

# Ensembles et applications

## Corrigé

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### Exercices.

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**Exercice 5.1 [◆◆◆]**

Soient  $A, B$  deux parties d'un ensemble  $E$ . Établir que

$$A \setminus (A \setminus B) = A \cap B \quad \text{et} \quad A \setminus (A \cap B) = A \setminus B = (A \cup B) \setminus B.$$

On a :

$$\begin{aligned} A \setminus (A \setminus B) &= A \cap \overline{(A \setminus B)} \\ &= A \cap (\overline{A} \cup B) \\ &= (A \cap \overline{A}) \cup (A \cap B) \\ &= A \cap B \end{aligned}$$

D'autre part :

$$\begin{aligned} A \setminus (A \cap B) &= A \cap \overline{(A \cap B)} \\ &= A \cap (\overline{A} \cup \overline{B}) \\ &= (A \cap \overline{A}) \cup (A \cap \overline{B}) \\ &= A \cap \overline{B} \\ &= A \setminus B \end{aligned}$$

Et :

$$\begin{aligned} (A \cup B) \setminus B &= (A \cup B) \cap \overline{B} \\ &= (A \cap \overline{B}) \cup (B \cap \overline{B}) \\ &= A \cap \overline{B} \\ &= A \setminus B \end{aligned}$$

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