

Combinatorics 2017 HW 1.2

Student ID:

Name:

Score:

1. How many different permutations for word "Combinatorics"? (Case sensitive)
2. The coefficient number of $a^2b^2c^2$ in the expanded equation of $(2a+b+c)^6$ is _____. **【Please calculate the exact number】**

Answer: 360

Explanation: $\frac{6!}{2!2!2!} \times 2^2 = 90 \times 4 = 360$

1. For the case of giving fruits to 3 children, in total there are 12 identical apples, each child may at least have a fruit, it contains ____ types of ways.

Answer: 55

Explanation: Set the fruit giving away for i^{th} child as x_i , $x_i \geq 1$ $x_1 + x_2 + x_3 = 12$ 令 $y_1 = x_1 - 1, y_2 = x_2 - 1, y_3 = x_3 - 1$ $y_1 + y_2 + y_3 = 9$ $y_i \geq 0$. The non-negative integer solution number is $C(9+3-1, 9) = 55$.

Think About: The number of non-negative integer solution number of $x_1 + x_2 + x_3 = 12$, and $x_1 \leq 5, x_2 \leq 8, x_3 \leq 5$

What is the number of integral solutions of the equation $x_1 + x_2 + x_3 = 30$; in which $x_1 \geq 5, x_2 \geq -8, x_3 \geq 5$