

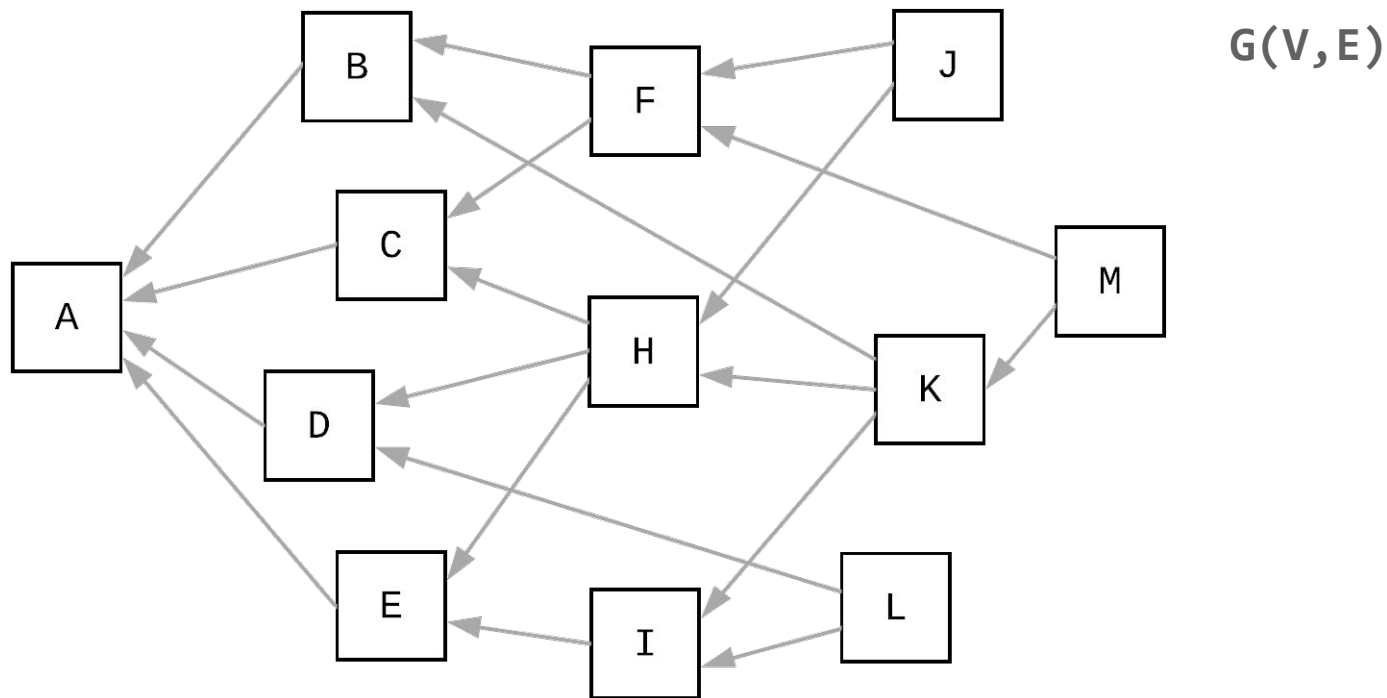
DAG-based distributed ledgers

Péter Garamvölgyi

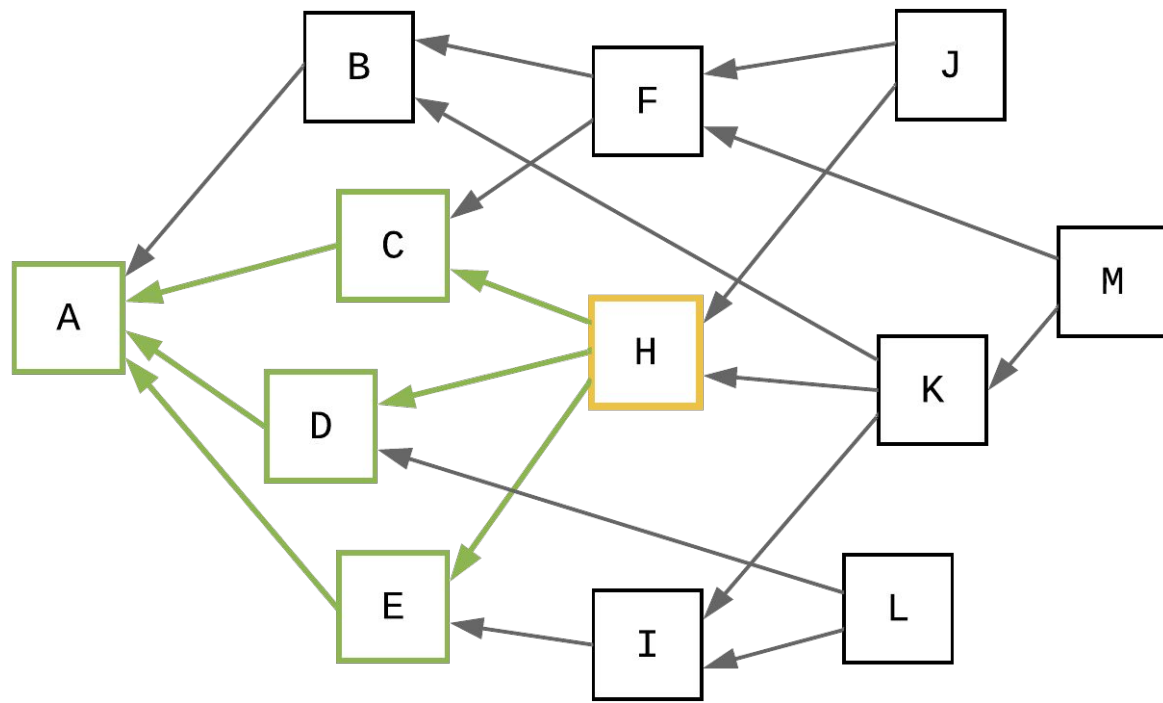
Outline

- DAGs of blocks
 - blockDAG / inclusive
 - SPECTRE
 - PHANTOM / GHOSTDAG
 - Conflux
- DAGs of transactions
 - tangle (IOTA)
 - Avalanche

DAGs - notation



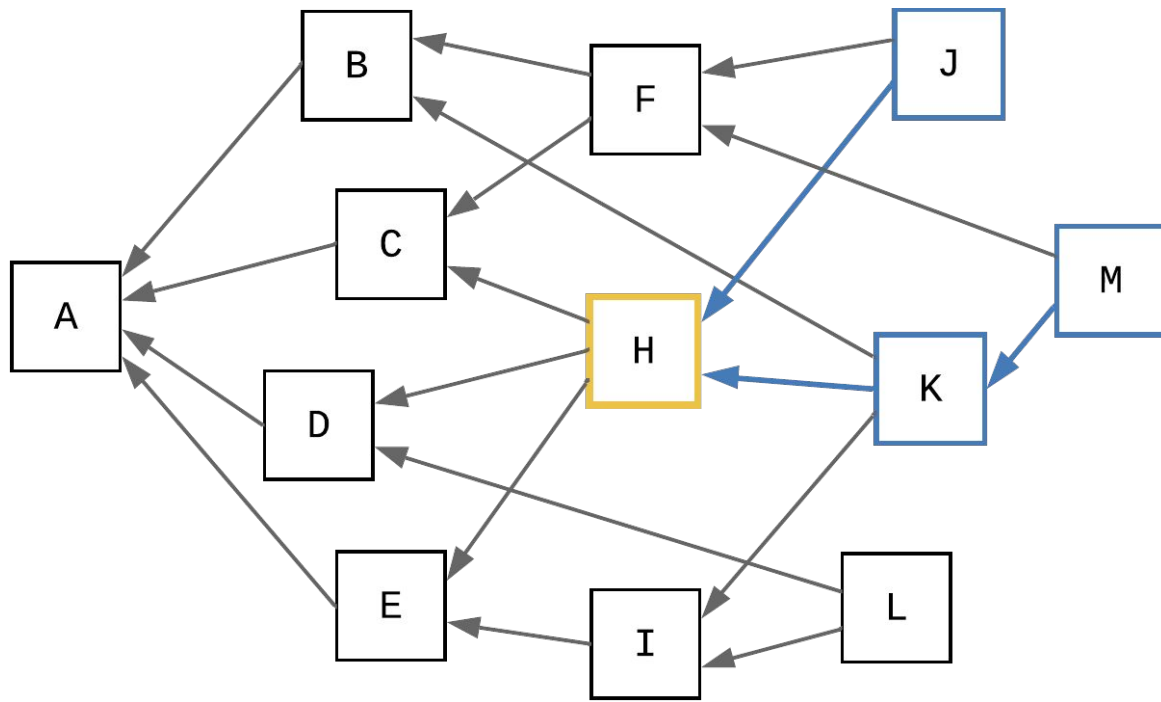
DAGs - notation



$G(V, E)$

$\text{past}(H) = \{A, C, D, E\}$

DAGs - notation

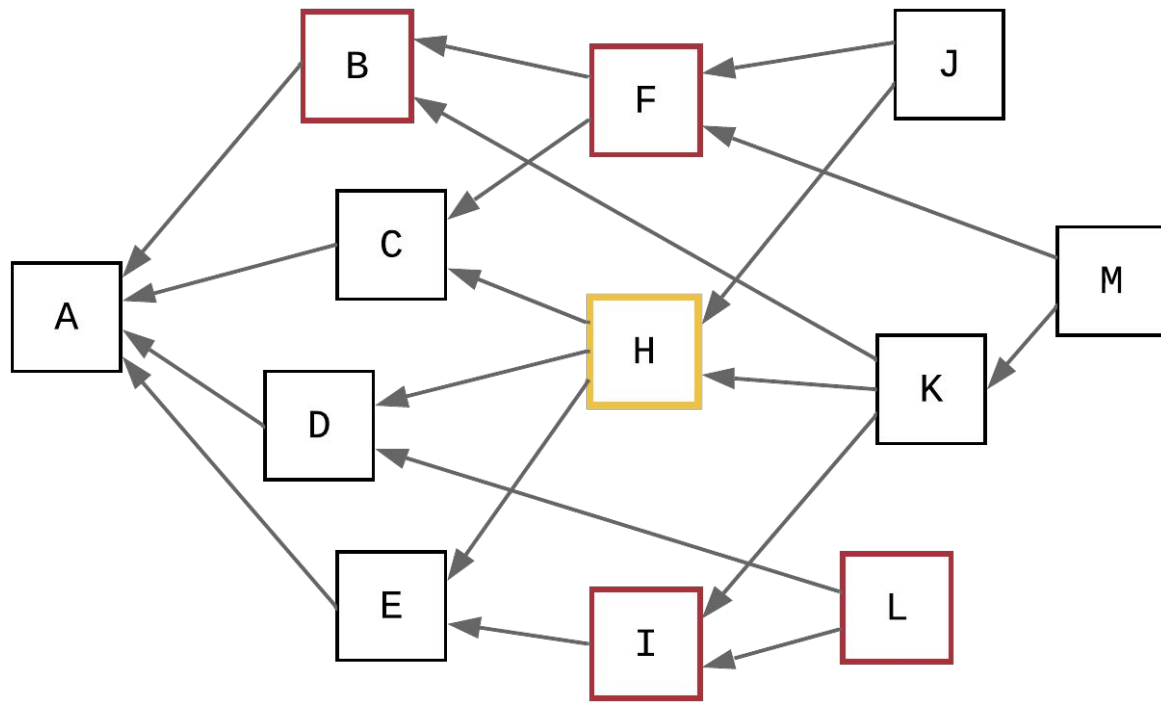


$G(V, E)$

$\text{past}(H) = \{A, C, D, E\}$

$\text{future}(H) = \{K, J, M\}$

DAGs - notation



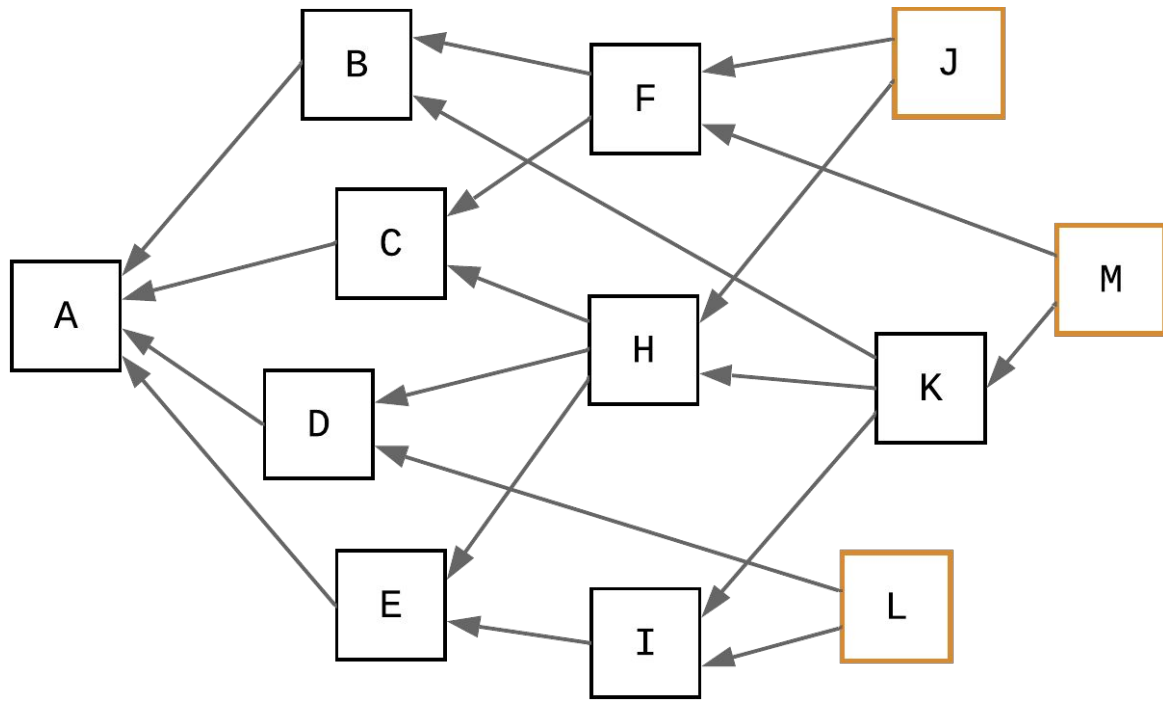
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$\text{past}(H) = \{A, C, D, E\}$

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$\text{anticone}(H) = \{B, F, I, L\}$

DAGs - notation



$G(V, E)$

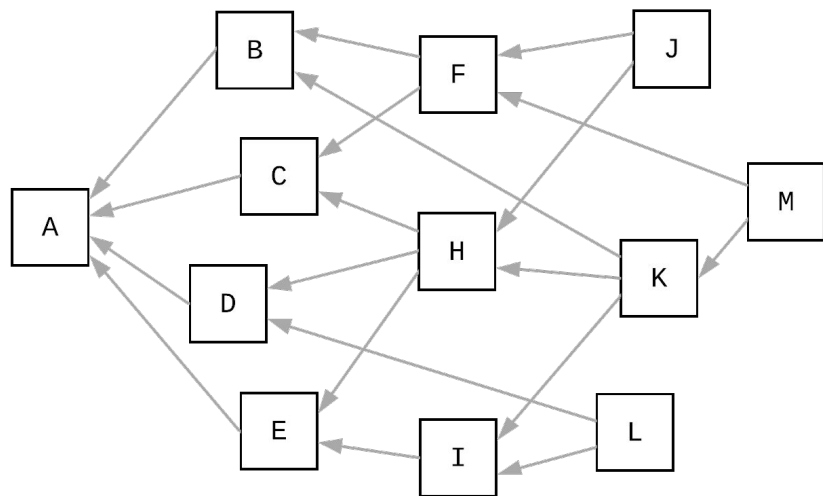
$\text{past}(H) = \{A, C, D, E\}$

$\text{future}(H) = \{K, J, M\}$

$\text{anticone}(H) = \{B, F, I, L\}$

$\text{tips}(G) = \{J, L, M\}$

DAGs - topological ordering



*“a topological sort or topological ordering of a directed graph is a a linear ordering of [...] vertices such that for every directed edge uv from vertex u to vertex v , u comes before v in the ordering”**

