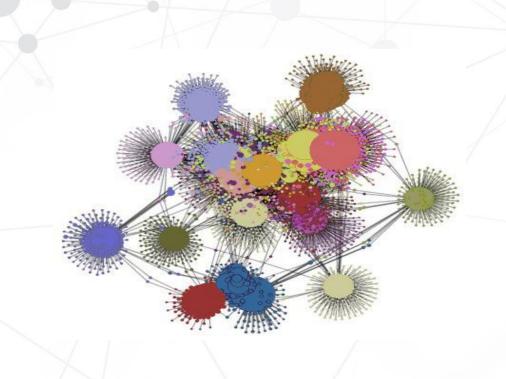


INTRODUCTION

- Most networks display a community structure where vertices are organized into groups called communities.
- Defining these communities is crucial in understanding the features and properties of a network
- In this presentation a review of eight algorithms where each of them proposes a novel approach in community detection is attempted

✓ ABCD ✓ AMKM ✓ HICODE ✓ ASOCCA ✓ EADP ✓ DSCAN ✓ DCK ✓ CC - GA

ATTRACTIVENESS-BASED COMMUNITY DETECTION (ABCD)



ABCD



- An agglomerative algorithm which introduces the weighted concept
- Aimed for large-scale networks, to represent the users' relationships on social networks on Internet

DEFINITIONS



Given a Graph G (V, E, W_V , S_E), V node set, E edge set, W_V the weight of the node set, S_E the weight of edge set, communities are identified as the Graph G clusters.

Given that the No of edges between clusters i and j is \mathbf{q} , the edges weight \mathbf{Se} , $\mathbf{e} \in 1, 2, ..., q$, communities i, j have \mathbf{Qi} , \mathbf{Qj} nodes, the node weight is $\mathbf{W_{a}}$, a set of definitions is constructed:

- **Cluster density:** $W_i = \frac{\sum_{a=1}^{Qi} Wa}{Qi}$
- Attractiveness between clusters i and j: $S_{ij} = \frac{\sum_{e=1}^{q} Se}{QixQj}$ which feeds the attractiveness matrix
- **Inter-interested** clusters: Clusters i, j are inter-interested, if $q \ge Q_i$, $q \ge Q_j$
- ightharpoonup Community: A cluster i is classified as community if $S_{ij} < W_i + W_j$

ABCD METHODOLOGY



Start with each node as a single cluster

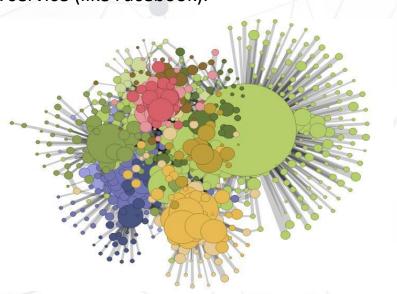
- ➤Two main steps
 - 1. Merge the pair of clusters with the highest value of attractiveness. The clusters are merged if the following condition applies: $Sij \ge Wi + Wj$
 - 2. Calculate/update the cluster density and cluster attractiveness matrix and then iterate between the two steps up to the point where the cluster structure remains unchangeable
- Prerequisites:
 - inter-interested clusters do exist
 - candidate clusters have weight higher than the attractiveness with other inter-interested clusters
 - there is no preference among possible inter-interested clusters.

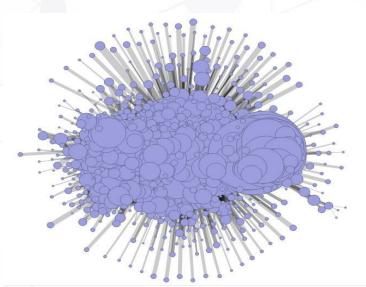
EVALUATION PROCESS

Metrics

✓ Number of Identified communities for three given datasets:
Sina Weibo, a Chinese micro-blogging site, College Football dataset, Renren: a Chinese social network service (like Facebook).







