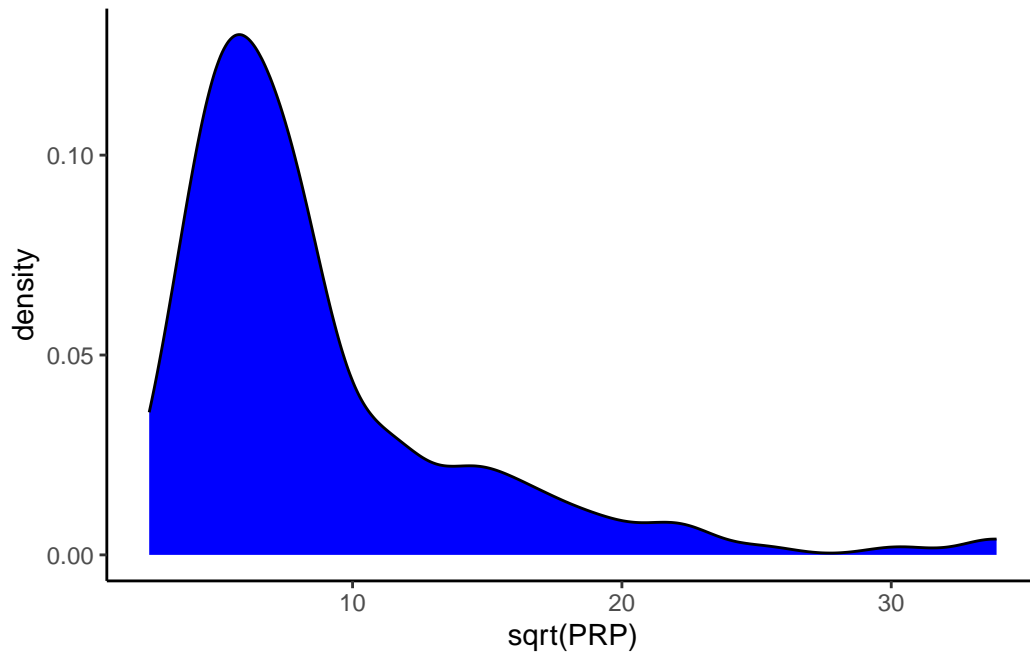
test: 42 7

### Training dataset

	MYCT	MMIN	MMAX	CACH	CHMIN	CHMAX	PRP
1	125	256	6000	256	16	128	198
2	29	8000	32000	32	8	32	269
3	29	8000	32000	32	8	32	220
6	26	8000	32000	64	8	32	318
7	23	16000	32000	64	16	32	367
9	23	16000	64000	64	16	32	636

Check distribution of PRP response variable





The log transformation of the PRP response variable is closer to normal so we will use that

### Log PRP

	MYCT	MMIN	MMAX	CACH	CHMIN	CHMAX	PRP
1	125	256	6000	256	16	128	5.288267
2	29	8000	32000	32	8	32	5.594711
3	29	8000	32000	32	8	32	5.393628
6	26	8000	32000	64	8	32	5.762051
7	23	16000	32000	64	16	32	5.905362
9	23	16000	64000	64	16	32	6.455199

### Regression model 1 - All features

Call:

```
lm(formula = PRP ~ ., data = train_df)
```

Coefficients:

(Intercept)	MYCT	MMIN	MMAX	CACH	CHMIN
3.361e+00	-7.937e-04	1.702e-05	4.948e-05	6.133e-03	6.244e-03
CHMAX					

-1.009e-04

## Summary Statistics

Call:

```
lm(formula = PRP ~ ., data = train_df)
```

Residuals:

	Min	1Q	Median	3Q	Max
	-1.49193	-0.25878	0.04092	0.30446	0.98896

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	3.361e+00	6.718e-02	50.029	< 2e-16 ***
MYCT	-7.937e-04	1.445e-04	-5.491	1.54e-07 ***
MMIN	1.702e-05	1.560e-05	1.091	0.277
MMAX	4.948e-05	5.661e-06	8.741	3.00e-15 ***
CACH	6.133e-03	1.200e-03	5.111	9.04e-07 ***
CHMIN	6.244e-03	6.740e-03	0.926	0.356
CHMAX	-1.009e-04	1.791e-03	-0.056	0.955

