

**A.A. 2021-2022**

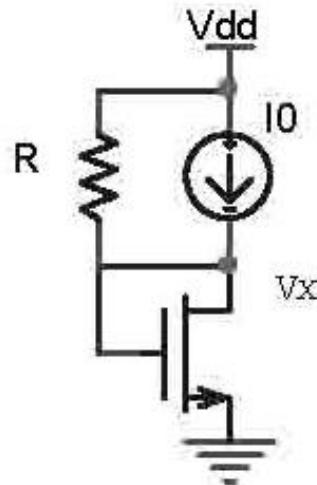
**Elementi di Elettronica (INF)**  
**Prof. Paolo Crippa**

**Esercizi – P4**

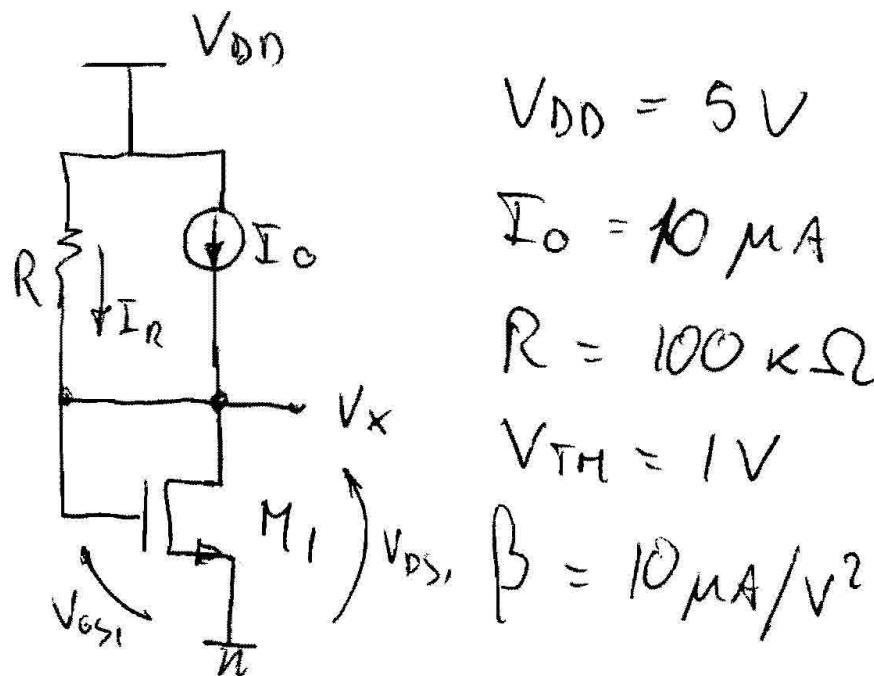
# Circuiti con MOSFET e BJT: Es. 1c

4) Dati  $V_{dd}=5V$ ,  $I_0=10\mu A$ ,  $R=100K\Omega$ ,  $V_{TH}=1V$ ,  $\beta=10\mu A/V^2$ , trovare: la zona di funzionamento dei MOSFET e le seguenti tensioni e correnti

M:  SAT  TRI  OFF     $I_D = \boxed{\quad} , \boxed{\quad} \mu A$ ,     $V_{out} = \boxed{\quad} , \boxed{\quad} , \boxed{\quad} V$ ,



# Es. 1c: Soluzione



$$V_{DD} = 5 \text{ V}$$

$$I_0 = 10 \mu\text{A}$$

$$R = 100 \text{ k}\Omega$$

$$V_{TH} = 1 \text{ V}$$

$$V_{DS1}, \beta = 10 \mu\text{A}/\text{V}^2$$

$M_1$  ?

$I_{D1}$  ?

$V_{out}$  ?

$$V_{GS1} = V_{DS1} \Rightarrow \boxed{M_1 \text{ SAT}}$$

$$I_{D1} = \frac{\beta}{2} (V_{GS1} - V_{TH1})^2$$

$$V_{GS1} = V_{DS1} = V_X ;$$

## Es. 1c: Soluzione

$$I_R = \frac{V_{DD} - V_x}{R} ;$$

$$I_{D1} = I_0 + I_R \Rightarrow$$

$$I_0 + \frac{V_{DD} - V_x}{R} = \frac{\beta_1}{2} (V_x - V_{TH1})^2$$

$$V_x = \begin{cases} +3.317 \\ -3.317 \end{cases} ?$$

$$V_{GS1} = V_x ; \text{ NMOS} \Rightarrow V_x = +3.317$$

$$I_{D1} = \frac{\beta}{2} (V_x - V_{TH1})^2 = 26.84 \mu A$$

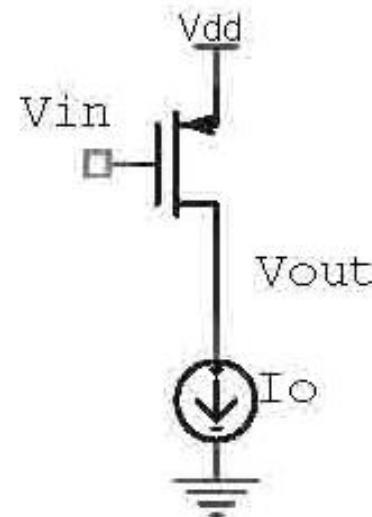
# Circuiti con MOSFET e BJT: Es. 2c

4) Dati  $V_{dd}=5V$ ,  $I_0=2\mu A$ ,  $V_{in}=3V$ ,  $V_{THP}=-1V$ ,  $\beta=20\mu A/V^2$ , trovare: la zona di funzionamento dei MOSFET e le seguenti tensioni e correnti, disegnare il circuito equivalente ed il guadagno di tensione

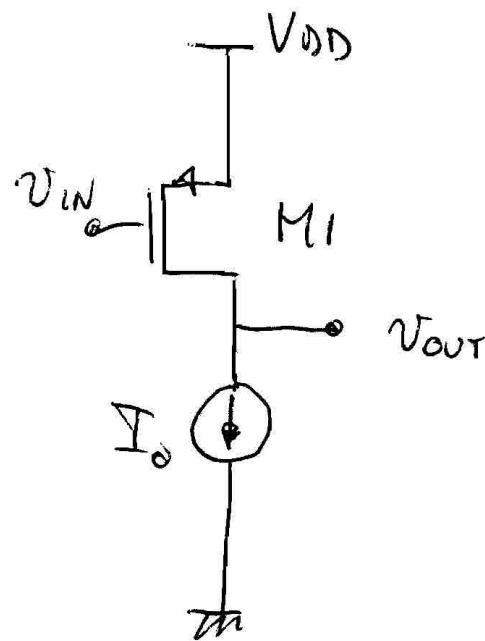
M:  SAT  TRI  OFF  $I_{D1} = \boxed{\phantom{000}}, \boxed{\phantom{000}} \mu A$ ,  $V_{out} = \boxed{\phantom{000}}, \boxed{\phantom{000}} V$ ,

$g_m = \boxed{\phantom{000}}, \boxed{\phantom{000}} \mu \Omega^{-1}$ ,  $g_o = \boxed{\phantom{000}}, \boxed{\phantom{000}} \mu \Omega^{-1}$ ,

$v_{out}/v_{in} = \boxed{\phantom{000}}, \boxed{\phantom{000}}$  (in forma simbolica)  $v_{out}/v_{in} =$



## Es. 2c: Soluzione



$$V_{DD} = 5V$$

$$I_o = 2\mu A$$

$$V_{IN} = 2V$$

$$V_{THP} = -1V$$

$$\beta_1 = 20 \text{ mA/V}^2$$

$$I_{D1} = ?$$

$$V_{OUT} = ?$$

$$g_m = ?$$

$$g_o = ?$$

$$\frac{V_{OUT}}{V_{IN}} = ?$$

$$V_{GS} = V_{IN} - V_{DD} = 3 - 5 = -2V \stackrel{?}{<} V_{TH1} = -1 \quad \text{or} \quad \boxed{M1 \text{ ON}}$$

M<sub>p</sub> (M<sub>1</sub> SAT)

$$I_{D1} = \frac{\beta_1}{2} (V_{GS} - V_{TH})^2 = \frac{20}{2} 10^{-6} \cdot (-2 - 1)^2 = 10 \mu A \neq I_o = 2 \mu A$$

→ ←

## Es. 2c: Soluzione

$\Rightarrow M1 \text{ TR1}$

$$V_{DS1} > V_{GS1} - V_{TH1},$$

$$I_D = \beta_1 \left[ (V_{GS1} - V_{TH1}) V_{DS1} - \frac{V_{DS1}^2}{2} \right] = I_0$$

$$5 V_{DS}^2 + 10 V_{DS} + 1 = 0 \quad V_{DS} = \begin{cases} -0.1055 \\ -1.894 \end{cases} ?$$

$$V_{DS} > V_{GS} - V_{TH} \Rightarrow -1.894 > -2 + 1 = -1 \quad \text{no!}$$

$$-0.1055 > -1 \quad \text{sì!}$$

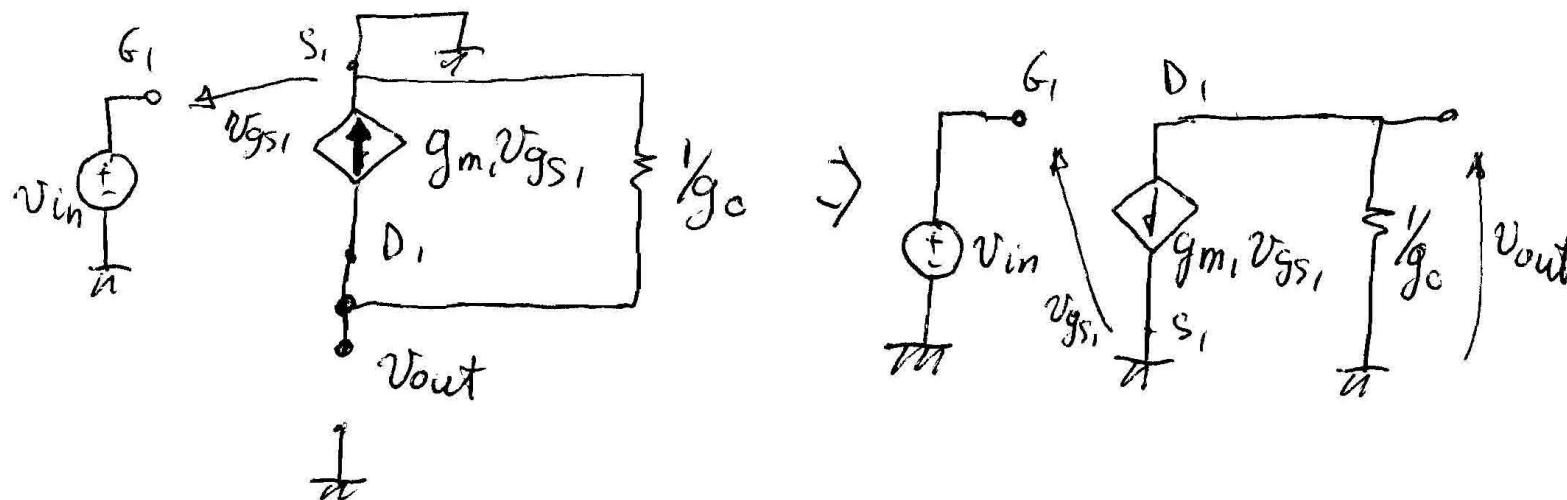
$$\Rightarrow V_{DS} = -0.1055 \text{ V}$$

$$V_{OUT} = V_{DD} + V_{DS} = V_{DD} - V_{SD} = 5 - 0.1055 = 4.8945 \text{ V}$$

## Es. 2c: Soluzione

$$g_{m1} = \beta V_{SD} = 20 \cdot 10^{-6} \cdot 0.1055 = 2.11 \mu S$$

$$g_0 = \beta (V_{SG} + V_{TH} - V_{SD}) = 20 \cdot 10^{-6} (2 - 1 - 0.1055) \\ = 17.89 \mu S$$



$$v_{out} = -g_{m1} v_{gs1} \cdot \frac{1}{g_0} ; \quad v_{gs1} = v_{in} \quad A_2 = \frac{v_{out}}{v_{in}} = -\frac{g_{m1}}{g_0} = -0.118 \frac{V/V}{V/V}$$

# Circuiti con MOSFET e BJT: Es. 3c

- 5) Dati  $V_{dd}=5V$ ,  $V_{in}=3V$ ,  $I_{in}=10\mu A$ ,  $V_{TH5}=1V$ ,  $V_{TH6}=-1V$ ,  $\beta_5=\beta_6=200\mu A/V^2$ , per i diodi  $V_g=0.6V$   $r_d=0\Omega$   
Trovare il valore delle seguenti tensioni e correnti. Trovare inoltre la zona di funzionamento dei MOSFET e dei diodi.

