## Deep Learning

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### Siamese Networks

Variational Auto-Encoders

Generative Adversarial Networks

## **Siamese Networks**

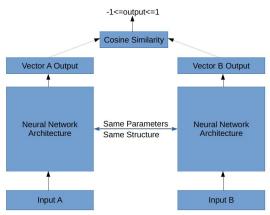


Classes or similarities ?

## **Principle**

- ▶ Neural Networks can be used to define a latent representation
- ► Siamese: optimize the related metrics

### **S**chema



## Siamese Networks, 2

#### Data

$$\mathcal{E} = \{x_i \in \mathbb{R}^d, i \in [[1, n]]\}; \mathcal{S} = \{(x_{i,\ell}, x_{j_\ell}, c_\ell) \text{ s.t. } c_\ell \in \{-1, 1\}, \ell \in [[1, L]]\}$$

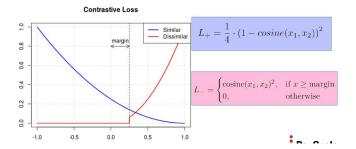
## **Experimental setting**

- ▶ Often: few similar pairs; by default, pairs are dissimilar
- ▶ Subsample dissimilar pairs (optimal ratio between 2/1 ou 10/1)
- Possible to use domain knowledge in selection of dissimilar pairs

### Loss

## Given similar and dissimilar pairs $(E_+ \text{ and } E_-)$

$$\mathcal{L} = \sum_{(i,j) \textit{inE}_+} L_+(i,j) + \sum_{(k,\ell) \textit{inE}_-} L_-(k,\ell)$$





## **Applications**

- ► Signature recognition
- ► Image recognition, search
- ► Article, Title
- Filter out typos
- ► Recommandation systems, collaborative filtering

## Siamese Networks for one-shot image recognition

Koch, Zemel, Salakhutdinov 15

## **Training similarity**

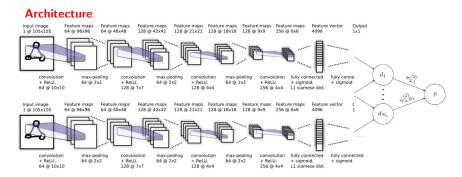


## One-shot setting

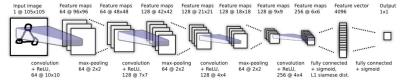


## **Ingredients**

Koch et al. 15



#### **Architecture**



#### Distance

$$d(x,x') = \sigma\left(\sum_{k} \alpha_{k} |z_{k}(x) - z_{k}(x')|\right)$$

#### Loss

Given a batch  $((x_i, x_i'), y_i)$  with  $y_i = 1$  iff  $x_i$  and  $x_i'$  are similar

$$\mathcal{L}(w) = \sum_{i} y_{i} \log d(x_{i}, x_{i}') + (1 - y_{i}) \log (1 - d(x_{i}, x_{i}')) + \lambda ||w||^{2}$$

### Results

## **Omniglot**



### Results

| Method                                 | Test |
|----------------------------------------|------|
| Humans                                 | 95.5 |
| Hierarchical Bayesian Program Learning | 95.2 |
| Affine model                           | 81.8 |
| Hierarchical Deep                      | 65.2 |
| Deep Boltzmann Machine                 | 62.0 |
| Simple Stroke                          | 35.2 |
| 1-Nearest Neighbor                     | 21.7 |
| Siamese Neural Net                     | 58.3 |
| <b>Convolutional Siamese Net</b>       | 92.0 |

### Siamese Networks

#### **PROS**

- Learn metrics, invariance operators
- ► Generalization beyond train data

#### **CONS**

- ► More computationally intensive
- ▶ More hyperparameters and fine-tuning, more training

Siamese Networks

Variational Auto-Encoders

Generative Adversarial Networks

## **Beyond AE**

► A compressed (latent) representation

$$x \in \mathbb{R}^D \mapsto z = Enc(x) \in \mathbb{R}^d \mapsto Dec(z) \in \mathbb{R}^D \approx x$$

- ▶ Distance in latent space is meaningful d(Enc(x), Enc(x')) reflects d(x, x')
- ▶ But  $\forall z \in \mathbb{R}^d$ : is  $Dec(z) \in \mathbb{R}^D$  meaningful ?