{A, B, C, F, D, E, H, J, I, K, M, L}

* https://en.wikipedia.org/wiki/Topological_sorting

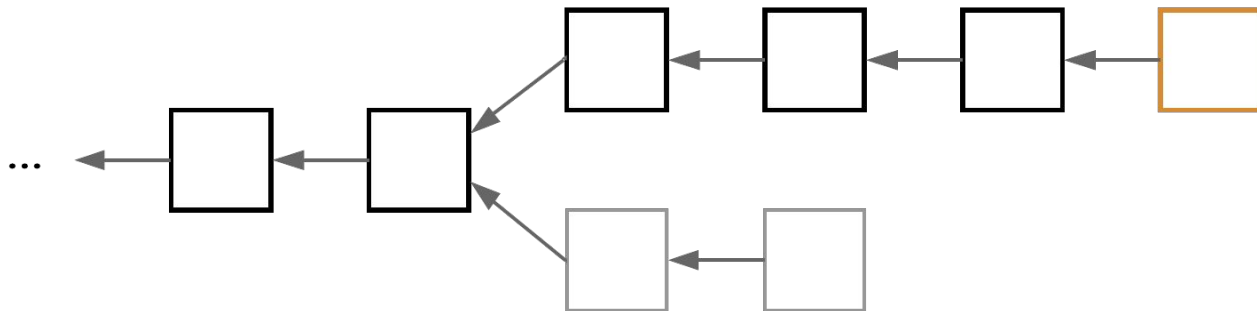
example and notation adopted from: Sompolinsky, Y. (2018). PHANTOM, GHOSTDAG - Two Scalable BlockDAG protocols

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blockDAG - main ideas

- **exclusive protocols** like the *longest chain rule* have numerous drawbacks
 - high block creation rate results in many conflicts
 - orphan blocks/chains: performance impact, wasted work
 - uneven mining rewards

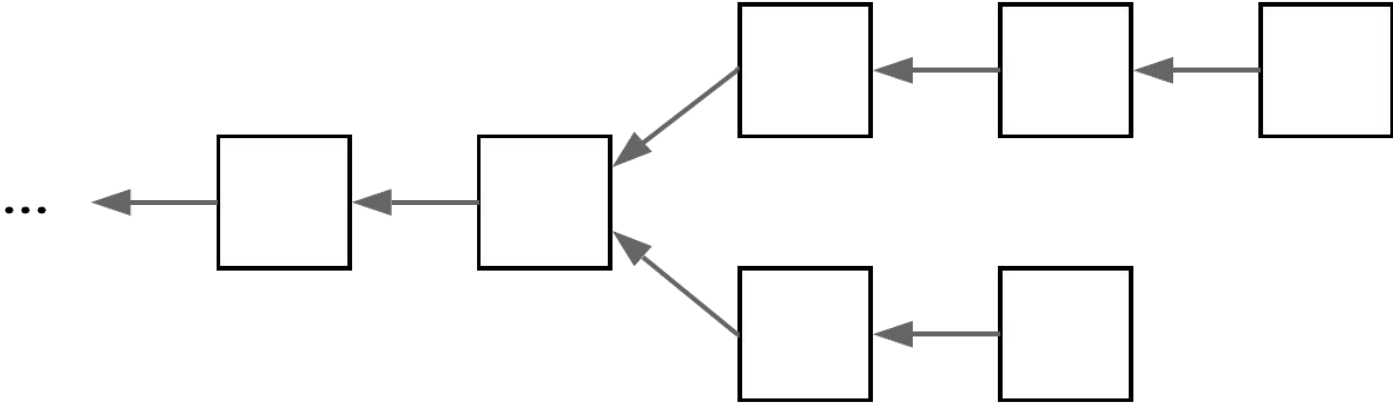


blockDAG - main ideas

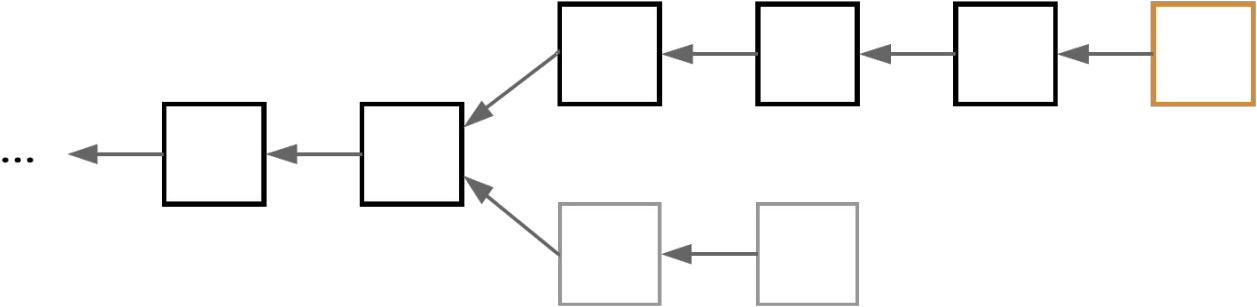
- use **inclusive protocols** instead
 - incorporate **all blocks** into a **DAG structure**
 - **separate mining and consensus**
 - no need to resolve conflicts during block creation
 - consensus on the transaction level
 - derive robust block order and accept transactions in order
- why is this good?
 - tolerance for larger blocks and slower connections (throughput & fairness)
 - incentivize miners to include smaller transactions to minimize collisions

blockDAG - overview

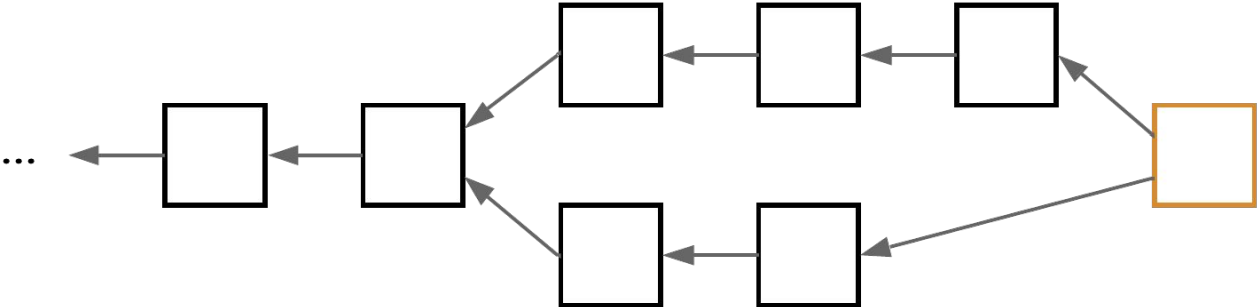
- 1. how to append new blocks?**
2. how to choose the main chain?
3. how to accept transactions?
4. how do distribute rewards?
5. how to choose which transactions to mine?
6. how to prevent attacks?



Bitcoin:

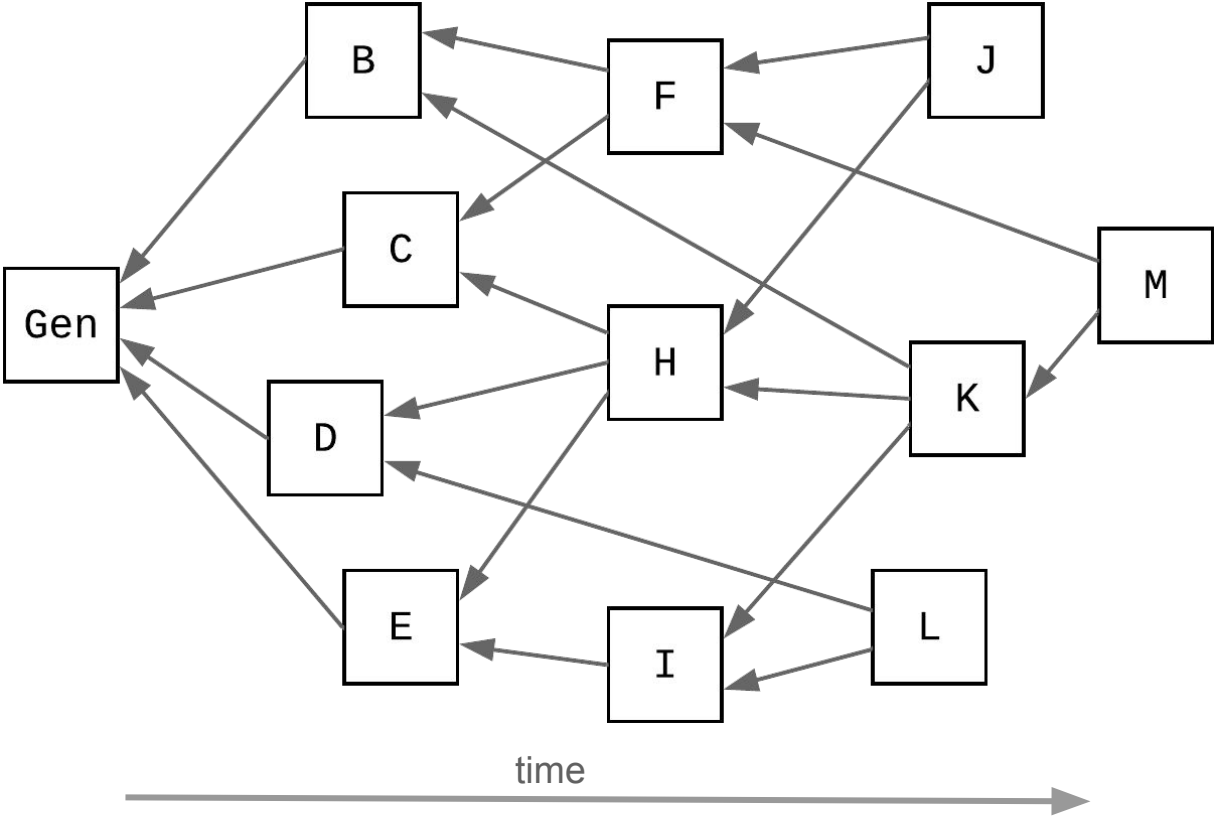


blockDAG:



mining in blockDAGs

- block creation rules
 1. when creating or receiving a block, transmit the block to all peers
 2. when creating a block, reference all tips of the locally-observed DAG
- potential attack scenarios
 1. withhold blocks
 2. omit references, build upon attacker subDAG



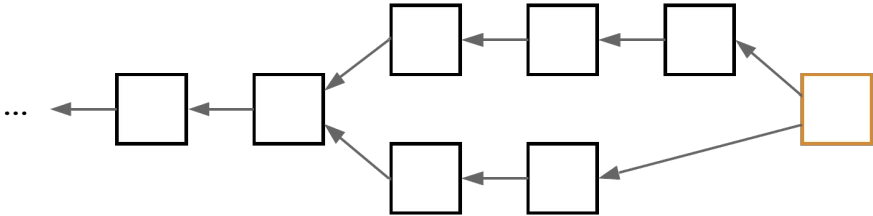
blockDAG - overview

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how to choose the main chain?

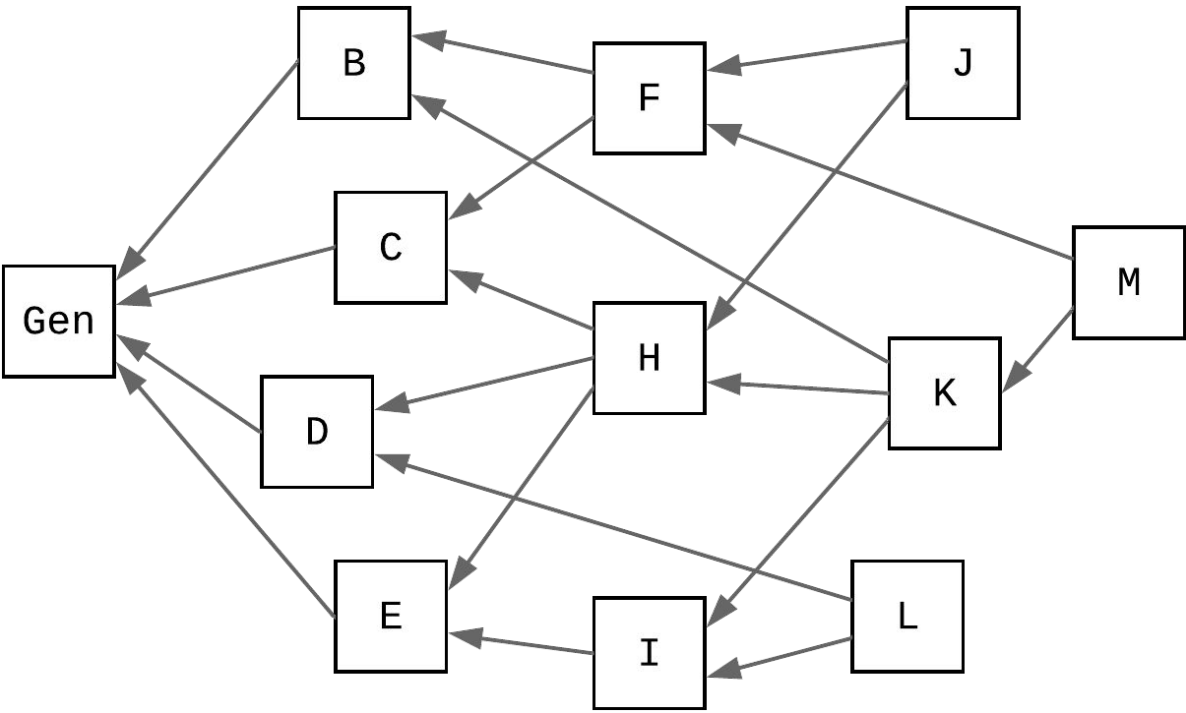
- main insight:

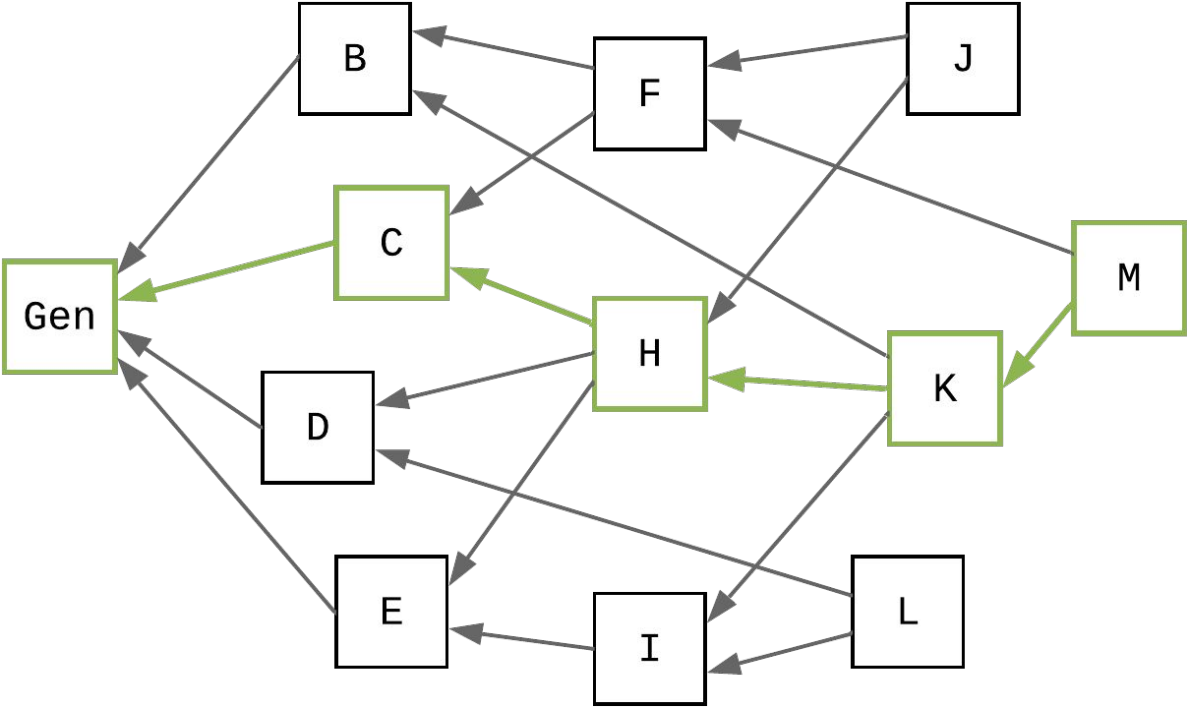
*Given a blockDAG, any node can **simulate** the underlying chain selection rule: we can simulate the longest-chain rule, for example, by recursively selecting in each block a single link—the one leading to the longest chain.*



- chain selection rule F:

$F(G)$ is a maximal chain in G





(longest-chain rule)

blockDAG - overview

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how to accept transactions?

