

# MOBILE ROBOTICS

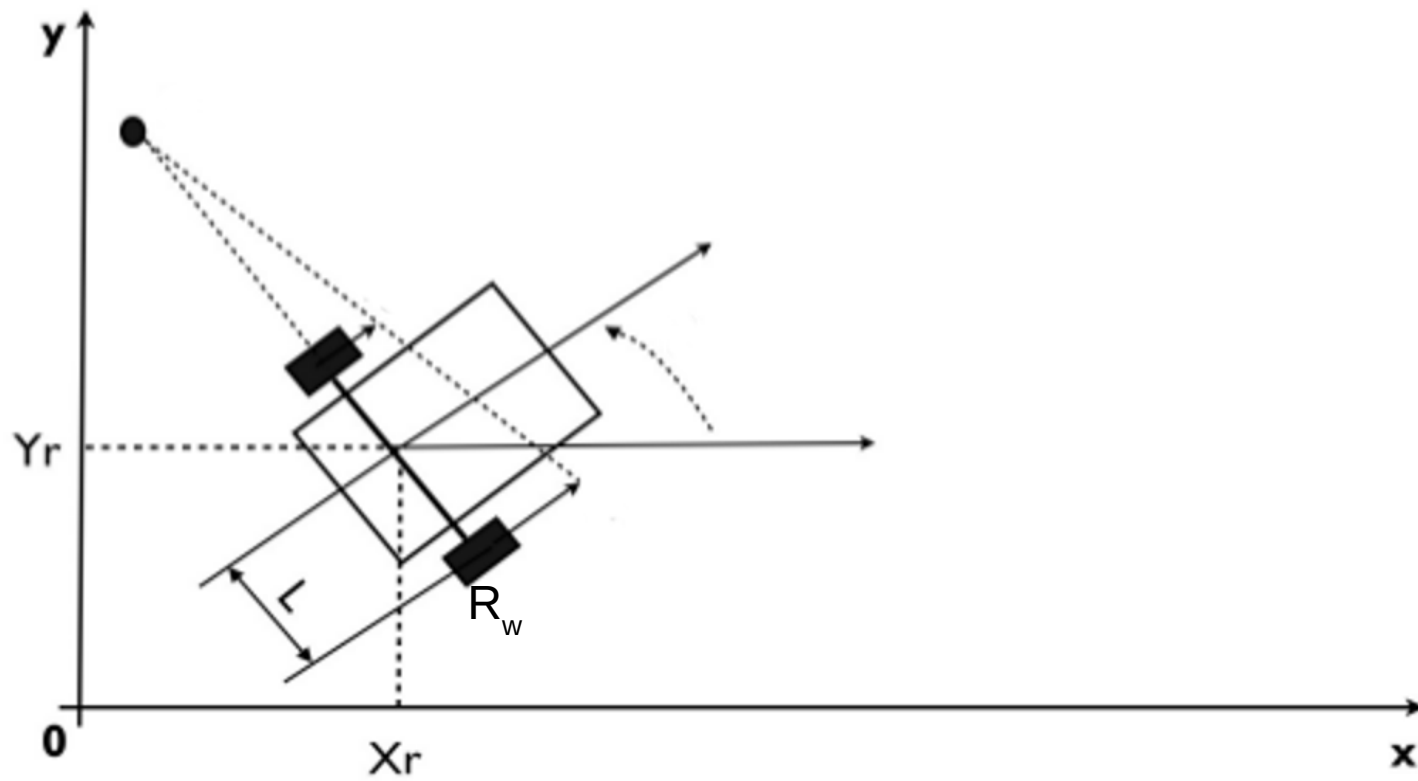
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# Goals of the day :

