Due: Sunday, November 24th, 2024 at 11:59pm EST on myCourses

Final weight: 25%

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Contents

1.1 Assignment Submission

1 Assignment Policies

Gather all the python source files within the taichi_tracer/ folder (i.e., everything except the scene_data_dir/

All future assignments, including this one, will build on top of Assignment 1.

YourStudentID.zip

For example, if your ID is **234567890**, your submission filename should be **234567890.zip**. DO NOT ADD ANYTHING BEFORE OR AFTER THE MCGILL ID.

Every time you submit a new file on *myCourses*, your previous submission will be overwritten. We will only

In accordance with article 15 of the Charter of Students' Rights, students may submit any written or programming components in either French or English.

folder) and compress them into a single zip file. Name your zip file according to your student ID, as:

1.2 Late policy All the assignments are to completed individually. You are expected to respect the late day policy and

Late Day Allotment and Late Policy Every student will be allowed a total of **six (6)** late days during the entire semester, without penalty.

Specifically, failure to submit a (valid) assignment on time will result in a late day (rounded up to the nearest day) being deducted from the student's late day allotment. Once the late day allotment is exhausted, any further late submissions will obtain a score of 0%. Exceptional circumstances will be

treated as per McGill's Policies on Student Rights and Responsibilities. If you require an accomodation, please advise McGill Student Accessibility and Achievement (514-398-6009) as early in the semester as possible. In the event of circumstances beyond our control, the evaluation scheme as detailed on the course website and on assignment handouts may require modification.

1.3 Collaboration & Plagiarism

You are expected to submit your own work. Assignments are individual tasks. This does not need to preclude forming an environment where you can be comfortable discussing ideas with your classmates. When in doubt, some good rules to follow include: fully understand every step of every solution you submit, only submit solution code that was written (not copy/pasted/modified, not ChatGPT'ed, etc.) by you, and

Plagiarism is an academic offense of misrepresenting authorship. This can result in penalties up to expulsion. It is also possible to plagiarise your own work, e.g., by submitting work from another course without proper attribution.

McGill values academic integrity and students should take the time to fully understand the meaning and consequences of cheating, plagiarism and other academic offenses (as defined in the Code of Student Conduct and Disciplinary Procedures — see these two links).

446/546. Students may only be notified of potential infractions at the end of the semester.

Computational plagiarism detection tools are employed as part of the evaluation procedure in ECSE

Additional policies governing academic issues which affect students can be found in the Handbook on Student

Rights and Responsibilities.

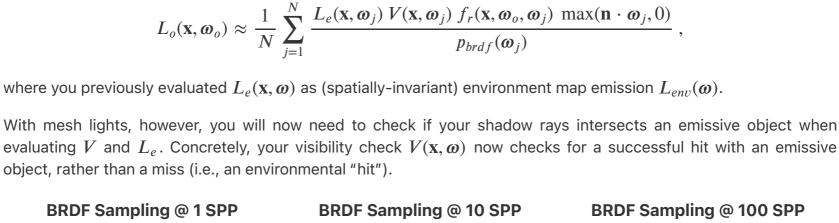
rather than environmental emitters, to light our scene.

emissivity associated to their material property Material. Ke.

2 Mesh Lights The most notable change from the previous assignment is the inclusion of mesh lights,

Mesh lights are treated as "first-class" physical objects in the scene, meaning they are associated with scene geometry (just like every other non-emitting object) and with

3 BRDF Importance Sampling You will begin by modifying your BRDF Importance Sampling direct illumination estimator to support mesh lights.



Mesh Lights.

sampling, you can just call your previous method.

1. first, you must choose an emissive triangle from your mesh by sampling

so, build a (1D) cumulative distribution function over all emissive triangle areas, and perform inversion sampling using 1D binary search over the

according to a probability distribution function $p_{\text{triangles}}(t)$ over triangles; to do

Deliverable 1 [10 points]

sampling.

To do so, we will proceed in two steps:

the surface of that triangle:

Light Importance Sampling The next Monte Carlo estimator that you will implement is one that conducts mesh light importance sampling.