M5: [SAT] [TRI] [OFF] M6: [SAT] [TRI] [OFF]

D1:[ON] [OFF] D2:[ON] [OFF] D3:[ON] [OFF] D4:[ON] [OFF]

$I_{D1}= \square, \square, \square, \square \mu A$ ,  $I_{D4}= \square, \square, \square, \square \mu A$ ,

$I_{D5}= \square, \square, \square, \square \mu A$ ,  $I_{D6}= \square, \square, \square, \square \mu A$ ,

$V_x= \square, \square, \square, \square V$ ,  $V_y= \square, \square, \square, \square V$ ,  $V_{out}= \square, \square, \square, \square V$ ,

- 6) Trovare i parametri differenziali del circuito dell'esercizio 5 e disegnare il circuito equivalente

circuito equivalente :

$gm_5= \square, \square, \square, \square, \square \mu \Omega^{-1}$ ,

$go_5= \square, \square, \square, \square, \square \mu \Omega^{-1}$ ,

$gm_6= \square, \square, \square, \square, \square \mu \Omega^{-1}$ ,

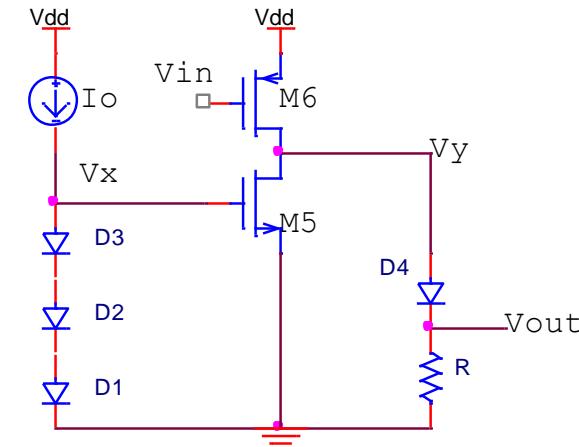
$go_6= \square, \square, \square, \square, \square \mu \Omega^{-1}$ ,

- 7) Trovare il guadagno di tensione del circuito dell'es. 5

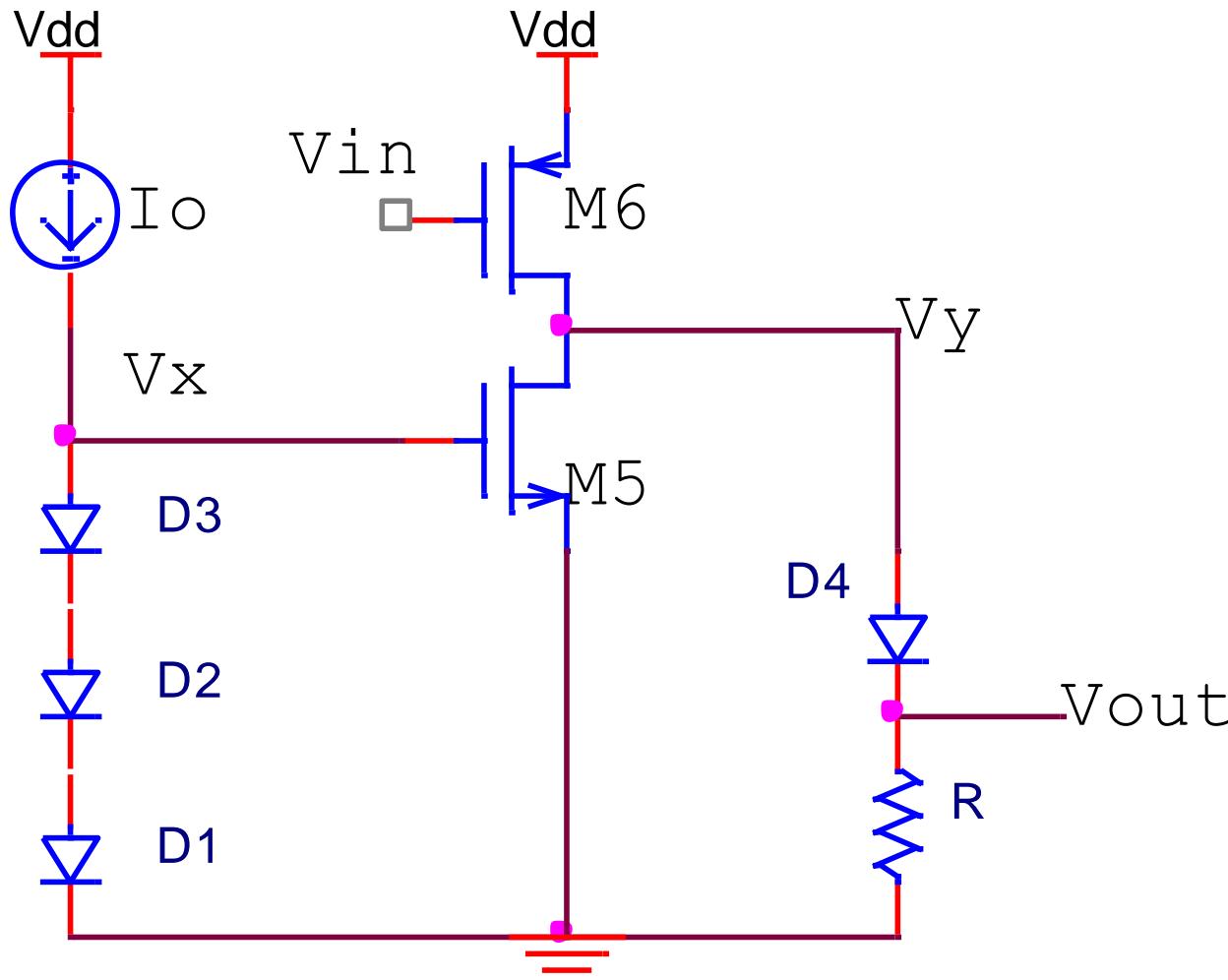
$v_{out}/v_{in}= \square, \square, \square, \square$

(in forma simbolica)

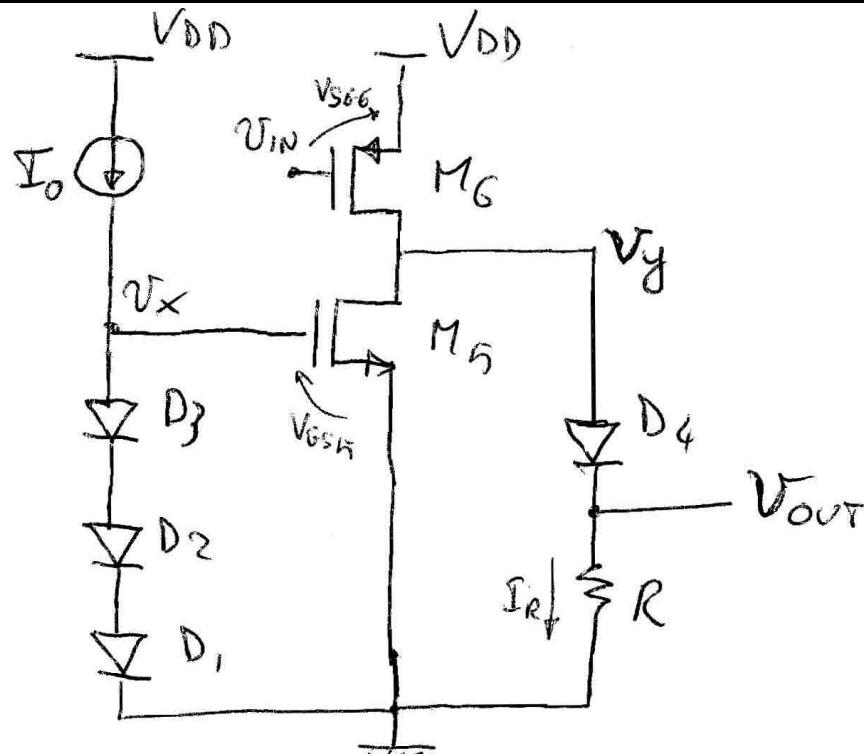
$v_{out}/v_{in}=$



# Circuiti con MOSFET e BJT: Es. 3c



# Es. 3c: Soluzione



$$V_{DD} = 5V$$

$$V_{IN} = 3V$$

$$I_0 = 10\mu A \quad R = 30 k\Omega$$

$$|V_{TH}| = 1V$$

$$\beta_5 = \beta_6 = 200 \mu A/V^2$$

$$\left. \begin{array}{l} V_T = 0.6V \\ R_d = 0\Omega \end{array} \right\} D_1, D_2, D_3, D_4$$

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$$I_{D1} = ? \quad I_{D2} = ? \quad I_{D3} = ? \quad I_{D5} = ? \quad I_{D6} = ? \quad V_x = ? \quad V_y = ? \quad V_{OUT} = ?$$


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$$I_{D1} = I_{D2} = I_{D3} = I_0 = 10\mu A \Rightarrow [D_1, D_2, D_3 \text{ ON}]$$

$$V_{GS6} = V_{IN} - V_{DD} = 3 - 5 = -2V < -1V = V_{TH6} \Rightarrow V_{GS6} < V_{TH6}$$

[M6 ON]

H.p. (M6 SAT)

## Es. 3c: Soluzione

Hp. M6 SAT

$$I_{D6} = \frac{\beta_6}{2} (V_{GS6} - V_{TH6})^2 = \frac{200 \cdot 10^{-6}}{2} (-2+1)^2 = 100 \cdot 10^{-6} = 100 \mu A$$

$$V_{GS5} = V_f + V_f + V_f = 3 \cdot 0.6 = 1.8 V > V_{TH5} = 1 V$$

M5 ON

Hp M5 SAT

$$I_{D5} = \frac{\beta_5}{2} (V_{GS5} - V_{TH5})^2 = \frac{200 \cdot 10^{-6}}{2} (1.8 - 1)^2 = 64 \mu A$$

$$I_R = I_{D6} - I_{D5} = 36 \mu A$$

$$I_{D4} = 36 \mu A \Rightarrow D4 \text{ ON}$$

$$V_{OUT} = R \cdot I_R = 36 \cdot 10^{-6} \cdot 30 \cdot 10^3 = 1.08 V$$

$$V_y = V_{OUT} + V_f = 1.68 V \quad V_x = V_{GS5} = 1.8 V$$

## Es. 3c: Soluzione

$$V_{DS5} = V_y = 1.68V \stackrel{?}{>} V_{GS5} - V_{TH5} = 1.8 - 1 = 0.8 \quad (\text{OK})$$

M5 SAT

$$V_{DS6} = V_y - V_{DD} = 1.68 - 5 = -3.32 \stackrel{?}{<} V_{GS6} - V_{TH6} = -2 + 1 = -1 \quad (\text{OK})$$

M6 SAT

$$g_{m5} = \beta_5 (V_{GS5} - V_{TH5}) = 160 \mu\text{S}$$

$$g_{o5} = 0 \mu\text{S}$$

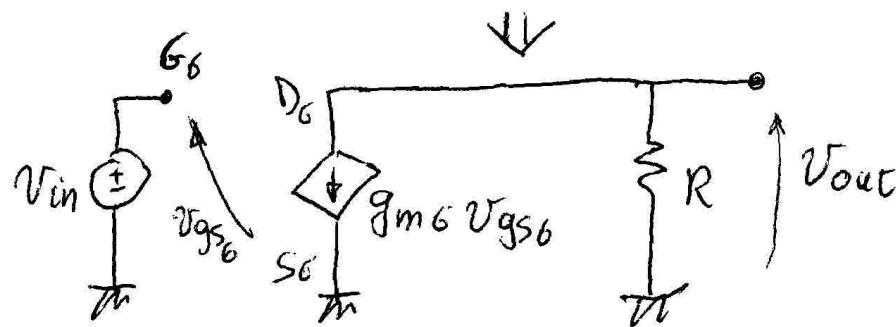
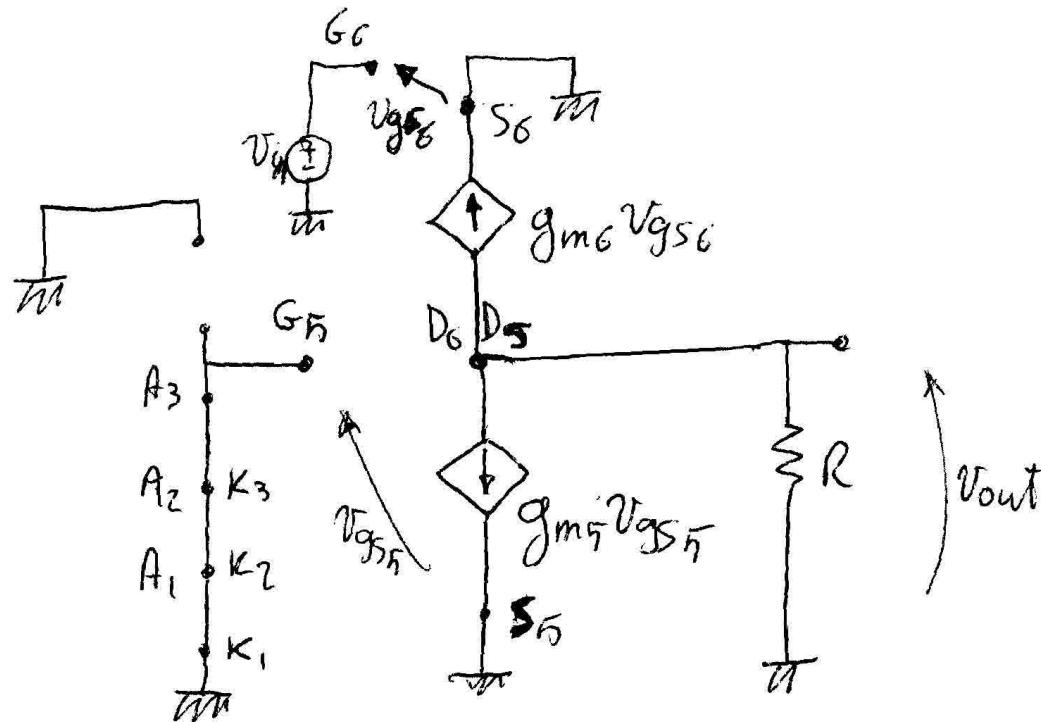
$$* g_{m6} = \beta_6 (V_{GS6} + V_{TH6}) = 200 \cdot 10^{-6} (2 - 1) = 200 \mu\text{S}$$

$$g_{o6} = 0 \mu\text{S}$$

$$R_d = 0$$

$$* g_{m6} = -\beta_6 (V_{GS6} - V_{TH6}) = \sqrt{2\beta_6 I_{D6}}$$

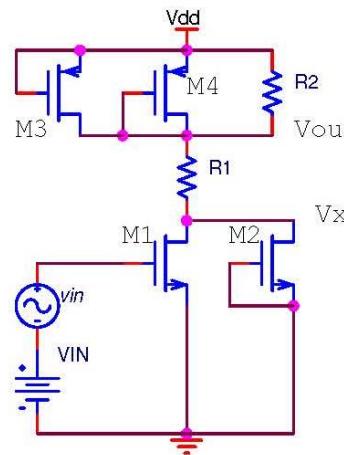
# Es. 3c: Soluzione



$$V_{out} = -g_{m6} v_{gs6} R ; \quad v_{gs6} = V_{in} ; \quad A_V = \frac{V_{out}}{V_{in}} = -g_{m6} R = -6 V/V$$