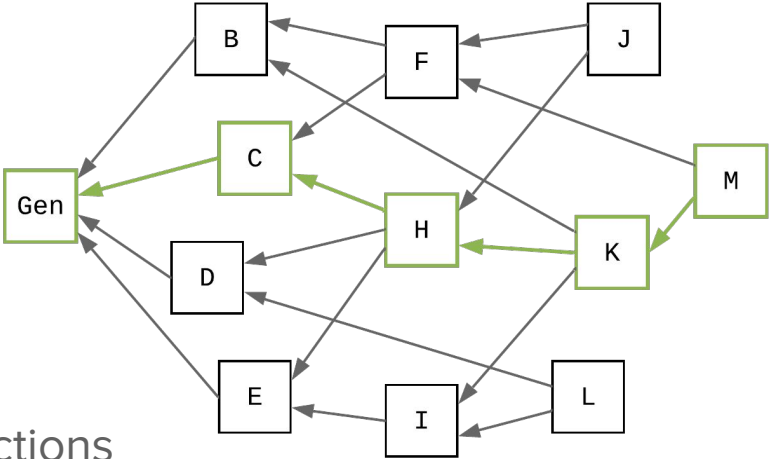
a) exclusive protocol

keep main-chain transactions only

b) inclusive protocol

accept non-conflicting off-chain transactions

- 1. order all blocks in $\text{past}(B)$
- 2. find maximal consistent set of transactions



inclusive protocol - linear block order

- order all blocks in `past(B)`:

post-order traversal

visit each predecessor recursively

follow order of references

main-chain parent is first in order

inclusive-F(G, B, T):

```
if visited(B): return T
```

```
visited(B) = true
```

```
for i = 1 to m:
```

```
    Bi = B.get_parent(i)
```

```
    T = inclusive-F(G, Bi, T)
```

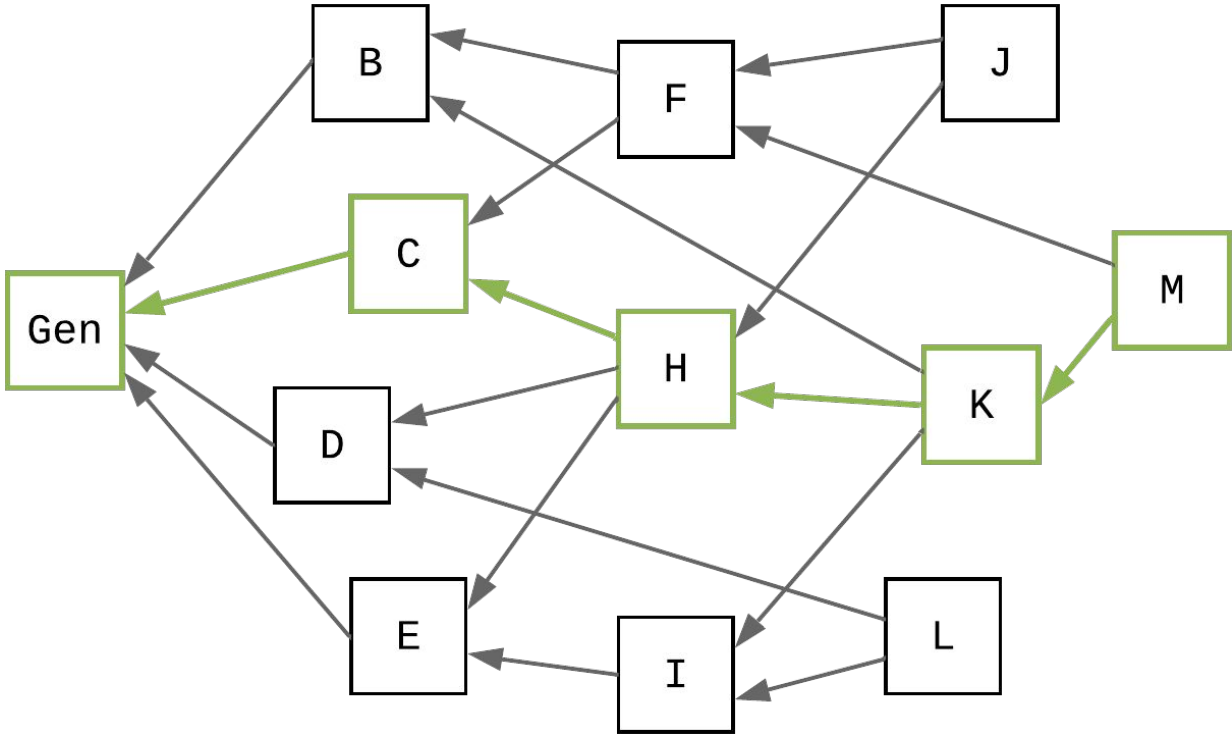
```
foreach tx in B:
```

```
    if (consistent(tx, T)):
```

```
        T = T.add(tx)
```

```
return T
```

$\text{post-order}(M) \sim \text{post-order}(K) + \text{post-order}(F) + \{M\}$
 $\text{post-order}(M) = \{\text{Gen}, C, D, E, H, B, I, K, F, M\}$



inclusive protocol - transaction order and acceptance

- find maximal consistent set of transactions

following block order, keep first valid occurrence of each transaction

- example

-----	-----	-----	
1c0e3160	1c0e3160	0b300750	
6e343f4a	a0a60aef	6e343f4a	...
-----	-----	-----	

1c0e3160, 6e343f4a, ~~1c0e3160~~, a0a60aef, 0b300750, ~~6e343f4a~~, ...

(Bitcoin: input transactions must have appeared before)

blockDAG - overview

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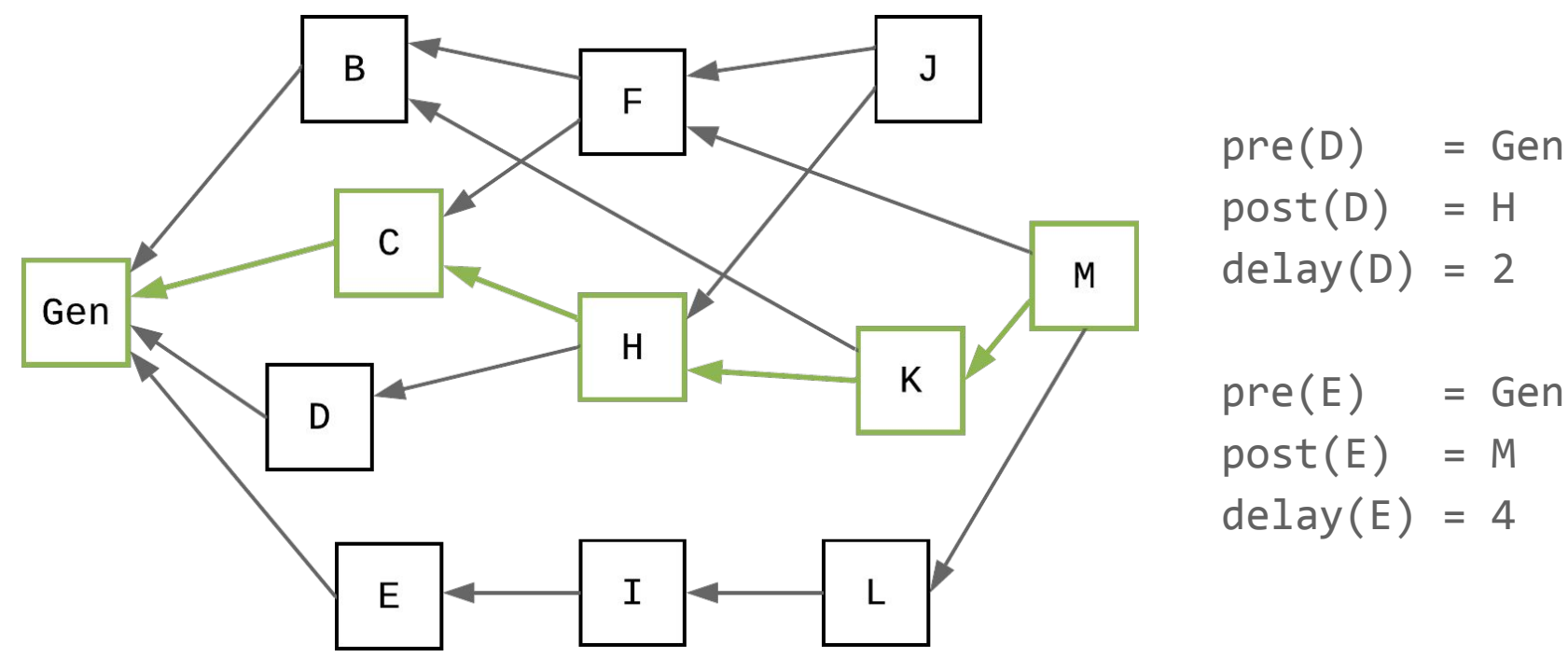
transaction fee distribution

- creator of block receives a portion of fees from each transaction accepted
 - reward including new transactions – even for slow or poorly-connected miners
 - but off-chain blocks might come from malicious nodes
- reward depends on how fast the block was referenced by the main chain

`pre(A) ~ latest main chain block reachable from A`

`post(A) ~ earliest main chain block from which A is reachable`

`delay(A) ~ post(A).height - pre(A).height`



* small change in example: removed H-E, K-I, L-D edges
Lewenberg, Y., Sompolinsky, Y., & Zohar, A. (2015). Inclusive Block Chain Protocols

discounted rewards

- introduce **discount factor** based on block delay to disincentivize malicious nodes

$$\text{reward}(A) = \gamma(\text{delay}(A)) \cdot \sum_{tx \in T(A)} \text{fee}(tx) \quad \text{where } \gamma: \mathbb{N} \cup \{0\} \rightarrow [0,1]; \quad \gamma(0) = 1$$

- example

$$\gamma_0(d) = \begin{cases} 1 & 0 \leq c \leq 3 \\ \frac{10-d}{7} & 3 \leq c \leq 10 \\ 0 & 10 \leq c \end{cases}$$

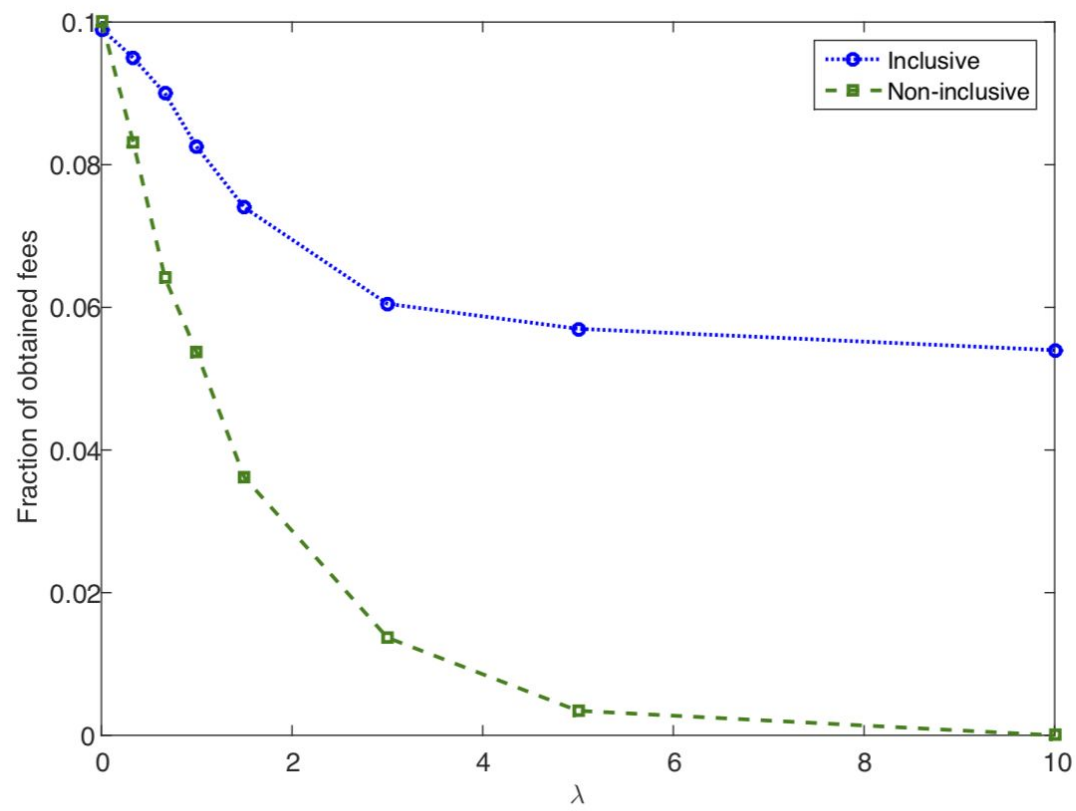


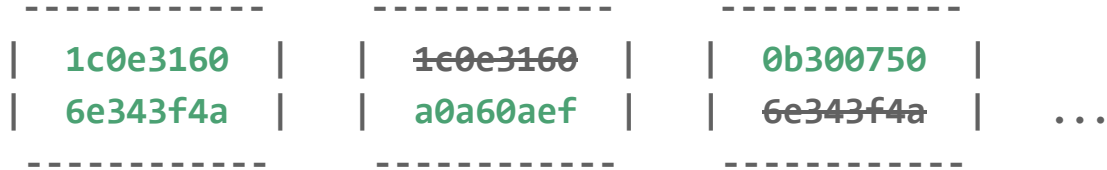
Fig. 3. The fraction of rewards obtained by a weak (10%) miner under delays.

blockDAG - overview

1. how to append new blocks?
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6. how to prevent attacks?

5. how to choose which transactions to mine?

- many collisions will reduce obtained block reward



- miners are incentivized to choose some low-fee transactions
- fewer collisions will increase overall throughput

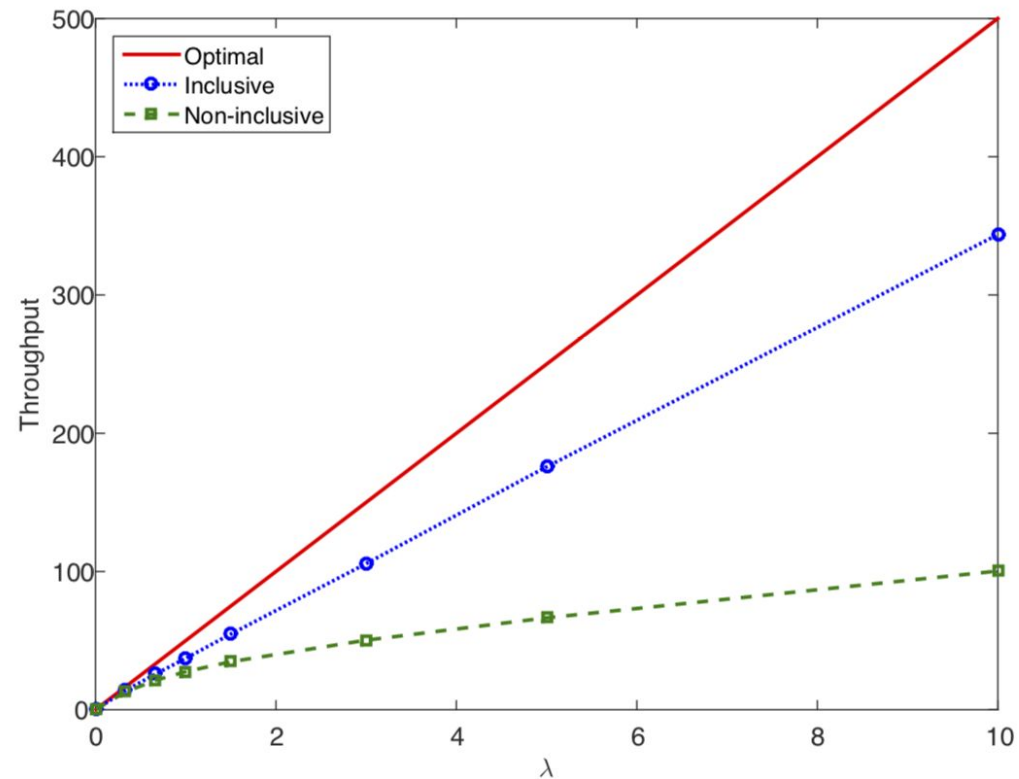


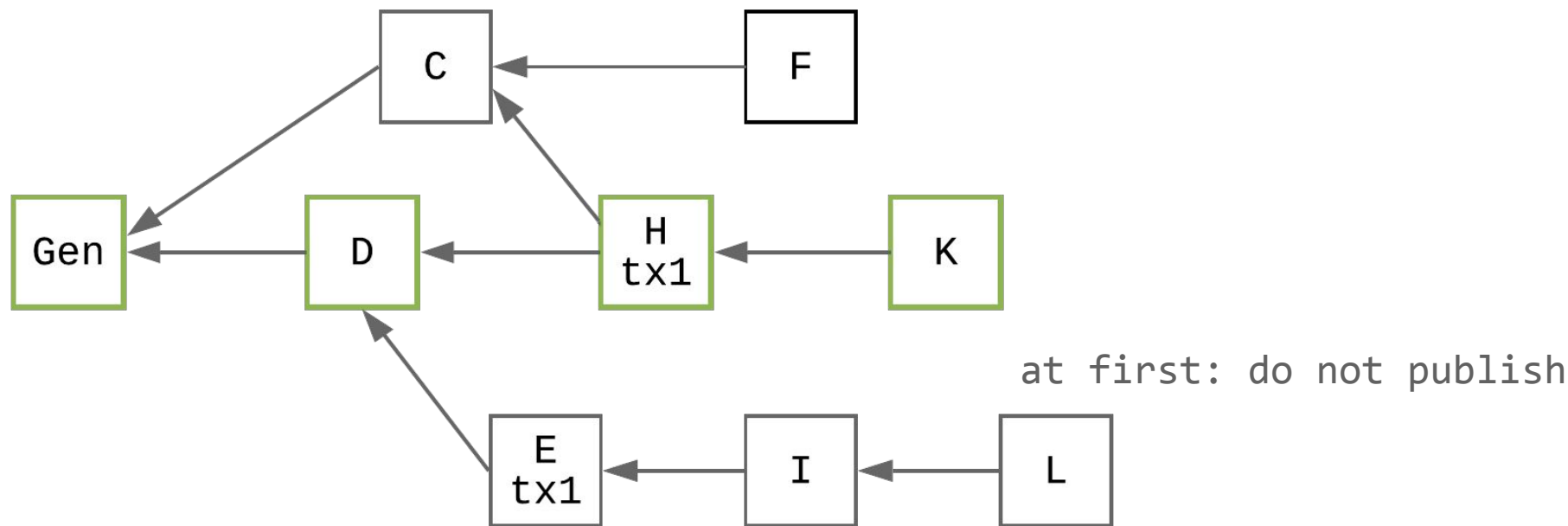
Fig. 2. The fraction of optimal throughput achieved in Inclusive and non-inclusive longest-chain protocols.