## **Beyond AE**

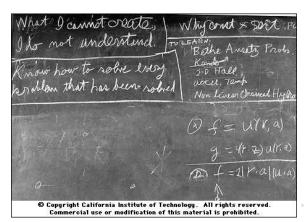
► A compressed (latent) representation

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- ▶ Distance in latent space is meaningful d(Enc(x), Enc(x')) reflects d(x, x')
- ▶ But  $\forall z \in \mathbb{R}^d$ : is  $Dec(z) \in \mathbb{R}^D$  meaningful ?

"What I cannot create I do not understand"

Feynman 88

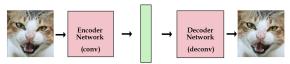


## Variational Auto-Encoders

Kingma Welling 14, Salimans Kingma Welling 15

#### What we have:

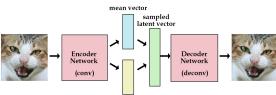
▶ Enc a memorization of the data s.t. exists  $Dec \approx Enc^{-1}$ 



latent vector/variables

#### What we want:

 $ightharpoonup z \sim \mathcal{P}$  s.t.  $Dec(z) \sim \mathcal{D}_{data}$ 



## **Distribution estimation**

### Data

$$\mathcal{E} = \{x_1, \ldots, x_n, x_i \in \mathcal{X}\}$$

#### Goal

Find a probability distribution that models the data

$$p_{ heta}: \mathcal{X} \mapsto [0,1]$$
 s.t.  $heta = rg \max \prod_i p_{ heta}(x_i)$ 

**≡** maximize the log likelihood of data

$$arg \max \prod_{i} p_{\theta}(x_i) = arg \max \sum_{i} log(p_{\theta}(x_i))$$

#### Gaussian case

$$heta = (\mu, \sigma) \qquad p_{ heta}(x) = rac{1}{\sigma \sqrt{2\pi}} exp\left(-rac{1}{2\sigma^2}(x-\mu)^2
ight)$$

## **Akin Graphical models**

Find hidden variables z s.t.

$$z \mapsto x \text{ s.t. good } p(x|z)$$

**Bayes relation** 

$$p(\mathbf{x}, \mathbf{z}) = p(\mathbf{z}|\mathbf{x}).p(\mathbf{x}) = p(\mathbf{x}|\mathbf{z}).p(\mathbf{z})$$

Hence

$$p(\mathbf{z}|\mathbf{x}) = p(\mathbf{x}|\mathbf{z}).p(\mathbf{z})/\int p(\mathbf{x}|\mathbf{z}).p(\mathbf{z})d\mathbf{z}$$

#### Problem:

denominator computationally intractable...

#### State of art

- Monte-Carlo estimation
- Variational Inference choose z well-behaved, and make q(z) "close" to p(z|x).

## **Variational Inference**

- Approximate  $p(\mathbf{z}|\mathbf{x})$  by  $q(\mathbf{z})$
- Minimize distance between both, using Kullback-Leibler divergence

#### Reminder

- ▶ information (x) = -log(p(x))
- entropy( $\mathbf{x}_1, \dots \mathbf{x}_k$ ) =  $-\sum_i p(\mathbf{x}_i) log(p(\mathbf{x}_i))$
- ► Kullback-Leibler divergence between distribution q and p

$$KL(q||p) = \sum_{\mathbf{x}} q(\mathbf{x}) log \frac{q(\mathbf{x})}{p(\mathbf{x})}$$

Beware: not symmetrical, hence not a distance; plus numerical issues when supports are different

#### Variational inference

Minimize 
$$KL(q(\mathbf{z})||p(\mathbf{z}|\mathbf{x})) = \int q(\mathbf{z})log\frac{q(\mathbf{z})}{p(\mathbf{z}|\mathbf{x})}d\mathbf{z}$$