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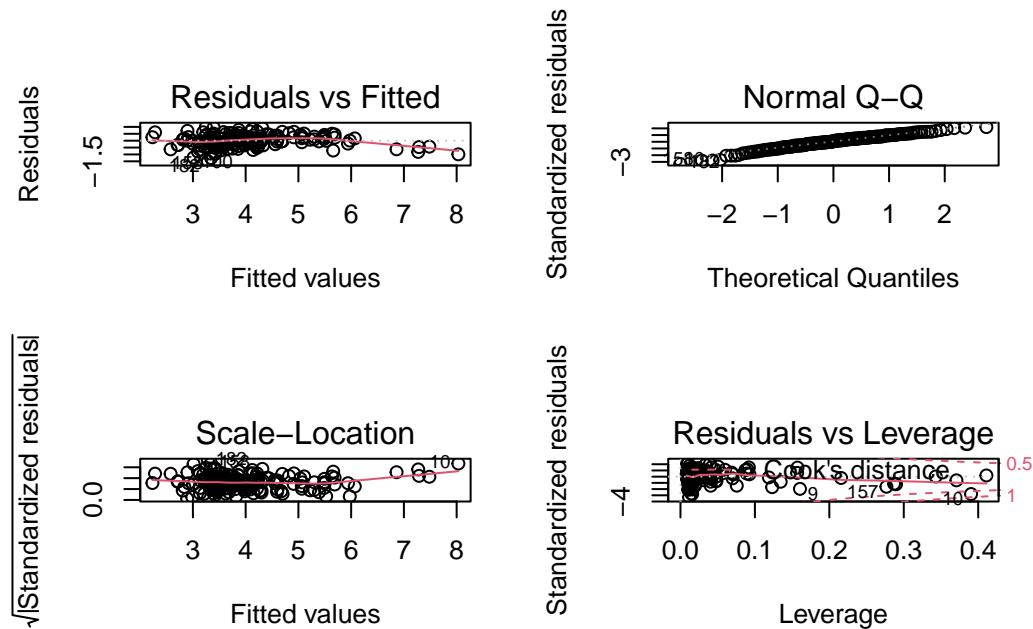
Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.454 on 160 degrees of freedom

Multiple R-squared: 0.8261, Adjusted R-squared: 0.8196

F-statistic: 126.7 on 6 and 160 DF, p-value: < 2.2e-16

## Visualize model



The adjusted R-squared is .8196, meaning the independent variables explain 82% of the variance of the CPU performance.

Three variables (MYCT, MMAX, CACH) show very low p-values (less than 0.05) and are significant

The residuals vs fitted plot show the trend line close to zero except after around 5.5

The Q-Q plot shows us that the features are normal except for the ends

## Regression Model 2 - features MYCT, MMAX, CACH only

Call:

```
lm(formula = PRP ~ MYCT + MMAX + CACH, data = train_df)
```

Coefficients:

(Intercept)	MYCT	MMAX	CACH
3.365e+00	-8.074e-04	5.447e-05	6.761e-03

## Summary Statistics

Call:

```
lm(formula = PRP ~ MYCT + MMAX + CACH, data = train_df)
```

Residuals:

Min	1Q	Median	3Q	Max
-1.48775	-0.27856	0.01263	0.29954	1.00502

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	3.365e+00	6.671e-02	50.436	< 2e-16 ***
MYCT	-8.074e-04	1.441e-04	-5.605	8.73e-08 ***
MMAX	5.448e-05	3.695e-06	14.741	< 2e-16 ***
CACH	6.761e-03	1.074e-03	6.293	2.76e-09 ***

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Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

