

Exercise M

Prove: $(o ((\text{curry map}) f) ((\text{curry map}) g)) == ((\text{curry map}) (o f g))$

To prove they are equal, I will prove that when applied to equal arguments, they return equal results.

$$\begin{aligned} & (o ((\text{curry map}) f) ((\text{curry map}) g)) xs \\ &= \{\text{apply-curried law}\} \\ & (o ((\text{curry map}) f) (\text{map } g \text{ } xs)) \\ &= \{\text{apply-compose law}\} \\ & (\text{map } f (\text{map } g \text{ } xs)) \\ &= \{\text{apply-compose law}\} \\ & (\text{map } (o f g) \text{ } xs) \\ &= \{\text{apply-curried law}\} \\ & (((\text{curry map}) (o f g)) xs) \end{aligned}$$

Since $(o ((\text{curry map}) f) ((\text{curry map}) g)) xs == (((\text{curry map}) (o f g)) xs)$, then
 $(o ((\text{curry map}) f) ((\text{curry map}) g)) == ((\text{curry map}) (o f g))$