Communities identified

ABCD vs CNM - Sina Weibo micro-blog source: Ruifang Liu et al. / Procedia Computer Science 31 (2014) 85 – 94

CRITIQUE

Pros

- √ Adopts a simple methodological approach
- √ Easy to assess based on a single metric
- √ Time Complexity addressed, indicated performance O(nk + tm²)

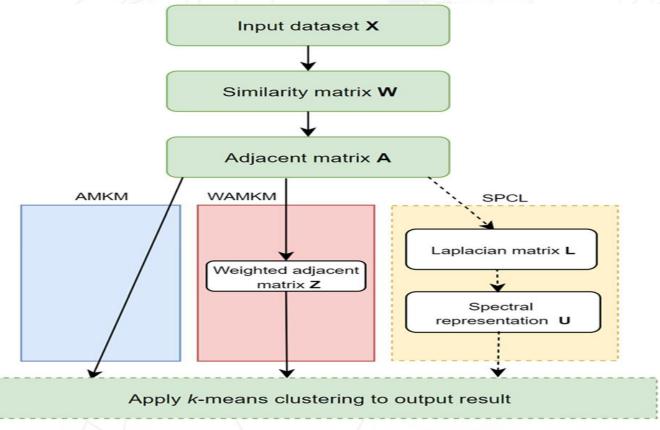
 (n: nodes No, k: average No of inter-interested clusters, m: average No of clusters at the beginning of iterations, t: max No of iterations)
- √ No requirement to specify the number of clusters in advance

Cons

- × Assessment only vs a single algorithm, via a single metric -> not adequate
- × Experimental tests are simplified, not all attributes used (e.g. in Sina Weibo)
- Ver bestellt ve



WEIGHTED ADJACENT MATRIX FOR K-MEANS CLUSTERING (AMKM-WAMKM)



source: Jukai Zhou, Tong Liu, Jingting Zhu, 2019. Weighted adjacent matrix for K-means clustering. # Springer Science + Business Media, LLC, part of Springer Nature 2019, https://doi.org/10.1007/s11042-019-08009-x

AMKM-WAMKM



- An algorithm building up on the classic K-means clustering
- Aimed to improve the K-means in terms of complexity on large datasets and to address the limitation of the similarity measurements

DEFINITIONS



- Arr G= (V, E): V = {v₁, ..., v_n} E = {e₁, ..., e_m} for a fully connected graph, (m = n×(n-1)/2)
- \rightarrow Input data points $X = \{x_1, ..., x_n\}$
- Similarity matrix $W = (wi, j)_{i,j=1}^n$ where $w_{i,j} \ge 0$ is the similarity between x_i and x_j

e.g. for the Euclidean distance for feature t:

$$w_{i,j} = \sqrt{\sum_{t=1}^{d} (x_{i,t} - x_{j,t})^2} \quad (i, j \in [1, n], t \in [1, d])$$

METHODOLOGY



> The same approach for both AMKM and WAMKM

but in WAMKM the features are weighted as % of all features

- Construction of the Similarity matrix W
- Construction of the adjacency matrix A based on W by determining the distance between two data points via a similarity function, i.e. a kernel function, Polynomial, Gaussian or Sigmoid (introducing a parameter σ). e.g. for Gaussian the corresponding element $\alpha_{i,j}$ is defined by:

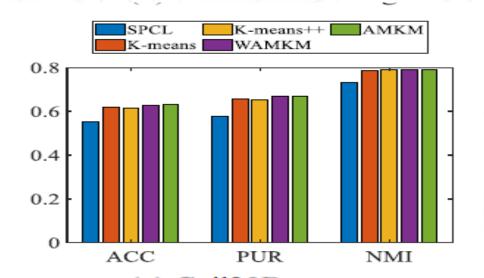
$$a_{i,j} = e^{-\left(\frac{\|w_i - w_j\|_2^2}{2*\sigma^2}\right)}$$
 $(i, j \in [1, n])$

Run the K-means on the adjacency matrix A

EVALUATION PROCESS

Metrics

Accuracy ACC, NMI, PUR* against three n clustering algorithms (k-means, k-means++, and normalised spectral clustering algorithms) Indicative Results for a given dataset:



*12 datasets (UCI Machine Learning Repository and the data mining centre website)

(g) Coil20Data source: Jukai Zhou, Tong Liu, Jingting Zhu, 2019. Weighted adjacent matrix for K-means clustering. # Springer Science + Business Media, LLC, part of Springer Nature 2019, https://doi.org/10.1007/s11042-019-08009-x

