# **Test Analysis**

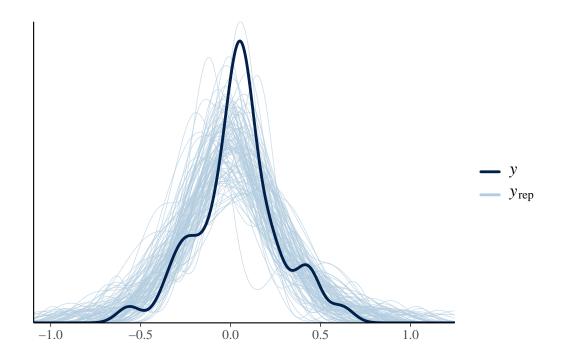
```
test_data <- read_csv("https://raw.githubusercontent.com/Theaang/so-sp-coupling/main/Data/
eszcor <- escalc(measure="ZCOR", ri=es, ni=n, data=test_data)</pre>
test_data$eszcor <- eszcor$yi</pre>
test_data$vi <- eszcor$vi
test_data$se <- sqrt(eszcor$vi)</pre>
priors <- c(prior(normal(0,1), class = b, coef = Intercept),</pre>
prior(cauchy(0,0.5), class = sd))
seed <- 2023
iter <- 5000
chains <- 4
priors <- c(prior(normal(0,1), class = b, coef = Intercept),</pre>
prior(cauchy(0,0.5), class = sd))
meta_prob <-
  brm(
    eszcor|se(se) ~ 0 + Intercept + (1|esid),
    data = test_data,
    family = gaussian(),
    prior = priors,
    sample_prior = T,
    iter = iter,
    save_pars = save_pars(all = TRUE),
    control = list(adapt_delta = 0.99, max_treedepth = 15),
    seed = seed,
    chains = chains
    )
```

```
Running /Library/Frameworks/R.framework/Resources/bin/R CMD SHLIB foo.c
clang -arch arm64 -I"/Library/Frameworks/R.framework/Resources/include" -DNDEBUG
                                                                                    -I"/Libra:
In file included from <built-in>:1:
In file included from /Library/Frameworks/R.framework/Versions/4.2-arm64/Resources/library/S
In file included from /Library/Frameworks/R.framework/Versions/4.2-arm64/Resources/library/R
In file included from /Library/Frameworks/R.framework/Versions/4.2-arm64/Resources/library/R
/Library/Frameworks/R.framework/Versions/4.2-arm64/Resources/library/RcppEigen/include/Eigen
namespace Eigen {
/Library/Frameworks/R.framework/Versions/4.2-arm64/Resources/library/RcppEigen/include/Eigen
namespace Eigen {
In file included from <built-in>:1:
In file included from /Library/Frameworks/R.framework/Versions/4.2-arm64/Resources/library/S
In file included from /Library/Frameworks/R.framework/Versions/4.2-arm64/Resources/library/R
/Library/Frameworks/R.framework/Versions/4.2-arm64/Resources/library/RcppEigen/include/Eigen
#include <complex>
3 errors generated.
make: *** [foo.o] Error 1
Start sampling
SAMPLING FOR MODEL '1d0f2777348f6b2e21c93c848f58a532' NOW (CHAIN 1).
Chain 1:
Chain 1: Gradient evaluation took 3.9e-05 seconds
Chain 1: 1000 transitions using 10 leapfrog steps per transition would take 0.39 seconds.
Chain 1: Adjust your expectations accordingly!
Chain 1:
Chain 1:
Chain 1: Iteration:
                       1 / 5000 [ 0%]
                                         (Warmup)
Chain 1: Iteration: 500 / 5000 [ 10%]
                                         (Warmup)
Chain 1: Iteration: 1000 / 5000 [ 20%]
                                         (Warmup)
Chain 1: Iteration: 1500 / 5000 [ 30%]
                                         (Warmup)
Chain 1: Iteration: 2000 / 5000 [ 40%]
                                         (Warmup)
Chain 1: Iteration: 2500 / 5000 [ 50%]
                                         (Warmup)
Chain 1: Iteration: 2501 / 5000 [ 50%]
                                         (Sampling)
Chain 1: Iteration: 3000 / 5000 [ 60%]
                                         (Sampling)
```

```
Chain 1: Iteration: 3500 / 5000 [ 70%]
                                         (Sampling)
Chain 1: Iteration: 4000 / 5000 [ 80%]
                                         (Sampling)
Chain 1: Iteration: 4500 / 5000 [ 90%]
                                         (Sampling)
Chain 1: Iteration: 5000 / 5000 [100%]
                                         (Sampling)
Chain 1:
Chain 1: Elapsed Time: 0.890596 seconds (Warm-up)
Chain 1:
                        1.27887 seconds (Sampling)
Chain 1:
                        2.16947 seconds (Total)
Chain 1:
SAMPLING FOR MODEL '1d0f2777348f6b2e21c93c848f58a532' NOW (CHAIN 2).
Chain 2:
Chain 2: Gradient evaluation took 1.8e-05 seconds
Chain 2: 1000 transitions using 10 leapfrog steps per transition would take 0.18 seconds.
Chain 2: Adjust your expectations accordingly!
Chain 2:
Chain 2:
Chain 2: Iteration:
                       1 / 5000 [ 0%]
                                         (Warmup)
Chain 2: Iteration: 500 / 5000 [ 10%]
                                         (Warmup)
Chain 2: Iteration: 1000 / 5000 [ 20%]
                                         (Warmup)
Chain 2: Iteration: 1500 / 5000 [ 30%]
                                         (Warmup)
Chain 2: Iteration: 2000 / 5000 [ 40%]
                                         (Warmup)
Chain 2: Iteration: 2500 / 5000 [ 50%]
                                         (Warmup)
Chain 2: Iteration: 2501 / 5000 [ 50%]
                                         (Sampling)
Chain 2: Iteration: 3000 / 5000 [ 60%]
                                         (Sampling)
Chain 2: Iteration: 3500 / 5000 [ 70%]
                                         (Sampling)
Chain 2: Iteration: 4000 / 5000 [ 80%]
                                         (Sampling)
Chain 2: Iteration: 4500 / 5000 [ 90%]
                                         (Sampling)
Chain 2: Iteration: 5000 / 5000 [100%]
                                         (Sampling)
Chain 2:
Chain 2: Elapsed Time: 0.958916 seconds (Warm-up)
Chain 2:
                        0.721962 seconds (Sampling)
Chain 2:
                        1.68088 seconds (Total)
Chain 2:
SAMPLING FOR MODEL '1d0f2777348f6b2e21c93c848f58a532' NOW (CHAIN 3).
Chain 3:
Chain 3: Gradient evaluation took 1.1e-05 seconds
Chain 3: 1000 transitions using 10 leapfrog steps per transition would take 0.11 seconds.
Chain 3: Adjust your expectations accordingly!
Chain 3:
Chain 3:
Chain 3: Iteration: 1 / 5000 [ 0%]
                                         (Warmup)
```

```
Chain 3: Iteration: 500 / 5000 [ 10%]
                                         (Warmup)
Chain 3: Iteration: 1000 / 5000 [ 20%]
                                         (Warmup)
Chain 3: Iteration: 1500 / 5000 [ 30%]
                                         (Warmup)
Chain 3: Iteration: 2000 / 5000 [ 40%]
                                         (Warmup)
Chain 3: Iteration: 2500 / 5000 [ 50%]
                                         (Warmup)
Chain 3: Iteration: 2501 / 5000 [ 50%]
                                         (Sampling)
Chain 3: Iteration: 3000 / 5000 [ 60%]
                                         (Sampling)
Chain 3: Iteration: 3500 / 5000 [ 70%]
                                         (Sampling)
Chain 3: Iteration: 4000 / 5000 [ 80%]
                                         (Sampling)
Chain 3: Iteration: 4500 / 5000 [ 90%]
                                         (Sampling)
Chain 3: Iteration: 5000 / 5000 [100%]
                                         (Sampling)
Chain 3:
Chain 3:
         Elapsed Time: 0.963621 seconds (Warm-up)
Chain 3:
                        0.689415 seconds (Sampling)
Chain 3:
                        1.65304 seconds (Total)
Chain 3:
SAMPLING FOR MODEL '1d0f2777348f6b2e21c93c848f58a532' NOW (CHAIN 4).
Chain 4:
Chain 4: Gradient evaluation took 1.6e-05 seconds
Chain 4: 1000 transitions using 10 leapfrog steps per transition would take 0.16 seconds.
Chain 4: Adjust your expectations accordingly!
Chain 4:
Chain 4:
Chain 4: Iteration:
                       1 / 5000 [ 0%]
                                         (Warmup)
Chain 4: Iteration: 500 / 5000 [ 10%]
                                         (Warmup)
Chain 4: Iteration: 1000 / 5000 [ 20%]
                                         (Warmup)
Chain 4: Iteration: 1500 / 5000 [ 30%]
                                         (Warmup)
Chain 4: Iteration: 2000 / 5000 [ 40%]
                                         (Warmup)
Chain 4: Iteration: 2500 / 5000 [ 50%]
                                         (Warmup)
Chain 4: Iteration: 2501 / 5000 [ 50%]
                                         (Sampling)
Chain 4: Iteration: 3000 / 5000 [ 60%]
                                         (Sampling)
Chain 4: Iteration: 3500 / 5000 [ 70%]
                                         (Sampling)
Chain 4: Iteration: 4000 / 5000 [ 80%]
                                         (Sampling)
Chain 4: Iteration: 4500 / 5000 [ 90%]
                                         (Sampling)
Chain 4: Iteration: 5000 / 5000 [100%]
                                         (Sampling)
Chain 4:
Chain 4: Elapsed Time: 1.3146 seconds (Warm-up)
Chain 4:
                        0.641053 seconds (Sampling)
Chain 4:
                        1.95566 seconds (Total)
Chain 4:
```