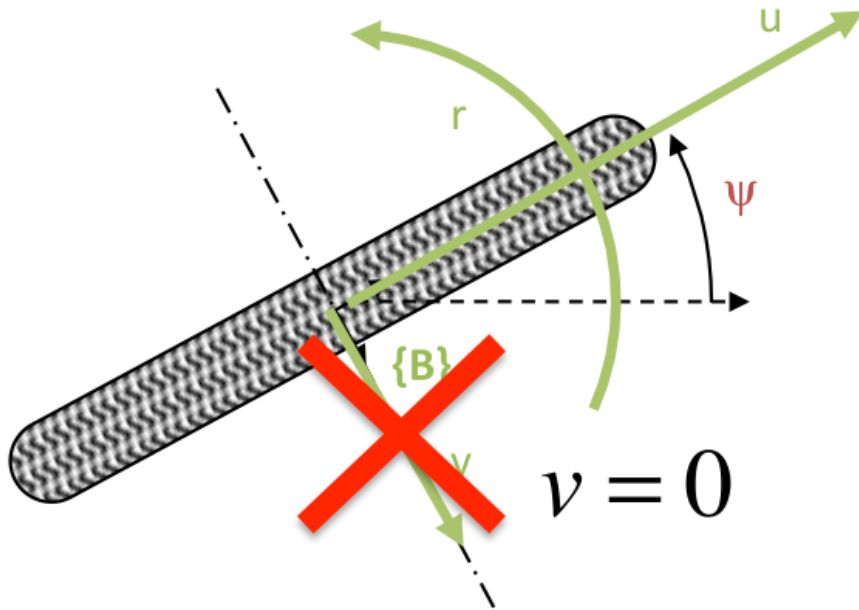
- Analyze three kinds of mobile robots :
  - Dual-wheel unicycle
  - Three-wheel omnidirectionnal
  - Four-wheel mecanum
- Wheels
  - Classic
  - Swedish wheel
  - Mecanum wheel
- Control processes
  - Mathematical model
  - Vector control
  - Command programming