# Circuiti con MOSFET e BJT: Es. 4c

5. Dato il circuito in figura ( $V_{dd} = 5 \text{ V}$ ,  $V_{in} = 2 \text{ V}$ ,  $V_{THn} = 1 \text{ V}$ ,  $V_{THp} = -1 \text{ V}$ ,  $\beta_1 = \beta_2 = 20 \mu\text{A/V}^2$ ,  $\beta_3 = \beta_4 = 10 \mu\text{A/V}^2$ ,  $R1 = 50 \text{ k}\Omega$ ,  $R2 = 1 \text{ M}\Omega$ ), determinare: i) la zona di funzionamento dei MOSFET; ii) le correnti  $I_{D1}$ ,  $I_{D2}$ ,  $I_{D3}$ ,  $I_{D4}$ ,  $I_{R1}$ ,  $I_{R2}$  e le tensioni  $V_X$ ,  $V_{out}$ ; iii) i parametri differenziali dei MOSFET.



M1 :	SAT	TRI	OFF
M2 :	SAT	TRI	OFF

M3 :	SAT	TRI	OFI
M4 :	SAT	TRI	OFI

$$\begin{array}{l}
 I_{D1} = \boxed{\phantom{000}} \cdot \boxed{\phantom{000}} \mu\text{A} \quad g_{m1} = \boxed{\phantom{000}} \cdot \boxed{\phantom{000}} \mu\text{A} \\
 I_{D2} = \boxed{\phantom{000}} \cdot \boxed{\phantom{000}} \mu\text{A} \quad g_{o1} = \boxed{\phantom{000}} \cdot \boxed{\phantom{000}} \mu\text{A} \\
 I_{D3} = \boxed{\phantom{000}} \cdot \boxed{\phantom{000}} \mu\text{A} \quad g_{m2} = \boxed{\phantom{000}} \cdot \boxed{\phantom{000}} \mu\text{A} \\
 I_{D4} = \boxed{\phantom{000}} \cdot \boxed{\phantom{000}} \mu\text{A} \quad g_{o2} = \boxed{\phantom{000}} \cdot \boxed{\phantom{000}} \mu\text{A} \\
 I_{R1} = \boxed{\phantom{000}} \cdot \boxed{\phantom{000}} \mu\text{A} \quad g_{m3} = \boxed{\phantom{000}} \cdot \boxed{\phantom{000}} \mu\text{A} \\
 I_{R2} = \boxed{\phantom{000}} \cdot \boxed{\phantom{000}} \mu\text{A} \quad g_{o3} = \boxed{\phantom{000}} \cdot \boxed{\phantom{000}} \mu\text{A} \\
 V_X = \boxed{\phantom{000}} \cdot \boxed{\phantom{000}} \text{V} \quad g_{m4} = \boxed{\phantom{000}} \cdot \boxed{\phantom{000}} \text{V} \\
 V_{\text{out}} = \boxed{\phantom{000}} \cdot \boxed{\phantom{000}} \text{V} \quad g_{o4} = \boxed{\phantom{000}} \cdot \boxed{\phantom{000}} \text{V}
 \end{array}$$

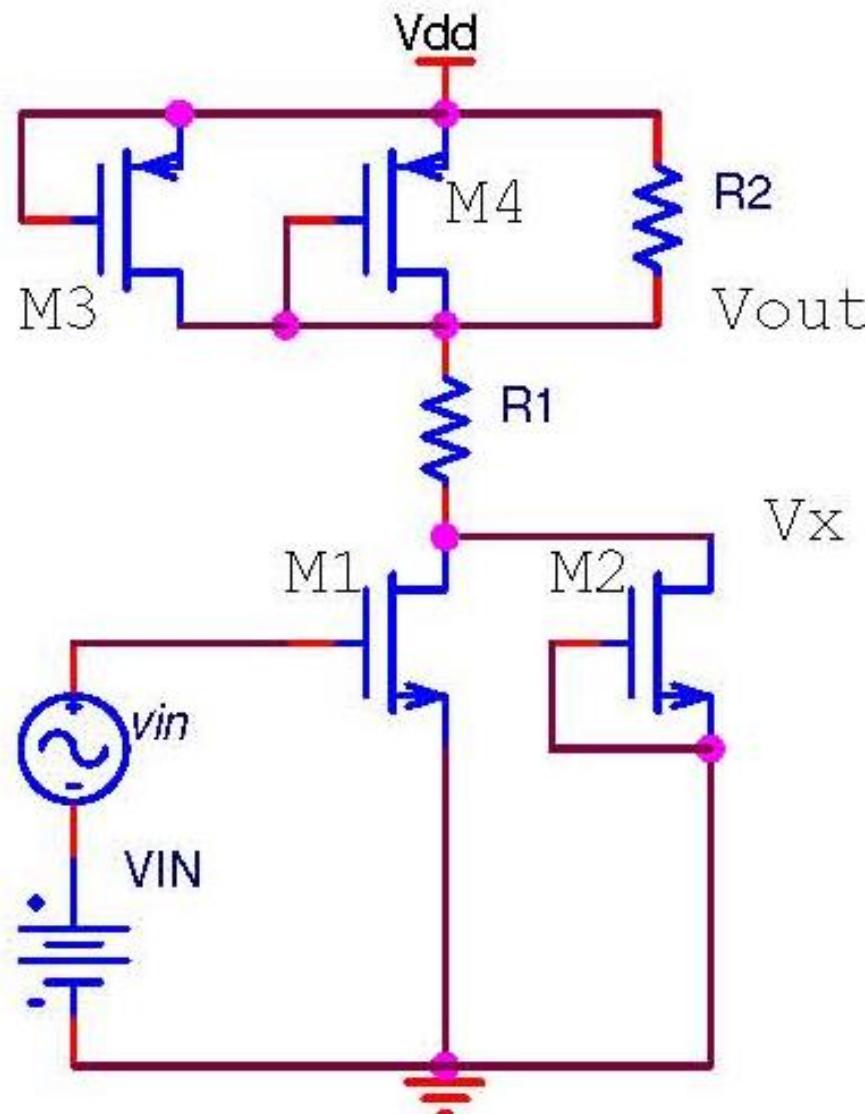
6. Relativamente all'esercizio precedente, disegnare il circuito equivalente alle variazioni e calcolare sia in forma simbolica che numerica il guadagno di tensione  $A_V = v_{\text{out}}/v_{\text{in}}$

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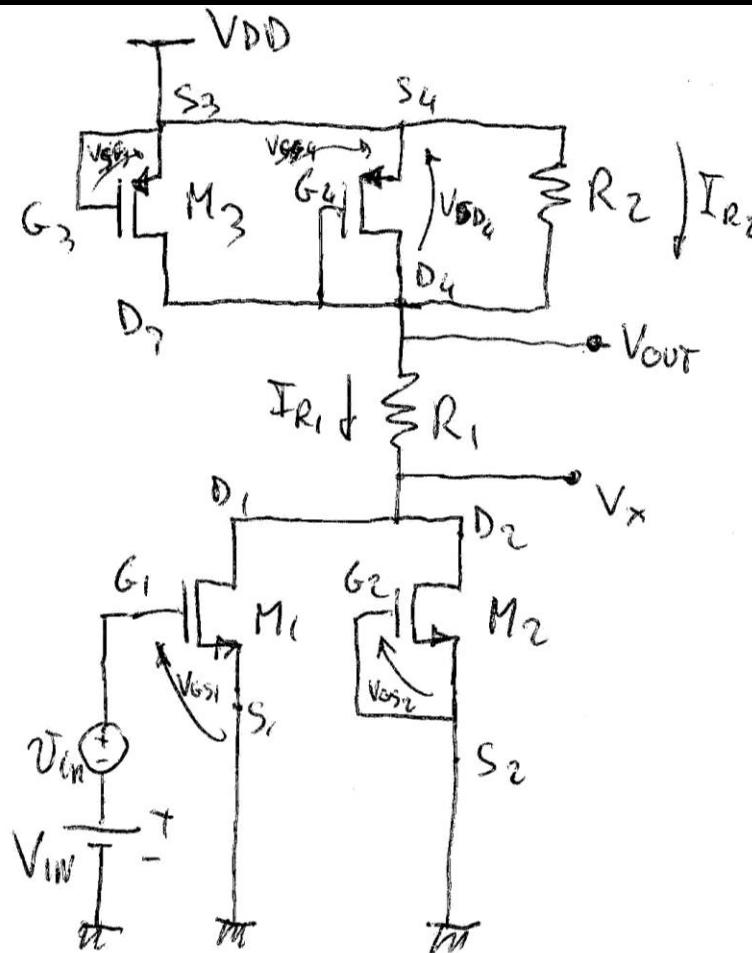
(espressione simbolica)  $v_{\text{out}}/v_{\text{in}} =$

$$v_{\text{out}}/v_{\text{in}} = \boxed{\phantom{0}} : \boxed{\phantom{00}} \text{ V/V}$$

# Circuiti con MOSFET e BJT: Es. 4c



# Es. 4c: Soluzione



$$V_{DD} = 5V$$

$$V_{IN} = 2V$$

$$V_{THN} = 1V$$

$$V_{THP} = -1V$$

$$\beta_1 = \beta_2 = 80 \mu A/V^2$$

$$\beta_3 = \beta_4 = 10 \mu A/V^2$$

$$R_1 = 50 k\Omega$$

$$R_2 = 1 M\Omega$$

$V_{GS3} = 0 > V_{TH3} = -1V$   $\xrightarrow{S1}$  M3 OFF  $I_{D3} = 0 \mu A$

$V_{GS2} = 0 > V_{TH2} = 1V$   $\xrightarrow{NO}$  M2 OFF  $I_{D2} = 0 \mu A$

## Es. 4c: Soluzione

$$V_{GS4} = V_{DS4} \Rightarrow V_{DS4} \leq V_{GS4} - V_{TH4} \xrightarrow{\quad} [M_4 \text{ SAT}]$$

Hp M1 SAT

$$V_{GS1} > V_{TH1}, \quad V_{DS1} \geq V_{GS1} - V_{TH1}$$

$$V_{GS1} = V_{IN} = 2V > V_{TH1}$$

[M1 ON]

$$I_{D1} = \frac{\beta_1}{2} (V_{GS1} - V_{TH1})^2 = \frac{20 \cdot 10^{-6}}{2} (2-1)^2 = 10 \mu A$$

$$I_{R1} = I_{D1} + I_{D2} = I_{D1} = 10 \mu A$$

$$\overline{I_{D4} = \frac{\beta_4}{2} (V_{GS4} - V_{TH4})^2}$$

$$V_{GS4} = V_{DS4} = -I_{R2} R_2 \quad ; \quad I_{R2} = -V_{GS4} / R_2$$

$$I_{D4} + I_{R2} = I_{R1}$$

## Es. 4c: Soluzione

$$\frac{\beta_4}{2} \left( V_{GS4} - V_{TH4} \right)^2 - \frac{V_{GS4}}{R_2} = I_{R_1}$$

$$\frac{\beta_4}{2} \left( V_{GS4}^2 + V_{TH4}^2 - 2V_{GS4}V_{TH4} \right) - \frac{V_{GS4}}{R_4} = I_{R_1}$$

$$\frac{\beta_4}{2} V_{GS4}^2 - \left( \beta_4 V_{TH4} + \frac{1}{R_2} \right) V_{GS4} + \frac{\beta_4}{2} V_{TH4}^2 - I_{R_1} = 0$$

$$5 \cdot 10^{-6} V_{GS4}^2 - \left( 10 \cdot 10^{-6} \cdot (-1) + 1 \cdot 10^{-6} \right) V_{GS4} + 5 \cdot 10^{-6} \cdot 1 - 10 \cdot 10^{-6} = 0$$

$$5 V_{GS4}^2 + 9 V_{GS4} - 5 = 0$$

$$V_{GS4} = \begin{cases} -2.245 \text{ V} \\ +0.445 \text{ V} \end{cases}$$

## Es. 4c: Soluzione

$$V_{GS4} = V_{DS4} = -2.245 \text{ V}$$

$$V_{out} = V_{DD} + V_{GS4} = 5 - 2.245 = 2.755 \text{ V}$$

$(V_{DD} - V_{GS4})$

$$\underline{I_{R2}} = \underline{-\frac{V_{GS4}}{R_2}} = \underline{2.245 \mu A}$$