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$$KL(q(z)||p(z|x)) = \int q(z)log\frac{q(z)}{p(z|x)}dz$$

use 
$$p(z|x) = p(z,x)/p(x)$$

$$KL(q(z)||p(z|x)) = \int q(z)log\frac{q(z)p(x)}{p(z,x)}dz$$

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$$\begin{aligned} \textit{KL}(q(\mathbf{z})||p(\mathbf{z}|\mathbf{x})) &= \int q(\mathbf{z})log\frac{q(\mathbf{z})}{p(\mathbf{z}|\mathbf{x})}d\mathbf{z} \\ \text{use } p(\mathbf{z}|\mathbf{x}) &= p(\mathbf{z},\mathbf{x})/p(\mathbf{x}) \\ \\ \textit{KL}(q(\mathbf{z})||p(\mathbf{z}|\mathbf{x})) &= \int q(\mathbf{z})log\frac{q(\mathbf{z})p(\mathbf{x})}{p(\mathbf{z},\mathbf{x})}d\mathbf{z} \\ \\ \textit{KL}(q(\mathbf{z})||p(\mathbf{z}|\mathbf{x})) &= \int q(\mathbf{z})log\frac{q(\mathbf{z})}{p(\mathbf{z},\mathbf{x})}d\mathbf{z} + \int q(\mathbf{z})log(p(\mathbf{x}))d\mathbf{z} \\ \\ \text{as } \int q(\mathbf{z})d\mathbf{z} &= 1 \end{aligned}$$

 $KL(q(\mathbf{z})||p(\mathbf{z}|\mathbf{x})) = \int q(\mathbf{z})\log\frac{q(\mathbf{z})}{p(\mathbf{z},\mathbf{x})}d\mathbf{z} + \log(p(\mathbf{x}))$ 

$$KL(q(\mathbf{z})||p(\mathbf{z}|\mathbf{x})) = \int q(\mathbf{z})log\frac{q(\mathbf{z})}{p(\mathbf{z}|\mathbf{x})}d\mathbf{z}$$

use p(z|x) = p(z,x)/p(x)

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as  $\int q(\mathbf{z})d\mathbf{z} = 1$ 

$$\mathit{KL}(q(\mathsf{z})||p(\mathsf{z}|\mathsf{x})) = \int q(\mathsf{z})log \frac{q(\mathsf{z})}{p(\mathsf{z},\mathsf{x})}d\mathsf{z} + log(p(\mathsf{x}))$$

recover KL(q(z)||p(z,x))

$$\mathit{KL}(q(\mathbf{z})||p(\mathbf{z}|\mathbf{x})) = -\int q(\mathbf{z})log \frac{p(\mathbf{z},\mathbf{x})}{q(\mathbf{z})}d\mathbf{z} + log(p(\mathbf{x}))$$



## **Evidence Lower Bound, 2**

**Define** 

$$L(q(z)) = \int q(z) log \frac{p(z, x)}{q(z)} dz$$

Last slide:

$$KL(q(\mathbf{z})||p(\mathbf{z}|\mathbf{x})) = log(p(\mathbf{x})) - L(q(\mathbf{z})))$$

#### Hence

Minimize Kullback-Leibler divergence  $\equiv$  Maximize L(q(z))

## **Evidence Lower Bound, 3**

## More formula massaging

$$L(q(z)) = \int q(z) log \frac{p(z, x)}{q(z)} dz$$

## Evidence Lower Bound, 3

## More formula massaging

$$L(q(z)) = \int q(z) log \frac{p(z, x)}{q(z)} dz$$

use p(z, x) = p(z|x)p(x)

$$\begin{split} L(q(\mathbf{z})) &= \int q(\mathbf{z}) log \frac{p(\mathbf{z}|\mathbf{x})p(\mathbf{x})}{q(\mathbf{z})} d\mathbf{z} \\ L(q(\mathbf{z})) &= \int q(\mathbf{z}) log \frac{p(\mathbf{z}|\mathbf{x})}{q(\mathbf{z})} d\mathbf{z} + \int q(\mathbf{z}) log(p(\mathbf{x})) d\mathbf{z} \\ L(q(\mathbf{z})) &= -KL(q(\mathbf{z})||p(\mathbf{z}|\mathbf{x})) + \mathbb{E}_q[log(p(\mathbf{x}))] \end{split}$$