#### pp\_check(meta\_prob, ndraws = 100)



#### summary(meta\_prob)

Family: gaussian

Links: mu = identity; sigma = identity

Formula: eszcor | se(se) ~ 0 + Intercept + (1 | esid)

Data: test\_data (Number of observations: 42)

Draws: 4 chains, each with iter = 5000; warmup = 2500; thin = 1;

total post-warmup draws = 10000

#### Group-Level Effects:

~esid (Number of levels: 42)

Estimate Est.Error 1-95% CI u-95% CI Rhat Bulk\_ESS Tail\_ESS sd(Intercept) 0.05 0.04 0.00 0.14 1.00 4350 4801

#### Population-Level Effects:

Estimate Est.Error 1-95% CI u-95% CI Rhat Bulk\_ESS Tail\_ESS Intercept 0.00 0.03 -0.06 0.06 1.00 17614 7616

#### Family Specific Parameters:

Estimate Est.Error 1-95% CI u-95% CI Rhat Bulk\_ESS Tail\_ESS

sigma 0.00 0.00 0.00 0.00 NA NA NA

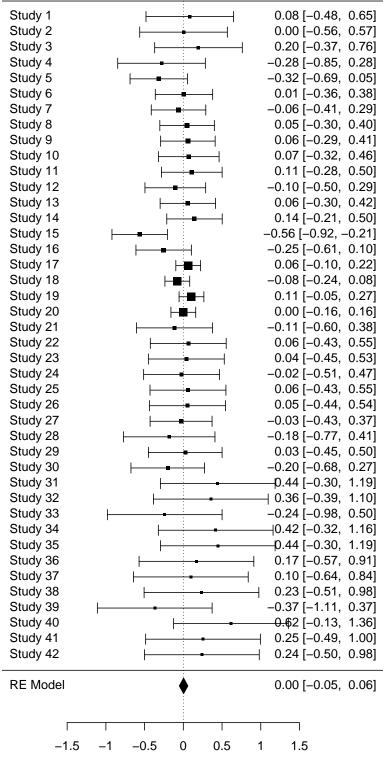
Draws were sampled using sampling(NUTS). For each parameter, Bulk\_ESS and Tail\_ESS are effective sample size measures, and Rhat is the potential scale reduction factor on split chains (at convergence, Rhat = 1).