$$I_{D4} = I_{R1} - I_{R2} = 10 - 2.245 = 7.755 \mu A$$

$$\underline{V_x} = V_{out} - I_{R1} \cdot R_1 = 2.755 - 10 \cdot 10^6 \cdot 50 \cdot 10^3 = \underline{2255 \text{ V}}$$

$$V_{DS1} = V_x = 2.255 > ? V_{GS1} - V_{TH1} = 2 - 1 = 1 \quad \text{or}$$

M1 SAT

## Es. 4c: Soluzione

$$g_{m1} = \beta_1 (V_{OS1} - V_{TH1}) = \sqrt{2\beta_1 I_{D1}} = \sqrt{2 \cdot 20 \cdot 10^{-6} \cdot 10^{-6}} = 20 \mu S$$

$$g_{01} = 0 \text{ } \mu\text{s}$$

$$g_m = 0 \mu S$$

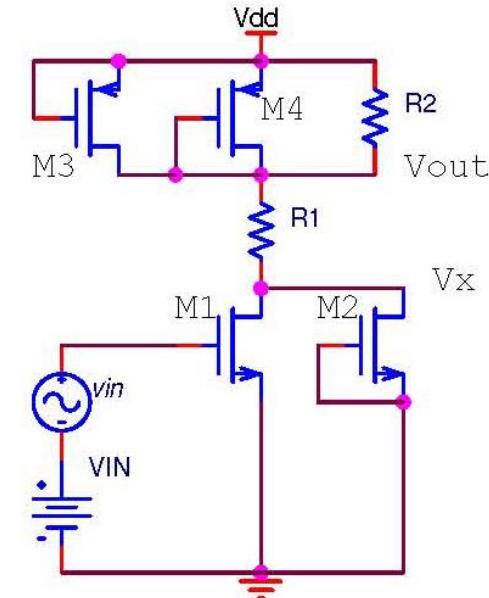
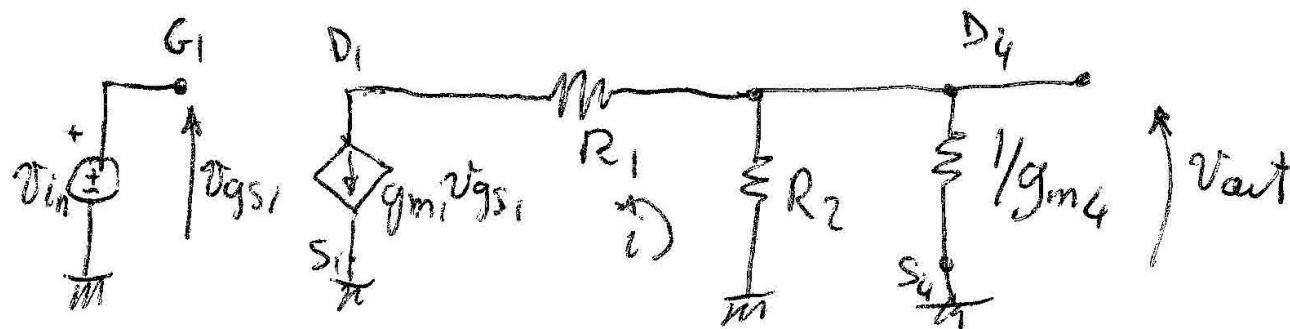
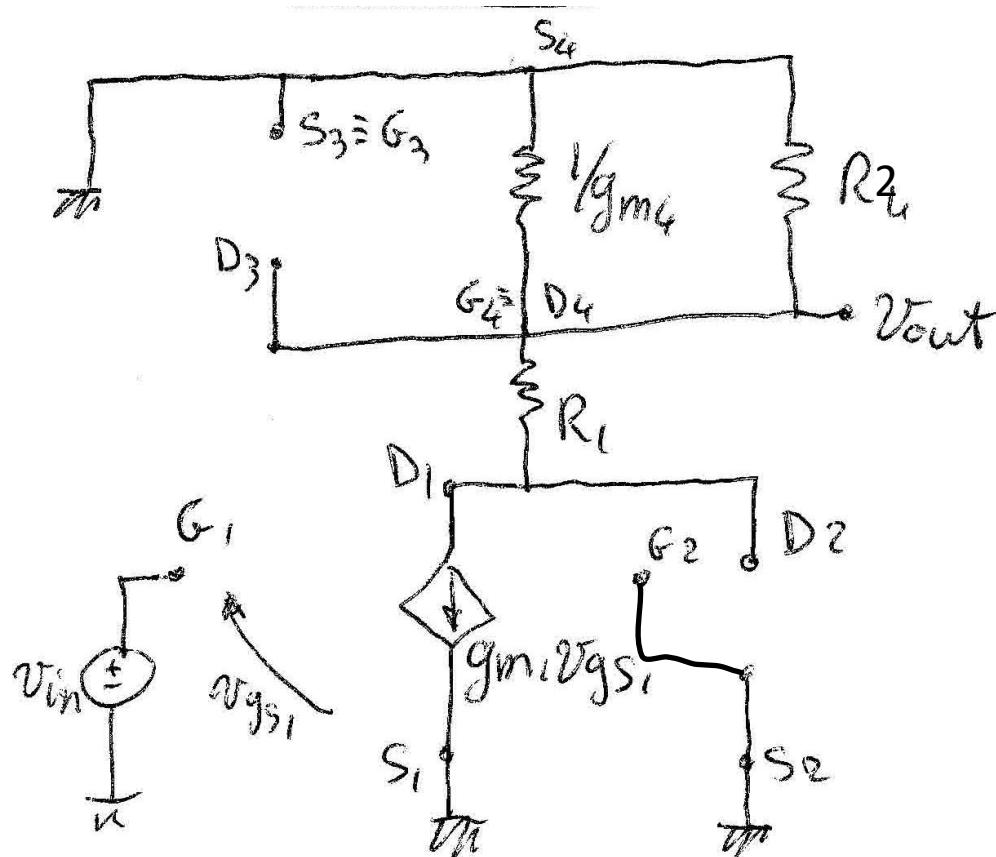
$$g_{02} = 0 \mu S$$

$$g_{m3} = 0 \mu S$$

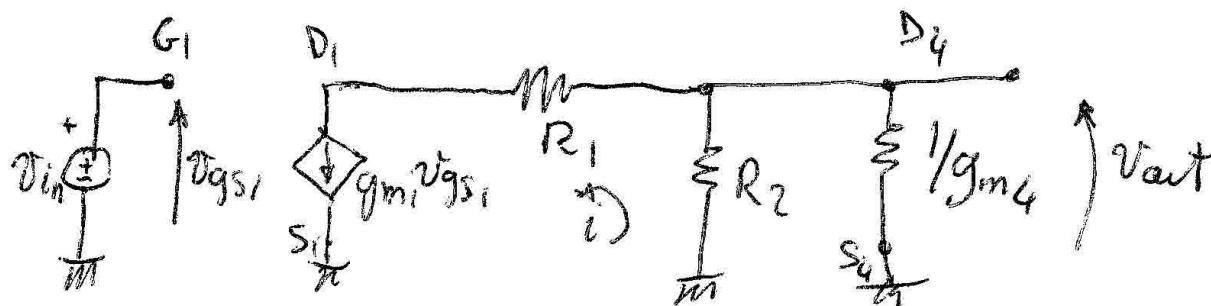
$$g_{03} = 0 \mu S$$

$$g_{m4} = \beta_4 (V_{SG4} + V_{TH4}) = 10 \cdot 10^{-6} (2.245 - 1) = 12.45 \text{ MS}$$

# Es. 4c: Soluzione



## Es. 4c: Soluzione



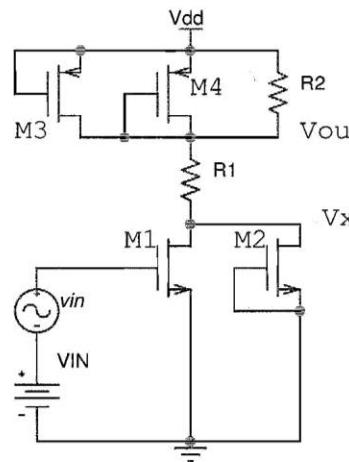
$$v_{gs1} = v_{in}; \quad i = g_{m1} v_{gs1}; \quad V_{out} = -i \left( R_2 \parallel \frac{1}{g_{m4}} \right) = -i \cdot \frac{R_2 / g_{m4}}{R_2 + \frac{1}{g_{m4}}}$$

$$V_{out} = -i \frac{R_2}{1 + g_{m4} R_2} = -\frac{g_{m1} R_2}{1 + g_{m4} R_2} v_{in}; \quad A_{v2} = \frac{V_{out}}{V_{in}} = -\frac{g_{m1} R_2}{1 + g_{m4} R_2}$$

$$A_{v2} = -1.487 \text{ V/V}$$

# Es. 4c: Soluzione

5. Dato il circuito in figura ( $V_{dd} = 5 \text{ V}$ ,  $V_{in} = 2 \text{ V}$ ,  $V_{THn} = 1 \text{ V}$ ,  $V_{THp} = -1 \text{ V}$ ,  $\beta_1 = \beta_2 = 20 \mu\text{A}/\text{V}^2$ ,  $\beta_3 = \beta_4 = 10 \mu\text{A}/\text{V}^2$ ,  $R1 = 50 \text{ k}\Omega$ ,  $R2 = 1 \text{ M}\Omega$ ), determinare: i) la zona di funzionamento dei MOSFET; ii) le correnti  $I_{D1}$ ,  $I_{D2}$ ,  $I_{D3}$ ,  $I_{D4}$ ,  $I_{R1}$ ,  $I_{R2}$  e le tensioni  $V_x$ ,  $V_{out}$ ; iii) i parametri differenziali dei MOSFET.

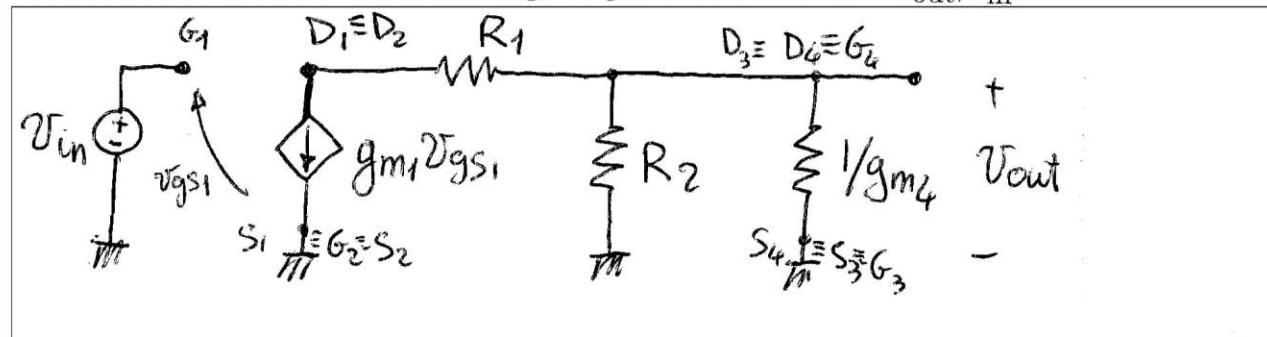


M1 : ~~SAT~~ TRI OFF  
M2 : SAT TRI ~~OFF~~

M3 : SAT TRI ~~OFF~~  
M4 : ~~SAT~~ TRI OFF

$I_{D1} =$	1	0	0	0	$\mu\text{A}$	$g_{m1} =$	2	0	0	0	$\mu\text{s}$
$I_{D2} =$	0	0	0	0	$\mu\text{A}$	$g_{o1} =$	0	0	0	0	$\mu\text{s}$
$I_{D3} =$	0	0	0	0	$\mu\text{A}$	$g_{m2} =$	0	0	0	0	$\mu\text{s}$
$I_{D4} =$	7	7	5	5	$\mu\text{A}$	$g_{o2} =$	0	0	0	0	$\mu\text{s}$
$I_{R1} =$	1	0	0	0	$\mu\text{A}$	$g_{m3} =$	0	0	0	0	$\mu\text{s}$
$I_{R2} =$	2	2	4	6	$\mu\text{A}$	$g_{o3} =$	0	0	0	0	$\mu\text{s}$
$V_x =$	2	2	5	4	$\text{V}$	$g_{m4} =$	1	2	4	5	$\mu\text{s}$
$V_{out} =$	2	2	7	5	$\text{V}$	$g_{o4} =$	0	0	0	0	$\mu\text{s}$

6. Relativamente all'esercizio precedente, disegnare il circuito equivalente alle variazioni e calcolare sia in forma simbolica che numerica il guadagno di tensione  $A_V = v_{out}/v_{in}$