blockDAG - overview

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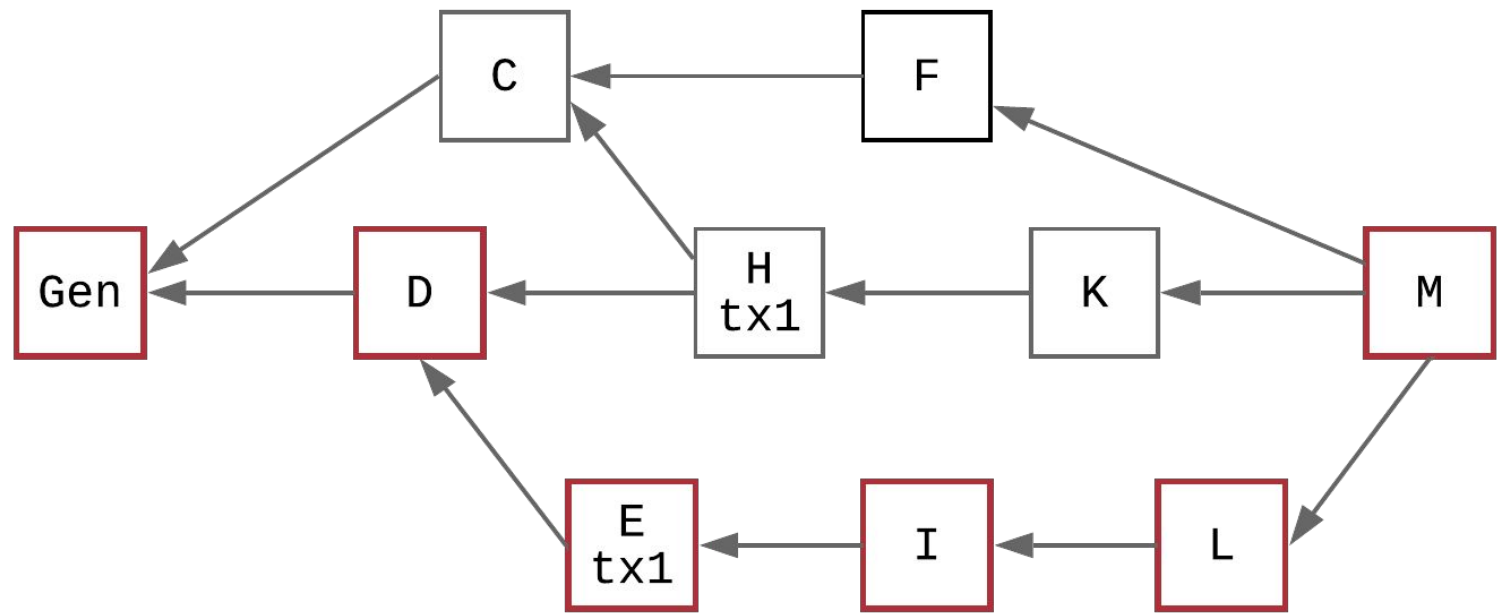
double spend attack

$\text{post-order}(K) = \{\text{Gen}, D, C, \underline{H}, K\}$



double spend attack

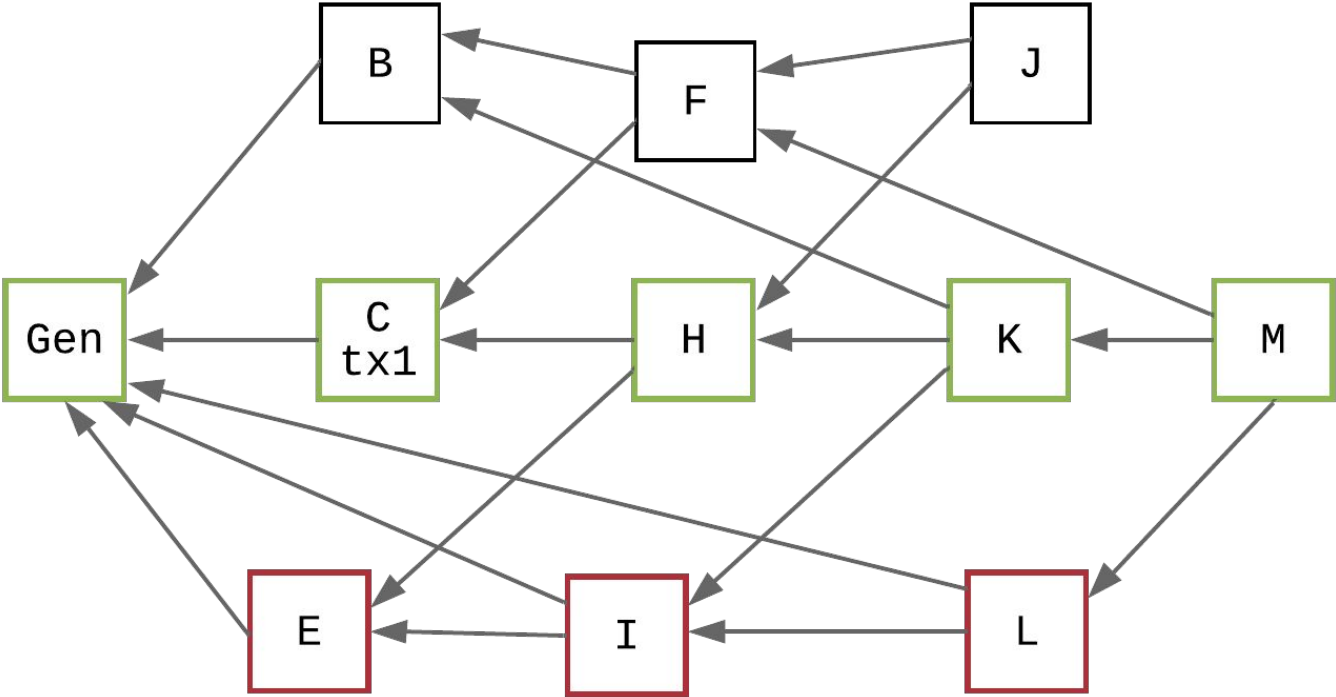
$\text{post-order}(M) = \{\text{Gen}, D, \underline{E}, I, L, C, \underline{H}, K, F, M\}$



security against double spend attacks

1. probability of successful attack
 - same security guarantees as non-inclusive version
 - security depends on underlying chain-selection mechanism
2. cost of attack
 - **off-chain block rewards reduce overall cost of attacks**
 - solution: discount factor, wait longer before accepting transaction

censorship (delayed service) attack



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SPECTRE* - main ideas

- before: all honest nodes must agree on the order of any two transactions
- SPECTRE: **weak liveness**
 - agree only on the order of transactions sent by honest nodes
 - conflicting transaction might stay pending indefinitely
 - cryptocurrency setting: conflicts are likely to be attempts at double spend

* Serialization of Proof-of-Work Events: Confirming Transactions via Recursive Elections
Sompolinsky, Y., Lewenberg, Y., & Zohar, A. (2016). SPECTRE - A Fast and Scalable Cryptocurrency Protocol

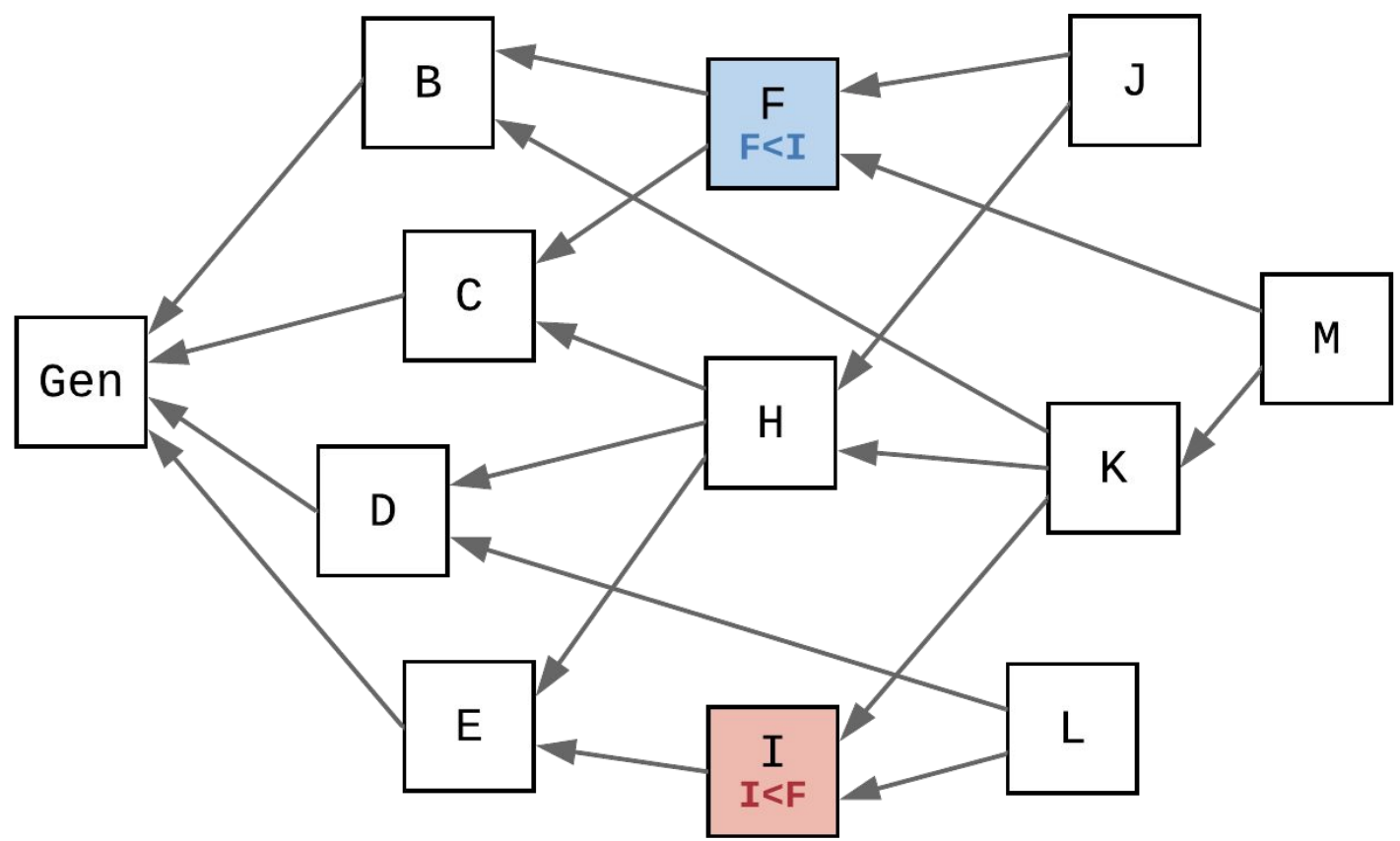
SPECTRE - overview

- 1. how to order blocks?**
2. how to accept transactions?
3. how to prevent attacks?

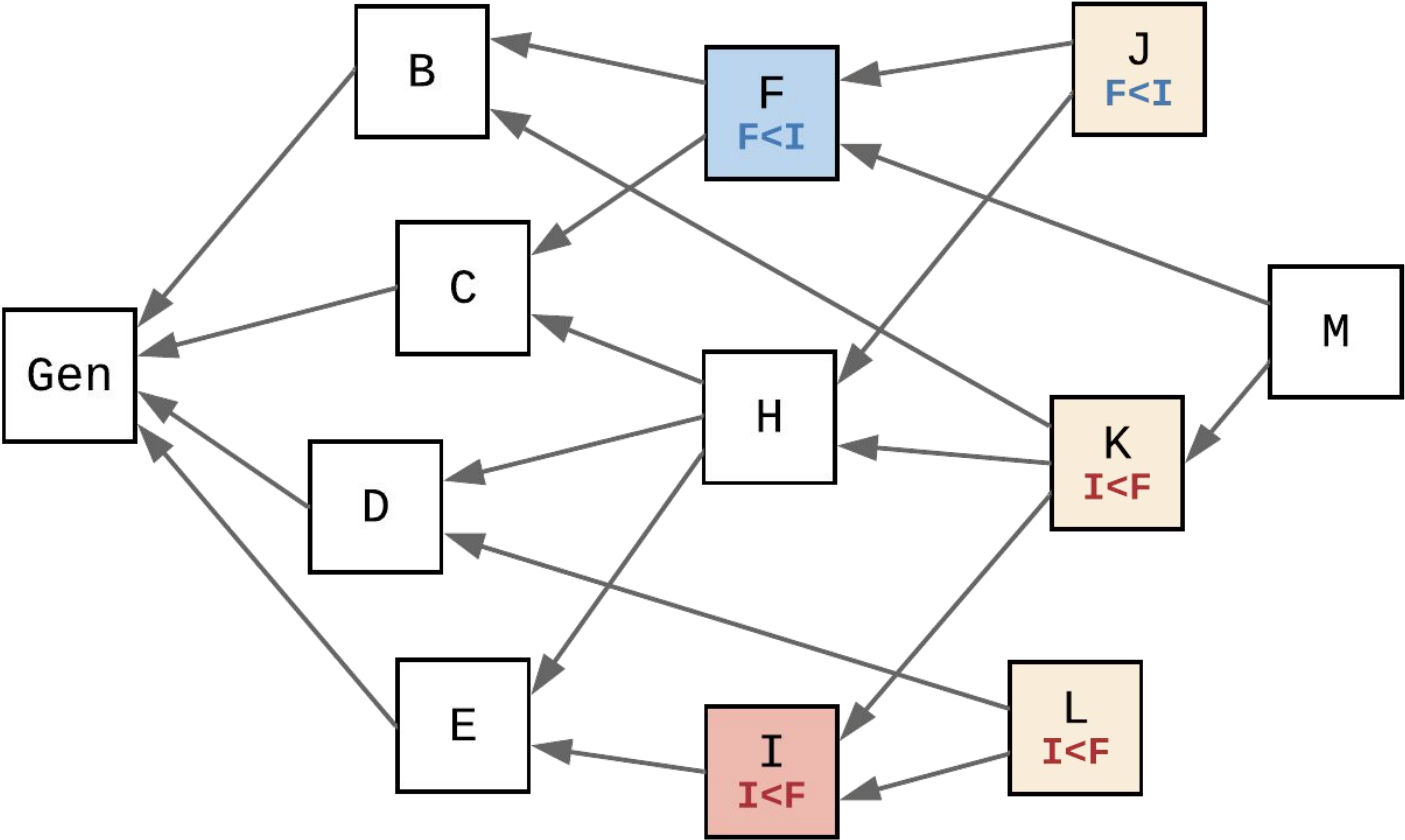
pairwise ordering of blocks

- each block \mathbf{z} votes about the order of every pair of blocks \mathbf{x} and \mathbf{y}
 - a) $\mathbf{x} \in \text{past}(\mathbf{z}), \mathbf{y} \notin \text{past}(\mathbf{z}) \Rightarrow \mathbf{x} < \mathbf{y}$
 - b) $\mathbf{x}, \mathbf{y} \in \text{past}(\mathbf{z}) \Rightarrow \text{majority on past}(\mathbf{z})$
 - c) $\mathbf{x}, \mathbf{y} \notin \text{past}(\mathbf{z}) \Rightarrow \text{majority on future}(\mathbf{z})$
 - d) $\mathbf{x} \in \text{past}(\mathbf{z}) \Rightarrow \mathbf{x} < \mathbf{z}$
 $\mathbf{x} \notin \text{past}(\mathbf{z}) \Rightarrow \mathbf{z} < \mathbf{x}$
- implicit vote based on location in DAG
- pairwise order, **not total order**
- compatible with topological order