#### get\_variables(meta\_prob)

```
"sd_esid__Intercept"
 [1] "b_Intercept"
                                                    "sigma"
[4] "r_esid[1,Intercept]"
                            "r_esid[2,Intercept]"
                                                    "r_esid[3,Intercept]"
                             "r_esid[5,Intercept]"
                                                    "r_esid[6,Intercept]"
[7] "r_esid[4,Intercept]"
[10] "r_esid[7,Intercept]"
                             "r_esid[8,Intercept]"
                                                    "r_esid[9,Intercept]"
[13] "r_esid[10,Intercept]" "r_esid[11,Intercept]" "r_esid[12,Intercept]"
[16] "r_esid[13,Intercept]" "r_esid[14,Intercept]" "r_esid[15,Intercept]"
[19] "r_esid[16,Intercept]" "r_esid[17,Intercept]" "r_esid[18,Intercept]"
[22] "r_esid[19,Intercept]" "r_esid[20,Intercept]" "r_esid[21,Intercept]"
[25] "r_esid[22,Intercept]" "r_esid[23,Intercept]" "r_esid[24,Intercept]"
[28] "r_esid[25,Intercept]" "r_esid[26,Intercept]" "r_esid[27,Intercept]"
[31] "r_esid[28,Intercept]" "r_esid[29,Intercept]" "r_esid[30,Intercept]"
[34] "r_esid[31,Intercept]" "r_esid[32,Intercept]" "r_esid[33,Intercept]"
[37] "r_esid[34,Intercept]" "r_esid[35,Intercept]" "r_esid[36,Intercept]"
[40] "r_esid[37,Intercept]" "r_esid[38,Intercept]" "r_esid[39,Intercept]"
[43] "r_esid[40,Intercept]" "r_esid[41,Intercept]" "r_esid[42,Intercept]"
[46] "prior_b_Intercept"
                            "prior_sd_esid"
                                                    "lprior"
[49] "lp__"
                            "z_1[1,1]"
                                                    "z_1[1,2]"
                                                    "z_1[1,5]"
[52] "z_1[1,3]"
                             "z_1[1,4]"
[55] "z_1[1,6]"
                             "z_1[1,7]"
                                                    "z_1[1,8]"
[58] "z_1[1,9]"
                             "z_1[1,10]"
                                                    "z_1[1,11]"
                                                    "z_1[1,14]"
[61] "z_1[1,12]"
                             "z_1[1,13]"
[64] "z_1[1,15]"
                             "z_1[1,16]"
                                                    "z_1[1,17]"
[67] "z_1[1,18]"
                            "z_1[1,19]"
                                                    "z_1[1,20]"
                             "z_1[1,22]"
                                                    "z_1[1,23]"
[70] "z_1[1,21]"
[73] "z_1[1,24]"
                             "z 1[1,25]"
                                                    "z 1[1,26]"
[76] "z_1[1,27]"
                             "z_1[1,28]"
                                                    "z_1[1,29]"
[79] "z_1[1,30]"
                             "z_1[1,31]"
                                                    "z_1[1,32]"
[82] "z_1[1,33]"
                             "z_1[1,34]"
                                                    "z_1[1,35]"
[85] "z_1[1,36]"
                             "z_1[1,37]"
                                                    "z_1[1,38]"
[88] "z_1[1,39]"
                            "z_1[1,40]"
                                                    "z_1[1,41]"
[91] "z_1[1,42]"
                             "accept_stat__"
                                                    "stepsize__"
[94] "treedepth__"
                             "n_leapfrog__"
                                                    "divergent__"
[97] "energy__"
```

```
fixef(meta_prob)
         Estimate Est.Error
                               Q2.5
Intercept 0.002241 0.03155 -0.05906 0.06494
  analysis <- metafor::rma.mv(yi = eszcor, V = vi, data = test_data, random = ~ 1 | esid/stu
  summary(analysis)
Multivariate Meta-Analysis Model (k = 42; method: REML)
  logLik Deviance
                       AIC
                                 BIC
                                          AICc
  5.0810 -10.1620 -4.1620
                              0.9787 -3.5133
Variance Components:
           estim
                                            factor
                    sqrt nlvls fixed
sigma^2.1 0.0000 0.0000
                            42
                                              esid
                                   no
sigma^2.2 0.0000 0.0000
                            42
                                   no esid/studyid
Test for Heterogeneity:
Q(df = 41) = 32.5378, p-val = 0.8245
Model Results:
estimate
                  zval pval ci.lb ci.ub
           se
 0.0033 0.0284 0.1164 0.9073 -0.0523 0.0589
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

metafor::forest(analysis)



Fisher's z Transformed Correlation Coefficient

```
meta_prob2 <-
    brm(
      eszcor|se(se) ~ 0 + Intercept + (1|studyid/esid),
      data = test_data,
      family = gaussian(),
      prior = priors,
      sample_prior = T,
      iter = iter,
      save_pars = save_pars(all = TRUE),
      control = list(adapt_delta = 0.99, max_treedepth = 15),
      seed = seed,
      chains = chains
Compiling Stan program...
Trying to compile a simple C file
Running /Library/Frameworks/R.framework/Resources/bin/R CMD SHLIB foo.c
clang -arch arm64 -I"/Library/Frameworks/R.framework/Resources/include" -DNDEBUG
                                                                                    -I"/Libra
In file included from <built-in>:1:
In file included from /Library/Frameworks/R.framework/Versions/4.2-arm64/Resources/library/S
In file included from /Library/Frameworks/R.framework/Versions/4.2-arm64/Resources/library/R
In file included from /Library/Frameworks/R.framework/Versions/4.2-arm64/Resources/library/R
/Library/Frameworks/R.framework/Versions/4.2-arm64/Resources/library/RcppEigen/include/Eigen
namespace Eigen {
/Library/Frameworks/R.framework/Versions/4.2-arm64/Resources/library/RcppEigen/include/Eigen
namespace Eigen {
In file included from <built-in>:1:
In file included from /Library/Frameworks/R.framework/Versions/4.2-arm64/Resources/library/S
In file included from /Library/Frameworks/R.framework/Versions/4.2-arm64/Resources/library/R
/Library/Frameworks/R.framework/Versions/4.2-arm64/Resources/library/RcppEigen/include/Eigen
#include <complex>
         ^~~~~~~
3 errors generated.
make: *** [foo.o] Error 1
```

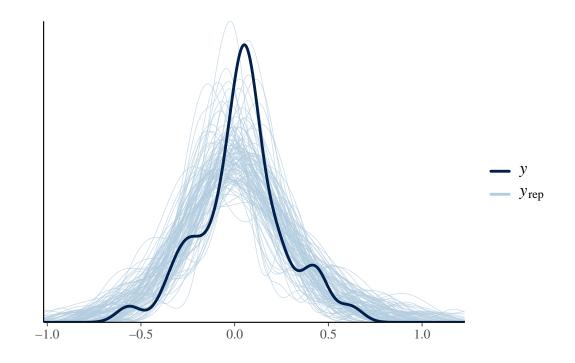
Start sampling