**Finally** 

Maximize 
$$\mathbb{E}_q[log(p(\mathbf{x})] - KL(q(\mathbf{z})||p(\mathbf{z}|x))$$

make p(x) great under q while minimizing the KL divergence between the two

akin data fitting akin regularization

## Where neural nets come in

## Searching p and q

- ▶ We want  $p(\mathbf{x}|\mathbf{z})$ , we search  $p(\mathbf{z}|x)$
- ▶ Let  $p(\mathbf{z}|\mathbf{x})$  be defined as a neural net (encoder)
- ightharpoonup We want it to be close to a well-behaved ( Gaussian) distribution q(z)

Minimize 
$$KL(q(\mathbf{z})||p(\mathbf{z}|x))$$

- And from z we generate a distribution p(x|z) (defined as a neural net, "decoder")
- $\triangleright$  such that p(x|z) gives a high probability mass to our data (next slide)

Maximize 
$$\mathbb{E}_q[log(p(\mathbf{x}))]$$

#### Good news

All these criteria are differentiable! can be used to train the neural net.

## The loss of the variational decoder

#### Continuous case

- ightharpoonup x  $\mapsto$  z; Gaussian case, z  $\sim p(z|x)$
- Now z is given as input to the decoder, generates  $\hat{x}$  (deterministic)
- $p(\mathbf{x}|\hat{\mathbf{x}}) = F(\exp\{-\|\mathbf{x} \hat{\mathbf{x}}\|^2\})$
- ▶ ... back to the L₂ loss

## **Binary case**

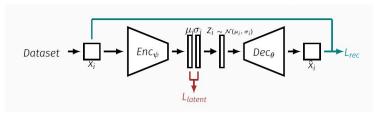
Exercize: back to the cross-entropy loss

## Variational auto-encoders

Kingma et al. 13

#### Position

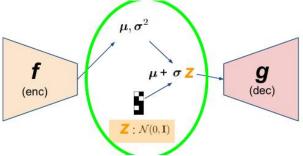
- Like an auto-encoder (data fitting term) with a regularizer, the KL divergence between the distribution of the hidden variables z and the target distribution.
- lacktriangle Say the hidden variable follows a Gaussian distribution:  $\mathbf{z} \sim \mathcal{N}(\mu, \mathbf{\Sigma})$
- lacktriangle Therefore, the encoder must compute the parameters  $\mu$  and  $\Sigma$



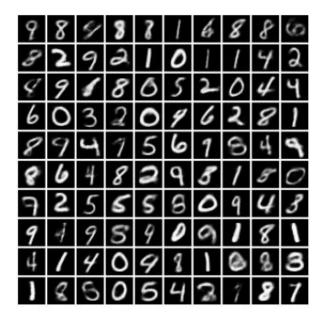
## The reparameterization trick

## **Principle**

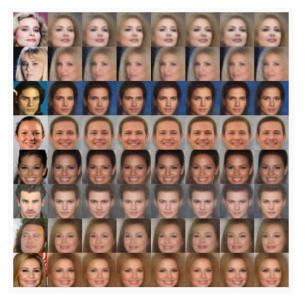
- ▶ Hidden layer: parameters of a distribution  $\mathcal{N}(\mu, \sigma^2)$
- ▶ Distribution used to generate values  $z = \mu + \sigma \times \mathcal{N}(0,1)$
- ► Enables backprop; reduces variances of gradient



# **Examples**



# **Examples**



Also: https://www.youtube.com/watch?v=XNZIN7Jh3Sg

## **Discussion**

#### **PROS**

► A trainable generative model

### **CONS**

▶ The generative model has a Gaussian distribution at its core: blurry

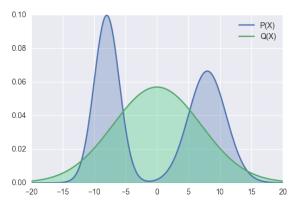
## **Discussion**

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#### **Generative Adversarial Networks**