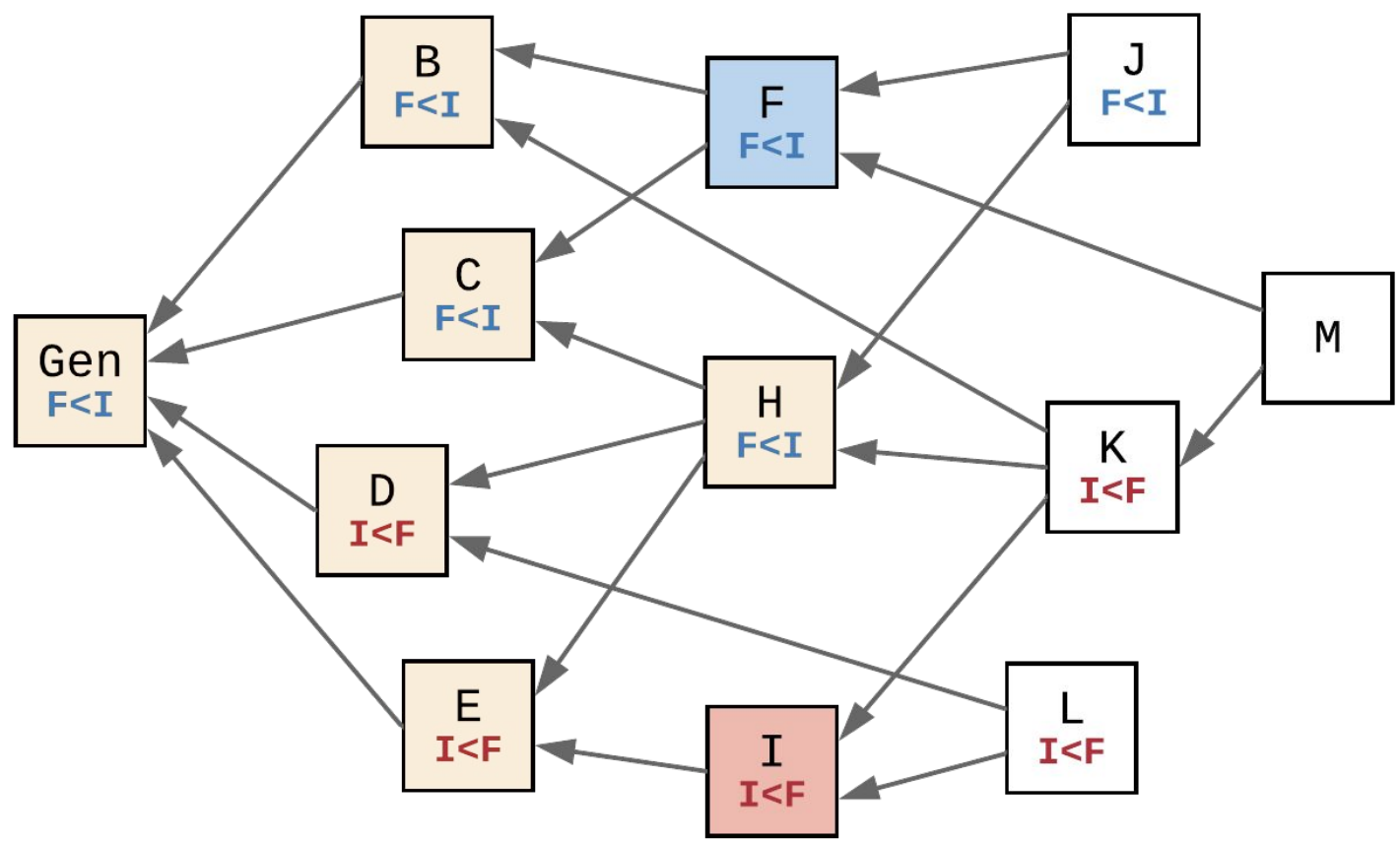
SPECTRE - 1. how to order blocks?



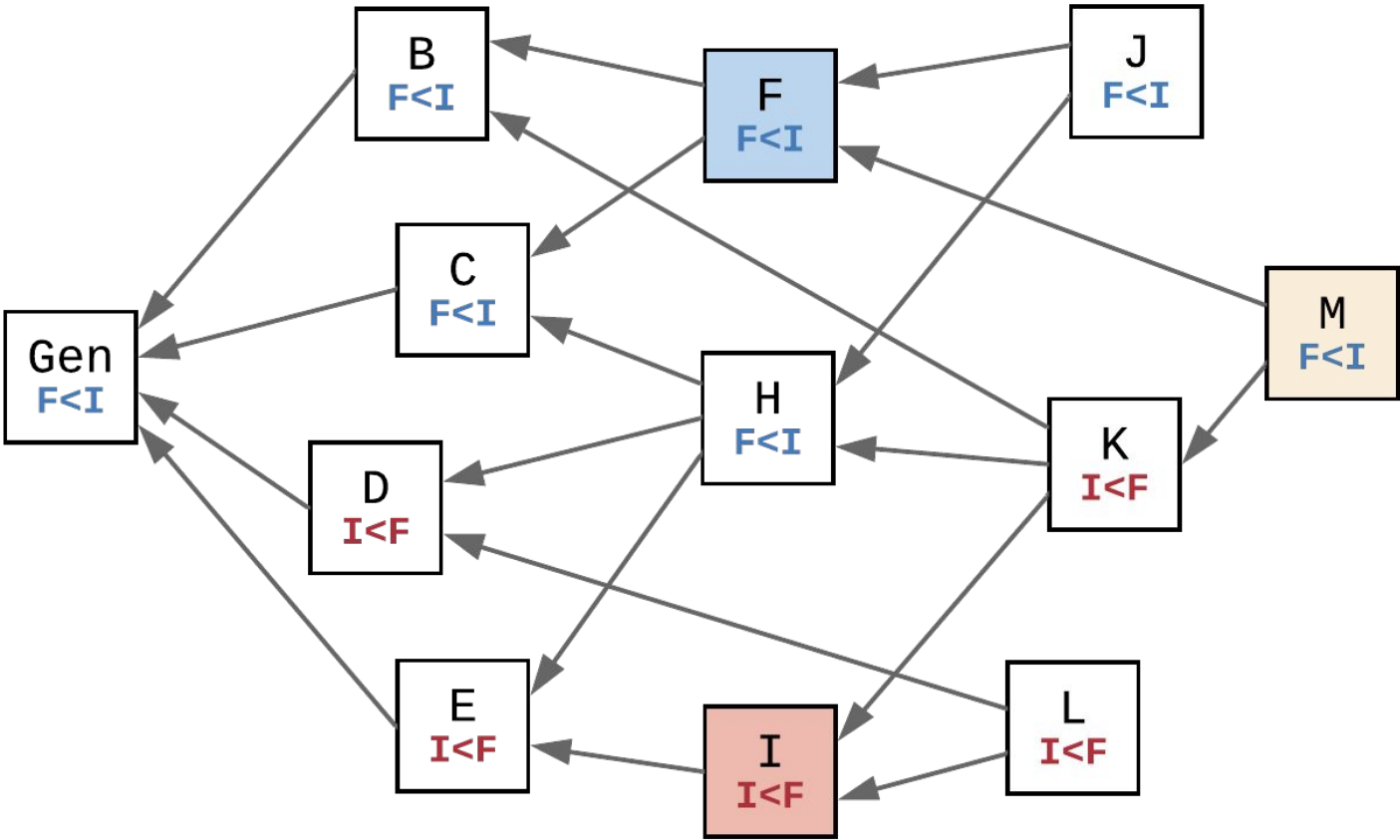
SPECTRE - 1. how to order blocks?



SPECTRE - 1. how to order blocks?

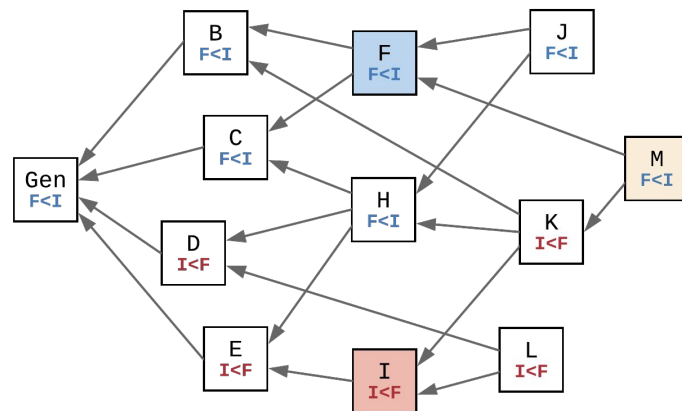


SPECTRE - 1. how to order blocks?



intuitions about votes

- vote in favor of visible blocks
attacker blocks lose votes as they are not referenced by honest blocks
- majority amplification
blocks added later will follow past majority decision about conflicts
- referencing recent blocks is beneficial
blocks from the past vote according to their future

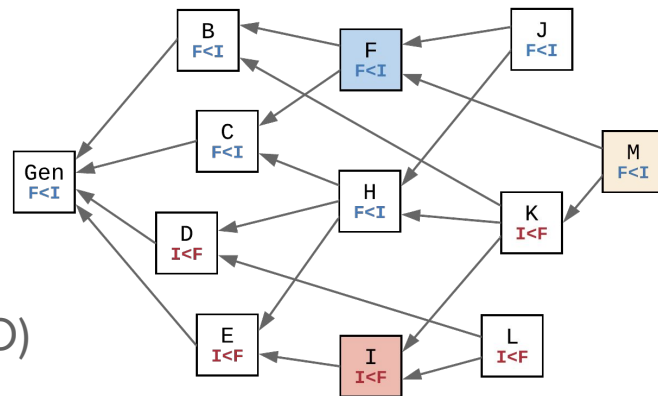


SPECTRE - overview

1. how to order blocks?
- 2. how to accept transactions?**
3. how to prevent attacks?

which transactions to accept?

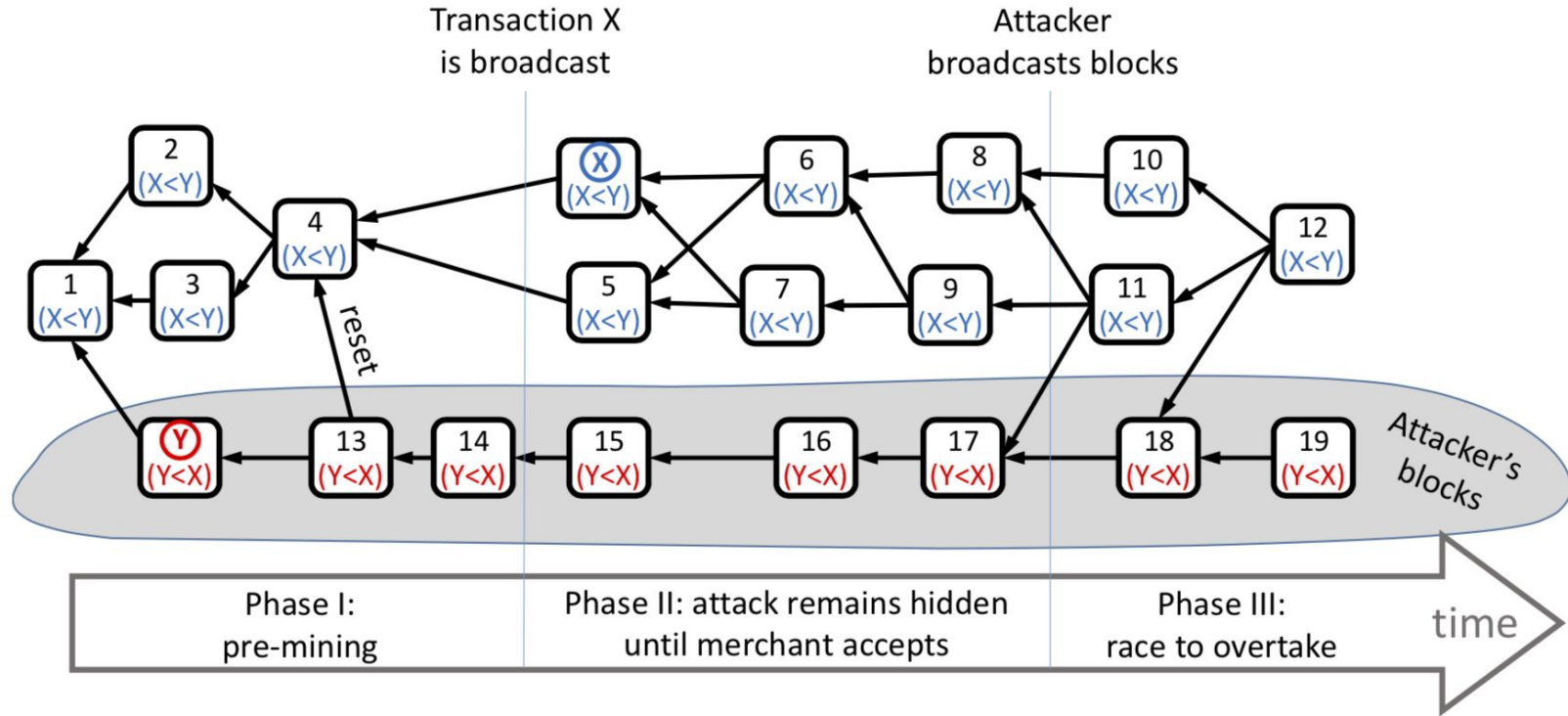
- **tx** is accepted iff
 1. all inputs of **tx** have been accepted (UTXO)
 2. for all conflicting transactions **tx'** in $\text{anticone}(\text{block}(\mathbf{tx}))$:
$$\text{block}(\mathbf{tx}) < \text{block}(\mathbf{tx}')$$
 3. for all conflicting transactions **tx''** in $\text{past}(\text{block}(\mathbf{tx}))$:
tx'' has been rejected



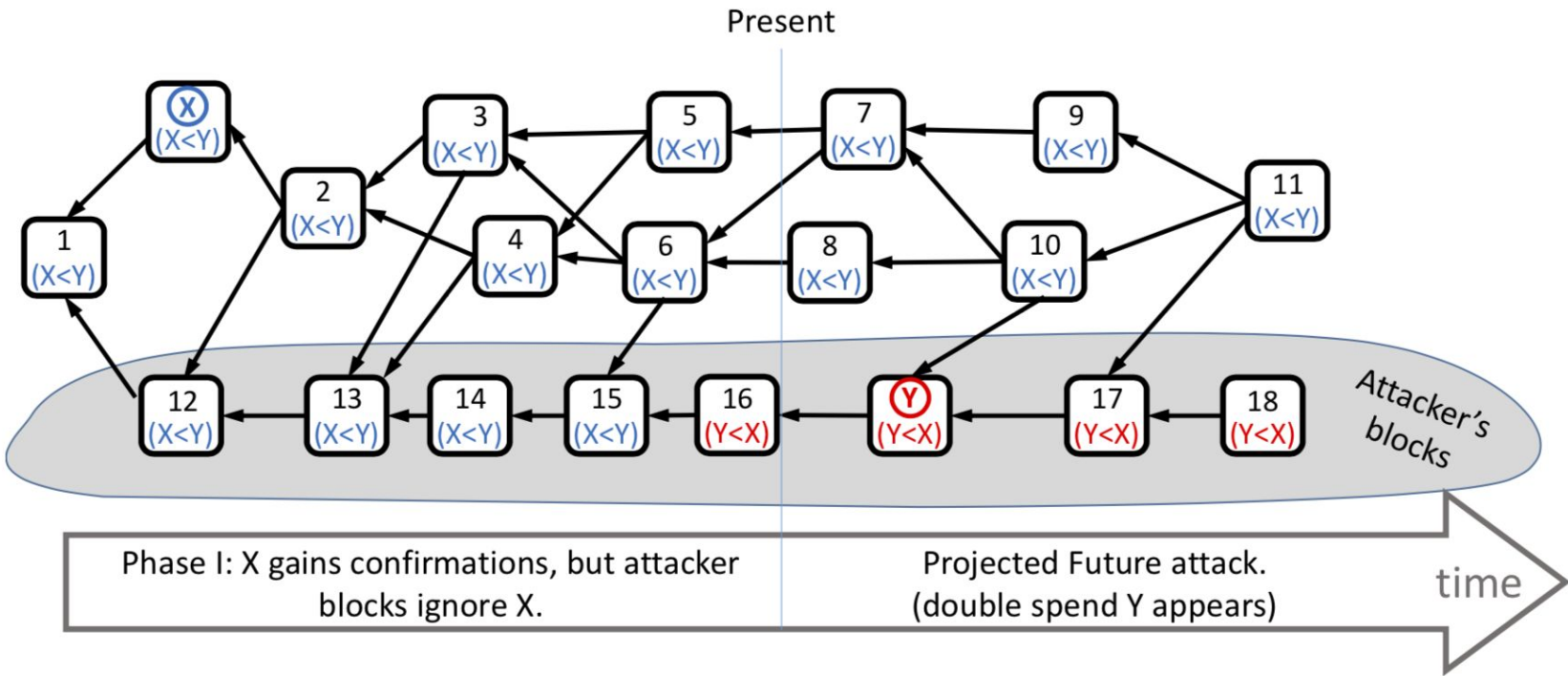
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double spend attack



censorship attack



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PHANTOM & GHOSTDAG - main ideas

- sacrifice some speed for total ordering
- honest blocks tend to form *well-connected* clusters

PHANTOM & GHOSTDAG - overview

1. incorporate all blocks into blockDAG
2. find a set of *well-connected* blocks
3. extend topological order to total order
4. accept transactions serially

what is “well-connected”?

