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KAMONYI DISTRICT

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MODEL QUATIONS OF MATHEMATICS S4 MCE & S4 MEG

1. Convert the following radian measures to degrees:

- a) $\frac{\pi}{5}$ b) $\frac{3\pi}{5}$ c) $\frac{3\pi}{4}$ d) $\frac{\pi}{18}$
e) $\frac{\pi}{9}$ f) $\frac{7\pi}{9}$ g) $\frac{\pi}{10}$ h) $\frac{3\pi}{20}$
i) $\frac{5\pi}{6}$ j) $\frac{\pi}{8}$

2. Copy and complete the tables:

a)

Degrees	0	45	90	135	180	225	270	315	360
Radians									

b)

Degrees	0	30	60	90	120	150	180	210	240	270	300	330	360
Radians													

3.

The following are other trigonometric identities. Use the unit circle to prove that the identities are correct.

1. $1 + \tan^2 \theta = \sec^2 \theta$ ($\cos \theta \neq 0$)
2. $1 + \cot^2 \theta = \csc^2 \theta$ ($\sin \theta \neq 0$)
3. $\tan \theta + \cot \theta = \sec \theta \csc \theta$
4. $\sin^2 A - 4 \cos^2 A + 1 = 3 \sin^2 A - 2 \cos^2 A - 1$
5. $\frac{\cos^2 A}{1 + \tan^2 A} - \frac{\sin^2 A}{1 + \tan^2 A} = 1 - 2 \sin^2 A$

4.

Simplify the following:

(a) $\sin^2 2A + \cos^2 2A$

(b) $1 + \tan^2 \frac{A}{4}$

(c) $\sin^2 B + \cos^2 B$

(d) $\cos^2 \theta + 1$

(e) $\cos^2 4A + \sin^2 4A$

(f) $\cos^2 1\frac{1}{2} + \sin^2 1\frac{1}{2}$

(g) $\frac{\sin \theta}{\csc \theta} + \frac{\cos \theta}{\sec \theta}$

(h) $(\sin A + \cos A)^2 + (\sin A - \cos A)^2$

(i) $1 - \sin^2 A$

(j) $1 - \cos^2 2B$

(k) $\sec^2 \theta - 1$

(l) $1 - \csc^2 A$

5.

2. Simplify each of the following expressions:

(a) $\sin \theta \cos 2\theta + \cos \theta \sin 2\theta$

(b) $\cos \alpha \cos (90^\circ - \alpha) - \sin \alpha \sin (90^\circ - \alpha)$

(c) $\frac{\tan a + \tan 2a}{1 - \tan a \tan 2a}$

(d) $\frac{\tan 3\beta + \tan 2\beta}{1 + \tan 3\beta \tan 2\beta}$

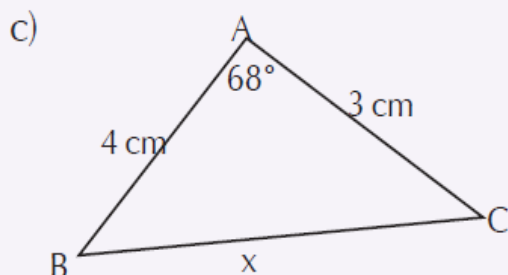
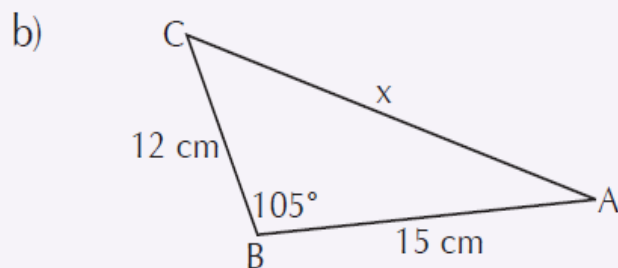
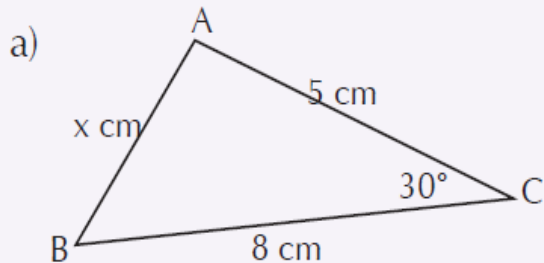
3. Angle A is an acute angle and $\sin A = \frac{7}{25}$. Angle B is obtuse and $\sin B = \frac{4}{5}$. Find an exact expression for:

(a) $\sin (A + B)$

(b) $\cos (A + B)$

(c) $\tan (A + B)$.