```
SAMPLING FOR MODEL '8630b7bdb90dfccf834b55a121fecbd8' NOW (CHAIN 1).
Chain 1:
Chain 1: Gradient evaluation took 7.3e-05 seconds
Chain 1: 1000 transitions using 10 leapfrog steps per transition would take 0.73 seconds.
Chain 1: Adjust your expectations accordingly!
Chain 1:
Chain 1:
Chain 1: Iteration:
                       1 / 5000 [ 0%]
                                         (Warmup)
Chain 1: Iteration: 500 / 5000 [ 10%]
                                         (Warmup)
Chain 1: Iteration: 1000 / 5000 [ 20%]
                                         (Warmup)
Chain 1: Iteration: 1500 / 5000 [ 30%]
                                         (Warmup)
Chain 1: Iteration: 2000 / 5000 [ 40%]
                                         (Warmup)
Chain 1: Iteration: 2500 / 5000 [ 50%]
                                         (Warmup)
Chain 1: Iteration: 2501 / 5000 [ 50%]
                                         (Sampling)
Chain 1: Iteration: 3000 / 5000 [ 60%]
                                         (Sampling)
Chain 1: Iteration: 3500 / 5000 [ 70%]
                                         (Sampling)
Chain 1: Iteration: 4000 / 5000 [ 80%]
                                         (Sampling)
Chain 1: Iteration: 4500 / 5000 [ 90%]
                                         (Sampling)
Chain 1: Iteration: 5000 / 5000 [100%]
                                         (Sampling)
Chain 1:
Chain 1: Elapsed Time: 1.36795 seconds (Warm-up)
Chain 1:
                        1.60654 seconds (Sampling)
Chain 1:
                        2.97449 seconds (Total)
Chain 1:
SAMPLING FOR MODEL '8630b7bdb90dfccf834b55a121fecbd8' NOW (CHAIN 2).
Chain 2:
Chain 2: Gradient evaluation took 1.5e-05 seconds
Chain 2: 1000 transitions using 10 leapfrog steps per transition would take 0.15 seconds.
Chain 2: Adjust your expectations accordingly!
Chain 2:
Chain 2:
Chain 2: Iteration:
                       1 / 5000 [ 0%]
                                         (Warmup)
Chain 2: Iteration: 500 / 5000 [ 10%]
                                         (Warmup)
Chain 2: Iteration: 1000 / 5000 [ 20%]
                                         (Warmup)
Chain 2: Iteration: 1500 / 5000 [ 30%]
                                         (Warmup)
Chain 2: Iteration: 2000 / 5000 [ 40%]
                                         (Warmup)
Chain 2: Iteration: 2500 / 5000 [ 50%]
                                         (Warmup)
Chain 2: Iteration: 2501 / 5000 [ 50%]
                                         (Sampling)
Chain 2: Iteration: 3000 / 5000 [ 60%]
                                         (Sampling)
Chain 2: Iteration: 3500 / 5000 [ 70%]
                                         (Sampling)
Chain 2: Iteration: 4000 / 5000 [ 80%]
                                         (Sampling)
```

```
Chain 2: Iteration: 4500 / 5000 [ 90%]
                                         (Sampling)
Chain 2: Iteration: 5000 / 5000 [100%]
                                         (Sampling)
Chain 2:
Chain 2: Elapsed Time: 1.3778 seconds (Warm-up)
Chain 2:
                        1.39262 seconds (Sampling)
Chain 2:
                        2.77042 seconds (Total)
Chain 2:
SAMPLING FOR MODEL '8630b7bdb90dfccf834b55a121fecbd8' NOW (CHAIN 3).
Chain 3:
Chain 3: Gradient evaluation took 1.6e-05 seconds
Chain 3: 1000 transitions using 10 leapfrog steps per transition would take 0.16 seconds.
Chain 3: Adjust your expectations accordingly!
Chain 3:
Chain 3:
Chain 3: Iteration:
                       1 / 5000 [ 0%]
                                         (Warmup)
Chain 3: Iteration: 500 / 5000 [ 10%]
                                         (Warmup)
Chain 3: Iteration: 1000 / 5000 [ 20%]
                                         (Warmup)
Chain 3: Iteration: 1500 / 5000 [ 30%]
                                         (Warmup)
Chain 3: Iteration: 2000 / 5000 [ 40%]
                                         (Warmup)
Chain 3: Iteration: 2500 / 5000 [ 50%]
                                         (Warmup)
Chain 3: Iteration: 2501 / 5000 [ 50%]
                                         (Sampling)
Chain 3: Iteration: 3000 / 5000 [ 60%]
                                         (Sampling)
Chain 3: Iteration: 3500 / 5000 [ 70%]
                                         (Sampling)
Chain 3: Iteration: 4000 / 5000 [ 80%]
                                         (Sampling)
Chain 3: Iteration: 4500 / 5000 [ 90%]
                                         (Sampling)
Chain 3: Iteration: 5000 / 5000 [100%]
                                         (Sampling)
Chain 3:
Chain 3: Elapsed Time: 1.55195 seconds (Warm-up)
Chain 3:
                        1.58028 seconds (Sampling)
Chain 3:
                        3.13223 seconds (Total)
Chain 3:
SAMPLING FOR MODEL '8630b7bdb90dfccf834b55a121fecbd8' NOW (CHAIN 4).
Chain 4:
Chain 4: Gradient evaluation took 1.4e-05 seconds
Chain 4: 1000 transitions using 10 leapfrog steps per transition would take 0.14 seconds.
Chain 4: Adjust your expectations accordingly!
Chain 4:
Chain 4:
Chain 4: Iteration:
                       1 / 5000 [ 0%]
                                         (Warmup)
Chain 4: Iteration: 500 / 5000 [ 10%]
                                         (Warmup)
Chain 4: Iteration: 1000 / 5000 [ 20%]
                                         (Warmup)
```

```
Chain 4: Iteration: 1500 / 5000 [ 30%]
                                         (Warmup)
Chain 4: Iteration: 2000 / 5000 [ 40%]
                                         (Warmup)
Chain 4: Iteration: 2500 / 5000 [ 50%]
                                         (Warmup)
Chain 4: Iteration: 2501 / 5000 [ 50%]
                                         (Sampling)
Chain 4: Iteration: 3000 / 5000 [ 60%]
                                         (Sampling)
Chain 4: Iteration: 3500 / 5000 [ 70%]
                                         (Sampling)
Chain 4: Iteration: 4000 / 5000 [ 80%]
                                         (Sampling)
Chain 4: Iteration: 4500 / 5000 [ 90%]
                                         (Sampling)
Chain 4: Iteration: 5000 / 5000 [100%]
                                         (Sampling)
Chain 4:
Chain 4:
         Elapsed Time: 1.33213 seconds (Warm-up)
Chain 4:
                        1.61514 seconds (Sampling)
Chain 4:
                        2.94727 seconds (Total)
Chain 4:
```

#### pp\_check(meta\_prob2, ndraws = 100)



summary(meta\_prob2)

Family: gaussian

Links: mu = identity; sigma = identity

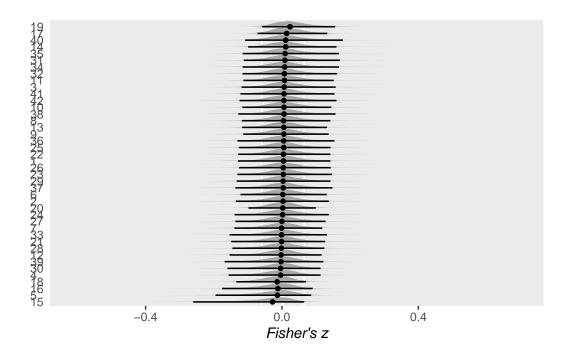
```
Formula: eszcor | se(se) ~ 0 + Intercept + (1 | studyid/esid)
   Data: test_data (Number of observations: 42)
  Draws: 4 chains, each with iter = 5000; warmup = 2500; thin = 1;
         total post-warmup draws = 10000
Group-Level Effects:
~studyid (Number of levels: 9)
              Estimate Est.Error 1-95% CI u-95% CI Rhat Bulk_ESS Tail_ESS
                  0.07
                            0.05
                                     0.00
                                              0.20 1.00
                                                             3605
sd(Intercept)
                                                                      5324
~studyid:esid (Number of levels: 42)
              Estimate Est.Error 1-95% CI u-95% CI Rhat Bulk_ESS Tail_ESS
                                              0.13 1.00
                  0.05
                            0.04
                                     0.00
                                                             4275
                                                                      4203
sd(Intercept)
Population-Level Effects:
          Estimate Est.Error 1-95% CI u-95% CI Rhat Bulk_ESS Tail_ESS
Intercept
             -0.00
                        0.05
                                -0.10
                                          0.08 1.00
                                                         6919
                                                                  6222
Family Specific Parameters:
      Estimate Est.Error 1-95% CI u-95% CI Rhat Bulk ESS Tail ESS
          0.00
                    0.00
                             0.00
                                      0.00
                                             NA
sigma
```

Draws were sampled using sampling(NUTS). For each parameter, Bulk\_ESS and Tail\_ESS are effective sample size measures, and Rhat is the potential scale reduction factor on split chains (at convergence, Rhat = 1).