CRITIQUE

Pros

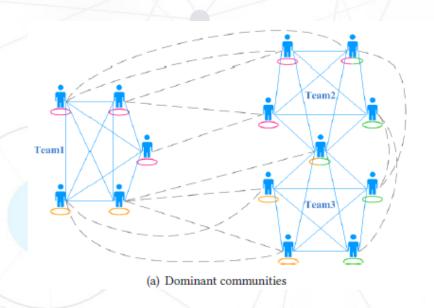
- √ Based on a widely applied algorithm
- √ Good Performance with multiple metrics and datasets
- √ Appropriate for multiple features

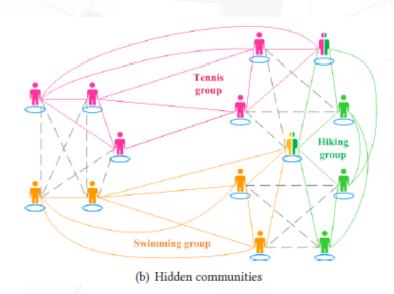
Cons

- × Time Complexity improvement is not convincingly addressed
- \times Results are data-driven, the impact of parameter σ is not clear
- × Not clear if it is suitable for sizeable networks, no concrete experimental data



HIDDEN COMMUNITY DETECTION (HICODE)





WHAT IS HICODE?

- > An approach to identify hidden community structure as well as the dominant one.
- By weakening the strength of dominant structure one can uncover the hidden structure beneath
- > By reducing the strength of the hidden structure one can more accurately identify the dominant structure

NECESSARY DEFINITIONS

- ➤ Hiddenness Value of a Community: The fraction of nodes of a community C_k belonging to another community with higher community quality score.
- ➤ Layer: A set of communities that partitions the nodes of a network
- ➤ Hiddenness Value of a Layer: The weighted average hiddenness values of the communities in the layer.

HOW DOES HICODE WORK?

> Identification

- ✓ Identify an initial layer using a base algorithm
- ✓ Weaken the structure of previous (stronger) detected layers
- Repeat until the appropriate number of layers are found
- Refinement (in each iteration we consider each layer)
 - ✓ Weaken the structure of all other layers from the original network
 - ✓ Apply the base algorithm to the resulting network

WEAKENING? HOW?

- Remove Edge: Weakens a detected community by removing all intra-community edges
- ➤ **Reduce Edge:** Each community is a block; Randomly remove edges within the community to match the background edge probability
- ➤ Reduce Weight: Like Reduce Edge but reduces the weight of each edge within community to match average weighted background probability

EVALUATION PROCESS

- **Metrics**
 - Modularity
 - ✓ NMI
- ✓ Jaccard-based Precision, Recall, F₁ Score
- Datasets
- ✓ 11 real-world networks
- √ 3 of them with ground-truth communities
- √ Small medium- large scale
- Performance strongly related to the base algorithm used. HICODE improved the precision of the base algorithms tested

CRITIQUE

- ➤ HICODE is an algorithm for hidden community identification with possible use in various fields such as security, counter-terrorism services and more.
- Uses a base algorithm so it's performance is strongly depended by this choice.
- Not only detects hidden communities but also leads to higher quality community structures than the base algorithm without HICODE.
- The authors experiment with networks of various types and sizes but do not test directed or weighted graphs.
- No serious assumptions are made.

ADJACENT NODE SIMILARITY OPTIMIZATION COMBINATION CONNECTIVITY ALGORITHM (ASOCCA)

(a) Highest similarity neighbor node list

node	0	0	1	1	2	2	3	4	4	5	6	7	8	8	8	9	10
Highest similarity neighbor	4	8	4	8	9	10	6	1	0	8	5	6	1	0	5	8	2

(b) Combination 1

	0	1	2	3	4	5	6	7	8	9	10
Γ	4	4	10	6	1	8	5	6	5	8	2

(c) Combination 2

0	1	2	3	4	5	6	7	8	9	10
8	4	10	6	1	8	5	6	5	8	2

(d) Combination 3

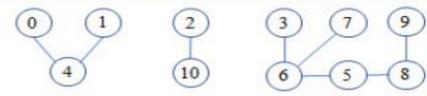
0	1	2	3	4	5	6	7	8	9	10
4	8	10	6	1	8	5	6	5	8	2

(e) Combination 4

0	1	2	3	4	5	6	7	8	9	10
8	8	10	6	1	8	5	6	5	8	2

(f)

(g) a fixed set of connected components generated by combination 1



WHAT IS ASOCCA?