# Dual-wheeled unicycle Robot

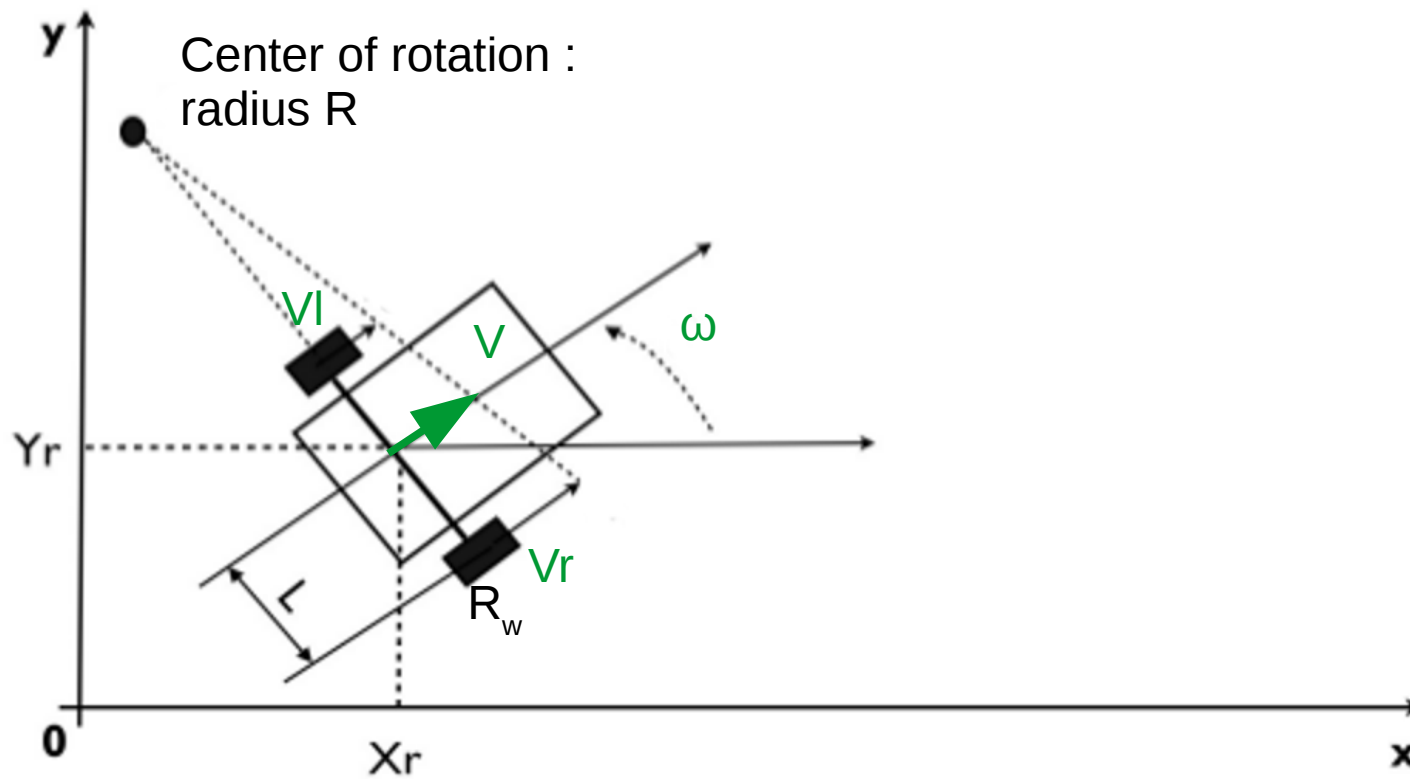


# Classic wheel



- rotates on itself
- moves on  $u$
- DOES NOT move on  $v$

# Dual-wheeled unicycle Robot



Using Thales's theorem

$$\frac{V_r}{R+L} = \frac{V_l}{R-L} = \frac{V}{R}$$

and

$$V = R \cdot \omega$$

$$V_r = R_w \cdot \omega_r \text{ and } V_l = R_w \cdot \omega_l$$

# Dual-wheeled unicycle Robot

Control parameters :  $\vec{V}, R$

Control vectors :  $\vec{V}, \vec{\omega}$

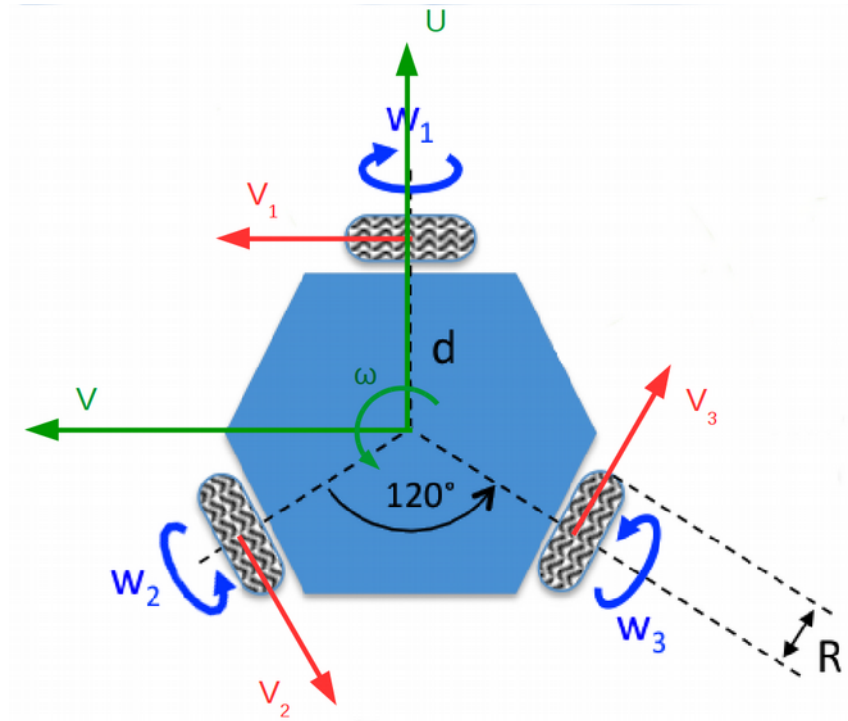
$$\omega_r = \frac{R + L}{R_w \cdot R} V$$

$$\omega_r = \frac{V + L \cdot \omega}{R_w}$$

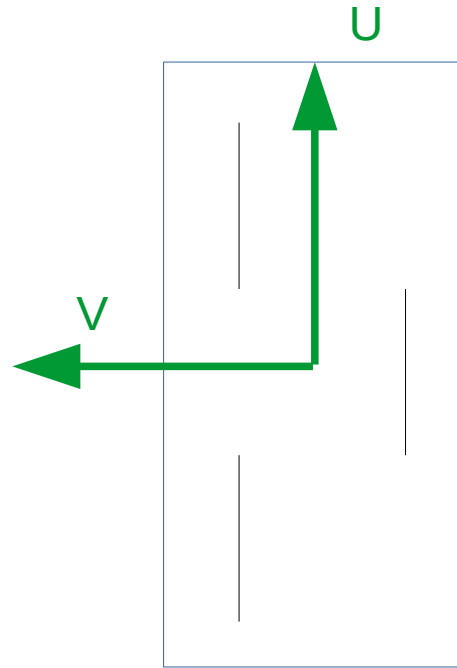
$$\omega_l = \frac{R - L}{R_w \cdot R} V$$