Your A3Renderer instantiates an A2Renderer object. You do not need to re-implement BRDF importance

Modify your A2Renderer's render() routine to support mesh lights with BRDF importance

the marginal density $i \sim p_{\rm triangle}$), you can sample a point uniformly over the mesh light. surface area of the (marginally) sampled triangle according to the (conditional) density p(y|i): \circ given canonical uniform random variates $\xi_0, \xi_1 \in [0,1]$, compute barycentric coordinates b_0 and b_1 as follows:

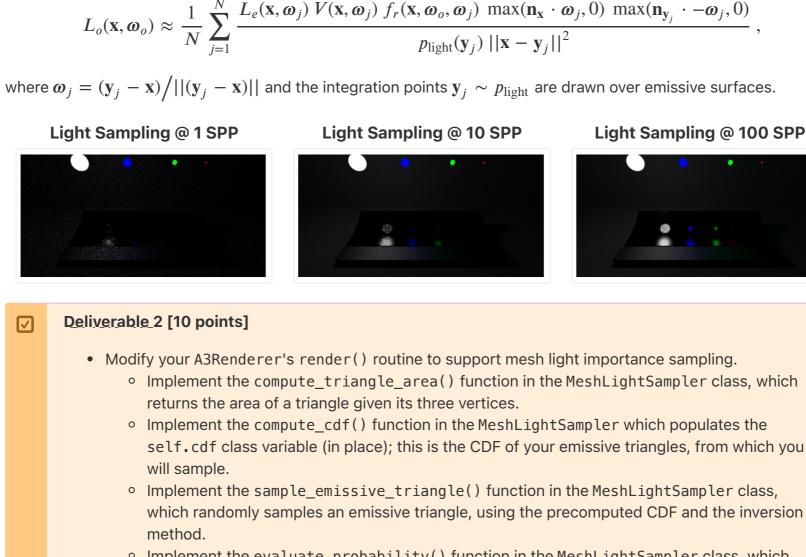
the mesh $\mathbf{y} = b_0 \mathbf{v}_0 + b_1 \mathbf{v}_1 + b_2 \mathbf{v}_2$, where $\mathbf{v}_0, \mathbf{v}_1, \mathbf{v}_2$ are triangle i's vertices.

if $\xi_0 < \xi_1$: $b_0 = \frac{\xi_0}{2}$ and $b_1 = \xi_1 - b_0$

otherwise: $b_1 = \frac{\xi_1}{2}$ and $b_0 = \xi_0 - b_1$

 \circ with the third barycentric coordinate as $b_2=1-b_0-b_1$, you arrive at the sampled surface point on

The probability of your sample is the product of the marginal probability of choosing the emissive triangle from the mesh light p_{triangle} propotional to its area, times the conditional probability $p(\mathbf{y}|t)$ of sampling a point uniformly on



 $p_{\text{light}}(\mathbf{y}) = p_{\text{triangle}}(t) p(\mathbf{y}|t) = \left(A_t / \sum_{i}^{N_{\text{triangles}}} A_i\right) \left(\frac{1}{A_t}\right) = \frac{1}{N_{\text{triangles}}} = \frac{1}{\text{total emissive area}},$

where A_i denotes the area of a triangle i and t is the index of the sampled triangle.

The light importance sampled Monte Carlo estimator is thus:

a general MIS MC estimator that uses both strategies, as

Multiple Importance Sampling

you see fit.

ti.loop_config(serialize=True)

for i in range(emissive_triangles):

decorating the loop as follows:

sum += pdf[i] cdf[i] = sum

sum = 0.0

SPP 10 SPP 10^{2} SPP **Deliverable 3** [10 points] Update your A3Renderer's render() routine to support (1-sample) MC estimation with an MIS estimate that combines BRDF and Light sampling distributions. **ECSE 546 Students Only** 6 Environment Light Importance Sampling

Deliverable 4 [10 points]

- $p(\theta)$ and store it the self.marginal_ptheta field • Implement the precompute_conditional_p_phi_given_theta() function in the Environment class which computes the conditional PDFs $p(\phi|\theta)$ and stores them in the self.conditional_p_phi_given_theta field • Implement the precompute_cdfs() function in the Environment class which computes the
- marginal and conditional CDFs and stores them in the self.cdf_ptheta and self.cdf_p_phi_given_theta fields • Implement the sample theta() and sample phi() functions in the Environment class which will sample a ϕ and θ using inversion sampling of the CDFs • Implement the importance_sample_envmap() function in the Environment class which will return

a normalized [u,v] texture coordinate for your sample on the environment map's latitude-longitude

grade the **final submitted file**, so feel free to submit often as you progress through the assignment.

collaboration/plagiarism polices, discussed below.