6.

Find the lengths of the unknown side x in the given triangles:

7 A.

Find the sizes of all angles in the triangles below:

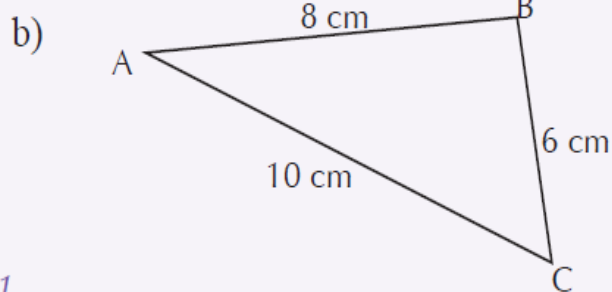
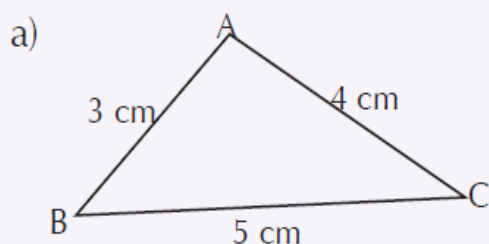


Fig 1.31

7 B.

Solve the triangles with the following sides:

- a) $a = 10 \text{ cm}$, $b = 8 \text{ cm}$, $c = 12 \text{ cm}$ b) $a = 6 \text{ cm}$, $b = 5 \text{ cm}$, $c = 7 \text{ cm}$

7 C.

Solve the triangles with the following measures:

- a) $a = 5 \text{ cm}$, $b = 6 \text{ cm}$, $C = 45^\circ$ b) $a = 12 \text{ cm}$, $B = 57^\circ$, $c = 15 \text{ cm}$
 c) $B = 117^\circ$, $a = 3.4 \text{ cm}$, $c = 2.7 \text{ cm}$ d) $B = 60^\circ$, $a = 12 \text{ cm}$, $c = 15 \text{ cm}$

1. Find the measures of the unknown sides x in the triangles below.

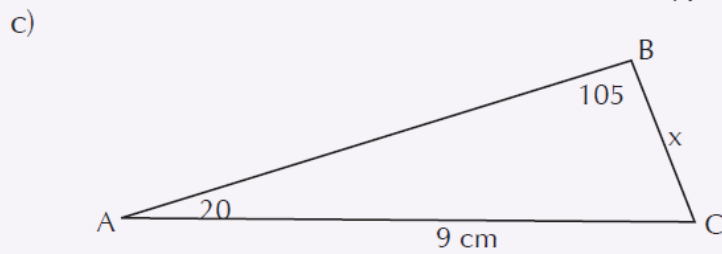
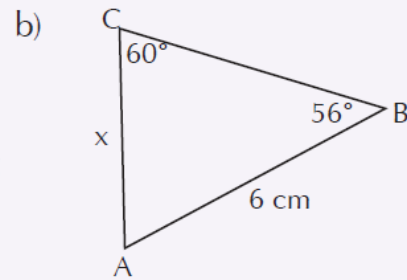
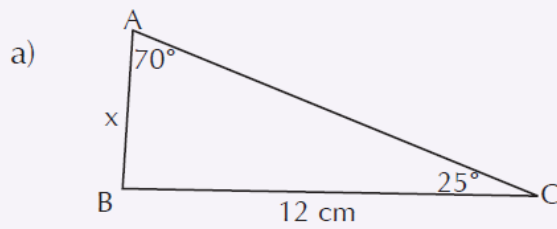