$$\omega_l = \frac{V - L \cdot \omega}{R_w}$$

# OMNIDIRECTIONAL Robot



# Omnidirectional wheel (Swedish wheel)

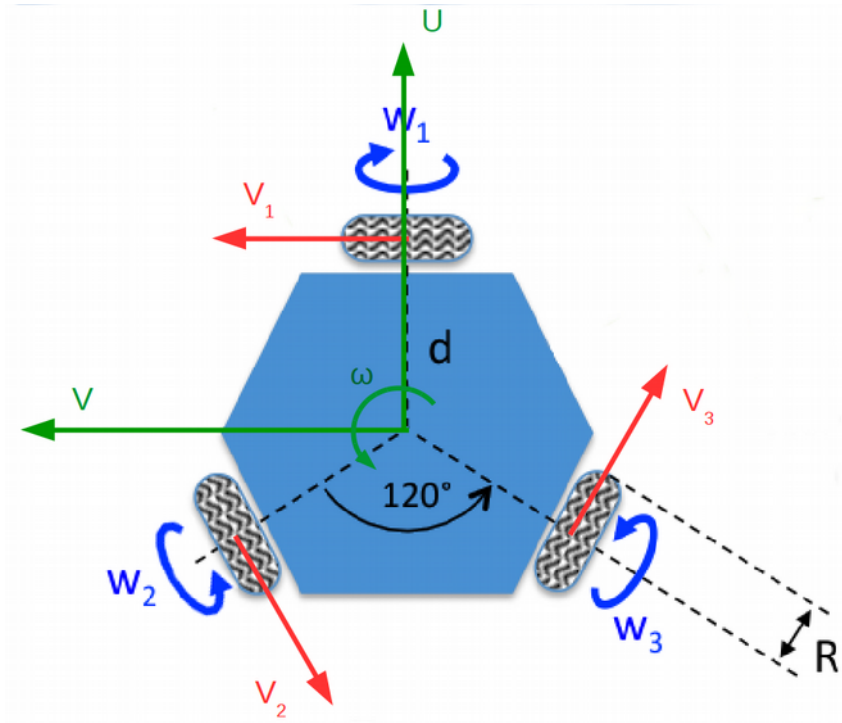


- rotates on itself
- moves on U (controlled)
- moves on V (free)

Bottom view



# OMNIDIRECTIONAL Robot



Independant control vectors :

$$\vec{u}, \vec{v}, \vec{\omega}$$

Any translation, rotation  
When and where you want...

# HOW IT WORKS...

Speed equation :

$$v_1 = -u \cdot \sin(0) + v \cdot \cos(0) + d \cdot \omega$$

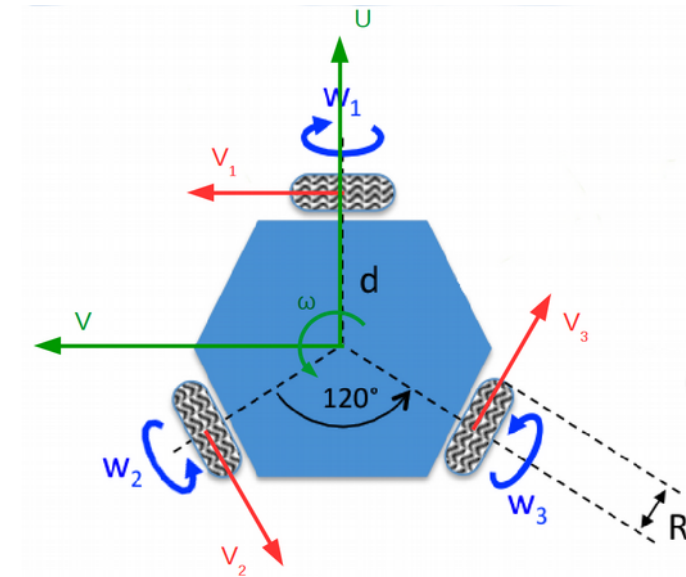
$$v_2 = -u \cdot \sin\left(\frac{2\pi}{3}\right) + v \cdot \cos\left(\frac{2\pi}{3}\right) + d \cdot \omega$$

$$v_3 = -u \cdot \sin\left(-\frac{2\pi}{3}\right) + v \cdot \cos\left(-\frac{2\pi}{3}\right) + d \cdot \omega$$