- An algorithm for accurate community detection utilizing a local similarity measure based on clustering coefficient.
- Focuses on non-overlapping community detection for undirected and unweighted graphs.

NECESSARY DEFINITIONS

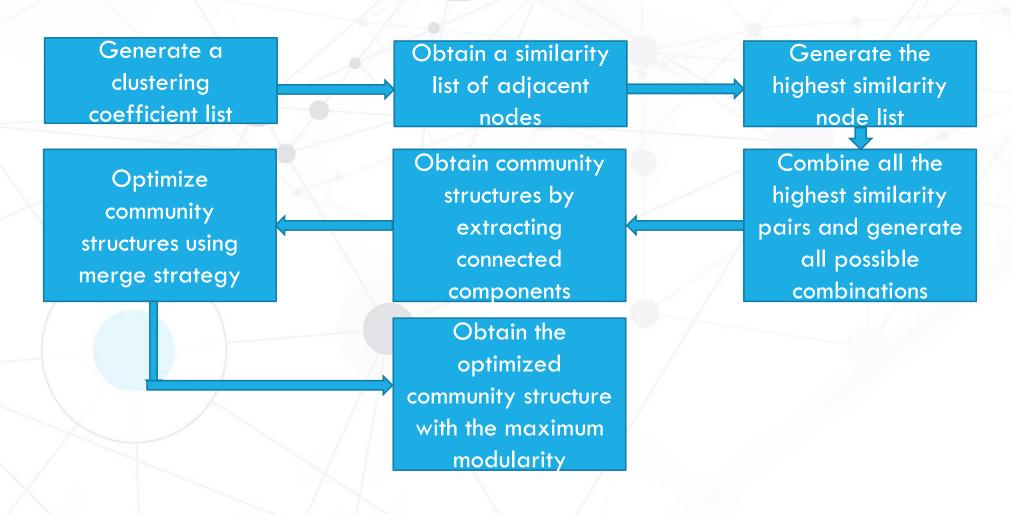
The authors propose a new similarity index based on local similarity, defined as follows:

$$Sim_{ij} = \sum_{t \in \Gamma_{(i)} \cap \Gamma_{(j)}} CC_t$$

Instead of any of the common used similarity indexes:

	similarity index	Formula
•	Salton index	$\frac{ \Gamma(i)\cap\Gamma(j) }{\sqrt{k_i \cdot k_j}}$
	Jaccard index	$\frac{ \Gamma(i)\cap\Gamma(j) }{ \Gamma(i)\cup\Gamma(j) }$
	Sørensen Index	$\frac{2 \Gamma(i)\cap\Gamma(j) }{k_i+k_j}$
	Resource Allocation (RA) index	$\sum_{t \in \Gamma(i) \cap \Gamma(j)} \frac{1}{k_t}$

ASOCCA's WORKFLOW



EVALUATION PROCESS

- Metrics
 - ✓ Modularity
 - ✓ NMI

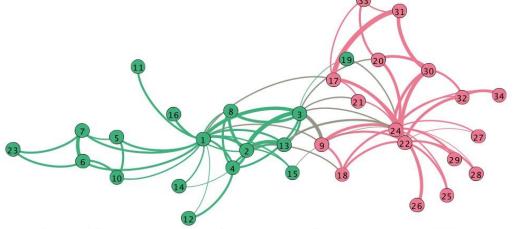
- **Datasets**
 - √ 6 real-world and 2 synthetic networks
 - √ 3 of them with ground-truth communities
- ✓ Small medium and large scale

CRITIQUE

- The metrics used for performance evaluation are modularity and NMI. Neither of them alone is considered enough for strongly documented results.
- A new Similarity Index is defined to measure similarity.
- The datasets used are considered adequate regarding their types and sizes, although there is no implementation or testing for weighted, directed or overlapping community networks.
- An important assumption is made by limiting the maximum combination number to 100.
- \geq Another crucial assumption is the minimum number of nodes in a community (λ) that has to be found by trial.
- The whole merging strategy is based on experimental results and is not strongly documented.
- The complexity of the algorithm is O(nm) a complexity acceptable even for large scale networks.