```
mutate(id = str_replace_all(id, "[.]", " ")) %>%

ggplot(aes(x = b_Intercept, y = reorder(id, b_Intercept))) +
    geom_vline(xintercept = fixef(meta_prob)[1, 1], color = "white", size = 1) +
    geom_vline(xintercept = fixef(meta_prob)[1, 3:4], color = "white", linetype = 2) +
    stat_halfeye(.width = .95, size = 2/3) +
    labs(x = expression(italic("Fisher's z")),
        y = NULL) +
    theme(panel.grid = element_blank(),
        axis.ticks.y = element_blank(),
        axis.text.y = element_text(hjust = 0))
```

Warning: Using `size` aesthetic for lines was deprecated in ggplot2 3.4.0. i Please use `linewidth` instead.



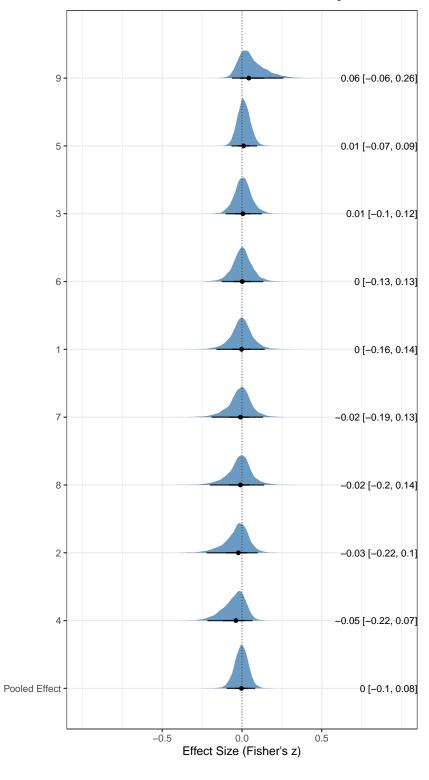
#### get\_variables(meta\_prob2)

```
"r_studyid[6,Intercept]"
 [9] "r_studyid[5,Intercept]"
[11] "r_studyid[7,Intercept]"
                                       "r_studyid[8,Intercept]"
[13] "r_studyid[9,Intercept]"
                                       "r_studyid:esid[1_1,Intercept]"
[15] "r_studyid:esid[1_2,Intercept]"
                                       "r_studyid:esid[1_3,Intercept]"
[17] "r studyid:esid[1 4,Intercept]"
                                       "r studyid:esid[2 5,Intercept]"
[19] "r_studyid:esid[2_6,Intercept]"
                                       "r_studyid:esid[3_10,Intercept]"
[21] "r_studyid:esid[3_11,Intercept]" "r_studyid:esid[3_12,Intercept]"
[23] "r_studyid:esid[3_7,Intercept]"
                                       "r_studyid:esid[3_8,Intercept]"
[25] "r_studyid:esid[3_9,Intercept]"
                                       "r_studyid:esid[4_13,Intercept]"
[27] "r_studyid:esid[4_14,Intercept]" "r_studyid:esid[4_15,Intercept]"
[29] "r_studyid:esid[4_16,Intercept]" "r_studyid:esid[5_17,Intercept]"
[31] "r_studyid:esid[5_18,Intercept]" "r_studyid:esid[5_19,Intercept]"
[33] "r_studyid:esid[5_20,Intercept]" "r_studyid:esid[6_21,Intercept]"
[35] "r_studyid:esid[6_22,Intercept]" "r_studyid:esid[6_23,Intercept]"
[37] "r_studyid:esid[6_24,Intercept]" "r_studyid:esid[6_25,Intercept]"
[39] "r_studyid:esid[6_26,Intercept]" "r_studyid:esid[7_27,Intercept]"
[41] "r_studyid:esid[7_28,Intercept]" "r_studyid:esid[8_29,Intercept]"
[43] "r_studyid:esid[8_30,Intercept]" "r_studyid:esid[9_31,Intercept]"
[45] "r_studyid:esid[9_32,Intercept]" "r_studyid:esid[9_33,Intercept]"
[47] "r_studyid:esid[9_34,Intercept]" "r_studyid:esid[9_35,Intercept]"
[49] "r_studyid:esid[9_36,Intercept]" "r_studyid:esid[9_37,Intercept]"
[51] "r_studyid:esid[9_38,Intercept]" "r_studyid:esid[9_39,Intercept]"
[53] "r_studyid:esid[9_40,Intercept]" "r_studyid:esid[9_41,Intercept]"
[55] "r_studyid:esid[9_42,Intercept]" "prior_b_Intercept"
[57] "prior_sd_studyid"
                                       "prior_sd_studyid:esid"
[59] "lprior"
                                       "lp__"
[61] "z<sub>1</sub>[1,1]"
                                       z_1[1,2]
[63] "z<sub>1</sub>[1,3]"
                                       "z_1[1,4]"
[65] "z<sub>1</sub>[1,5]"
                                       "z_1[1,6]"
[67] "z_1[1,7]"
                                       "z_1[1,8]"
[69] "z_1[1,9]"
                                       "z_2[1,1]"
[71] "z_2[1,2]"
                                       z_2[1,3]
[73] "z_2[1,4]"
                                       z_2[1,5]
[75] "z_2[1,6]"
                                       "z_2[1,7]"
[77] "z 2[1,8]"
                                       "z 2[1,9]"
[79] "z_2[1,10]"
                                       "z 2[1,11]"
[81] "z 2[1,12]"
                                       "z 2[1,13]"
[83] "z_2[1,14]"
                                       "z_2[1,15]"
[85] "z_2[1,16]"
                                       "z_2[1,17]"
                                       "z_2[1,19]"
[87] "z_2[1,18]"
[89] "z_2[1,20]"
                                       "z_2[1,21]"
[91] "z_2[1,22]"
                                       "z_2[1,23]"
[93] "z<sub>2</sub>[1,24]"
                                       "z_2[1,25]"
```