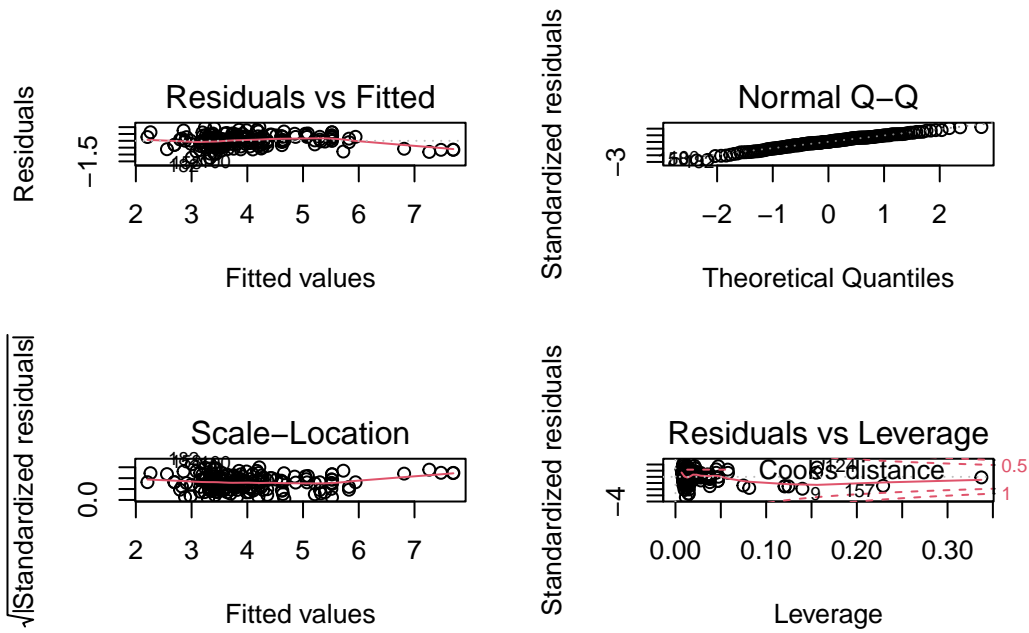
Residual standard error: 0.4533 on 163 degrees of freedom

Multiple R-squared: 0.8234, Adjusted R-squared: 0.8201

F-statistic: 253.3 on 3 and 163 DF, p-value: < 2.2e-16

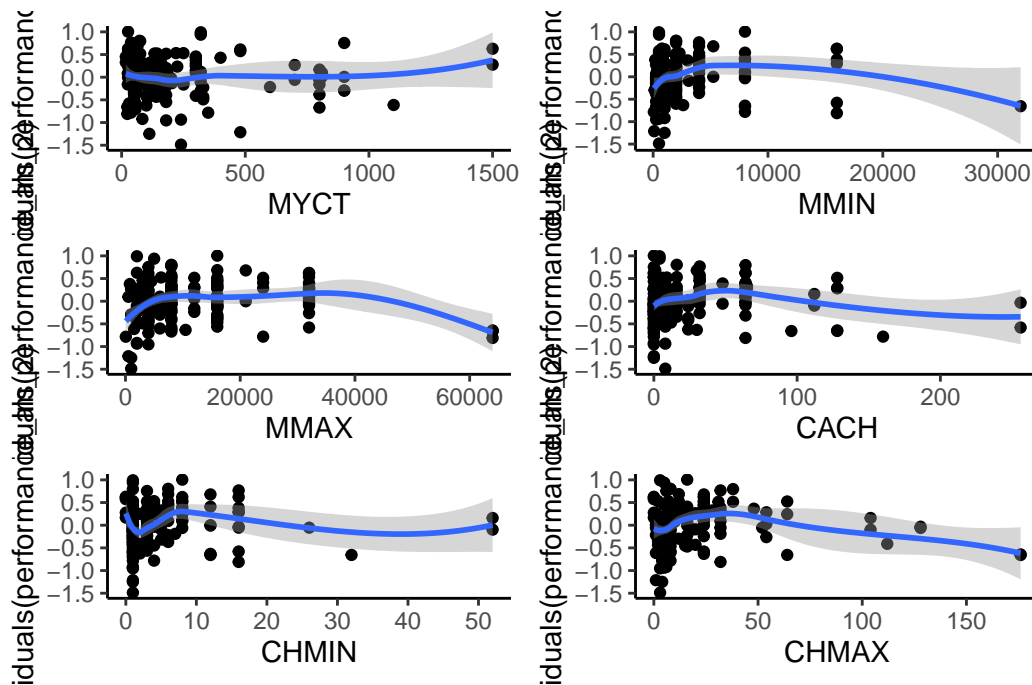


## Visualize model



The F-statistic is much higher than in model 1 and all features are significant. The R<sup>2</sup> is a little higher than in model 1.