Motor command :

$$\omega_1 = \frac{v_1}{R} \quad \omega_2 = \frac{v_2}{R} \quad \omega_3 = \frac{v_3}{R}$$

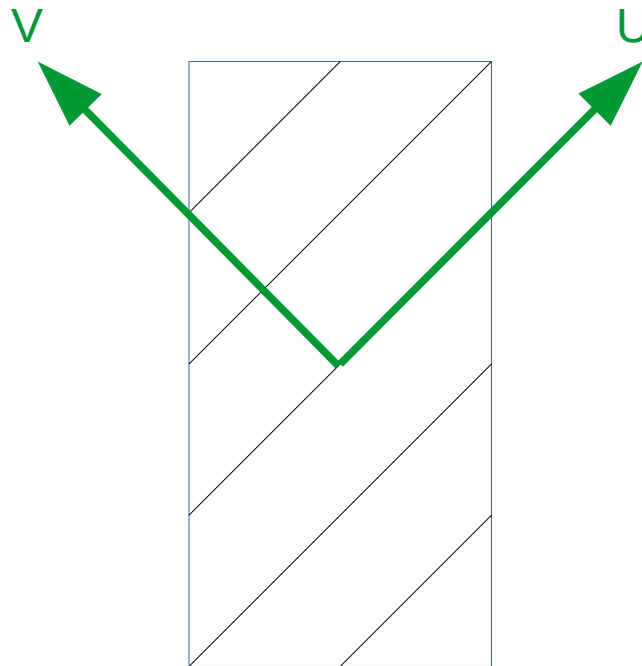
Control Vectors :  $\vec{u}, \vec{v}, \vec{\omega}$



# Robot MECANUM



# Mecanum wheel

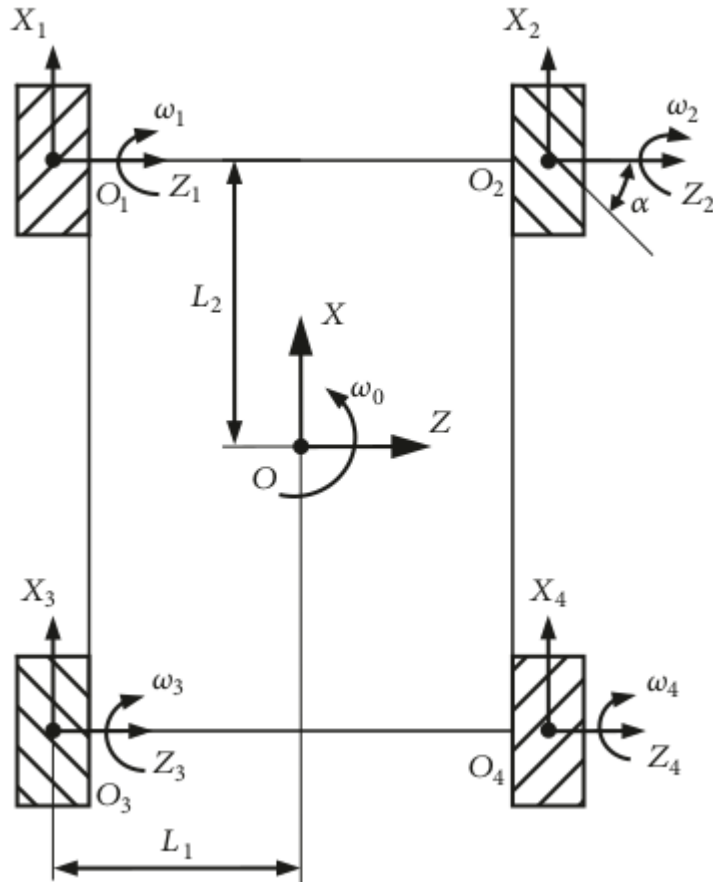


- rotates on itself
- moves on U (controlled)
- moves on V (free)