EXTENDED ADAPTIVE DENSITY PEAKS (EADP)

- An approach to identify overlapping communities in social networks
- Is based in Density Peaks Clustering (DPC) and extends it



HOW DOES EADP WORK?

In the calculation of the **Distance** between nodes takes into consideration the weights of the edges and the common nodes

Automatically finds the Cluster Centers by calculating the Local Density and the Separation Distance of each node

Allocates the remaining nodes to the Clusters in two steps

EVALUATION PROCESS

- Baseline Algorithms
 - ✓ MOSES, SPLA, HOCTracker, OCDDP, SMFRW
- Metrics
 - \checkmark ONMI, Ω Index, F1 Score for ground truth communities
 - ✓ Overlapping Modularity for unknown ground truth communities
- **Datasets**
 - √ 12 real-world networks and synthetic networks
- Better performance, in most cases
- Average speed

CRITIQUE

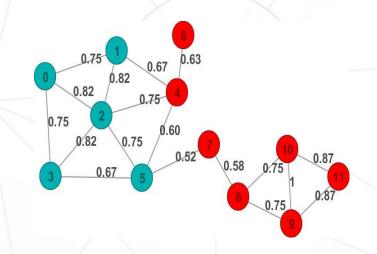
The method is generally better than the baseline algorithms and can be used for finding overlapping communities in social networks

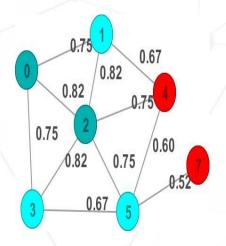
Two parameters related to its performance must be appointed manually

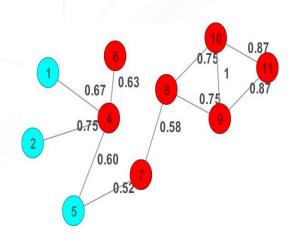
> It is not recommended in large networks because of its average speed

DISTRIBUTED STRUCTURAL CLUSTERING ALGORITHM FOR NETWORKS(DSCAN)

- An approach for finding communities in very large networks
- A distributed implementation of SCAN method







SCAN OVERVIEW

Determines the Core Nodes of the network by finding their strong connections and forming their ϵ -Neighborhood

Allocates the nodes with strong connections to the same **Cluster**

Identifies Bridges and Outliers

HOW DOES DSCAN WORK?

- > Is based on a distributed Master/Slave architecture
- > Divides the graph file to partitions and send it to the workers
- Finds the **Frontier** nodes from neighboring partitions
- Copies the Frontier nodes to the partitions

HOW DOES DSCAN WORK?

- Performs the SCAN algorithm
- Merges the results from all workers
- Solves Disputes

EVALUATION PROCESS

- Baseline Algorithms
 - ✓ SCAN, pSCAN, AnySCAN, ppSCAN
- **→** Datasets
 - √ 5 large real-world networks
- Only time-related tests
- Slowest of all but horizontally scalable
- Only one able to compute the largest network

CRITIQUE

The method can compute very large networks because of its distributed nature

Time complexity was not given

Very slow, especially in the merging step

> No information for its accuracy compared to related methods

COMMUNITY DETECTION AND VISUALIZATION IN COMPLEX NETWORK BY THE DENSITY-CANOPY-KMEANS ALGORITHM AND MDS EMBEDDING

OBJECTIVES OF THE STUDY

- Improve basic K-means algorithm
 - Improve accuracy
 - Improve stability
 - Improve time complexity, $O(n^{Kd+1})$ n: number of nodes in network, d: dimensionality, K: number of clusters
- > Acceleration of algorithm by dimensionality reduction
 - > MDS (MultiDimensional Scaling) algorithm

