$\begin{array}{c} {\rm Primitives\ et\ int\'egrales} \\ {\rm \tiny Corrig\'e} \end{array}$

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Exercices.	
Exercice 8.1	2

Exercice 8.1 $[\Diamond \Diamond \Diamond]$

Donner les primitives des fonctions suivantes (on précisera l'intervalle que l'on considère).

$$a: x \mapsto \cos x e^{\sin x}; \qquad b: x \mapsto \frac{\cos x}{\sin x}; \qquad c: x \mapsto \frac{\cos x}{\sqrt{\sin x}}; \qquad d: x \mapsto \frac{1}{3x+1};$$

$$e: x \mapsto \frac{\ln x}{x}; \qquad f: x \mapsto \frac{1}{x \ln x}; \qquad g: x \mapsto \sqrt{3x+1}; \qquad h: x \mapsto \frac{x+x^2}{1+x^2}.$$

$$A: \begin{cases} \mathbb{R} \to \mathbb{R} \\ x \mapsto e^{\sin x} + c \end{cases}; \quad B: \begin{cases} \mathbb{R} \setminus \{k\pi, k \in \mathbb{Z}\} \to \mathbb{R} \\ x \mapsto \ln(\sin x) + c \end{cases}; \quad C: x \mapsto \begin{cases}]2k\pi, (2k+1)\pi[, k \in \mathbb{Z} \to \mathbb{R} \\ x \mapsto 2\sqrt{\sin x} + c \end{cases};$$

$$D: \begin{cases} \mathbb{R} \setminus \{-\frac{1}{3}\} \to \mathbb{R} \\ x \mapsto \frac{1}{3}\ln(3x+1) + c \end{cases}; \quad E: \begin{cases} \mathbb{R}_+^* \to \mathbb{R} \\ x \mapsto \frac{1}{2}\ln^2 x + c \end{cases}; \quad F: \begin{cases} \mathbb{R}_+^* \to \mathbb{R} \\ x \mapsto \ln(\ln x) + c \end{cases};$$

$$G: \begin{cases} [-\frac{1}{3}, +\infty] \to \mathbb{R} \\ x \mapsto \frac{2}{9}(3x+1)^{\frac{3}{2}} + c \end{cases}; \quad H: \begin{cases} \mathbb{R} \to \mathbb{R} \\ x \mapsto \frac{1}{2}\ln(1+x^2) + x - \arctan(x) + c \end{cases}.$$

$$D: \begin{cases} \mathbb{R} \setminus \{-\frac{1}{3}\} \to \mathbb{R} \\ x \mapsto \frac{1}{3}\ln(3x+1) + c \end{cases} ; \quad E: \begin{cases} \mathbb{R}_+^* \to \mathbb{R} \\ x \mapsto \frac{1}{2}\ln^2 x + c \end{cases} ; \quad F: \begin{cases} \mathbb{R}_+^* \to \mathbb{R} \\ x \mapsto \ln(\ln x) + c \end{cases} ;$$

$$G: \begin{cases} \left[-\frac{1}{3}, +\infty\right] \to \mathbb{R} \\ x \mapsto \frac{2}{9}(3x+1)^{\frac{3}{2}} + c \end{cases} ; \quad H: \begin{cases} \mathbb{R} \to \mathbb{R} \\ x \mapsto \frac{1}{2}\ln(1+x^2) + x - \arctan(x) + c \end{cases}$$

Avec c les constantes d'intégration.