## Check predictor vs residual plot



## ANOVA Test - Model 2

### Analysis of Variance Table

Response: PRP

	Df	Sum Sq	Mean Sq	F value	Pr(>F)
MYCT	1	52.791	52.791	256.913	< 2.2e-16 ***
MMAX	1	95.199	95.199	463.291	< 2.2e-16 ***
CACH	1	8.138	8.138	39.604	2.76e-09 ***
Residuals	163	33.494	0.205		

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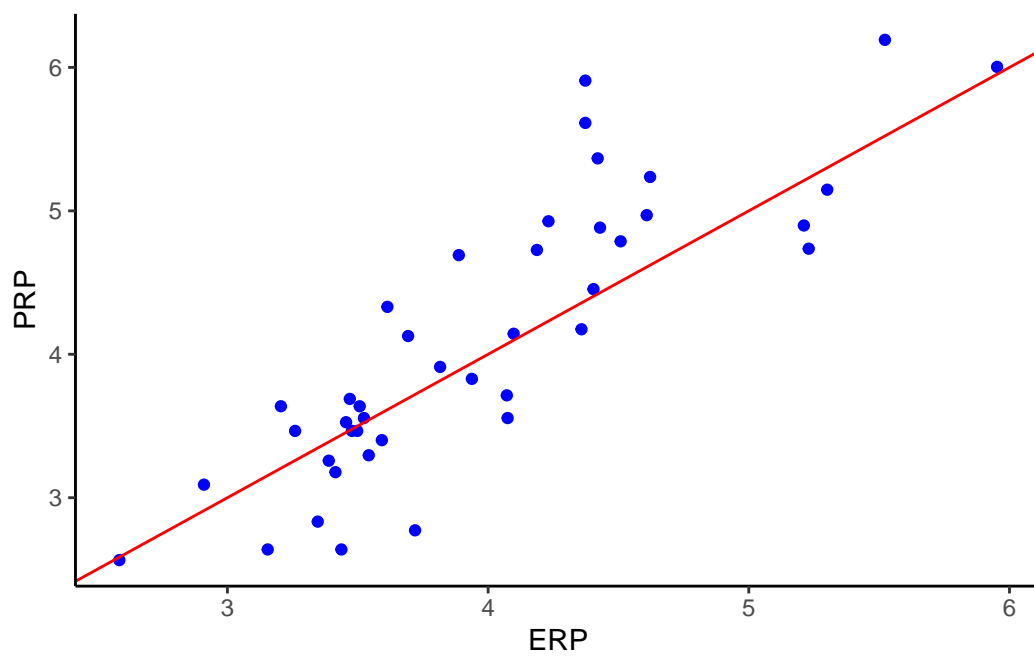
Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

## Predict PRP with model 2

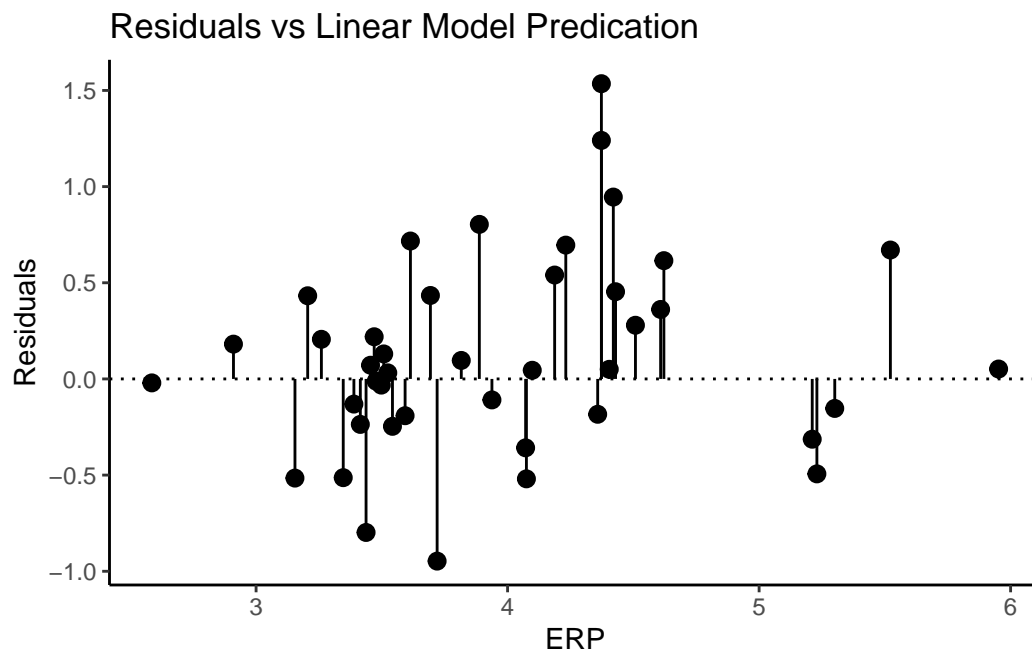
	ERP	PRP	MYCT	MMIN	MMAX	CACH	CHMIN	CHMAX
4	5.300864	5.147494	29	8000	32000	32	8	32
5	4.429265	4.882802	29	8000	16000	32	8	16
8	5.522059	6.192362	23	16000	32000	64	16	32