Fig 1.35

1. Find the measures of the unknown sides x in the triangles below.

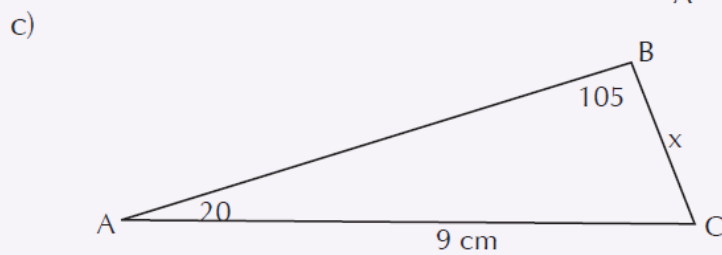
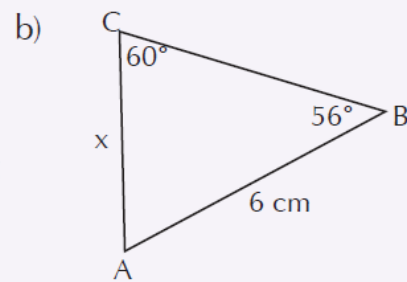
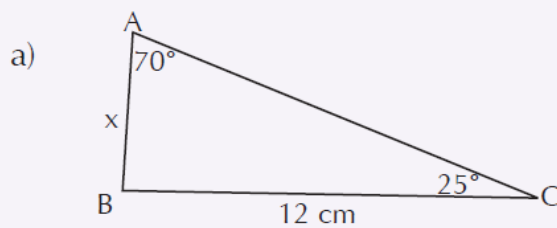


Fig 1.35

8

Find the measures of the unknown sides x in the triangles below.

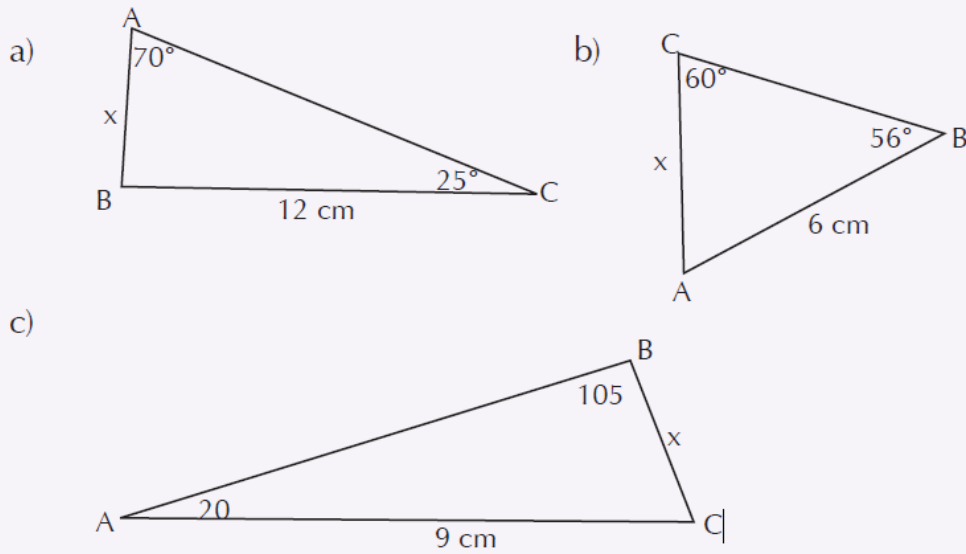


Fig 1.35

9.

Find the measures of the unknown sides x in the triangles below.