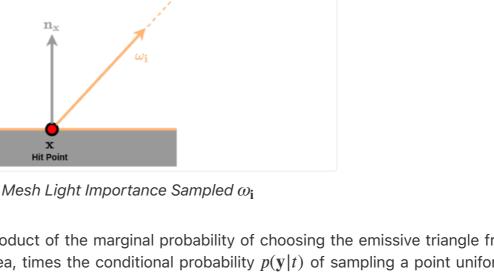
When in doubt, attribute!

• never refer to another student's code — if at all possible, we recommend that you avoid looking at another classmates code.

Recall the formula for this MC estimator:

object, rather than a miss (i.e., an environmental "hit"). **BRDF Sampling @ 1 SPP BRDF Sampling @ 10 SPP**

(inverted) CDF, using a canonical uniform variate $\xi_{\text{triangle}} \in [0, 1]$; and, sampled emissive 2. after choosing your emissive triangle (i.e., sampling a triangle i proportional to triangle (green) on the



 Modify your A3Renderer's render() routine to support mesh light importance sampling. Implement the compute_triangle_area() function in the MeshLightSampler class, which Implement the compute_cdf() function in the MeshLightSampler which populates the self.cdf class variable (in place); this is the CDF of your emissive triangles, from which you Implement the sample_emissive_triangle() function in the MeshLightSampler class, which randomly samples an emissive triangle, using the precomputed CDF and the inversion Implement the evaluate_probability() function in the MeshLightSampler class, which returns the probability of your sampled direction ω_i (converted from a sampled point y_i).

Implement the sampled_mesh_lights() function in MeshLightSampler, which returns both a

• You do not need to implement every helper function as described: these helpers are put in place to

Taichi loops are highly optimized, and are not guaranteed to run in sequential order. In fact, they almost never will. If you want to perform an operation that requires specific sequential processing (e.g., computing a CDF), you can force taichi to run a specific loop in "serialized" mode, which will force the order of operations to be respected, by

This obviously runs slower than a regular loop, however this is the only way to guarantee a sequential operation. You

will need to be mindful of taichi's optimization when performing certain tasks in this assignment.

help guide you towards the solution; you can feel free to implement the entirety of this deliverable as

direction ω_i but also the ID of your sampled emissive triangle.

You will need the ID of the sampled emissive triangle during your visibily check.

Recall that, given two sampling distributions p_f and p_g used to estimate an integral $F = \int f(x) dx$, we can express $\frac{1}{n_f} \sum_{i=1}^{n_f} \frac{f(x_j) \, w_f(x_j)}{p_f(x_j)} + \frac{1}{n_g} \sum_{k=1}^{n_g} \frac{f(x_k) \, w_g(x_k)}{p_g(x_k)},$ where n_f and n_g are the number of samples $(x_j \sim p_f)$ and $x_k \sim p_g$) drawn from the p_f and p_g distributions, and w_f and w_g are special weighing functions chosen so that the expectation of the estimator is the desired integral F. One provably good choice of weighing functions follows the balance heuristic: $w_s(x) = \frac{n_s p_s(x)}{\sum_{i \in S} n_i p_i(x)},$ where $s \in S = \{f, g\}$, in our two-strategy setting, above. While this general MIS formulation is suitable, in the context of our 1-sample per-render-iteration progressive rendering setting, it poses a problem: with the smallest setting of $n_f = n_g = 1$, each iteration will generate two samples.

Since we absolutely wish to maintain the 1-sample-per-pass property instead, we can exploit an important property of the balance heuristic: when using an equal number of samples per strategy, samples drawn in the MIS estimator

In other words, in our two-strategy setting, if you draw samples ω_i according to the average of the light and BRDF

 $L_o(\mathbf{x}, \omega_o) \approx \frac{1}{N} \sum_{i=1}^{N} \frac{L_e(\mathbf{x}, \omega_i) V(\mathbf{x}, \omega_i) f_r(\mathbf{x}, \omega_o, \omega_i) \max(\mathbf{n} \cdot \omega_i, 0)}{p_{mis}(\omega_i)},$

then your estimator will be statistically equivalent to the more general MIS-with-balance-heuristic estimator above, in the $w_{brdf} = 1/2$ and $w_{light} = 1/2$ setting. More generally, for weighins that favour one of the strategies more than the other (i.e., where $w_{brdf} \neq w_{light}$), you can employ the 1-sample strategy discussed during during the lectures, where you first stochastically choose a strategy and then sample according to it (with an appropriate 1-sample MIS weight). In these cases, you can explore the design space of trade-offs between pure-BRDF vs. pure-Light