11	3.205190	3.637586	400	1000	3000	0	1	2
16	4.074847	3.555348	200	512	16000	0	4	32
20	4.508345	4.787492	110	5000	5000	142	8	64

**Plot predicted PRP vs PRP**

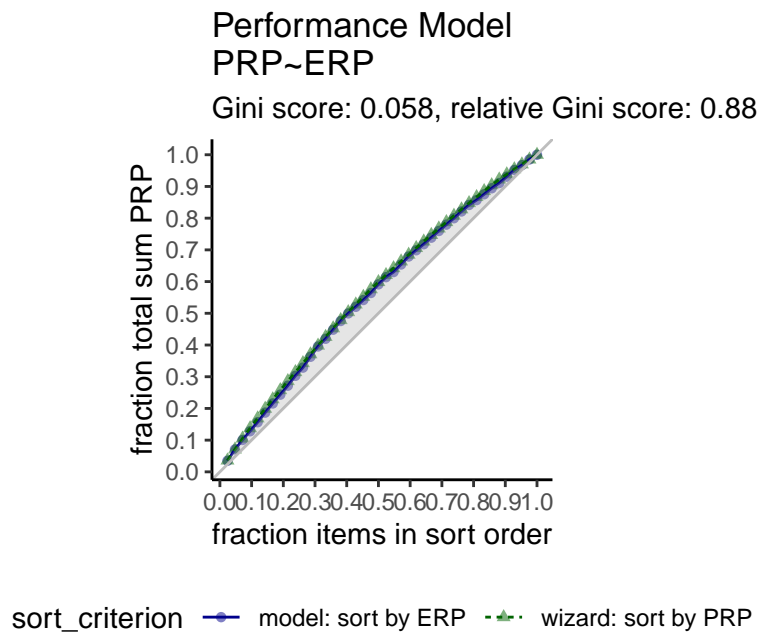


## Residuals vs Prediction



The plot shows the prediction errors vary from the PRP

## Gain Curve plot



The Gini score of 0.88 shows that the model correctly sorts high performance from lower ones.

## Performance on Test data

RMSE: 0.5243939

Std Deviation: 0.9720138

r2: 0.7283943

The RMSE is lower than the Std deviation so the model predicts the PRP well. The R2 is 73% which shows that the model predicts pretty well

## Cross Validation

### Split data

```
List of 3
$ :List of 2
..$ train: int [1:140] 2 3 4 5 7 9 10 11 12 13 ...
..$ app  : int [1:69] 57 161 74 25 85 170 189 145 104 93 ...
$ :List of 2
..$ train: int [1:139] 1 2 4 6 8 10 13 16 17 18 ...
..$ app  : int [1:70] 192 148 66 133 136 45 159 105 173 184 ...
$ :List of 2
..$ train: int [1:139] 1 3 5 6 7 8 9 11 12 14 ...
..$ app  : int [1:70] 165 163 4 117 55 146 134 176 53 63 ...
- attr(*, "splitmethod")= chr "kwaycross"
```

### Run Crossfold

RMSE on full model : 71.13728

RMSE of the cross-validation predictions: 81.09387