Bottom view

# Robot MECANUM

Speed motor equation

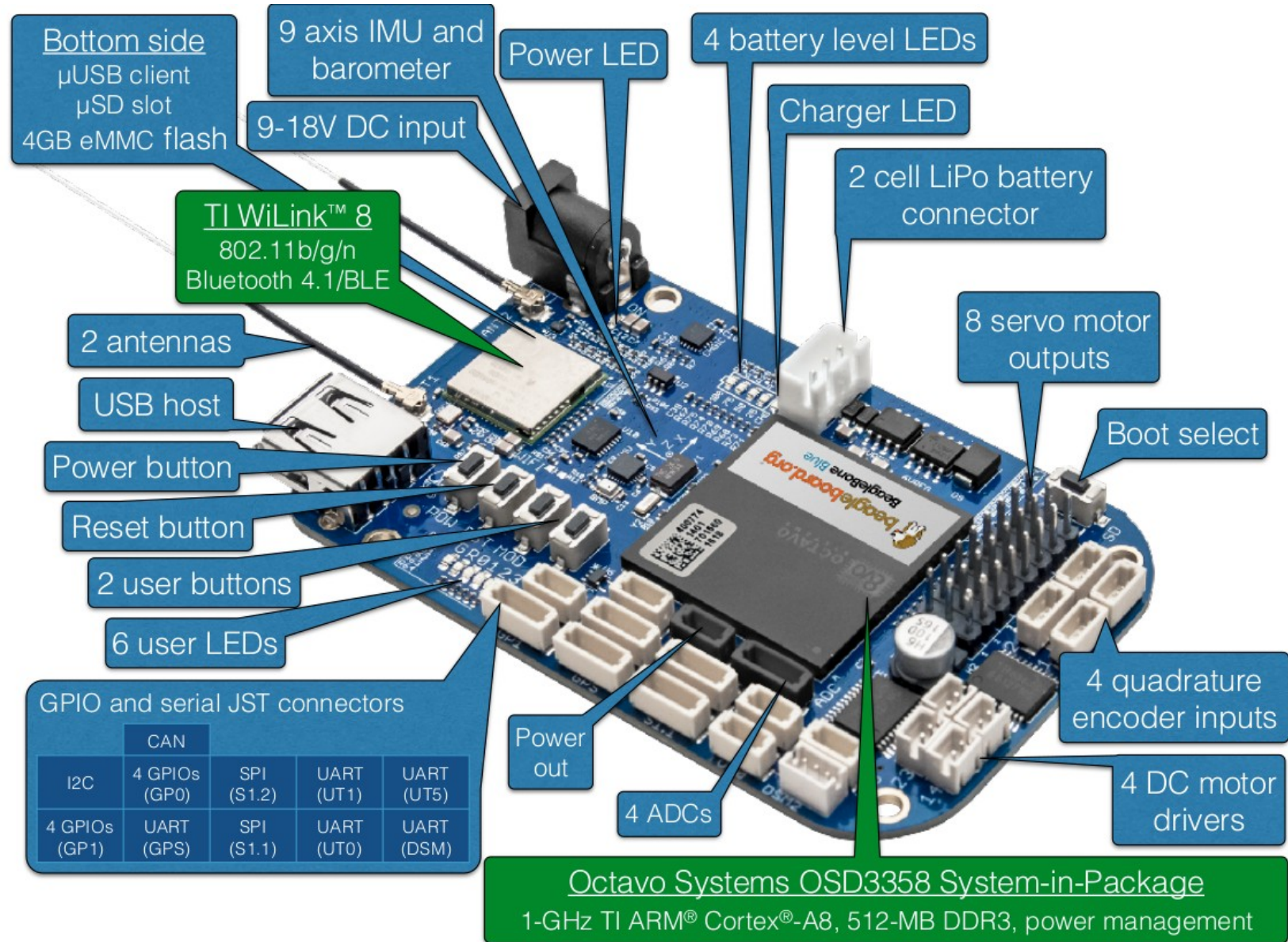


$$\begin{pmatrix} \omega_1 \\ \omega_2 \\ \omega_3 \\ \omega_4 \end{pmatrix} = \frac{1}{r} \begin{pmatrix} 1 & 1 & -(L_1 + L_2) \\ -1 & 1 & -(L_1 + L_2) \\ 1 & -1 & -(L_1 + L_2) \\ -1 & -1 & -(L_1 + L_2) \end{pmatrix} \cdot \begin{pmatrix} u \\ v \\ \omega_0 \end{pmatrix}$$

