

## MATHEMATICS ACTIVITIES FOR S5

1. Simplify the following expression

a)  $\frac{\cos\theta \tan\theta \sin\theta}{\tan\theta}$

b)  $\sin\frac{\pi}{3}\cos\frac{\pi}{6} + \cos\frac{\pi}{3}\sin\frac{\pi}{6}$

c)  $\cos\phi\cos(90-\phi) - \sin\phi\sin(90-\phi)$

2. Angle A is an acute angle and  $\sin A = \frac{7}{25}$ , angle B is obtuse and  $\sin B = \frac{4}{5}$

Find an exact expression for : a)  $\sin(A+B)$

b) calculate the value of x if  $\sin(x+B)=15$

3. construct a circuit of the following statements and explain the observation

a)  $p \cup (q \cup r)$

b)  $(p \cup q) \cap (p \cup r)$

4. i) show that  $p \Rightarrow q$  and  $\neg p \cup q$  are logical equivalent and justify your answer

ii) How do we call this tautology ?

5. i) Write down the Cayley table for addition Modulo 5 on the set  $\mathbb{Z}$

Or  $(\mathbb{Z}_5, +) = ((\text{mod}5), +)$

ii) Verify if  $(\mathbb{Z}_5, +)$  Cayley table in ( bi) above is a commutative group

6. Express the following in symbolic form and then draw its truth table.

“ if you go to the market, you will need money and you will be able to buy anything”.

7. construct the truth table of this statement

$$[(p \Rightarrow q) \cap (q \cap r)] \Leftrightarrow (p \cup r)$$

8. prove that : a)  $\sin(x+30^\circ) + \sqrt{3}\cos(x+30^\circ) = 2\cos x$

b)  $\operatorname{cosec}\theta - \sin\theta = \cot\theta \cos\theta$

c) hence express  $\sin(165^\circ)$  in surd form

9. Mutesi stand on the bank of river and observes that the angle subtended by a tree on the opposite the bank is  $60^\circ$ , when she retreats from the bank she finds the angle to be  $30^\circ$

Find the height of the tree and the breath of the river

10. In the set  $\mathfrak{R}$  is defined the binary law “\*” by  $a * b = 2a + b + 1$

a) Evaluate i)  $\left[ \frac{2}{3} * \left( \frac{-1}{2} \right) \right] * (-1)$       ii)  $\left( 0 * \frac{4}{3} \right) * \left( -2 * \frac{1}{3} \right)$

b) is the law \* commutative ,associative ?

c) Find The real number x such that :  $x * 2 = \frac{5}{2} * x$

11. two side of triangle have lengths 25cm and 40cm respectively .the measure of their included angle is  $30^\circ$ , find the length of the opposite  $30^\circ$  approximately

12. a) convert the following degree :

i)  $135^\circ$  to radians

iii) 250 grad to radians

ii)  $6\frac{\pi}{6}$  to grades

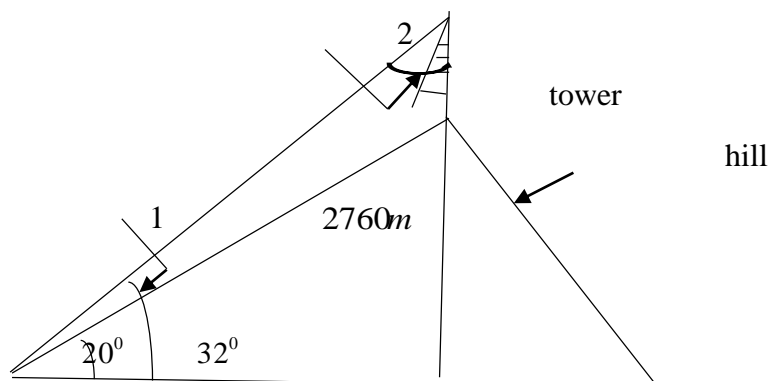
iv)  $2\frac{\pi}{3}$  to degrees

b) convert from  $60.26388889^\circ$  to  $d^\circ m' s''$  system

c) convert from  $30^\circ 15' 60''$  to decimal degrees

d) define the word “ complementary angle”

13. The distance from point A to the top of the hill is  $2760m$  .the angle of elevation from A to the base of the tower is  $28^\circ$  and the angle of elevation from A to the top of the tower is  $32^\circ$ .



- a) find the measures of angles 1 and 2
- b) find the height of the tower

14.Solve:

$$a) \cos 2x + 7 \sin x - 4 = 0$$

$$b) 2 \cos^2 x - 11 \sin x \cos x + 4 = 0$$

15.A ray of light is incident through glass with refractive index 1.5 , on an interface separating glass and water with refractive index 1.32.what is the angle of refraction if the angle of incident of the ray in glass is  $25^\circ$ ?

16.Given that  $24, 5x + 1, x^2 - 1$  are three consecutive terms of an arithmetic progression , find the values of  $x$  and the numerical value of the fourth term for each value of  $x$  found.

17. The product of three consecutive numbers in geometric progression is 27. The sum of the first two and nine times the third is -79. Find the numbers.

18.Insert 6 geometric means between 1 and  $-\frac{1}{128}$  .

19.Find the general solution of  $9^{\cos x} - 2 \cdot 3^{\cos x} + 1 = 0$

20.Solve for  $x$  : a)  $\begin{cases} \ln(xy) = 7 \\ \ln \frac{x}{y} = 1 \end{cases}$

$$b) \log_x 5 = \log_5 x$$

$$c) \sin 3x \cos 7x = 0$$

21.A man deposits 800,000frw his savings account on which interest is 15% per annum.If he makes no withdrawals ,after how many years will his balance exceed 8millions frw?

22.The end points of a straight line are given by  $(0.3, 0.8)$  and  $(1.8, 2.7)$ . Extrapolate the value of  $x = 2.3$

23.If  $A = \begin{pmatrix} -1 & -3 \\ 1 & 1 \end{pmatrix}$  and  $B = \begin{pmatrix} 6 & 3 \\ 2 & 1 \end{pmatrix}$ , Find a)  $A^{-1}$ , b)  $B^{-1}$  and c)  $(AB)^{-1}$

24.Consider the following linear transformation defined on  $R^2$  by  $f(x, y) = (4x - 2y, 2x + y)$ . Determine its matrix relative to the basis  $e_1 = (1, 1), e_2 = (-1, 0)$

25.The heights (in meters) of six children are 1.42, 1.35, 1.37, 1.50, 1.38 and 1.30. Calculate the mean height and the standard deviation of the heights.

**GOOD-LUCK!!!!!!!!!!!!**