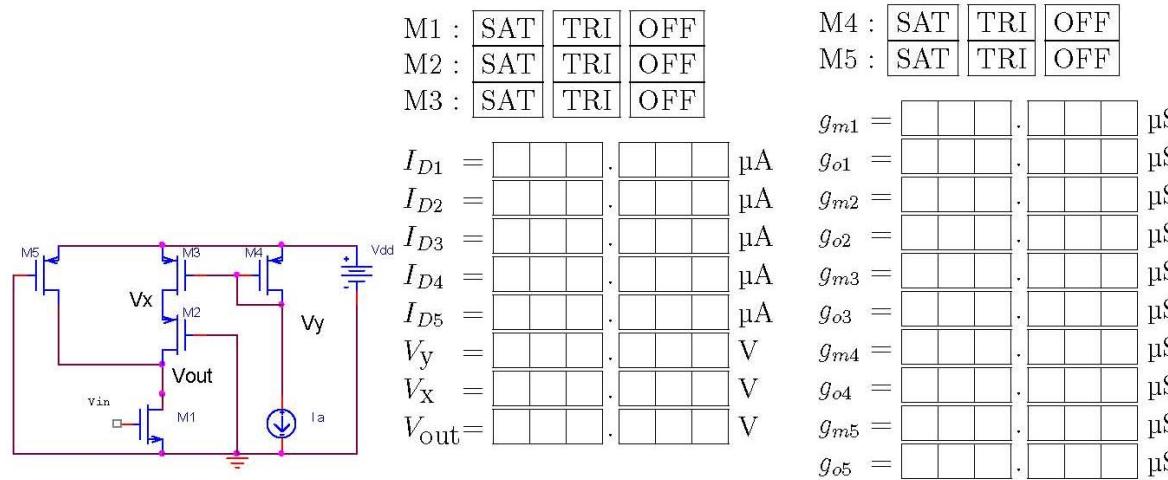


(espressione simbolica)  $v_{out}/v_{in} = -gm_1 R_2 / (1 + gm_4 R_2)$

$v_{out}/v_{in} = \boxed{\text{-}} \cdot \boxed{1} \cdot \boxed{4} \boxed{8} \boxed{7} \text{ V/V}$

# Circuiti con MOSFET e BJT: Es. 5c

5. Dato il circuito in figura ( $V_{dd} = 6 \text{ V}$ ,  $V_{in} = 3 \text{ V}$ ,  $V_{THn} = 0.5 \text{ V}$ ,  $V_{THp} = -0.5 \text{ V}$ ,  $I_a = 5 \mu\text{A}$ ,  $\beta_1 = 40 \mu\text{A}/\text{V}^2$ ,  $\beta_2 = 2 \mu\text{A}/\text{V}^2$ ,  $\beta_3 = \beta_4 = 40 \mu\text{A}/\text{V}^2$ ,  $\beta_5 = 2 \mu\text{A}/\text{V}^2$ ), determinare: *i)* la zona di funzionamento dei MOSFET; *ii)* le correnti  $I_{D1}, I_{D2}, I_{D3}, I_{D4}, I_{D5}$  e le tensioni  $V_x, V_y, V_{out}$ ; *iii)* i parametri differenziali dei MOSFET.

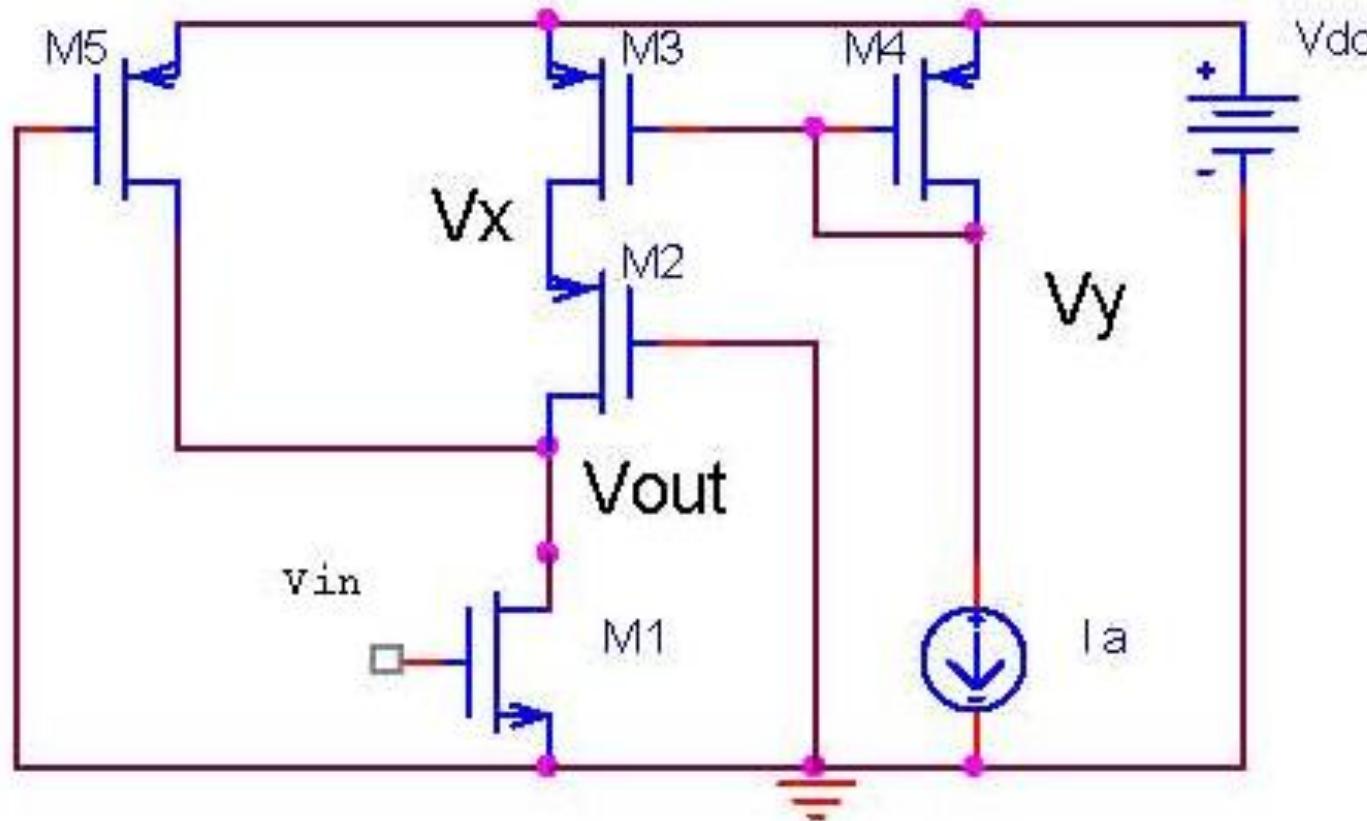


6. Relativamente all'esercizio precedente, disegnare il circuito equivalente alle variazioni e calcolare sia in forma simbolica che numerica il guadagno di tensione  $A_V = v_{out}/v_{in}$

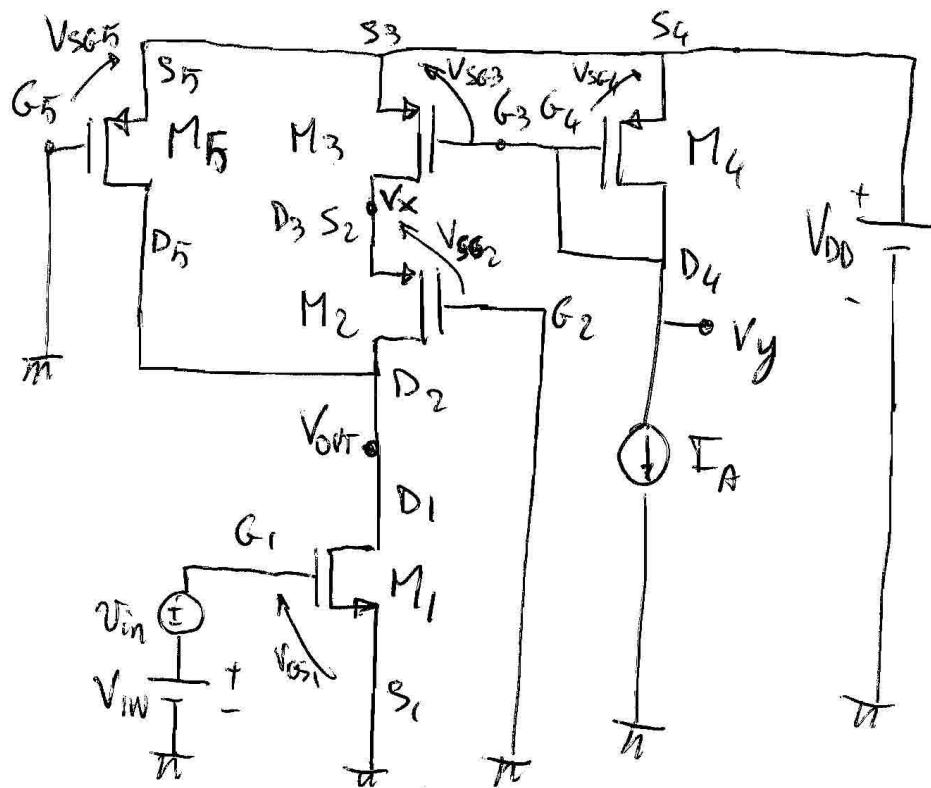
(espressione simbolica)  $v_{out}/v_{in} =$

$$v_{out}/v_{in} = [ ] . [ ] \text{ V/V}$$

# Circuiti con MOSFET e BJT: Es. 5c



# Es. 5c: Soluzione



$$V_{DD} = 6V \quad |V_{TH}| = 0.5V$$

$$I_A = 5\mu A$$

$$\beta_1 = 40\mu A/V^2$$

$$\beta_3 = \beta_4 = 40\mu A/V^2$$

$$\beta_2 = 2\mu A/V^2$$

$$\beta_5 = 2\mu A/V^2$$

Hp.

M4 SAT

$$V_{GS4} > V_{TH4} \quad V_{DS4} > V_{GS4} - V_{TH4}$$



$$I_{D4} = \frac{\beta_4}{2} (V_{GS4} - V_{TH4})^2$$

$$I_{D4} = I_A = 5\mu A$$

## Es. 5c: Soluzione

$$V_{GS4} = -\sqrt{\frac{2I_{D4}}{P_4}} + V_{TH4} = -0.5 \sim 0.5 = -1 \text{ V}$$

$$V_y = V_{DD} - V_{GS4} = V_{DD} + V_{GS4} = 6 - 1 = \underline{5 \text{ V}}$$

$$V_{GS3} = V_{GS4} = -1 \text{ V}$$

M<sub>3</sub> ON

Hp M<sub>3</sub> SAT       $V_{DS3} < V_{GS3} - V_{TH3}$

$$I_{D3} = \frac{P_3}{2} (V_{GS3} - V_{TH3})^2 \xrightarrow{\beta_3 = \beta_4} I_{D3} = I_{D4} = \underline{5 \text{ mA}}$$

Hp M<sub>2</sub> SAT

$$I_{D2} = I_{D3} = \underline{5 \text{ mA}}$$

## Es. 5c: Soluzione

$$V_{GS2} = \pm \sqrt{\frac{2ID_2}{P_2}} + V_{TH2} = \pm \sqrt{5} - 0.5 \quad \begin{matrix} -2.736 \\ 1.736 \end{matrix}$$

$$V_x = V_{SG2} = -V_{GS2} = \underline{2.736} \text{ V}$$

$$V_{DS3} = V_x - V_{DD} = 2.736 - 6 = -3.264 \quad ?$$

$$V_{GS3} - V_{TH3} = -1 + 0.5 = -0.5 \quad ok$$

M3 SAT

Hp M5 SAT

$$V_{GS5} = 0 - V_{DD} = -6 \text{ V}$$

$$I_{D5} = \frac{P_5}{2} (V_{GS5} - V_{TH5})^2 = \frac{2 \cdot 10^{-6}}{2} (-6 + 0.5)^2 = \underline{30.25 \mu A}$$

$$I_{D1} = I_{D5} + I_{D2} = \underline{35.25 \mu A}$$

## Es. 5c: Soluzione

H<sub>p</sub> M<sub>1</sub> SAT

$$I_{D1} = \frac{\beta_1}{2} (V_{GS1} - V_{TH1})^2 = \frac{40 \cdot 10^{-6}}{2} (3 - 1)^2 = 80 \mu A \neq 35.25 \mu A$$

$\uparrow$   
 $V_{GS1} = V_{IN}$

→ ↘

⇒ M<sub>1</sub> TR<sub>1</sub>

$$V_{DS1} < V_{GS1} - V_{TH1}$$

$$I_{D1} = \beta_1 \left[ (V_{GS1} - V_{TH1}) V_{DS1} - \frac{V_{DS1}^2}{2} \right]$$

$$V_{DS1}^2 - 5 V_{DS1} + 1.7625 = 0$$

$$V_{DS1} = \begin{cases} 0.382 \text{ V} \\ \cancel{4.6185 \text{ V}} \end{cases}$$

NO!

