

## MATHEMATICS ACTIVITIES FOR S6

1.Solve : a)  $3^{2x+1} - 3^{x+1} - 3^x + 1 = 0$

b) Use matrix inverse method to solve the following systems

$$\begin{cases} 4x + y - z = 1 \\ x - 3y + z = 2 \\ 5x - 2y = 4 \end{cases}$$

2.Solve the simultaneous equations :  $\begin{cases} z_1 + z_2 = 8 \\ 4z_1 - 3iz_2 = 26 + 8i \end{cases}$

Using values of  $z_1$  and  $z_2$ , Find the modulus and argument of  $z_1 + z_2 - z_1 z_2$

3.Differentiate  $y = [2x^2 + \sqrt[3]{(3x-1)^4}]^n$ , n is any constant.

4.Find the first derivative of  $f(x) = (\sin x)^{\log x}$

5.Event A and B are such that  $P(A) = 0.3$ ,  $P(B) = 0.8$  and  $P(A \cap B) = 0.4$  State ,giving a reason in each case whether events A and B are : a) independent

b) mutually exclusive.

6.Let the binary operation \*be defined on Z (ring of integers) by  $x * y = x + xy + y$

a) Calculate  $2*(-1)$ ,  $(-1)*9$ , and  $6*1$

b) Determine whether \* is commutative, associative or neither.

c)Determine whether or not there exist an identity for \* /1Mrk

7.A and B are points whose position vectors are  $a = 2i + k$  and  $b = i - j + 3k$  respectively, Determine the position vector of the point p that divided AB in the ratio 4:1

8.Given that  $\sin x + \sin y = \omega_1$  and  $\cos x + \cos y = \omega_2$ .show that

$$\tan\left(\frac{x+y}{2}\right) = \frac{\omega_1}{\omega_2}$$

9. The line  $x+2y$  intersects the curve  $xy+18=0$  at the points A and B. Find the coordinates of A and B. 10.Find the angle between planes  $\pi \equiv x + y + z = 1$  and  $\beta \equiv x - 2y + 3z = 1$  11.a)

Let  $f(x) = \frac{4x}{(3x+1)(x+1)^2}$

i) Express  $f(x)$  in partial fractions.

12.Obtain the regression equation of x on y and y on x taking the origin as 2 and 200 for x and y respectively:/15Marks

X	1	2	3	4	5
Y	166	184	142	180	338

13. Let  $f$  be a linear transformation so that  $f(x) = (x + 2y, 3x - 3y)$  and  $g(x) = (x + y, y)$  find:

i)  $fg(x, y)$

ii)  $gof(x, y)gf(x, y)$

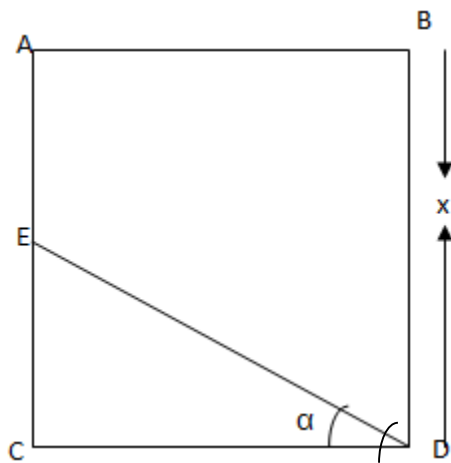
ii)  $f^{-1}(x, y)f^{-1}(x, y)$

14.a) Determine the domain of the function  $f(x) = \sqrt{4 - x^2} + \frac{1}{x}$

b) Find the period of the function  $f(x) = \tan(4\pi^2 - \frac{\pi}{3})$

15. Solve in  $\mathbb{R}$  the following equation:  $(x + \sqrt{x})^4 - (x + \sqrt{x})^2 = 159600$  16. a) Find the Cartesian equation of the plane  $\alpha$  which passes through the point  $p = (2, -3, 4)$  and is perpendicular to the line defined by the points  $a = (1, 5, 7)$  and  $b = (-2, 2, 3)$  b) for what value of  $\lambda$  are the vectors  $\vec{i} + 2\vec{j} - 3\vec{k}$ ,  $3\vec{i} + \lambda\vec{j} + \vec{k}$  and  $\vec{i} + 2\vec{j} + 3\vec{k}$  coplanar?

17. Consider the following figure



ABCD is a square,  $CE = AE$ ,  $\overline{BD} = X$ . Find

$\sin \alpha$ ,  $\cos \alpha$  and  $\tan \alpha$ .

18.a) show that  $c_{n-1,p-1} + c_{n-1,p} = c_{n,p}$   $0 \leq p \leq n$

b) Solve the equation  $c_{n-1,n-5} = 3c_{n-3,n-7}$  in the set of positive integers.

19. Evaluate the following limits:

a)  $\lim_{x \rightarrow \pm\infty} \sqrt{x^2 + x + 2} - \sqrt{x^2 - x + 3}$

b)  $\lim_{x \rightarrow 0} \frac{x^2 - x \sin x}{x^2 - \sin^2 x}$

20. Consider the vectors  $\vec{u} = (1, -3, 2)$   $\vec{v} = (2, -1, 1)$  of  $\mathbb{R}^3$

a) If  $\vec{w} = (1, 7, -4)$  is  $\{\vec{u}, \vec{v}, \vec{w}\}$  a basis of  $\mathbb{R}^3$ ?

b) For what value of real number  $k$ , the vector  $(1,k,5)$  is a linear combination of  $\vec{u}$  and  $\vec{v}$ ?

21. Consider the following linear mapping defined on  $\mathbb{R}^3$  by  $f(x, y, z) = (4x - 2z, 2x + y, z + y)$ . Calculate its matrix relative to the basis  $\{\vec{e}_1 = (1,1,1), \vec{e}_2 = (-1,0,1), \vec{e}_3 = (0,1,1)\}$

22. Use matrix inverse method to solve this system

$$\begin{cases} 4x + y - z = 1 \\ x - 3y + z = 2 \\ 5x - 2y = 4 \end{cases}$$

23.a) Find the equation of sphere which passes through the points  $(1,2,3)$ ,  $(0,-2,4)$ ,  $(4,-4,2)$  and  $(3,1,4)$

b) Find the center and radius of the sphere:

$$x^2 + y^2 + z^2 - 22x - 6y + 66$$

24. The coefficient of  $x^5$  in the expansion of  $(1 + 5x)^5$  is equal to the coefficient of  $x^4$  in the expansion of  $(a + 5x)^7$ . Find the value of  $a$ .

25. the perimeter of rectangle is 36 cm.

a) What are the dimensions (length and width) of that rectangle?

b) What is its greatest possible area?

26. In a physics experiment, a bottle of milk was brought from a cool room into a warm room. Its temperature  $y^\circ\text{C}$ , was recorded at  $t$  minutes after it was brought in, for 11 different values of  $t$ . The results are summarized as:  $\sum t = 44$ ,  $\sum y = 205$ ,  $\sum t^2 = 180.4$ ,  $\sum ty = 824.5$

(i) Calculate the equation of the line of regression of  $y$  on  $t$  in the form  $y = a + bt$ .

(ii) Explain the practical significance of the value of  $a$ .

(iii) Use your equation to estimate the values of  $y$  at  $t = 4.5$

**GOOD-LUCK**