DEFINING NODE DISTANCE

- Plenty of metrics can be used
- > Jaccard similarity: $s_{ij} = \frac{L_{11}}{L_{01} + L_{10} + L_{11}}$
 - Exploit of adjacency matrix A
 - \triangleright L₁₁: Number of common neighbors of nodes *i* and *j*
 - $ightharpoonup L_{01} + L_{10} + L_{11}$: total number of neighbors of nodes *i* and *j*
- Distance between nodes: $dist_{ij} = 1 s_{ij} \Rightarrow dist_{ij} = \frac{L_{01} + L_{10}}{L_{01} + L_{10} + L_{11}}$
- Problem when applying MDS on zero distance nodes
 - New distance metric: $d_{ij} = \gamma \cdot dist_{ij} + dist_{ij} + adist_{ij} + adist_{ij}$
 - \triangleright γ : community structure coefficient, $dist_random_{ij}$ in [0,1]
 - Creation of distance matrix D

DIMENSIONALITY REDUCTION

- \rightarrow MDS algorithm, reduction to m (< d) dimensions
 - Use of dimension matrix D
 - Computation of a new matrix B

$$b_{ij} = -\frac{1}{2} \left(d_{ij}^2 - \frac{\sum_{j=1}^n d_{ij}^2 - \sum_{i=1}^n d_{ij}^2}{n} + \frac{\sum_{i=1}^n \sum_{j=1}^n d_{ij}^2}{n^2} \right)$$

- Decomposition of matrix D to eigenvalues and eigenvectors matrices
 - \triangleright Selection of m largest eignevalues, creation of diagonal matrix Λ
 - \triangleright Selection of the corresponding m eigenvectors, creation of matrix Ψ
- Projection of nodes to new coordination system

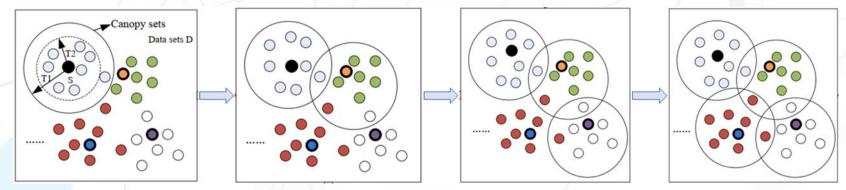
$$X = \Psi \sqrt{\Lambda}$$

DENSITY-CANOPY-K-MEANS ALGORITHM

- K-means algorithm
 - Reliable algorithm for unsupervised clustering
 - Has a high time complexity O(n^{dK+1})
 d: node dimensionality, K: number of clusters (communities)
 - Finding an optimum solution to K-means is an NP-hard problem
 - Optimum number K of clusters,
 - Optimum initial seed

DENSITY-CANOPY-K-MEANS ALGORITHM

- Canopy algorithm
 - > Simple, fast and efficient algorithm for unsupervised clustering
 - > Uses a random initial node and two predefined radial distances T_1 and T_2 ($T_1 > T_2$), to assign every node to a specific canopy (cluster)



- The number of detected clusters and their centers are entered to the K-means algorithm as value of hyperparameter K and as initial seed respectively
- \triangleright How to set optimum values for hyperparameters T_1 and T_2 ?

DENSITY—CANOPY—K-MEANS ALGORITHM

- Density clustering algorithm
 - To improve the stability and complexity of Canopy algorithm, the principle of density clustering is applied
 - \triangleright Two new hyperparameters r and t are defined in order to compute variables R and T
 - $R = d_{\min} + r \cdot (d_{\max} d_{\min})$
 - $T = d_{\min} + t \cdot (d_{\max} d_{\min})$

 d_{min} : the average value of the minimum distance between each node and other nodes

 d_{max} : the average value of the maximum distance between each node and other nodes

r: the density radius coefficient

t: the distance threshold coefficient

 \triangleright Variables R and T correspond to hyperparameters T_1 and T_2 of Canopy algorithm

DCK ALGORITHM, FINAL RESULTS

- The hyperparameters values of each individual algorithm are determined by the immediately preceding algorithm
- In total 3 new hyperparameters are introduced to system
 - $\triangleright \gamma$: is used in distance metric
 - > r and t: are used in density clustering
 - Their optimal values are determined by maximizing the modularity metric, which estimates the quality of the algorithm detected communities
 - r = t = 1/6 and y = 100
- \triangleright Reduction of overall algorithm complexity to $O(n^3)$