$V_{DS1} < V_{GS1} - V_{TH1} = 2.5 \text{ V}$

## Es. 5c: Soluzione

$$V_{DS1} = 0.382 \text{ V}$$

$$V_{OUT} = \underline{V_{DS1} = 0.382 \text{ V}}$$

$$V_{DS5} = V_{OUT} - V_{DD} = -5.618 \quad ? \quad < V_{GS5} - V_{TH5} = -6 + 0.5 = -5.5 \text{ on}$$

M5 SAT

$$V_{DS2} = V_{OUT} - V_x = 0.382 - 2.736 = -2.354 \quad ? \quad < V_{GS2} - V_{TH2} = -2.736 + 0.5 \\ = -2.236 \text{ on}$$

M2 SAT

## Es. 5c: Soluzione

$$g_{m1} = \beta_1 V_{DS1} = 15.264 \mu\text{s}$$

$$g_{o1} = \beta_1 (V_{GS1} - V_{TH1} - V_{DS1}) = 84.736 \mu\text{s}$$

$$g_{m2} = \beta_2 (V_{SG2} + V_{TH2}) = 4.472 \mu\text{s}$$

$$g_{o2} = 0 \mu\text{s}$$

$$g_{m3} = \beta_3 (V_{SG3} + V_{TH3}) = 20 \mu\text{s}$$

$$g_{o3} = 0 \mu\text{s}$$

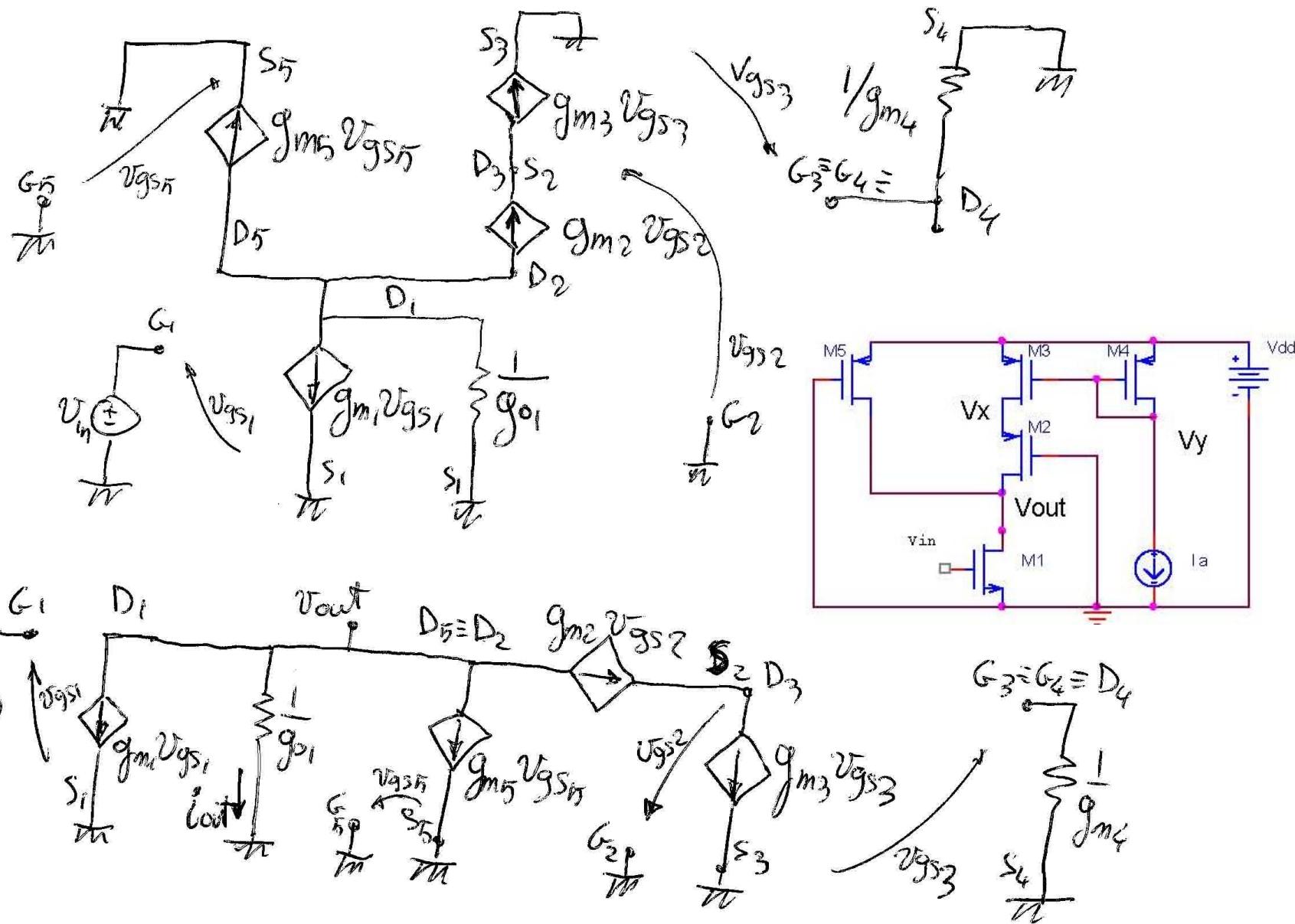
$$g_{m4} = \beta_4 (V_{SG4} + V_{TH4}) = 20 \mu\text{s}$$

$$g_{o4} = 0 \mu\text{s}$$

$$g_{m5} = \beta_5 (V_{SG5} + V_{TH5}) = 11.0 \mu\text{s}$$

$$g_{o5} = 0$$

# Es. 5c: Soluzione



## Es. 5c: Soluzione

$$V_{GS3} = 0$$

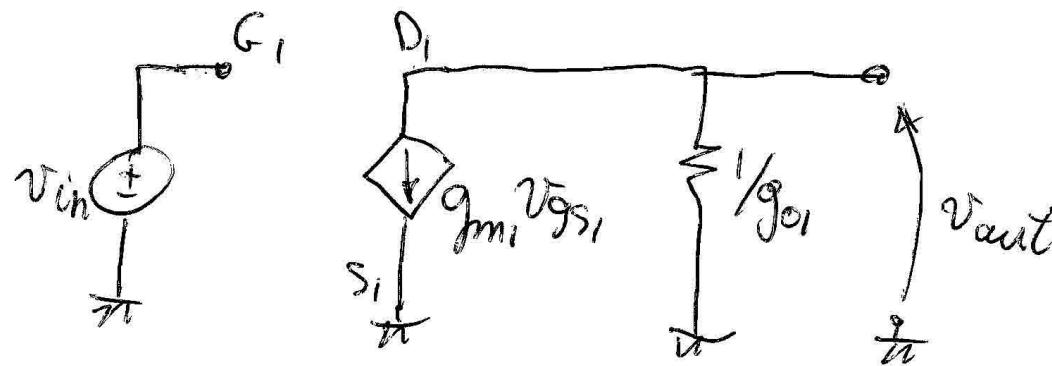
$$; \quad g_{m2} V_{GS2} = g_{m3} V_{GS3} \Rightarrow V_{GS2} = 0$$

$$V_{GS5} = 0$$

$$i_{out} = -g_{m1} V_{GS1} - \cancel{g_{m5} V_{GS5}} - \cancel{g_{m2} V_{GS2}} = -g_{m1} V_{GS1}$$

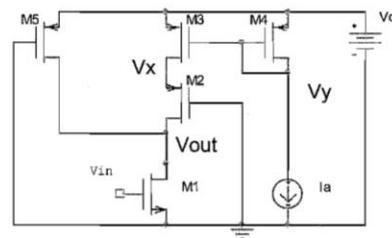
$$V_{GS1} = V_{in} ; \quad V_{out} = i_{out} \cdot \frac{1}{g_{o1}} \quad V_{out} = -\frac{g_{m1}}{g_{o1}} V_{in}$$

$$A_V = \frac{V_{out}}{V_{in}} = -g_{m1}/g_{o1} \quad A_V = -0.180 \text{ V/V}$$



# Es. 5c: Soluzione

5. Dato il circuito in figura ( $V_{dd} = 6 \text{ V}$ ,  $V_{in} = 3 \text{ V}$ ,  $V_{THn} = 0.5 \text{ V}$ ,  $V_{THp} = -0.5 \text{ V}$ ,  $I_a = 5 \mu\text{A}$ ,  $\beta_1 = 40 \mu\text{A}/\text{V}^2$ ,  $\beta_2 = 2 \mu\text{A}/\text{V}^2$ ,  $\beta_3 = \beta_4 = 40 \mu\text{A}/\text{V}^2$ ,  $\beta_5 = 2 \mu\text{A}/\text{V}^2$ ), determinare: i) la zona di funzionamento dei MOSFET; ii) le correnti  $I_{D1}, I_{D2}, I_{D3}, I_{D4}, I_{D5}$  e le tensioni  $V_x, V_y, V_{out}$ ; iii) i parametri differenziali dei MOSFET.



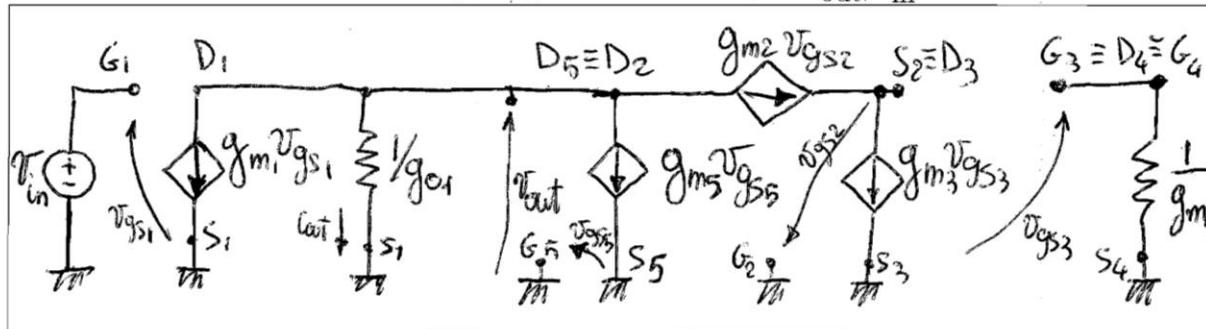
M1 :	SAT		OFF
M2 :	<del>SAT</del>	TRI	OFF
M3 :	<del>SAT</del>	TRI	OFF

$I_{D1} =$	35	.250	$\mu\text{A}$
$I_{D2} =$	5	.000	$\mu\text{A}$
$I_{D3} =$	5	.000	$\mu\text{A}$
$I_{D4} =$	5	.000	$\mu\text{A}$
$I_{D5} =$	30	.250	$\mu\text{A}$
$V_y =$	5	.000	$\text{V}$
$V_x =$	2	.736	$\text{V}$
$V_{out} =$	0	.382	$\text{V}$

M4 :	<del>SAT</del>	TRI	OFF
M5 :	<del>SAT</del>	TRI	OFF

$g_{m1} =$	15	.264	$\mu\text{S}$
$g_{o1} =$	84	.736	$\mu\text{S}$
$g_{m2} =$	4	.472	$\mu\text{S}$
$g_{o2} =$	0	.000	$\mu\text{S}$
$g_{m3} =$	20	.000	$\mu\text{S}$
$g_{o3} =$	0	.000	$\mu\text{S}$
$g_{m4} =$	20	.000	$\mu\text{S}$
$g_{o4} =$	0	.000	$\mu\text{S}$
$g_{m5} =$	11	.000	$\mu\text{S}$
$g_{o5} =$	0	.000	$\mu\text{S}$

6. Relativamente all'esercizio precedente, disegnare il circuito equivalente alle variazioni e calcolare sia in forma simbolica che numerica il guadagno di tensione  $A_V = v_{out}/v_{in}$

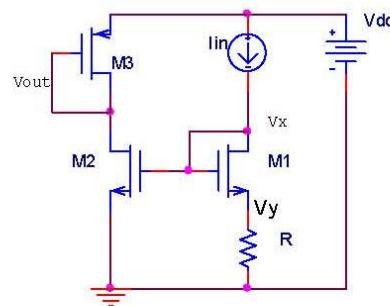


(espressione simbolica)  $v_{out}/v_{in} = -g_{m1}/g_{o1}$

$v_{out}/v_{in} = [-0.180] \text{ V/V}$

# Circuiti con MOSFET e BJT: Es. 6c

5. Dato il circuito in figura ( $V_{dd} = 5 \text{ V}$ ,  $I_{in} = 5 \mu\text{A}$ ,  $V_{THn} = 1 \text{ V}$ ,  $V_{THp} = -1 \text{ V}$ ,  $R = 100 \text{ k}\Omega$   $\beta_1 = \beta_2 = 10 \mu\text{A/V}^2$ ,  $\beta_3 = 15 \mu\text{A/V}^2$ ), determinare: i) la zona di funzionamento dei MOSFET; ii) le correnti  $I_{D1}$ ,  $I_{D2}$ ,  $I_{D3}$  e le tensioni  $V_x$ ,  $V_y$ ,  $V_{out}$ ; iii) i parametri differenziali dei MOSFET.