Goodfellow et al., 14

## Goal: Find a generative model

► Classical: learn a distribution

hard

▶ Idea: replace a distribution evaluation by a 2-sample test

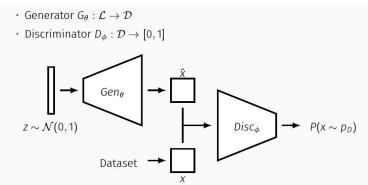
#### **Principle**

 Find a good generative model, s.t. generated samples cannot be discriminated from real samples

(not easy)

#### **Elements**

- ► True samples x ( real)
- A generator G (variational auto-encoder): generates from x ( reconstructed) or from scratch (fake)
- A discriminator D: discriminates fake from others ( real and reconstructed)



# Principle, 2

Goodfellow, 2017

#### Mechanism

- ► Alternate minimization
- Optimize D to tell fake from rest
- Optimize G to deceive D

Turing test

$$\mathit{Min}_{G} \ \mathit{Max}_{D} \mathbb{E}_{x \in \mathit{data}}[\log(D(\mathbf{x}))] + \mathbb{E}_{z \sim p_{\mathbf{x}}(z)}[\log(1 - D(z))]$$

#### Caveat

- ▶ The above loss has a vanishing gradient problem because of the terms in log(1 D(z)).
- ▶ We can replace it with  $-\log((1 D(z)/D(z)))$ , which has the same fixed point (the true distribution) but doesn't saturate.

#### GAN vs VAE

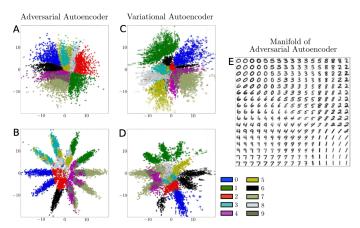


Figure 2: Comparison of adversarial and variational autoencoder on MNIST. The hidden code z of the hold-our images for an adversarial autoencoder fit to (a) a 2-D Gaussian and (b) a mixture of 10 2-D Gaussians. Each color represents the associated label. Same for variational autoencoder with (e) a 2-D gaussian and (d) a mixture of 10 2-D Gaussians. (e) Images generated by uniformly sampling the Gaussian percentiles along each hidden code dimension z in the 2-D Gaussian adversarial autoencoder.

## **Generative adversarial networks**







## Generative adversarial networks, 2

Goodfellow, 2017

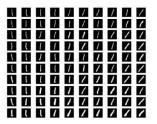


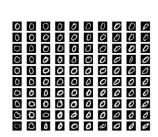
#### Limitations

#### Training instable

co-evolution of Generator / Discriminator

#### Mode collapse





# Limitations, 2

## **Generating monsters**













(Goodfellow 2016)

Arjovsky, Bottou 17

## Why minimizing KL fails

Minimizing 
$$KL(P_{real}||P_{gen}) = \int P_{real} \log \frac{P_{real}}{P_{gen}}$$

- For  $P_{real}$  high and  $P_{gen}$  low (mode dropping), high cost
- ▶ For  $P_{real}$  low and  $P_{gen}$  high (gen. monsters), no cost

#### The GAN solution: minimizing

$$\mathbb{E}_{\mathbf{x} \sim P_r}[\log D(\mathbf{x})] + \mathbb{E}_{\mathbf{x} \sim P_\sigma}[\log 1 - D(\mathbf{x})]$$

with

$$D^*(x) = \frac{P_r(x)}{P_r(x) + P_g(x)}$$

i.e., up to a constant, GAN minimizes

$$JS(P_{\mathit{real}}, P_{\mathit{gen}}) = rac{1}{2} \left( \mathit{KL}(P_{\mathit{real}}||\mathit{M}) + \mathit{KL}(P_{\mathit{gen}}||\mathit{M}) 
ight)$$

with 
$$M = \frac{1}{2}(P_{real} + P_{gen})$$

# Towards Principled Methods for Training Generative Adversarial Networks, 2

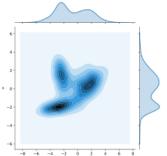
Arjovsky, Bottou 17

#### Unfortunately

If  $P_r$  and  $P_g$  lie on non-aligned manifolds, exists a perfect discriminator; this is the end of optimization !