DCK ALGORITHM, EVALUATION

- The efficiency of the DCK algorithm was evaluated in a series of artificial and real-world networks and compared to other known algorithms (in real-world networks only)
 - Various network sizes, from small to medium (~5K)
 - Known community structure
- Accuracy in identifying the number of communities were assessed
- The quality of the identified communities was assessed through the modularity metric.
- Other metrics used:
 - Accuracy, F-measure, Rand Index (RI), Adjusted Rand Index (ARI), Normalized Mutual Information (NMI)

DCK ALGORITHM, EVALUATION

- > Results in artificial networks:
 - ➤ High accuracy in identifying the number of communities, which is decreasing as the network size increases (~2K nodes)
- ➤ Results compared to simple *K*-means algorithm in real-world networks:
 - Higher accuracy in identifying the number of communities

DCK ALGORITHM, CRITIQUE

Pros

- √ Simple and easy-to-implement algorithm
- √ As input it only requires the network adjacency matrix
- √ No additional prior knowledge about community structure is needed
- √ Reduced time complexity compared to simple K-means algorithm

Cons

- × Requires the optimization of additional hyperparameters
- Very slow on large scale networks

CC-GA. A CLUSTERING COEFFICIENT BASED GENETIC ALGORITHM FOR DETECTING COMMUNITIES IN SOCIAL NETWORKS

OBJECTIVES OF THE STUDY

- > GAs are used in a wide variety of real-world applications
 - Optimization problems
 - Search problems
- GAs limitations
 - ✓ Random generation of initial population
 - Trapped in local optimum
 - Takes much longer to converge to a near-global optimum
- > Find a better technique to generate initial population
 - √ Faster convergence to near-global optimum
 - ✓ Improve efficiency and accuracy of community detection

TYPICAL GENETIC ALGORITHM STEPS

- Generation of initial population
 - ✓ Finite number of (random) chromosomes
- Fitness Function
 - ✓ Evaluation of chromosome/population performance
 - ✓ Select best performing chromosomes
- Crossover operator
 - Combines the gene structures of two chromosomes to generate the gene of the next generation's chromosomes
- Mutation operator
 - ✓ Alters a random gene of a random chromosome
- Population update
 - Replaces the least performing chromosomes with new best performing ones
 - ✓ Creates new generation

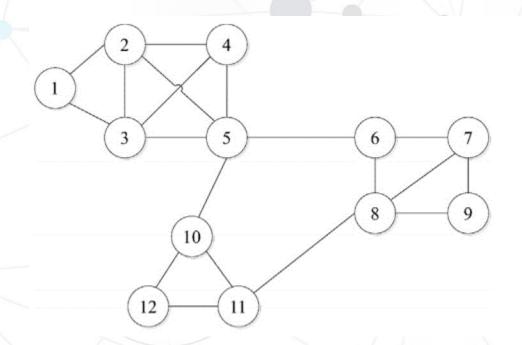
- Generation of initial population
 - ✓ Algorithm connects each node to only one of its neighbors in the original network
 - ✓ Instead of random selection of the neighbor, algorithm exploit the *Clustering Coefficient* (CC)

$$C_i = 2 \times \frac{L_i}{k_i \left(k_i - 1 \right)}$$

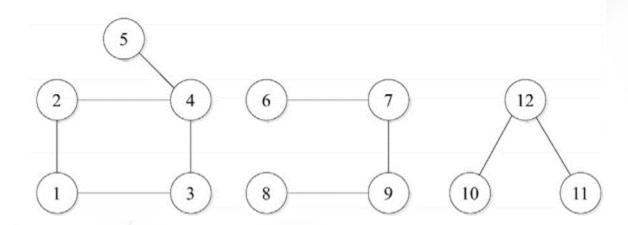
 L_1 : the total number of edges among v_i 's neighbors, excluding the node itself, k_i : node's degree