```
[95] "z_2[1,26]"
                                      z_2[1,27]
 [97] "z_2[1,28]"
                                      "z_2[1,29]"
 [99] "z_2[1,30]"
                                      z_2[1,31]
[101] "z_2[1,32]"
                                      "z_2[1,33]"
[103] "z 2[1,34]"
                                      "z 2[1,35]"
[105] "z_2[1,36]"
                                      "z_2[1,37]"
[107] "z_2[1,38]"
                                      "z_2[1,39]"
[109] "z_2[1,40]"
                                      "z_2[1,41]"
[111] "z_2[1,42]"
                                      "accept_stat__"
[113] "stepsize__"
                                      "treedepth__"
[115] "n_leapfrog__"
                                      "divergent__"
[117] "energy__"
  fixef(meta_prob2)
         Estimate Est.Error
                                Q2.5
                                       Q97.5
#extract data from the intercepts-only model:
  study.draws <- spread_rvars(meta_prob2, `r_studyid`[`esid`, ], b_Intercept) %>%
    mutate(b_Intercept = `r_studyid` + b_Intercept) %>%
    mutate(esid = 1:9) %>%
    mutate(esid = as.factor(esid)) %>%
    select(esid, b_Intercept)
  pooled.effect.draws <- spread_rvars(meta_prob2, b_Intercept) %>%
    mutate(esid = "Pooled Effect") %>%
    mutate(esid = as.factor(esid)) %>%
    select(esid, b_Intercept)
  forest.data <- rbind(study.draws, pooled.effect.draws) %>%
    ungroup() %>%
    mutate(esid = reorder(esid, b_Intercept))
  forest.data.summary <- group_by(forest.data, esid) %>%
    mean_qi(b_Intercept)
  #plot the results:
  forest_plot_F0 <- ggplot(aes(dist = b_Intercept, y = relevel(esid, "Pooled Effect", after</pre>
                          data = forest.data) +
```

```
stat_dist_halfeye(fill = "steelblue", scale = 0.7, alpha = 0.8, size = 0.8, show_point =
geom_vline(xintercept = 0.0, color = "black", size = 0.3, linetype="dotted") +
geom_text(data = mutate_if(forest.data.summary, is.numeric, round, 2), aes(label = glue(
labs(x = "placeholder", y = element_blank()) +
scale_x_continuous("Effect Size (Fisher's z)", limits = c(-1, 1), breaks = c(-0.5, 0, 0.
ggtitle(expression(paste("Forest Plot for Studies on ", italic(f)[o]))) +
theme_bw()
forest_plot_F0 <- forest_plot_F0 + theme(plot.title = element_text(hjust = 0.5, size=15))
forest_plot_F0</pre>
```

## Forest Plot for Studies on $f_o$



```
meta_prob3 <-
    brm(
      eszcor|se(se) ~ 0 + Intercept + (1|studyid/esid),
      data = test_data,
      family = gaussian(),
      sample_prior = T,
      iter = iter,
      prior = priors,
      save_pars = save_pars(all = TRUE),
      control = list(adapt_delta = 0.99, max_treedepth = 15),
      seed = seed,
      chains = chains
      )
Compiling Stan program...
recompiling to avoid crashing R session
Trying to compile a simple C file
Running /Library/Frameworks/R.framework/Resources/bin/R CMD SHLIB foo.c
clang -arch arm64 -I"/Library/Frameworks/R.framework/Resources/include" -DNDEBUG
                                                                                    -I"/Libra:
In file included from <built-in>:1:
In file included from /Library/Frameworks/R.framework/Versions/4.2-arm64/Resources/library/S
In file included from /Library/Frameworks/R.framework/Versions/4.2-arm64/Resources/library/R
In file included from /Library/Frameworks/R.framework/Versions/4.2-arm64/Resources/library/R
/Library/Frameworks/R.framework/Versions/4.2-arm64/Resources/library/RcppEigen/include/Eigen
namespace Eigen {
/Library/Frameworks/R.framework/Versions/4.2-arm64/Resources/library/RcppEigen/include/Eigen
namespace Eigen {
In file included from <built-in>:1:
In file included from /Library/Frameworks/R.framework/Versions/4.2-arm64/Resources/library/S
In file included from /Library/Frameworks/R.framework/Versions/4.2-arm64/Resources/library/R
/Library/Frameworks/R.framework/Versions/4.2-arm64/Resources/library/RcppEigen/include/Eigen
#include <complex>
         ^~~~~~~
3 errors generated.
make: *** [foo.o] Error 1
```

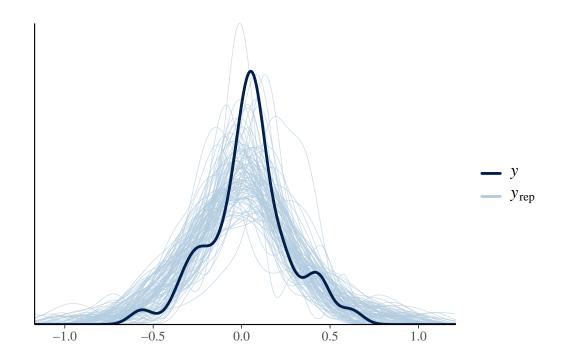
#### Start sampling