Proposed alternative: use Wasserstein distance

$$min_G max_D \mathbb{E}_{x \sim P_g}[D(x)] - \mathbb{E}_{x \sim P_r}[D(x)] = min_G W(P_r, P_g)$$



#### Does not solve all issues!

Pb of vanishing/exploding gradients in WGAN, addressed through weight clipping  $% \left( \frac{1}{2}\right) =0$  careful tuning needed

New Regularizations

Improved Training of Wasserstein GANs

Gulrajani, Ahmed, Arjovsky, Dumoulin, Courville 17

Stabilizing Training of Generative Adversarial Networks through Regularization

Roth, Lucchi, Nowozin, Hofmann, 17

## Which Training Methods for GANs do actually Converge?

Mescheder, Geiger and Nowozin, 18

Simple experiments, simple theorems are the building blocks that help us understand more complicated systems. Ali Rahimi - Test of Time Award speech, NIPS 2017

# Which Training Methods for GANs do actually Converge? 2

Mescheder, Geiger and Nowozin, 18

#### Toy example

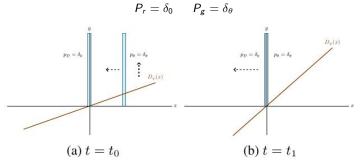
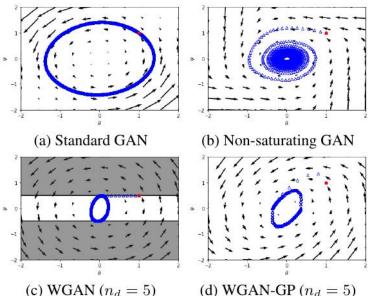


Figure 1. Visualization of the counterexample showing that in the general case, gradient descent GAN optimization is not convergent: (a) In the beginning, the discriminator pushes the generator towards the true data distribution and the discriminator's slope increases. (b) When the generator reaches the target distribution, the slope of the discriminator is largest, pushing the generator away from the target distribution. This results in oscillatory training dynamics that never converge.

# Which Training Methods for GANs do actually Converge? 2

Mescheder, Geiger and Nowozin, 18

Lesson learned: cyclic behavior for GAN and WGAN



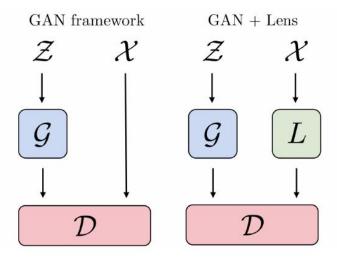
## State-of-the-art Generative Adversarial Networks



## **Tempered Adversarial Networks**

Sajjadi, Parascandolo, Mehrjou, Scholkopf 18

Principle: Life too easy for the discriminator!



## **Tempered Adversarial Networks**

Sajjadi, Parascandolo, Mehrjou, Scholkopf 18

## Principle: An adversary to the adversary

▶ ⇒ Provide L(X) instead, with L aimed at: i) deceiving the discriminator; ii) staying close from original images

$$min_{G} max_{D} \mathbb{E}_{x \sim P_{r}}[logD(x)] + \mathbb{E}_{x \sim P_{g}}[log(1D(x))]$$

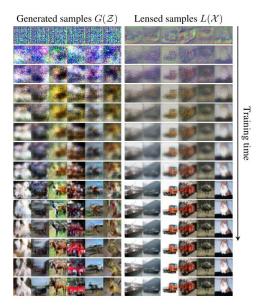
with D trained from  $\{(L(x),1)\} \cup \{G(z),0\}$  and Lens L optimized

$$L^* = \arg\min -\lambda \mathcal{L}(D) + \sum_i \|L(x_i) - x_i\|^2$$

and  $\lambda \to 0$ .

## Tempered Adversarial Networks, 2

Sajjadi, Parascandolo, Mehrjou, Scholkopf 18



#### **Partial conclusions**

- ▶ Deep revolution: Learning representations
- Adversarial revolution: a Turing test for machines
- Where is the limitation ? VAE: great but blurry GAN: great but mode dropping the loss function needs more work.

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