- ✓ CC quantifies how close are the neighbors of a specific node to being a clique.
- ✓ If a node has multiple neighbors, the algorithm links it to only one neighbor, the one with the *highest* value of CC
- ✓ Nodes connected with a *bridge* edge in original network, have lower values of CC, and are *less* possible to be selected by algorithm
- As a final result:
 - Algorithm splits the original network to simpler connected components, by removing preferably the edge-local bridges
 - <u>Each</u> connected component is a different *community*
 - Local bridges are the natural cut points separating various communities

Generation of initial population

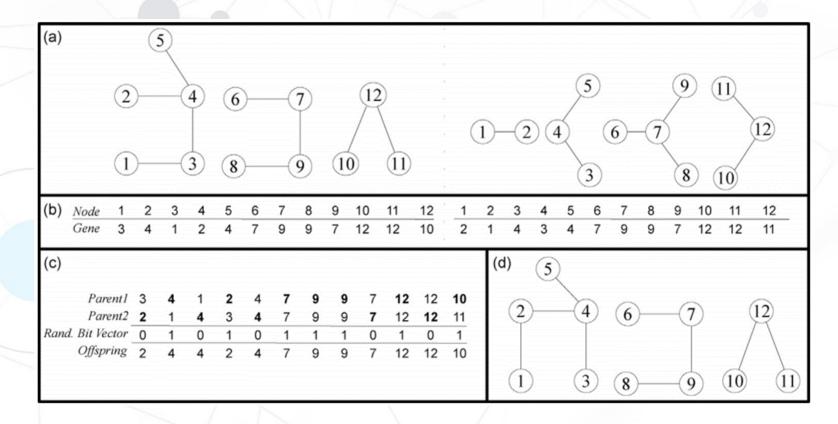


Nodes	1	2	3	4	5	6	7	8	9	10	11	12	
Genes	3	1	4	2	4	7	9	9	8	12	12	11	



- Fitness Function
 - ✓ Modularity is used to evaluate the quality of community structure in each chromosome.
 - ✓ Select best performing chromosomes
- Crossover operator
 - ✓ Uniform random crossover of two chromosomes' genes
- Mutation operator
 - ✓ Introduced a novel mutation operator
 - ✓ Algorithm selects random chromosomes from different communities and joins them
 - Ensures that smaller communities are merged into larger ones, and increases the community structure quality (modularity value) at the same time
- Population update
 - Replaces the least performing chromosomes with new best performing ones
 - Creates new generation

Crossover operator



CC-GA ALGORITHM HYPERPARAMETERS

- Must be carefully set before execution
 - Population size
 - Crossover rate
 - Mutation rate
 - Mutation extension rate
 - Percentage of chromosomes from the current population to be involved in the next iteration (generation) of genetic operators
 - Maximum number of iterations without any improvement (termination criterion)

CC-GA ALGORITHM, EVALUATION

- √ The efficiency of the CC-GA algorithm was evaluated using 13 artificial and 11 real-world networks and compared to 3 other GA and 6 other community detection algorithms
 - Various network sizes, from small to medium (~23K)
 - Known community structure
 - Modularity measure used to compare results of CC-GA with other techniques
- ✓ Compared to other GA approaches
 - CC-GA provides a better community structure than existing GA-based approaches
- ✓ Compared to other non-GA-based community detection approaches
 - CC-GA delivers competitive results for various real-world networks
 - CC-GA is capable of detecting the community structure within a few iterations

CC-GA ALGORITHM, CRITIQUE

Pros

- √ Clustering Coefficient provides high quality initial population
- √ No prior knowledge of the size, number or structure of the communities
- √ Extensive evaluation of the algorithm against many state of-the-art algorithms, using many real or artificial networks of different sizes

Cons

- × A relatively large number of hyperparameters are required to be set as algorithm's input
- × Authors don't report overall algorithm time complexity
- \times Calculating Clustering Coefficient process has polynomial time complexity $O(n^k)$, where k<2.376

CONCLUSION

- Community detection is a problem that can be addressed by a variety of methodological approaches.
- > The algorithms reviewed in this presentation cover a wide range of these approaches.
- The majority of them are structural (except HICODE which extends any base algorithm).
- For their evaluation networks of various types and sizes are used.
- Two very common evaluation metrics are modularity and NMI. In some cases other metrics are used adding credibility to the process.
- Parameters and thresholds are factors that can seriously affect the performance of algorithms depending on them.