M1 : SAT TRI OFF

M2 : SAT TRI OFF

M3 : SAT TRI OFF

$$I_{D1} = \boxed{\phantom{000}} \cdot \boxed{\phantom{000}} \mu\text{A}$$

$$I_{D2} = \boxed{\phantom{000}} \cdot \boxed{\phantom{000}} \mu\text{A}$$

$$I_{D3} = \boxed{\phantom{000}} \cdot \boxed{\phantom{000}} \mu\text{A}$$

$$V_y = \boxed{\phantom{000}} \cdot \boxed{\phantom{000}} \text{ V}$$

$$V_x = \boxed{\phantom{000}} \cdot \boxed{\phantom{000}} \text{ V}$$

$$V_{out} = \boxed{\phantom{000}} \cdot \boxed{\phantom{000}} \text{ V}$$

$$g_{m1} = \boxed{\phantom{000}} \cdot \boxed{\phantom{000}} \mu\text{s}$$

$$g_{o1} = \boxed{\phantom{000}} \cdot \boxed{\phantom{000}} \mu\text{s}$$

$$g_{m2} = \boxed{\phantom{000}} \cdot \boxed{\phantom{000}} \mu\text{s}$$

$$g_{o2} = \boxed{\phantom{000}} \cdot \boxed{\phantom{000}} \mu\text{s}$$

$$g_{m3} = \boxed{\phantom{000}} \cdot \boxed{\phantom{000}} \mu\text{s}$$

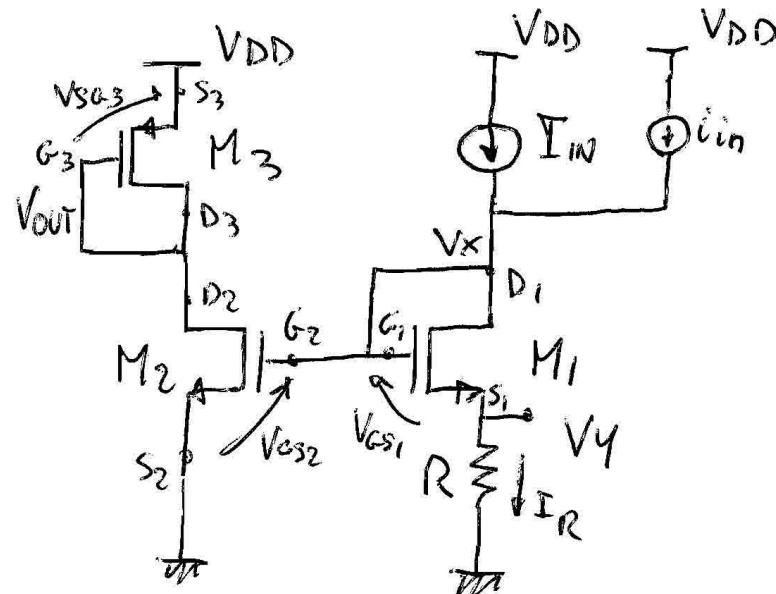
$$g_{o3} = \boxed{\phantom{000}} \cdot \boxed{\phantom{000}} \mu\text{s}$$

6. Relativamente all'esercizio precedente, disegnare il circuito equivalente alle variazioni e calcolare sia in forma simbolica che numerica il guadagno di transresistenza  $A_R = v_{out}/i_{in}$

(espressione simbolica)  $v_{out}/i_{in} =$

$$v_{out}/i_{in} = \boxed{\phantom{000}} \cdot \boxed{\phantom{000}} \text{ V/A}$$

# Es. 6c: Soluzione



$$V_{DD} = 5V$$

$$I_{IN} = 5 \mu A$$

$$V_{THN} = 1V$$

$$V_{THP} = -1V$$

$$R = 100 k\Omega$$

$$\beta_1 = \beta_2 = 10 \mu A/V^2$$

$$\beta_3 = 15 \mu A/V^2$$

M<sub>1</sub> SAT

$$V_{GS1} = V_{DS1}$$

M<sub>3</sub> SAT

$$V_{GS3} = V_{DS3}$$

$$I_{IN} = I_{G1} + I_{G2} + I_{D1} = I_{D1} \quad I_{D1} = I_{IN} = 5 \mu A$$

$$I_R = I_{D1} ; \quad V_y = I_R \cdot R = 5 \cdot 10^{-6} \cdot 100 \cdot 10^3 = 0.5 V$$

## Es. 6c: Soluzione

$$I_{D1} = \frac{\beta_1}{2} (V_{GS1} - V_{TH1})^2 \Rightarrow V_{GS1} = \sqrt{\frac{2I_D}{\beta_1}} + V_{TH1} = 1+1=2V$$

$$V_x = V_{GS1} + V_y = 2 + 0.5 = \underline{2.5V}$$

$$V_{GS2} = V_x = 2.5V \geq 1V = V_{TH2} \quad M_2 \text{ ON}$$

$M_p$  M2 SAT  $V_{DS} \geq V_{GS2} - V_{TH2}$

$$I_{D2} = \frac{\beta_2}{2} (V_{GS2} - V_{TH2})^2 = \frac{10 \cdot 10^{-6}}{2} (2.5 - 1)^2 = \underline{11.25 \mu A}$$

$$I_{D3} = I_{D2} = \underline{11.25 \mu A}$$

$$I_{D3} = \frac{\beta_3}{2} (V_{GS3} - V_{TH3})^2 \Rightarrow V_{GS3} = -\sqrt{\frac{2I_{D3}}{\beta_3}} + V_{TH3} = -\sqrt{\frac{2 \cdot 11.25 \cdot 10^{-6}}{15 \cdot 10^{-6}}} + 1 = \underline{2.25V}$$

## Es. 6c: Soluzione

$$V_{SG3} = +2.225 \text{ V}$$

$$V_{OUT} = V_{DD} + V_{GS3} = V_{DD} - V_{SG3} = 5 - 2.225 = \underline{\underline{2.775 \text{ V}}}$$

$$V_{DS2} = V_{OUT} = 2.775 \stackrel{?}{>} V_{GS2} - V_{TH2} = 2.5 - 1 = 1.5 \text{ V} \quad \text{OK}$$

M<sub>2</sub> SAT

## Es. 6c: Soluzione

$$g_{m1} = \overline{\beta_1(V_{GS1} - V_{TH1})} = \sqrt{2\beta_1 I_{D1}} = 10 \cdot 10^{-6} \cdot (2-1) = 10 \mu\text{s}$$

$$g_{o1} = 0 \mu\text{s}$$

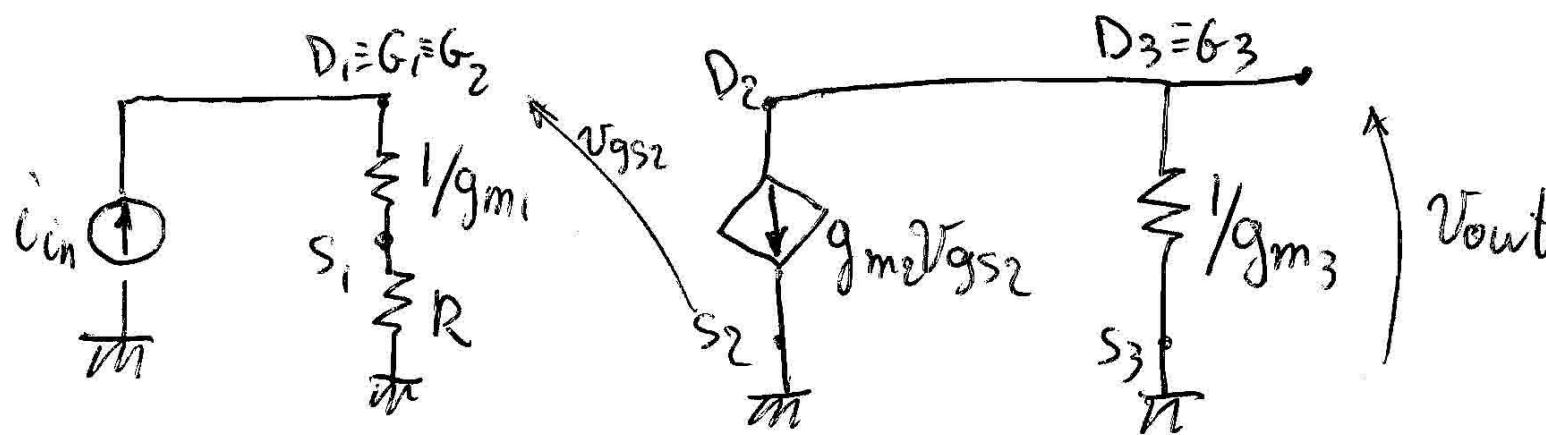
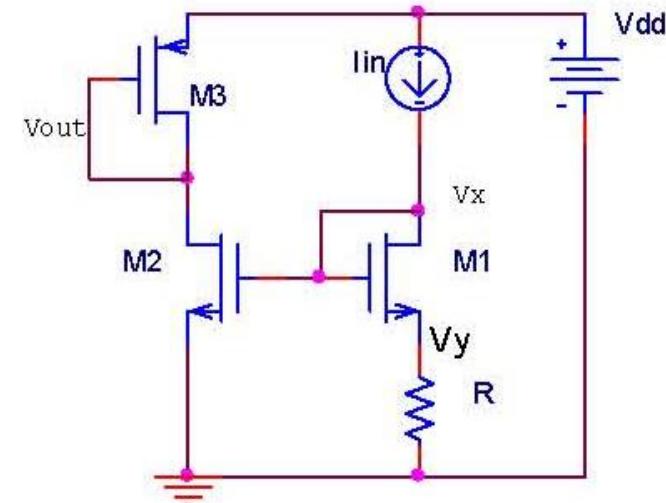
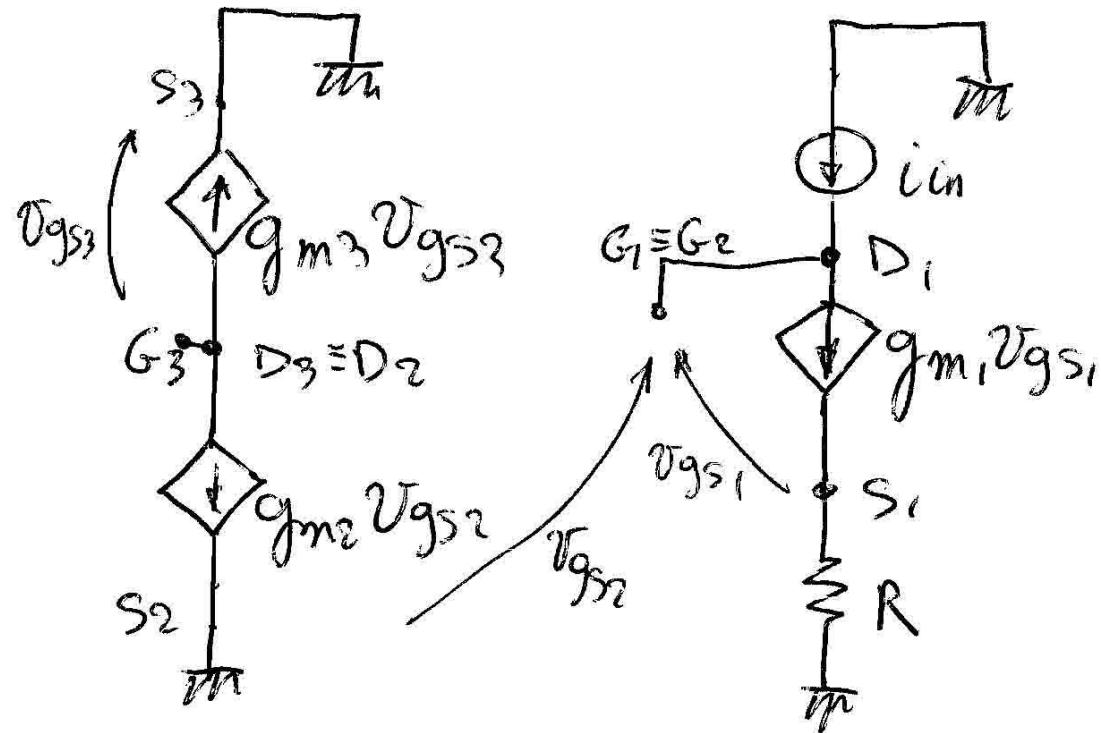
$$g_{m2} = \overline{\beta_2(V_{GS2} - V_{TH2})} = \sqrt{2\beta_2 I_{D2}} = 10 \cdot 10^{-6} \cdot (25-1) = 15 \mu\text{s}$$

$$g_{o2} = 0 \mu\text{s}$$

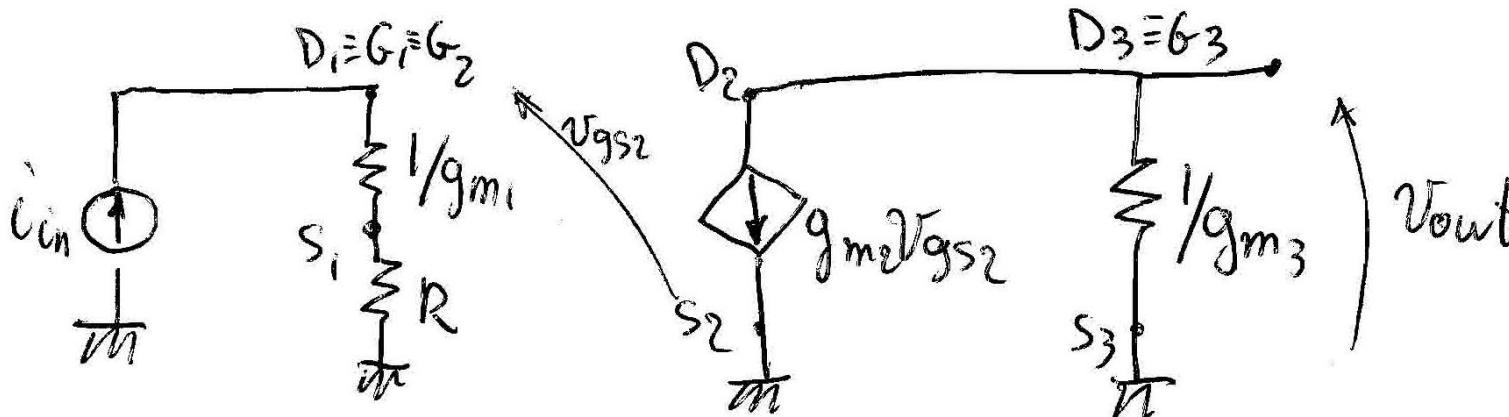
$$g_{m3} = \overline{\beta_3(V_{GS3} + V_{TH3})} = \sqrt{2\beta_3 I_{D3}} = 15 \cdot 10^{-6} \cdot (2225-1) = 18.375 \mu\text{s}$$

$$g_{o3} = 0 \mu\text{s}$$

# Es. 6c: Soluzione



## Es. 6c: Soluzione



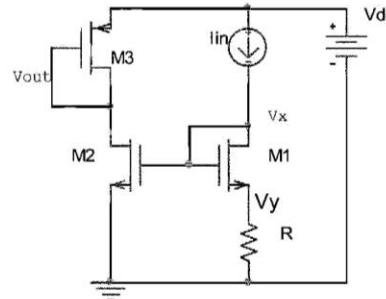
$$V_{out} = -g_{m2} V_{gs2} \cdot \frac{1}{g_{m3}} ; \quad V_{gs2} = i_{in} \cdot \left( \frac{1}{g_{m1}} + R \right)$$

$$V_{out} = -\frac{g_{m2}}{g_{m3}} \left( \frac{1}{g_{m1}} + R \right) i_{in}$$

$$\frac{V_{out}}{i_{in}} = -\frac{g_{m2}}{g_{m3}} \left( \frac{1}{g_{m1}} + R \right)$$

# Es. 6c: Soluzione

5. Dato il circuito in figura ( $V_{dd} = 5 \text{ V}$ ,  $I_{in} = 5 \mu\text{A}$ ,  $V_{THn} = 1 \text{ V}$ ,  $V_{THp} = -1 \text{ V}$ ,  $R = 100 \text{ k}\Omega$   $\beta_1 = \beta_2 = 10 \mu\text{A}/\text{V}^2$ ,  $\beta_3 = 15 \mu\text{A}/\text{V}^2$ ), determinare: *i)* la zona di funzionamento dei MOSFET; *ii)* le correnti  $I_{D1}$ ,  $I_{D2}$ ,  $I_{D3}$  e le tensioni  $V_x$ ,  $V_y$ ,  $V_{out}$ ; *iii)* i parametri differenziali dei MOSFET.