- key insight

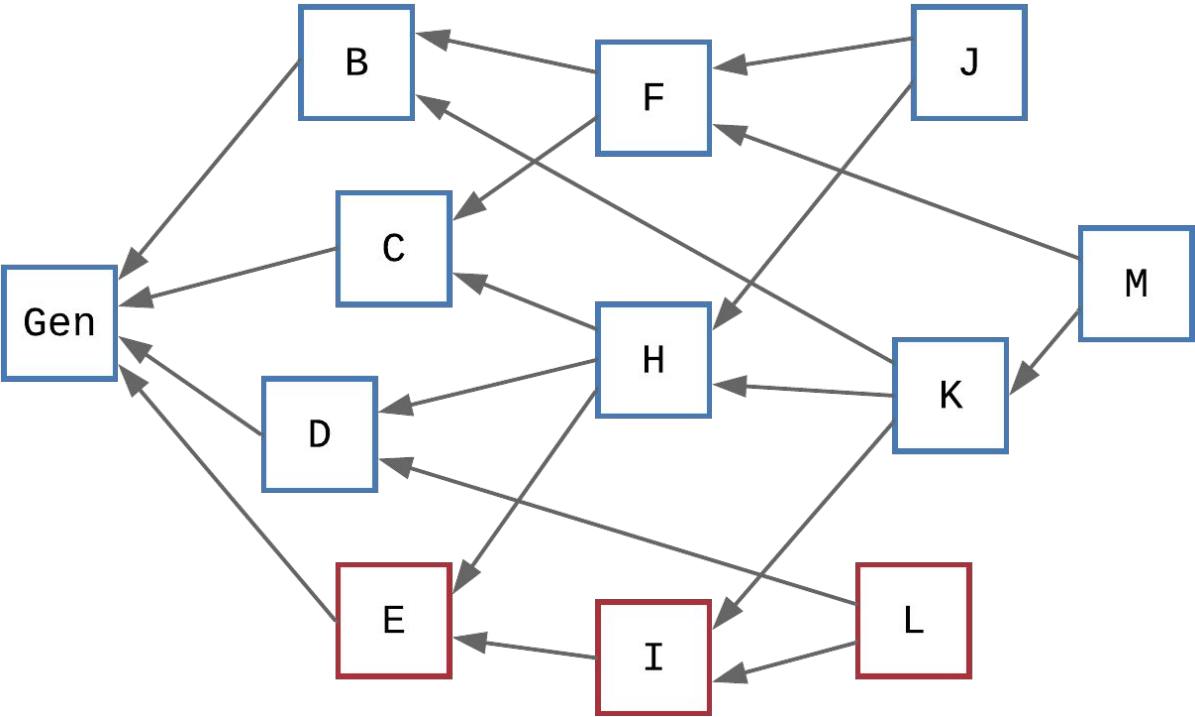
blocks will have a limited number of “honest blocks” in their anticone
i.e. blocks created in the interval $[t - D, t + D]$

- Def. a set of blocks S is a k -cluster if

$$\forall B \in S: |\text{anticone}(B) \cap S| \leq k$$

- $\text{MCS}_k(G)$: find maximum k -cluster subDAG

what is “well-connected”?



maximum 3-cluster

how to find the maximum cluster?

- PHANTOM

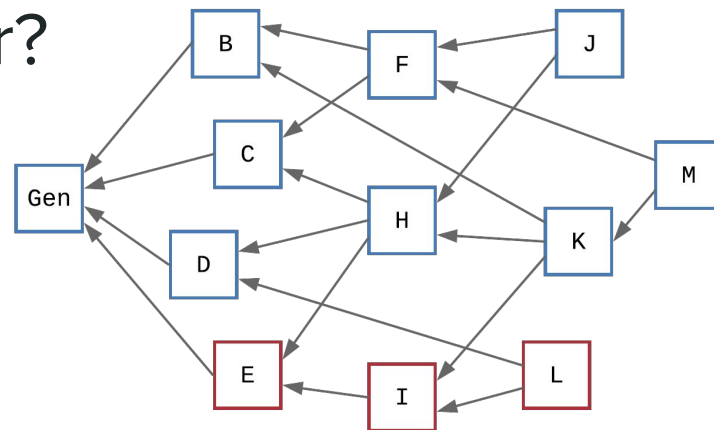
solve the $MCS_k(G)$ optimization problem

NP-hard

- GHOSTDAG: greedy version

inherit blue set of best tip from past

extend in a way that preserves the k-cluster property



how to find the maximum cluster?

```
orderDAG(G, k):
```

```
if G == {genesis}:
```

```
    return ({genesis}, [genesis])
```

```
# inherit from best tip
```

```
blue_G = {}
```

```
foreach B in tips(G):
```

```
    (blue_B, ord_B) = orderDAG(past(B, G), k)
```

```
    if blue_B > blue_G:
```

```
        Bmax = B
```

```
        blue_G = blue_B.add(B)
```

```
        ord_G = ord_B.append(B)
```

```
# extend with blocks from anticone
```

```
foreach B in anticone(Bmax, G):
```

```
    if is_cluster(k, blue_G.add(B)):
```

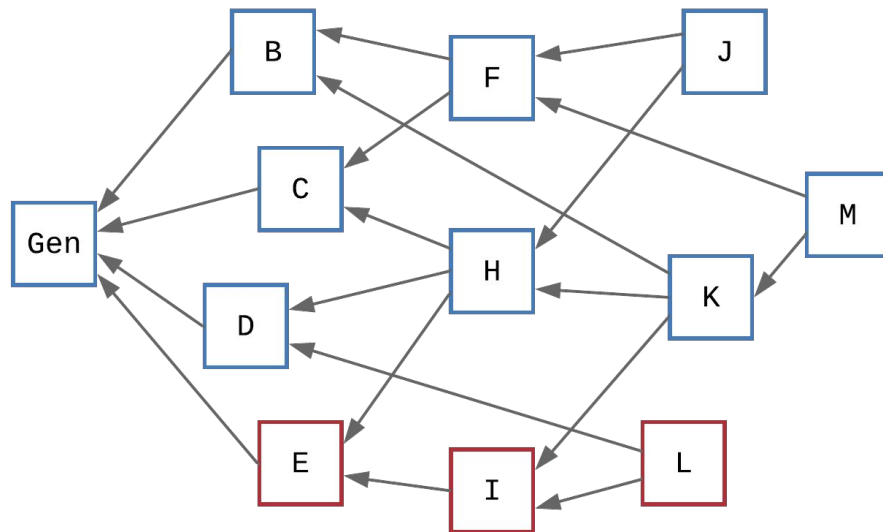
```
        blue_G = blue_G.add(B)
```

```
        ord_G = ord_G.append(B)
```

```
return [blue_G, ord_G]
```

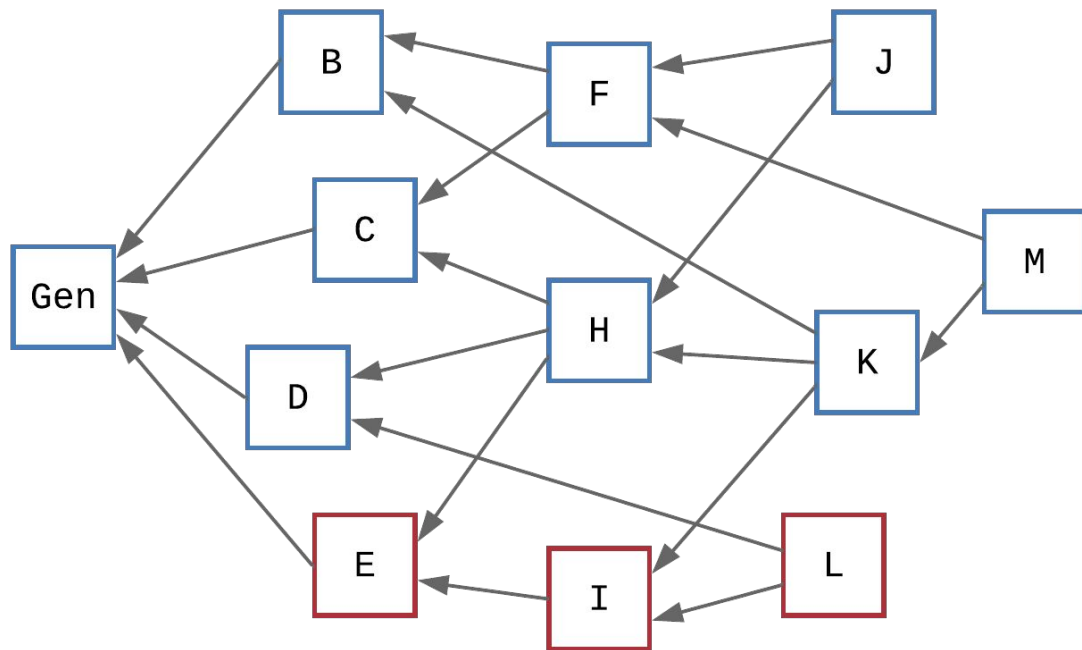
how to order blocks?

- order **blue** blocks in some topological order
- for any **blue** block B, add **red** blocks from $\text{past}(B)$ just before B in top. order



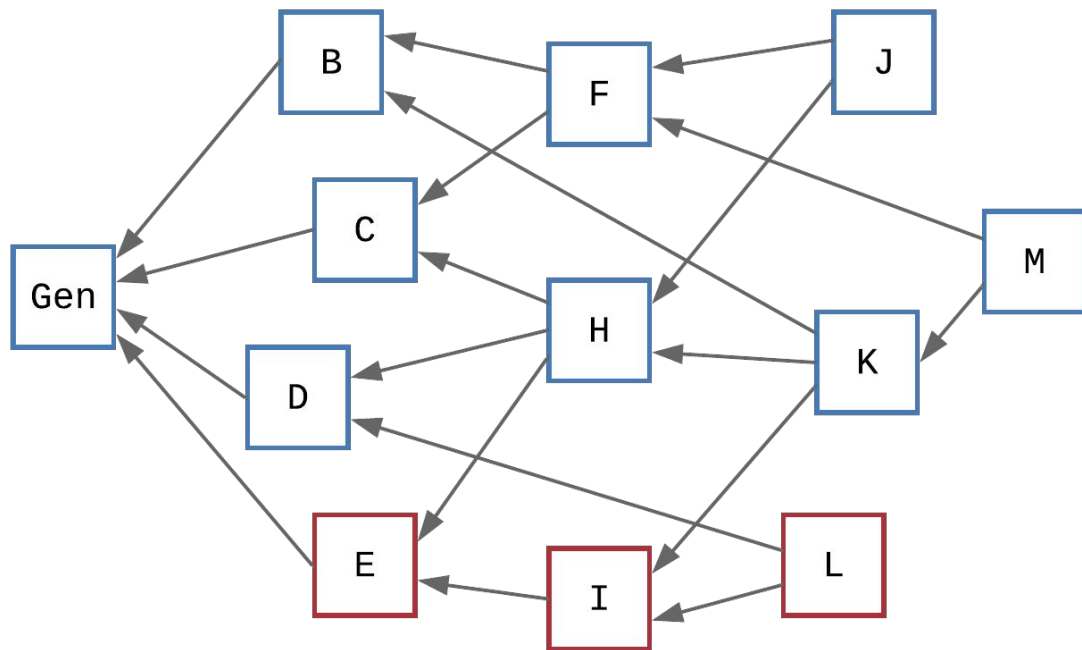
how to order blocks?

{Gen, B, C, F, D, H, J, K, M}



how to order blocks?

{Gen, B, C, F, D, E, H, J, I, K, M}



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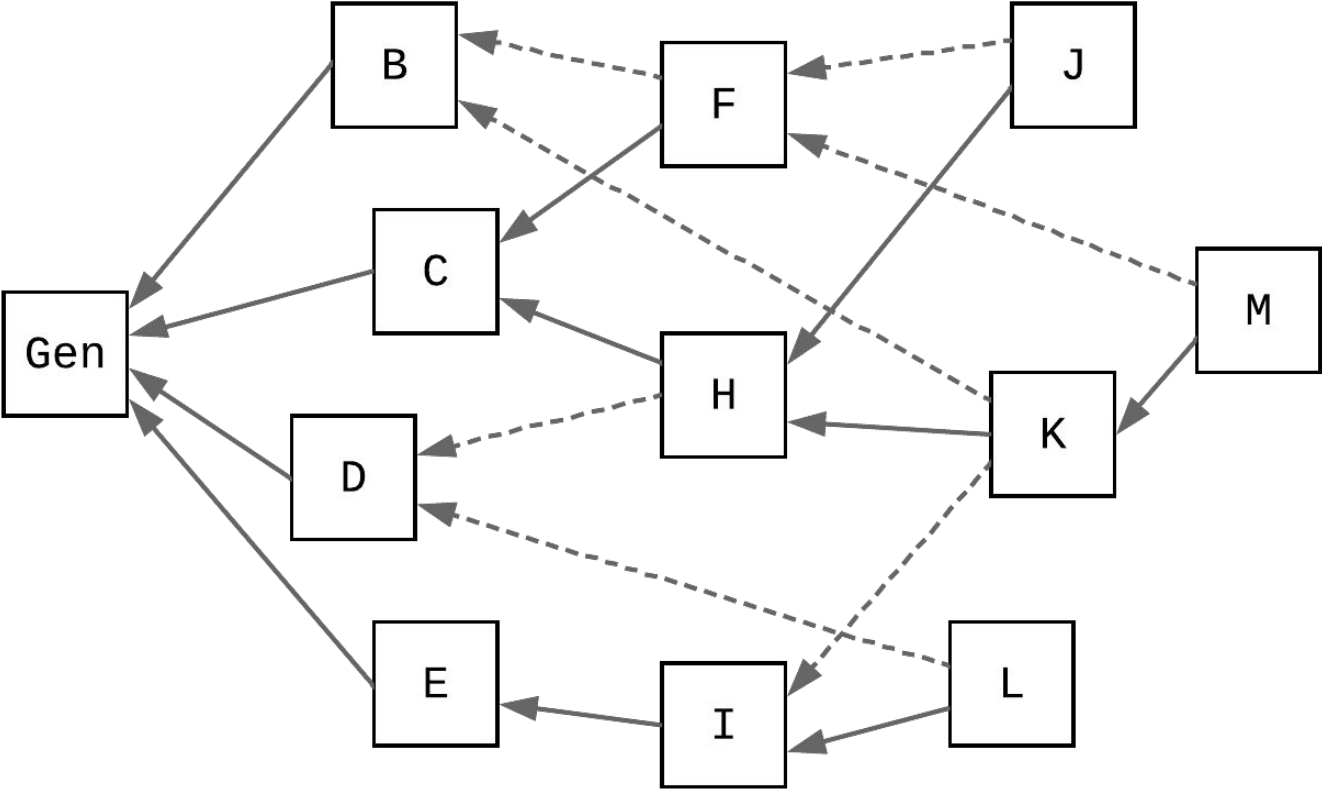
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Conflux - overview