```
SAMPLING FOR MODEL '8630b7bdb90dfccf834b55a121fecbd8' NOW (CHAIN 1).
Chain 1:
Chain 1: Gradient evaluation took 8.9e-05 seconds
Chain 1: 1000 transitions using 10 leapfrog steps per transition would take 0.89 seconds.
Chain 1: Adjust your expectations accordingly!
Chain 1:
Chain 1:
Chain 1: Iteration:
                       1 / 5000 [ 0%]
                                         (Warmup)
Chain 1: Iteration: 500 / 5000 [ 10%]
                                         (Warmup)
Chain 1: Iteration: 1000 / 5000 [ 20%]
                                         (Warmup)
Chain 1: Iteration: 1500 / 5000 [ 30%]
                                         (Warmup)
Chain 1: Iteration: 2000 / 5000 [ 40%]
                                         (Warmup)
Chain 1: Iteration: 2500 / 5000 [ 50%]
                                         (Warmup)
Chain 1: Iteration: 2501 / 5000 [ 50%]
                                         (Sampling)
Chain 1: Iteration: 3000 / 5000 [ 60%]
                                         (Sampling)
Chain 1: Iteration: 3500 / 5000 [ 70%]
                                         (Sampling)
Chain 1: Iteration: 4000 / 5000 [ 80%]
                                         (Sampling)
Chain 1: Iteration: 4500 / 5000 [ 90%]
                                         (Sampling)
Chain 1: Iteration: 5000 / 5000 [100%]
                                         (Sampling)
Chain 1:
Chain 1: Elapsed Time: 1.43314 seconds (Warm-up)
Chain 1:
                        1.59289 seconds (Sampling)
Chain 1:
                        3.02603 seconds (Total)
Chain 1:
SAMPLING FOR MODEL '8630b7bdb90dfccf834b55a121fecbd8' NOW (CHAIN 2).
Chain 2:
Chain 2: Gradient evaluation took 1.5e-05 seconds
Chain 2: 1000 transitions using 10 leapfrog steps per transition would take 0.15 seconds.
Chain 2: Adjust your expectations accordingly!
Chain 2:
Chain 2:
Chain 2: Iteration:
                       1 / 5000 [ 0%]
                                         (Warmup)
Chain 2: Iteration: 500 / 5000 [ 10%]
                                         (Warmup)
Chain 2: Iteration: 1000 / 5000 [ 20%]
                                         (Warmup)
Chain 2: Iteration: 1500 / 5000 [ 30%]
                                         (Warmup)
Chain 2: Iteration: 2000 / 5000 [ 40%]
                                         (Warmup)
Chain 2: Iteration: 2500 / 5000 [ 50%]
                                         (Warmup)
Chain 2: Iteration: 2501 / 5000 [ 50%]
                                         (Sampling)
```

```
Chain 2: Iteration: 3000 / 5000 [ 60%]
                                         (Sampling)
Chain 2: Iteration: 3500 / 5000 [ 70%]
                                         (Sampling)
Chain 2: Iteration: 4000 / 5000 [ 80%]
                                         (Sampling)
Chain 2: Iteration: 4500 / 5000 [ 90%]
                                         (Sampling)
Chain 2: Iteration: 5000 / 5000 [100%]
                                         (Sampling)
Chain 2:
Chain 2: Elapsed Time: 1.40761 seconds (Warm-up)
Chain 2:
                        1.37556 seconds (Sampling)
Chain 2:
                        2.78317 seconds (Total)
Chain 2:
SAMPLING FOR MODEL '8630b7bdb90dfccf834b55a121fecbd8' NOW (CHAIN 3).
Chain 3:
Chain 3: Gradient evaluation took 1.9e-05 seconds
Chain 3: 1000 transitions using 10 leapfrog steps per transition would take 0.19 seconds.
Chain 3: Adjust your expectations accordingly!
Chain 3:
Chain 3:
Chain 3: Iteration:
                       1 / 5000 [ 0%]
                                         (Warmup)
Chain 3: Iteration: 500 / 5000 [ 10%]
                                         (Warmup)
Chain 3: Iteration: 1000 / 5000 [ 20%]
                                         (Warmup)
Chain 3: Iteration: 1500 / 5000 [ 30%]
                                         (Warmup)
Chain 3: Iteration: 2000 / 5000 [ 40%]
                                         (Warmup)
Chain 3: Iteration: 2500 / 5000 [ 50%]
                                         (Warmup)
Chain 3: Iteration: 2501 / 5000 [ 50%]
                                         (Sampling)
Chain 3: Iteration: 3000 / 5000 [ 60%]
                                         (Sampling)
Chain 3: Iteration: 3500 / 5000 [ 70%]
                                         (Sampling)
Chain 3: Iteration: 4000 / 5000 [ 80%]
                                         (Sampling)
Chain 3: Iteration: 4500 / 5000 [ 90%]
                                         (Sampling)
Chain 3: Iteration: 5000 / 5000 [100%]
                                         (Sampling)
Chain 3:
Chain 3: Elapsed Time: 1.60766 seconds (Warm-up)
Chain 3:
                        1.61346 seconds (Sampling)
Chain 3:
                        3.22111 seconds (Total)
Chain 3:
SAMPLING FOR MODEL '8630b7bdb90dfccf834b55a121fecbd8' NOW (CHAIN 4).
Chain 4:
Chain 4: Gradient evaluation took 1.6e-05 seconds
Chain 4: 1000 transitions using 10 leapfrog steps per transition would take 0.16 seconds.
Chain 4: Adjust your expectations accordingly!
Chain 4:
Chain 4:
```

```
Chain 4: Iteration:
                       1 / 5000 [ 0%]
                                         (Warmup)
Chain 4: Iteration: 500 / 5000 [ 10%]
                                         (Warmup)
Chain 4: Iteration: 1000 / 5000 [ 20%]
                                         (Warmup)
Chain 4: Iteration: 1500 / 5000 [ 30%]
                                         (Warmup)
Chain 4: Iteration: 2000 / 5000 [ 40%]
                                         (Warmup)
Chain 4: Iteration: 2500 / 5000 [ 50%]
                                         (Warmup)
Chain 4: Iteration: 2501 / 5000 [ 50%]
                                         (Sampling)
Chain 4: Iteration: 3000 / 5000 [ 60%]
                                         (Sampling)
Chain 4: Iteration: 3500 / 5000 [ 70%]
                                         (Sampling)
Chain 4: Iteration: 4000 / 5000 [ 80%]
                                         (Sampling)
Chain 4: Iteration: 4500 / 5000 [ 90%]
                                         (Sampling)
Chain 4: Iteration: 5000 / 5000 [100%]
                                         (Sampling)
Chain 4:
Chain 4:
          Elapsed Time: 1.36081 seconds (Warm-up)
Chain 4:
                        1.61777 seconds (Sampling)
Chain 4:
                        2.97858 seconds (Total)
Chain 4:
```

#### pp\_check(meta\_prob3, ndraws = 100)



summary(meta\_prob3)

