Statistical Inference Course Project - A simulation exercise

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Overview

This is an R Markdown document for Statistical Inference Course Project - part 1. Here, we investigate the exponential distribution in R and compare it with the Central Limit Theorem.

```
# Load necessary libs
library(ggplot2)
```

Simulations

Do the simulation to calculate the mean value of 1000 randomly generated exponential distributions.

Sample Mean versus Theoretical Mean

Calculate the sample mean and theoretical mean.

```
# Get theoretical mean
theo.mean <- 1/lambda

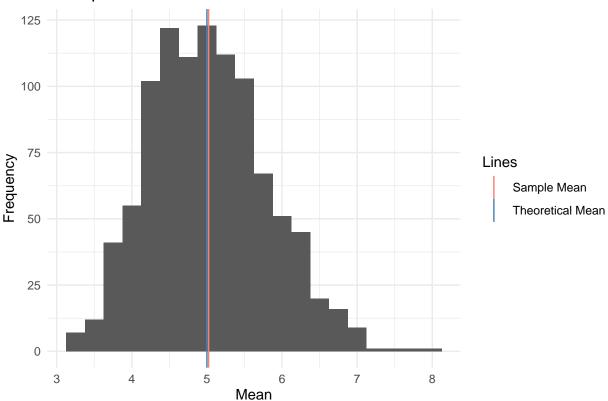
# Get sample mean
sample.mean <- mean(df_sim$mean)

print(cbind(theo.mean, sample.mean))</pre>
```

```
## theo.mean sample.mean
## [1,] 5 5.022343
```

Visualize the results where the sample mean and theoretical mean are illustrated.

40 Exponentials over 1000 Simulations



Sample Variance versus Theoretical Variance

Calculate the sample variance and theoretical variance.

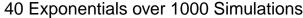
```
# Get theoretical variance
theo.var <- (1/lambda)^2

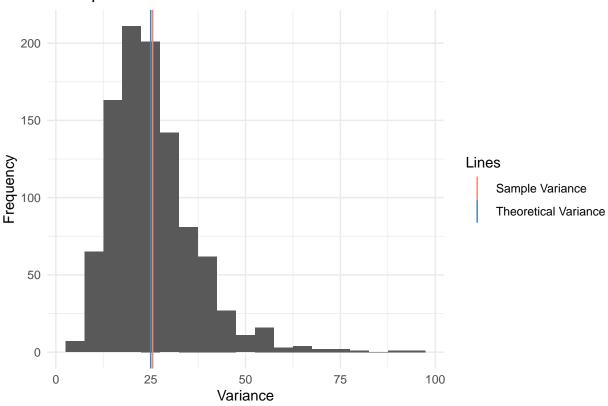
# Get sample variance mean
sample.var <- mean(df_sim$var)

print(cbind(theo.var, sample.var))</pre>
```

```
## theo.var sample.var
## [1,] 25 25.51103
```

Visualize the results where the sample variance and theoretical variance are illustrated.





Distribution

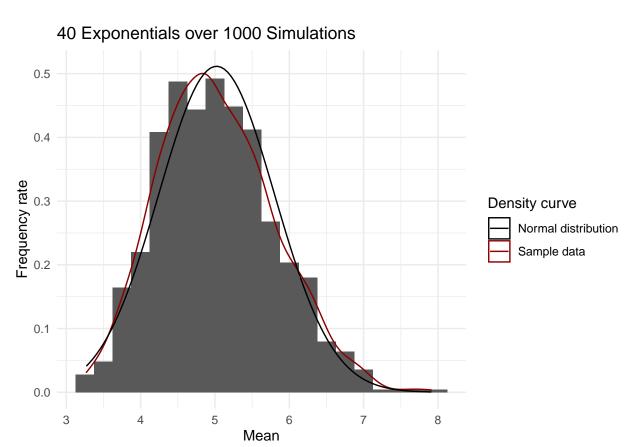
One can tell the distribution is approximately normal. We first generate a Gaussian distribution with the same mean and variance as the simulated mean results.

```
# Get sample mean
sample.mean <- mean(df_sim$mean)

# Get variance of sample mean
sample.var <- var(df_sim$mean)</pre>
```

Visualize the results where the sample density curve looks similar to the normal distribution with the sample mean and standard deviation.

```
x='Mean',
y='Frequency rate') +
theme_minimal()
```



Conclusions

Given the assumption that the sample represents the population, the results confirms the Central Limit Theorem.