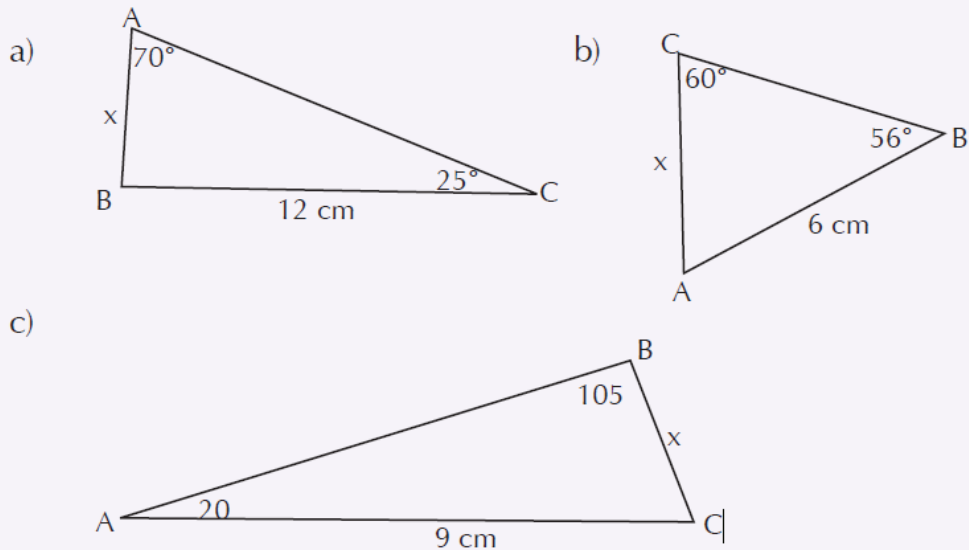


Fig 1.35

10.

Construct a circuit for each of the following statements:

1. $p \vee (q \vee r)$

3. $p \wedge (q \vee r)$

2. $(p \vee q) \vee r$

4. $(p \wedge q) \vee (p \wedge r)$

11.

Solve and graph the following:

1. $y \leq 3$

2. $y = \frac{1}{2}x - 3$

3. $y = -3x + 2$

4. $y \geq -2$

5. $2y - x \leq 6$

6. $\frac{y}{2} + 2 > x$

12.

1. Construct truth tables for each of the following statements:

a) $p \wedge (\sim p)$

b) $\sim [p \wedge (\sim p)]$

c) $p \wedge (\sim q)$

d) $\sim p \vee q$

e) $\sim [p \wedge (\sim q)]$

f) $p \wedge (q \vee r)$

g) $(p \wedge q) \wedge (\sim p)$

h) $\sim [(\sim p) \vee (\sim q)]$

i) $(\sim p \vee q) \wedge ((\sim p) \wedge (\sim q))$

13. Discuss about the solution of the equation, where **m is a parameter**

1. $Mx + 56 = 0$

2. $(m+1)x = 2x + m+2$

3. $\frac{m+5}{x+1} = \frac{m+2}{x}$

4. $(m-2)x + 3m = 2$

5. $x + 4 = m$

6. $(m-1)x = x - m$

7. $\frac{mx+3}{m} = \frac{1}{2}$

8. $\frac{x}{3m+2} = \frac{2x+2}{m}$

14. Discuss about the following inequalities

1. $mx - 34 < 0$

2. $(m-2)x \leq 3x - m + m$

3. $\frac{m+3}{x+2} > \frac{m-2}{x}$

4. $(m-1)x - 2m < 2$

5. $x - 4 \geq m$

6. $(m-3)x > x - m$

7. $\frac{mx-3}{m} \leq \frac{1}{4}$

8. $\frac{x}{m+2} \leq \frac{x-2}{m}$

15. Solve the following inequalities

1. $|2x-1| > 5$

2. $2 \left| \frac{2x}{3} + 1 \right| \geq 4$

3. $|3-2x| < 3$

16. Rationalize the denominator

1. $\frac{5}{\sqrt{7}}$

2. $\frac{3-\sqrt{2}}{1-\sqrt{2}}$

3. $\frac{2\sqrt{6}}{\sqrt{2}+\sqrt{3}+\sqrt{5}}$

4. $\frac{2\sqrt{2}}{4+3\sqrt{3}}$

5. $\frac{a-\sqrt{b}}{\sqrt{d}}$

6. $\frac{3\sqrt{3}+2\sqrt{2}}{1+2\sqrt{2}}$

7. $\frac{2}{\sqrt{2}-\sqrt{3}+\sqrt{5}}$