```
Links: mu = identity; sigma = identity
Formula: eszcor | se(se) ~ 0 + Intercept + (1 | studyid/esid)
   Data: test_data (Number of observations: 42)
  Draws: 4 chains, each with iter = 5000; warmup = 2500; thin = 1;
         total post-warmup draws = 10000
Group-Level Effects:
~studyid (Number of levels: 9)
              Estimate Est.Error 1-95% CI u-95% CI Rhat Bulk_ESS Tail_ESS
                                     0.00
                                              0.20 1.00
                                                             3605
                  0.07
                            0.05
                                                                      5324
sd(Intercept)
~studyid:esid (Number of levels: 42)
              Estimate Est.Error 1-95% CI u-95% CI Rhat Bulk_ESS Tail_ESS
sd(Intercept)
                            0.04
                                     0.00
                                              0.13 1.00
                                                             4275
                                                                      4203
Population-Level Effects:
          Estimate Est.Error 1-95% CI u-95% CI Rhat Bulk_ESS Tail_ESS
             -0.00
                        0.05
                                -0.10
                                          0.08 1.00
                                                         6919
                                                                  6222
Intercept
Family Specific Parameters:
      Estimate Est.Error 1-95% CI u-95% CI Rhat Bulk_ESS Tail_ESS
sigma
          0.00
                    0.00
                             0.00
                                      0.00
                                             NΑ
Draws were sampled using sampling(NUTS). For each parameter, Bulk_ESS
and Tail ESS are effective sample size measures, and Rhat is the potential
scale reduction factor on split chains (at convergence, Rhat = 1).
  #extract data from the intercepts-only model:
  study.draws1 <- spread_rvars(meta_prob3, `r_studyid`[`esid1`, ], `r_studyid:esid`[`esid2`,
  study.draws2 <- study.draws1 %>%
    mutate(esid3 = as.integer(sub("_.*", "", esid2))) %>%
    filter(esid3 == esid1)
```

Family: gaussian

mutate(b\_Intercept = `r\_studyid` + `r\_studyid:esid` + b\_Intercept) %>%

study.draws <- study.draws2 %>%

mutate(esid = as.factor(esid)) %>%

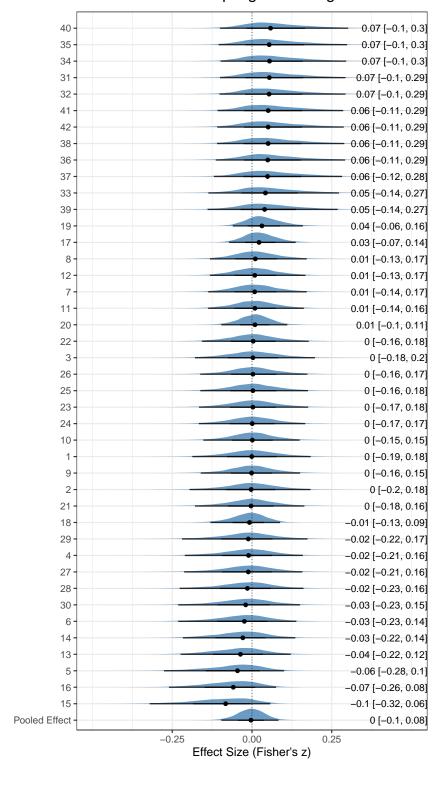
mutate(esid = 1:42) %>%

select(esid, b\_Intercept)

```
pooled.effect.draws <- spread_rvars(meta_prob3, b_Intercept) %>%
  mutate(esid = "Pooled Effect") %>%
  mutate(esid = as.factor(esid)) %>%
  select(esid, b_Intercept)
forest.data <- rbind(study.draws, pooled.effect.draws) %>%
  ungroup() %>%
  mutate(esid = reorder(esid, b_Intercept))
forest.data.summary <- group_by(forest.data, esid) %>%
  mean_qi(b_Intercept)
#plot the results:
forest_plot_F0 <- ggplot(aes(dist = b_Intercept, y = relevel(esid, "Pooled Effect", after</pre>
                         data = forest.data) +
  stat_dist_halfeye(fill = "steelblue", scale = 0.7, alpha = 0.8, size = 0.8, show_point =
  geom_vline(xintercept = 0.0, color = "black", size = 0.3, linetype="dotted") +
  geom_text(data = mutate_if(forest.data.summary, is.numeric, round, 2), aes(label = glue(
  labs(x = "placeholder", y = element_blank()) +
  scale_x_continuous("Effect Size (Fisher's z)", limits = c(-0.5, 0.5), breaks = c(-0.25, 0.5)
  ggtitle(expression(paste("Forest Plot for Coupling Percentage Test Data"))) +
  theme bw()
forest_plot_F0 <- forest_plot_F0 + theme(plot.title = element_text(hjust = 0.5, size=15))</pre>
forest_plot_F0
```

Warning: Removed 863 rows containing missing values (`geom\_slabinterval()`).

## Forest Plot for Coupling Percentage Test Data



```
#extract data from the intercepts-only model:
study.draws1 <- spread_rvars(meta_prob3, `r_studyid`[`esid1`, ], `r_studyid:esid`[`esid2`,
study.draws2 <- study.draws1 %>%
  mutate(esid3 = as.integer(sub("_.*", "", esid2))) %>%
  filter(esid3 == esid1)
study.draws <- study.draws2 %>%
  mutate(b_Intercept = `r_studyid` + `r_studyid:esid` + b_Intercept) %>%
  mutate(esid = 1:42) %>%
  mutate(esid = as.factor(esid)) %>%
  select(esid, b_Intercept)
pooled.effect.draws <- spread_rvars(meta_prob3, b_Intercept) %>%
  mutate(esid = "Pooled Effect") %>%
  mutate(esid = as.factor(esid)) %>%
  select(esid, b_Intercept)
forest.data <- rbind(study.draws, pooled.effect.draws) %>%
  ungroup() %>%
  mutate(esid = reorder(esid, b_Intercept))
forest.data.summary <- group_by(forest.data, esid) %>%
  mean_qi(b_Intercept)
#plot the results:
forest_plot_F0 <- ggplot(aes(dist = b_Intercept, y = relevel(esid, "Pooled Effect", after</pre>
                         data = forest.data) +
  stat_dist_halfeye(fill = "steelblue", scale = 0.7, alpha = 0.8, size = 0.8, show_point =
  geom_vline(xintercept = 0.0, color = "black", size = 0.3, linetype="dotted") +
  geom_text(data = mutate_if(forest.data.summary, is.numeric, round, 2), aes(label = glue(
  labs(x = "placeholder", y = element_blank()) +
  scale_x_continuous("Effect Size (Fisher's z)", limits = c(-1, 1), breaks = c(-0.5, 0, 0.5)
  ggtitle(expression(paste("Forest Plot for Coupling Percentage Test Data"))) +
  theme_bw()
forest_plot_F0 <- forest_plot_F0 + theme(plot.title = element_text(hjust = 0.5, size=15))</pre>
forest_plot_F0
```

## Forest Plot for Coupling Percentage Test Data