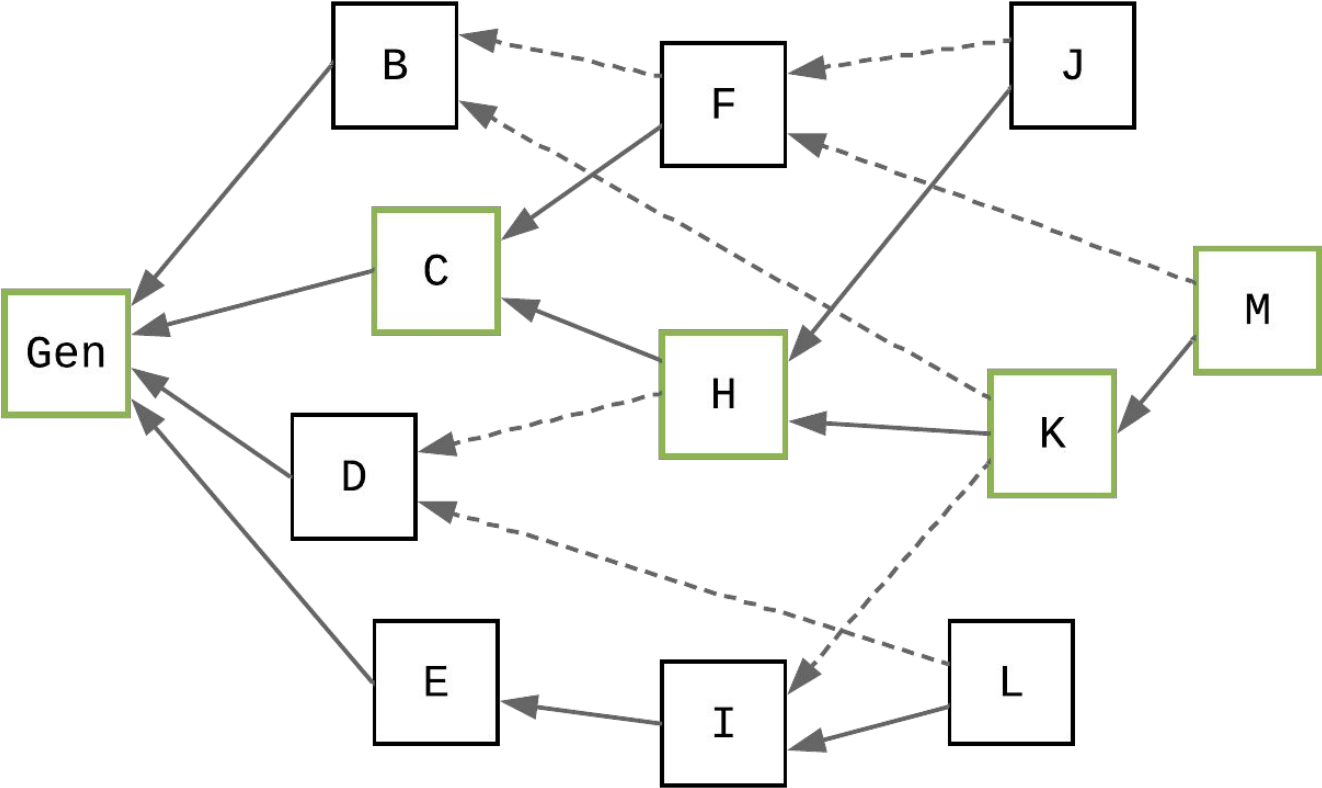
1. blocks have one **parent edge** and multiple **reference edges**
2. choose **pivot chain** based on parent edges
3. partition DAG into multiple epochs
4. derive total order

how are blocks created?

1. compute pivot chain (e.g. according to GHOST)
2. set last block as parent
3. reference all tips



* small change in example: removed H-E edge

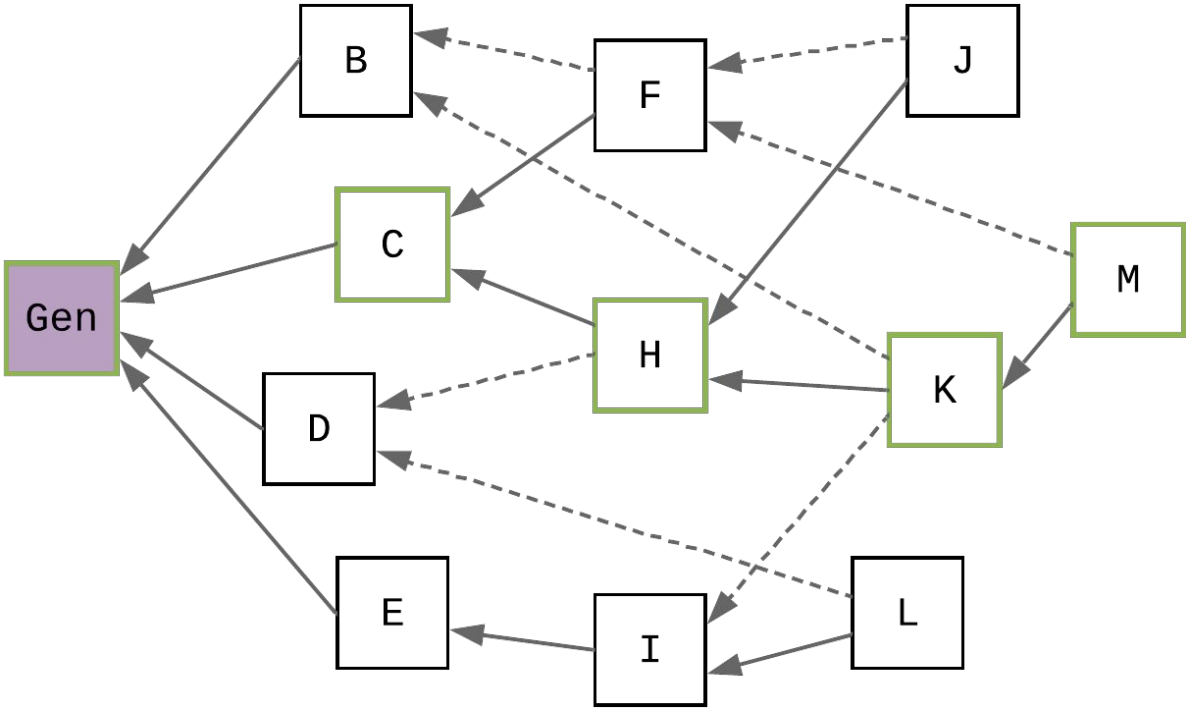


* small change in example: removed H-E edge

how are blocks ordered?

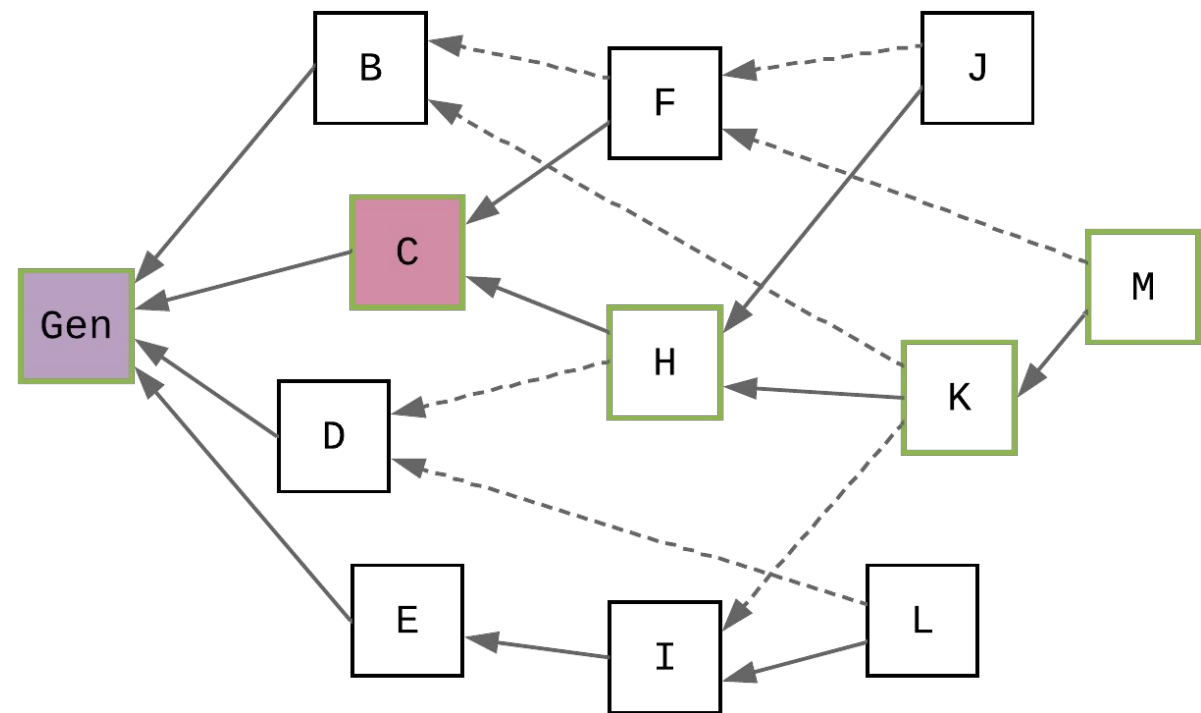
1. find epochs
 - B_i in pivot chain defines one epoch $_i$
 - epoch $_i$ contains blocks reachable from B_i that are not included previously
2. derive total order
 - sort epochs
 - sort blocks within epoch based on topological order
 - break ties deterministically using block hash

how are blocks ordered?



$$\text{epoch}_{\text{Gen}} = \{\text{Gen}\}$$

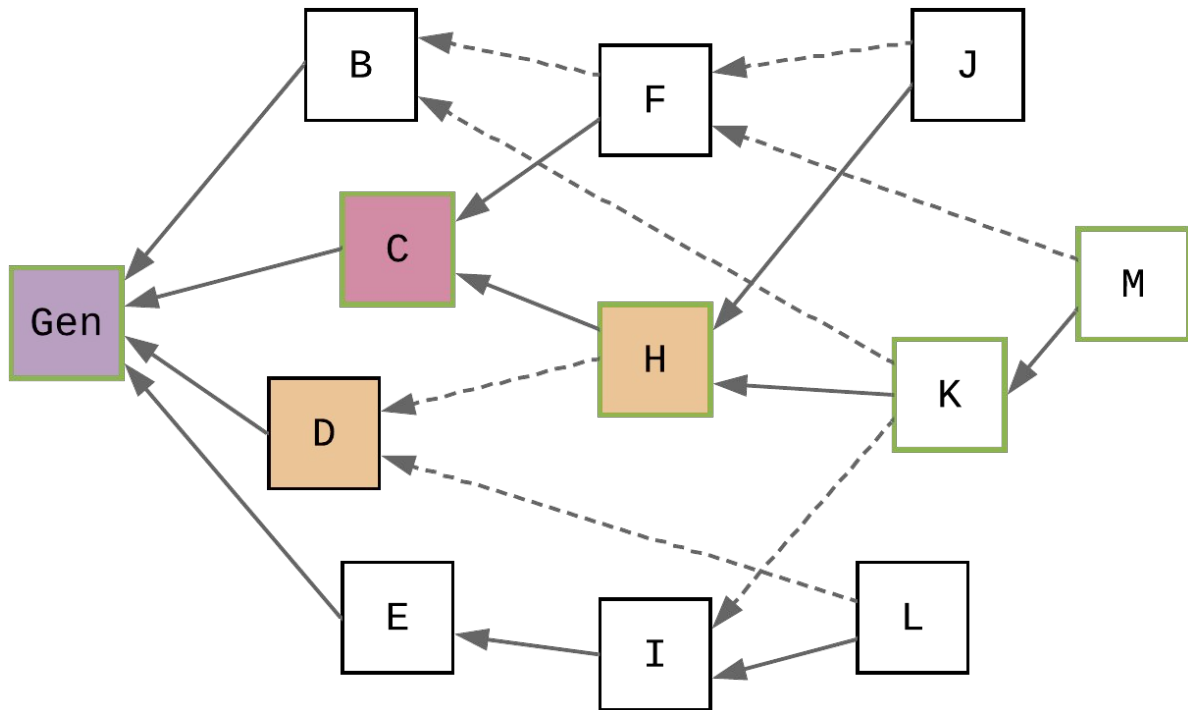
how are blocks ordered?



$epoch_{Gen} = \{Gen\}$

$epoch_C = \{C\}$

how are blocks ordered?

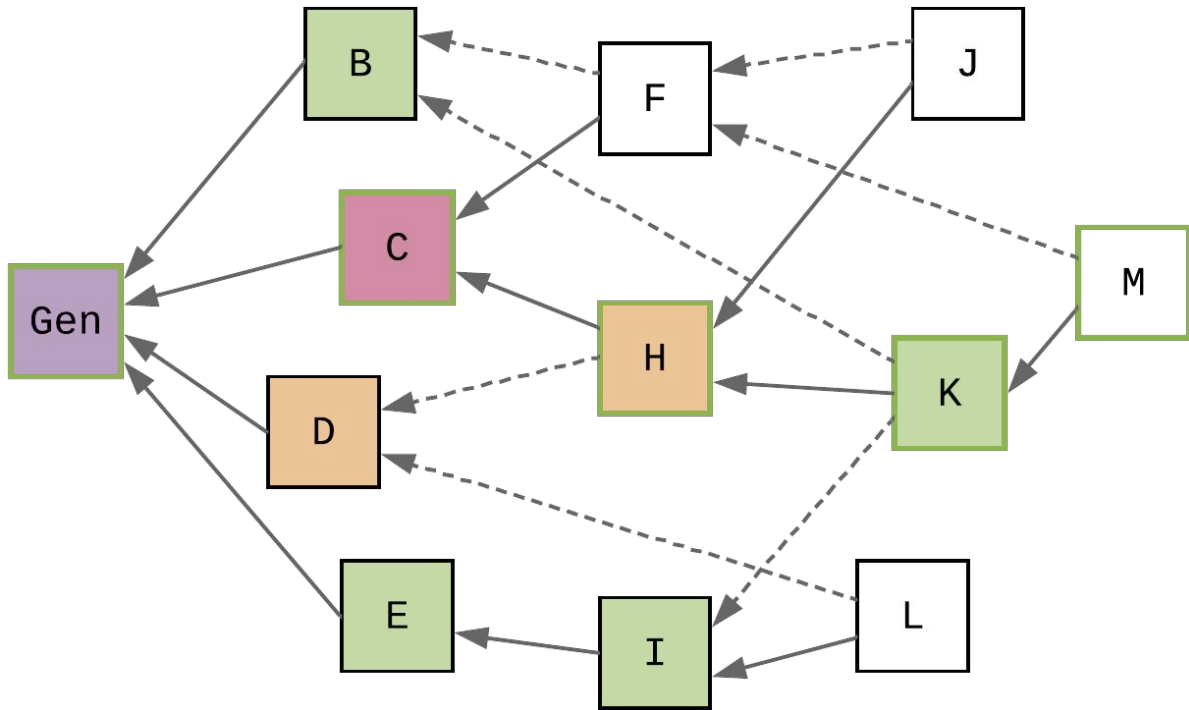


$\text{epoch}_{\text{Gen}} = \{\text{Gen}\}$

$\text{epoch}_C = \{C\}$

$\text{epoch}_H = \{D, H\}$

how are blocks ordered?



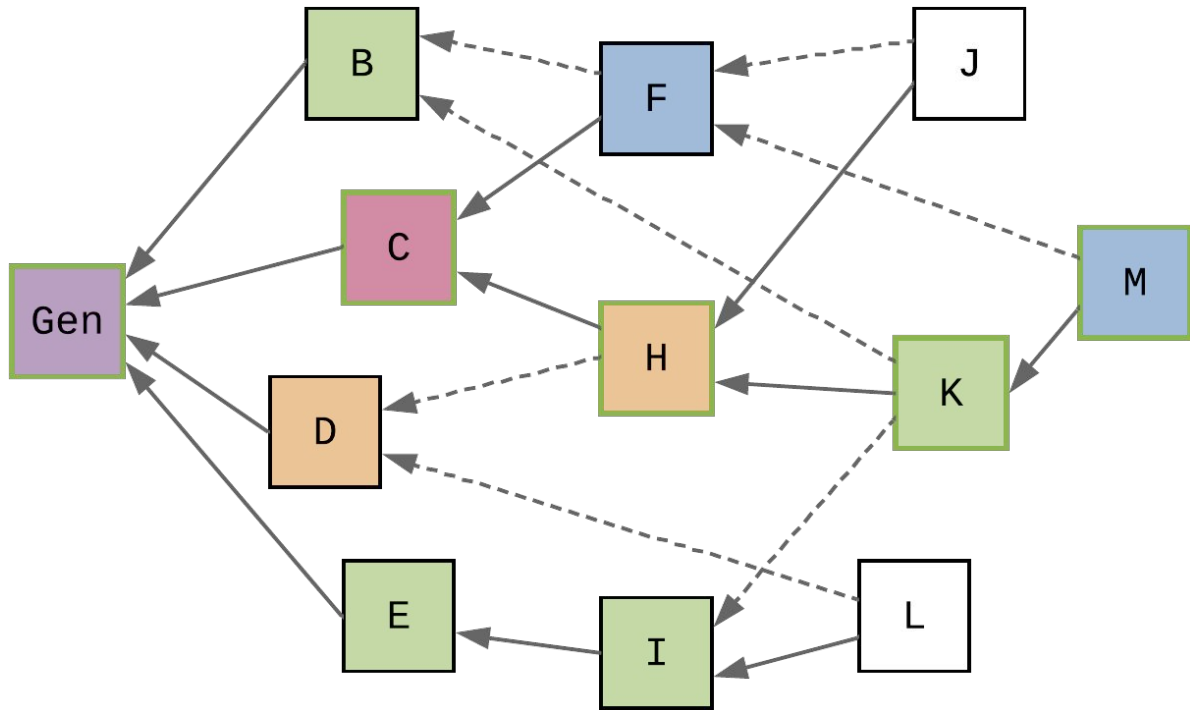
$\text{epoch}_{\text{Gen}} = \{\text{Gen}\}$

$\text{epoch}_C = \{C\}$

$\text{epoch}_H = \{D, H\}$

$\text{epoch}_K = \{B, E, I, K\}$

how are blocks ordered?