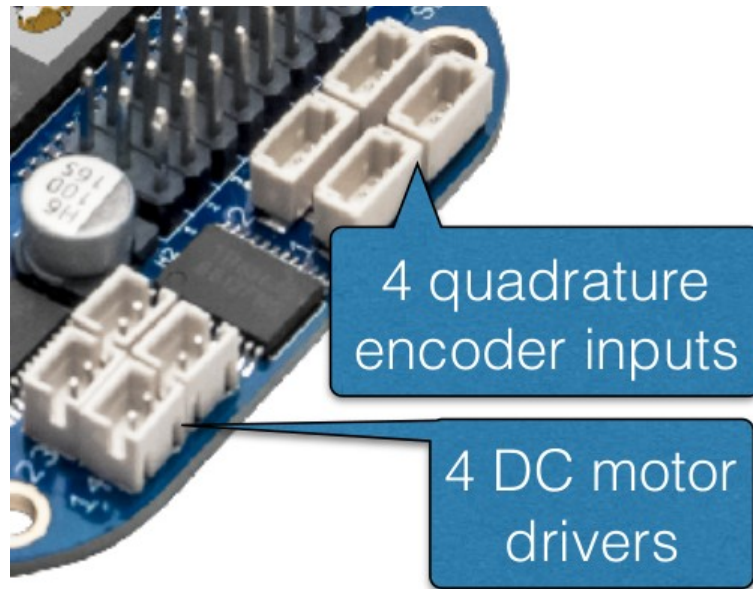
$$\begin{pmatrix} u \\ v \\ \omega_0 \end{pmatrix} = \frac{r}{4} \begin{pmatrix} 1 & 1 & 1 & 1 \\ -1 & 1 & 1 & -1 \\ -\frac{1}{L_1 + L_2} & \frac{1}{L_1 + L_2} & -\frac{1}{L_1 + L_2} & \frac{1}{L_1 + L_2} \end{pmatrix} \cdot \begin{pmatrix} \omega_1 \\ \omega_2 \\ \omega_3 \\ \omega_4 \end{pmatrix}$$



# The BeagleBoneBlue

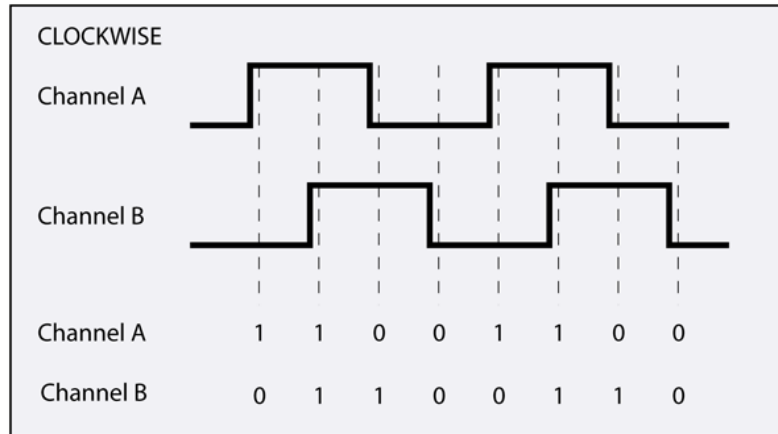


# The BeagleBoneBlue

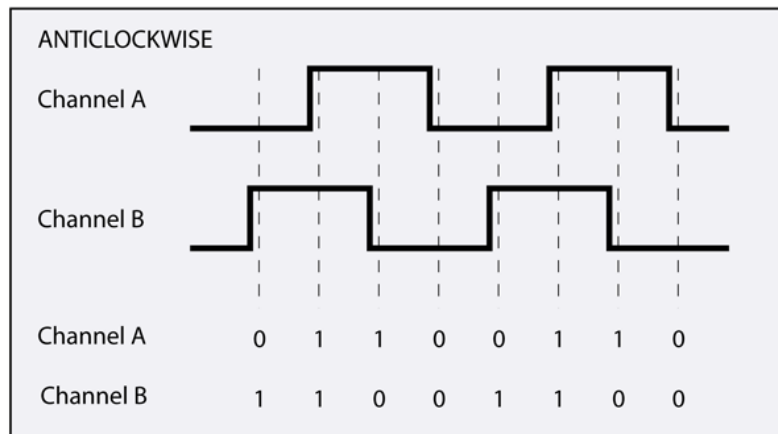


Code example in tutorial, and in the BeagleBone...

# Quadrature encoders



Counter up



Counter down

<http://www.creative-robotics.com/quadrature-intro>



# To Work !

- Choose your robot
- Follow the tutorial
- And make them move correctly