 $w_{brdf} = \frac{1}{2}, w_{light} = \frac{1}{2}$

 $w_{brdf} = \frac{1}{4}, w_{light} = \frac{3}{4}$

with the balance heuristic weights are — in aggregate — proportional to the average of all the strategies.

PDFs, $\omega_j \sim p_{mis}(\omega) = \frac{p_{light}(\omega)}{2} + \frac{p_{brdf}(\omega)}{2}$ and use them in a standard MC estimator, as

Importance Sampling, and every combined strategy in between them (as illustrated, below).

 $w_{brdf} = \frac{3}{4}, w_{light} = \frac{1}{4}$

into a renderer to those interested students. To perform our experiments, we provide you with a custom visualization pipeline, EnvISRenderer. This visualizer samples points on the environment map, and displays a normalized distribution of your points on a latitude-longitude In order to importance sample an enivronment map, you will need to implement the following marginal-conditional sampling procedure, as discussed in class: • Step 1: Initializing the joint probabilty distribution $p(\phi, \theta)$

so (e.g., max or average RGB value) but we will perform the following **luminance** conversion:

distribution $p(\phi, \theta)$ we will aim to importance sample:

Step 3: Conditional probability distribution $p(\phi|\theta)$

the joint and marginal PDFs at your disposal.

Uniform Samples

Uniform Samples

Uniform Samples

• Step 4:

• Step 2: Precomputing the marginal probabilty distribution $p(\theta)$

by summing and normalizing over each row of your joint distribution.

The final deliverable (for ECSE 546 students) for this assignment will be environment light importance sampling. Rather than rendering a scene directly, we will in the environment map space to validate that our importance sampling routine generates appropriate sampling distributions — we leave the exercise of integrating these samples

The first step is to convert the RGB environment map into a scalar luminance map. There are many ways to do

Luminance(RGB) = 0.2126R + 0.7152G + 0.0722B.

Once you have your luminance map, you then need to scale it by $\sin(\theta)$ to arrive at the joint probabilty

 $p(\phi, \theta) = \text{Luminance}(L_{env}(\phi, \theta)) \sin(\theta)$

Next, we need to compute and store the marginal distribution $p(\theta)=\int_0^{2\pi}p(\phi,\theta)d\phi$, which you can generate

When it comes time to evaluate the 1D conditional probability distribution $p(\phi|\theta)=rac{p(\phi,\theta)}{p(\theta)}$, you already have

The final step is to actually perform the (importance) sampling! To sample proportional to your luminance map, first sample a $\theta_i \sim p(\theta)$ and then sample $\phi_i \sim p(\phi|\theta_i)$. You'll do this by building 1D CDFs for the marginal (one) $p(\theta)$ and (many) conditional $p(\phi|\theta)$ PDFs, and then sample them using (discrete) inversion sampling.

Importance Samples

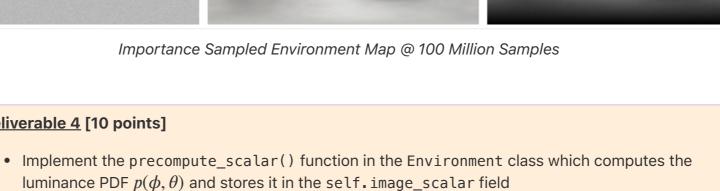
Importance Samples

Importance Samples

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Importance Sampled Environment Map @ 1 Million Samples

Importance Sampled Environment Map @ 10 Million Samples



Implement the precompute_marginal_ptheta() function in the Environment class to precompute

Since you are sampling from a discretized CDF, when computing the normalized [u, v] coordinates, you will need to linearly interpolate (i.e., using a lerp()) the θ and ϕ values that you sampled.

coordinate system

start of this handout before submitting your assignment solution.

7 You're Done! Congratulations, you've completed the 3rd assignment. Review the submission procedures and guidelines at the