$\text{epoch}_{\text{Gen}} = \{\text{Gen}\}$

$\text{epoch}_{\text{C}} = \{\text{C}\}$

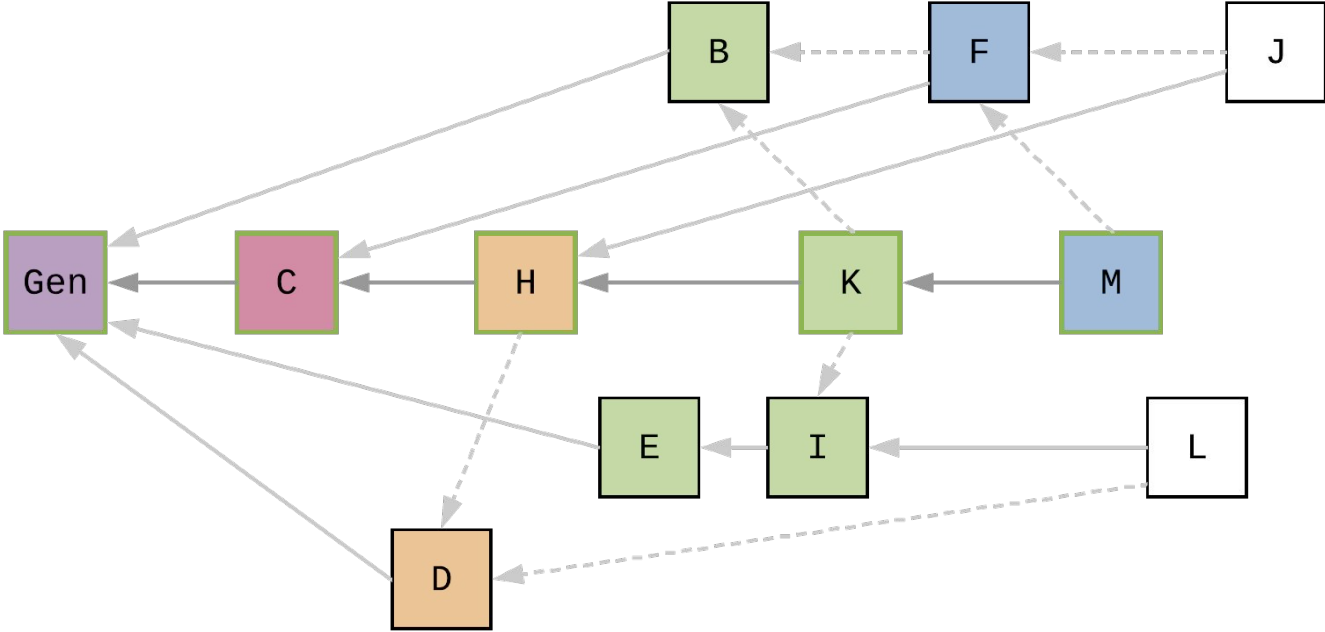
$\text{epoch}_{\text{H}} = \{\text{D}, \text{H}\}$

$\text{epoch}_{\text{K}} = \{\text{B}, \text{E}, \text{I}, \text{K}\}$

$\text{epoch}_{\text{M}} = \{\text{F}, \text{M}\}$

how are blocks ordered?

{Gen, C, D, H, B, E, I, K, F, M}



References

Lewenberg, Y., Sompolinsky, Y., & Zohar, A. (2015). Inclusive Block Chain Protocols

<https://eprint.iacr.org/2018/087.pdf>

Sompolinsky, Y., Lewenberg, Y., & Zohar, A. (2016). SPECTRE - A Fast and Scalable Cryptocurrency Protocol

<https://eprint.iacr.org/2016/1159.pdf>

Sompolinsky, Y. (2018). PHANTOM, GHOSTDAG - Two Scalable BlockDAG protocols

<https://eprint.iacr.org/2018/104.pdf>

Li, Chenxing et al. (2018). Scaling Nakamoto Consensus to Thousands of Transactions per Second

<https://arxiv.org/pdf/1805.03870>

References

An Introduction to the BlockDAG Paradigm

<https://blog.daglabs.com/an-introduction-to-the-blockdag-paradigm-50027f44facb>

Transaction Selection Games in BlockDAGs

<https://blog.daglabs.com/transaction-selection-games-in-blockdags-602177f0f726>

SPECTRE: Serialization of Proof-of-Work Events, Confirming Transactions via Recursive Elections

<https://medium.com/@avivzohar/the-spectre-protocol-7dbbebb707b5>

An overview of SPECTRE - a blockDAG consensus protocol (part 2)

<https://medium.com/@drstone/an-overview-of-spectre-a-blockdag-consensus-protocol-part-2-36d3d2bd33fc>

An overview of PHANTOM: A blockDAG consensus protocol (part 3)

<https://medium.com/@drstone/an-overview-of-phantom-a-blockdag-consensus-protocol-part-3-f28fa5d76ef7>

Outline

- DAGs of blocks
 - blockDAG
 - SPECTRE
 - PHANTOM / GHOSTDAG
 - Conflux
- **DAGs of transactions**
 - tangle (IOTA)
 - Avalanche

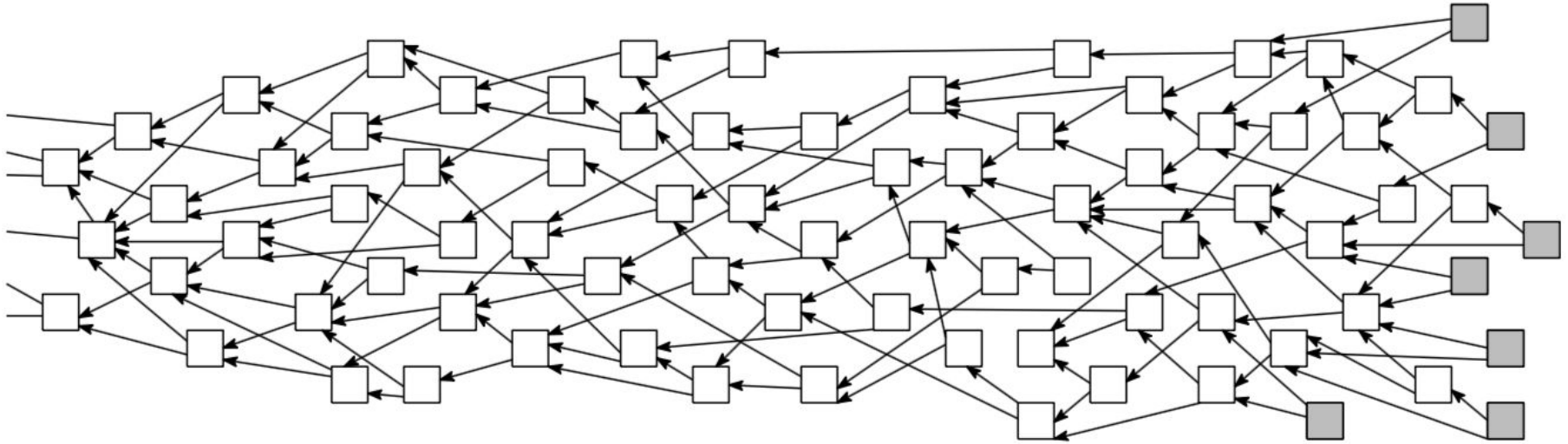
tangle - overview

1. each transaction approves two previous non-conflicting transactions
2. Markov Chain Monte Carlo (MCMC) tip-selection algorithm
3. confidence is derived from number of approvals
4. transactions include PoW to prevent spamming

how to add transactions?

1. choose two transactions to approve
 - the two transactions should not conflict
 - the two transactions should not approve conflicting transactions indirectly
 - the two transactions should be tips in the observed tangle
2. calculate a proof-of-work
 - make it somewhat hard to create transactions
3. publish new transaction

how to add transactions?



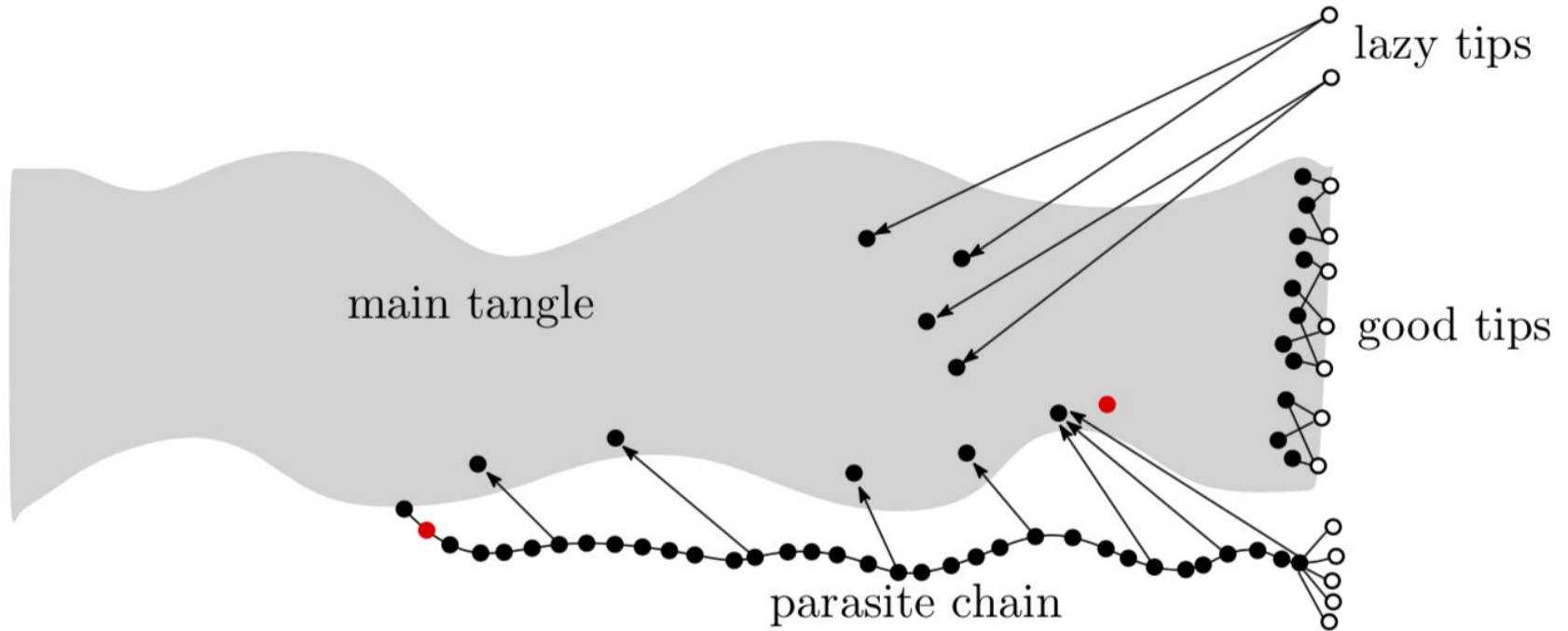
how are transactions approved?

- every transaction has a positive weight associated with it
- transaction acceptance is proportional to its cumulative weight

double-spend attacks

- issue transaction **a** and wait for the merchant to accept it
- issue conflicting transaction **b** and a sub-tangle secretly built on it
 - this sub-tangle does not approve **a**
- make the network accept the double-spending sub-tangle

double-spend attacks

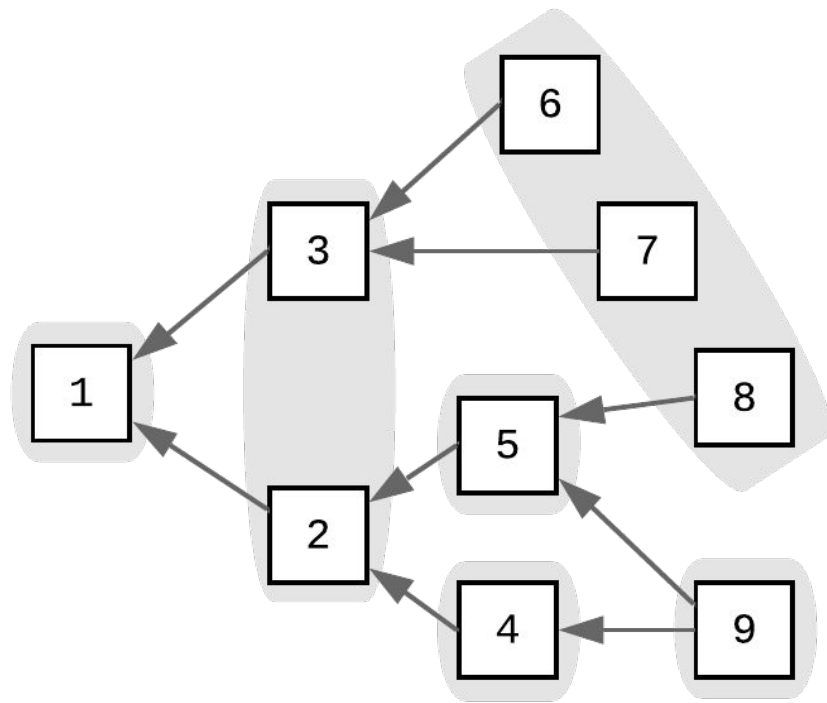


Avalanche - overview

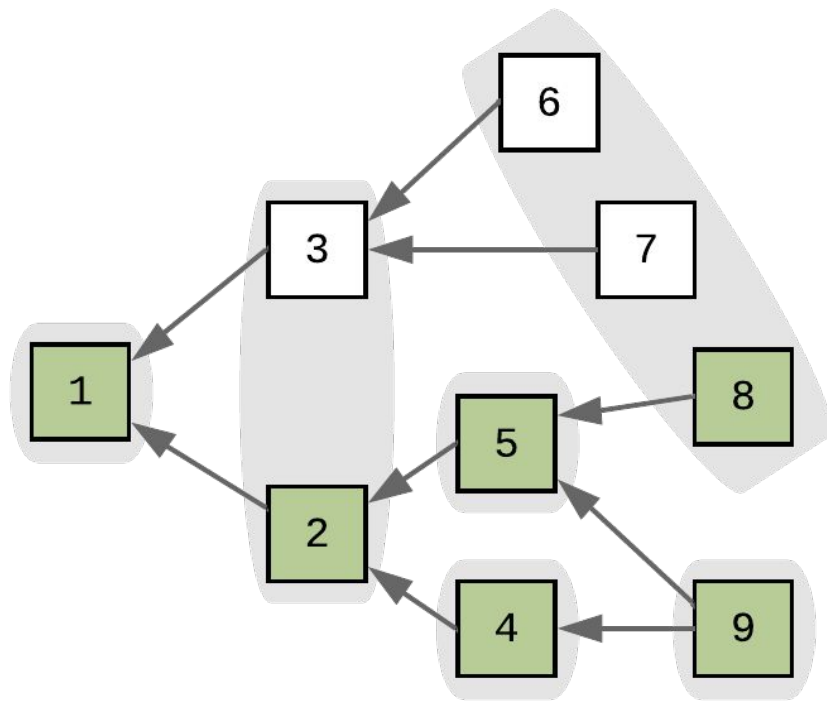
how to approve transactions?

- transactions are partitioned into conflict sets
- accept a single transaction from each conflict set using a metastable protocol

how to approve transactions?



how to approve transactions?



metastable consensus: Snowball

- recurring subsampled voting process
- each node queries a random subset of the network a few times
- the