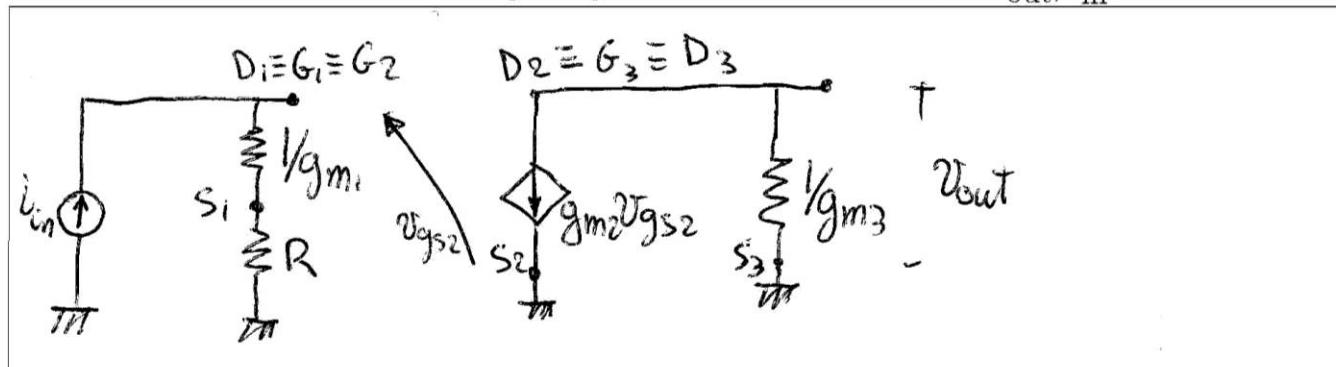


M1 : ~~SAT~~ TRI OFF  
M2 : ~~SAT~~ TRI OFF

M3 : ~~SAT~~ TRI OFF

$$\begin{array}{l}
 I_{D1} = \boxed{\phantom{0}} \boxed{5} \cdot \boxed{0} \boxed{0} \text{ } \mu\text{A} \quad g_{m1} = \boxed{1} \boxed{0} \cdot \boxed{0} \boxed{0} \text{ } \mu\text{s} \\
 I_{D2} = \boxed{\phantom{0}} \boxed{1} \boxed{1} \cdot \boxed{2} \boxed{5} \text{ } \mu\text{A} \quad g_{o1} = \boxed{0} \cdot \boxed{0} \boxed{0} \text{ } \mu\text{s} \\
 I_{D3} = \boxed{\phantom{0}} \boxed{1} \boxed{1} \cdot \boxed{2} \boxed{5} \text{ } \mu\text{A} \quad g_{m2} = \boxed{1} \boxed{5} \cdot \boxed{0} \boxed{0} \text{ } \mu\text{s} \\
 V_y = \boxed{\phantom{0}} \boxed{0} \cdot \boxed{5} \boxed{0} \text{ } \text{V} \quad g_{o2} = \boxed{0} \cdot \boxed{0} \boxed{0} \text{ } \mu\text{s} \\
 V_x = \boxed{\phantom{0}} \boxed{2} \cdot \boxed{5} \boxed{0} \text{ } \text{V} \quad g_{m3} = \boxed{1} \boxed{8} \cdot \boxed{3} \boxed{7} \text{ } \mu\text{s} \\
 V_{out} = \boxed{\phantom{0}} \boxed{2} \cdot \boxed{7} \boxed{7} \text{ } \text{V} \quad g_{o3} = \boxed{0} \cdot \boxed{0} \boxed{0} \text{ } \mu\text{s}
 \end{array}$$

6. Relativamente all'esercizio precedente, disegnare il circuito equivalente alle variazioni e calcolare sia in forma simbolica che numerica il guadagno di transresistenza  $A_R = v_{out}/i_{in}$



(espressione simbolica)  $v_{out}/i_{in} = -\left(g_{m2}/g_{m3}\right) \cdot \left(R + 1/g_{m1}\right)$

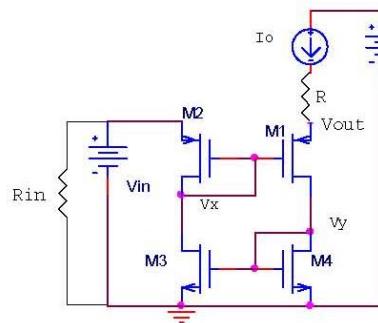
$v_{out}/i_{in} = \boxed{1} \boxed{6} \boxed{6} \cdot \boxed{6} \boxed{6} \text{ } \cancel{\text{K}\Omega}$

# Circuiti con MOSFET e BJT: Es. 7c

5. Dato il circuito in figura ( $V_{dd} = 8 \text{ V}$ ,  $V_{in} = 6 \text{ V}$ ,  $I_O = 200 \mu\text{A}$ ,  $V_{THn} = 1 \text{ V}$ ,  $V_{THp} = -1 \text{ V}$ ,  $R_{in} = 100 \text{ k}\Omega$ ,  $R = 1 \text{ k}\Omega$ ,  $\beta_1 = \beta_2 = \beta_4 = 200 \mu\text{A/V}^2$ ,  $\beta_3 = 400 \mu\text{A/V}^2$ ), determinare: *i)* la zona di funzionamento dei MOSFET; *ii)* le correnti  $I_{D1}$ ,  $I_{D2}$ ,  $I_{D3}$ ,  $I_{D4}$  e le tensioni  $V_x$ ,  $V_y$ ,  $V_{out}$ ; *iii)* i parametri differenziali dei MOSFET.

M1 :	SAT	TRI	OFF
M2 :	SAT	TRI	OFF

M3 :	SAT	TRI	OFF
M4 :	SAT	TRI	OFF



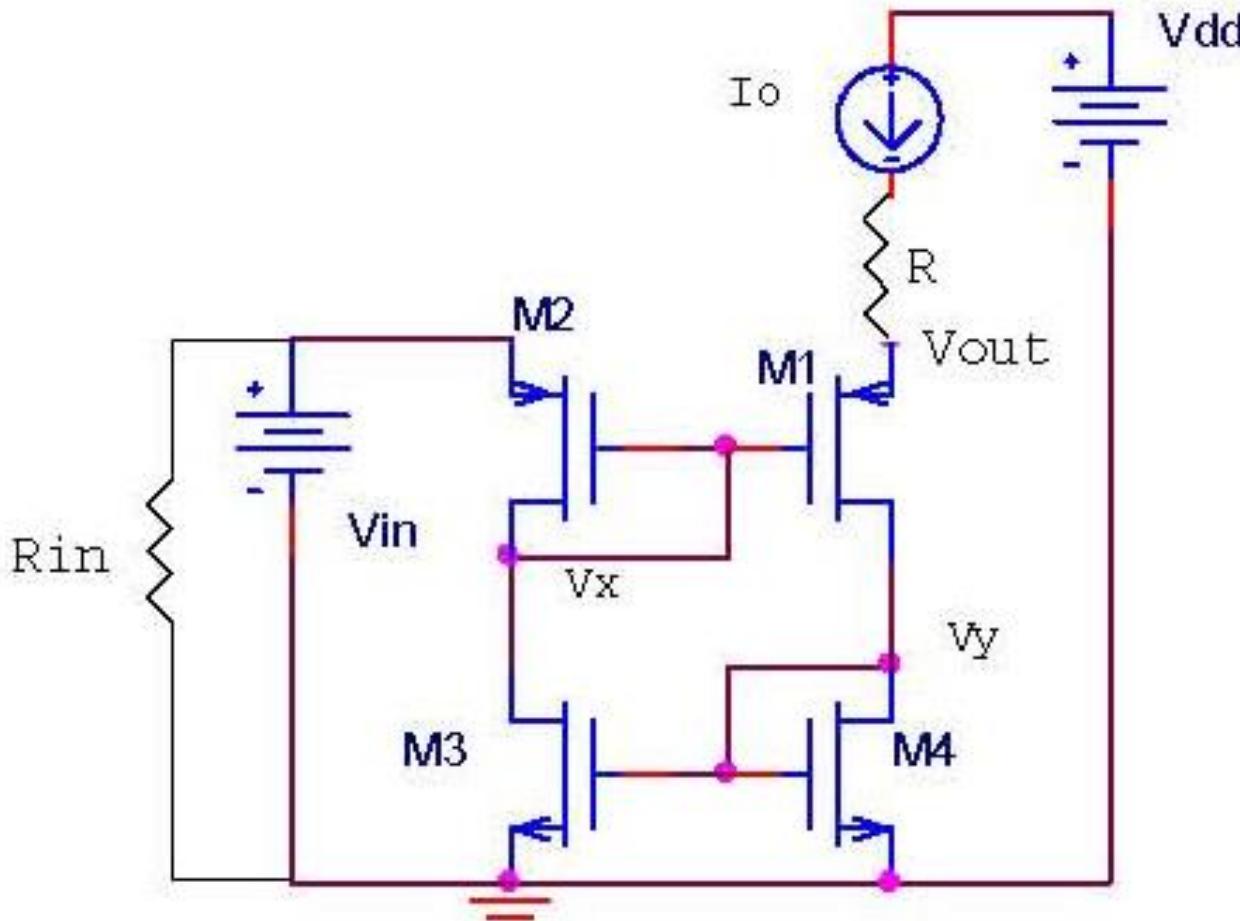
$I_{D1} =$	[ ]	[ ]	[ ]	. [ ]	[ ]	[ ]	[ ]	$\mu\text{A}$	$g_{m1} =$	[ ]	[ ]	[ ]	[ ]	. [ ]	[ ]	[ ]	$\mu\text{s}$
$I_{D2} =$	[ ]	[ ]	[ ]	. [ ]	[ ]	[ ]	[ ]	$\mu\text{A}$	$g_{o1} =$	[ ]	[ ]	[ ]	[ ]	. [ ]	[ ]	[ ]	$\mu\text{s}$
$I_{D3} =$	[ ]	[ ]	[ ]	. [ ]	[ ]	[ ]	[ ]	$\mu\text{A}$	$g_{m2} =$	[ ]	[ ]	[ ]	[ ]	. [ ]	[ ]	[ ]	$\mu\text{s}$
$I_{D4} =$	[ ]	[ ]	[ ]	. [ ]	[ ]	[ ]	[ ]	$\mu\text{A}$	$g_{o2} =$	[ ]	[ ]	[ ]	[ ]	. [ ]	[ ]	[ ]	$\mu\text{s}$
$V_y =$	[ ]	[ ]	[ ]	. [ ]	[ ]	[ ]	[ ]	$\text{V}$	$g_{m3} =$	[ ]	[ ]	[ ]	[ ]	. [ ]	[ ]	[ ]	$\mu\text{s}$
$V_x =$	[ ]	[ ]	[ ]	. [ ]	[ ]	[ ]	[ ]	$\text{V}$	$g_{o3} =$	[ ]	[ ]	[ ]	[ ]	. [ ]	[ ]	[ ]	$\mu\text{s}$
$V_{out} =$	[ ]	[ ]	[ ]	. [ ]	[ ]	[ ]	[ ]	$\text{V}$	$g_{m4} =$	[ ]	[ ]	[ ]	[ ]	. [ ]	[ ]	[ ]	$\mu\text{s}$
									$g_{o4} =$	[ ]	[ ]	[ ]	[ ]	. [ ]	[ ]	[ ]	$\mu\text{s}$

6. Relativamente all'esercizio precedente, disegnare il circuito equivalente alle variazioni e calcolare sia in forma simbolica che numerica il guadagno di tensione  $A_v = v_{out}/v_{in}$

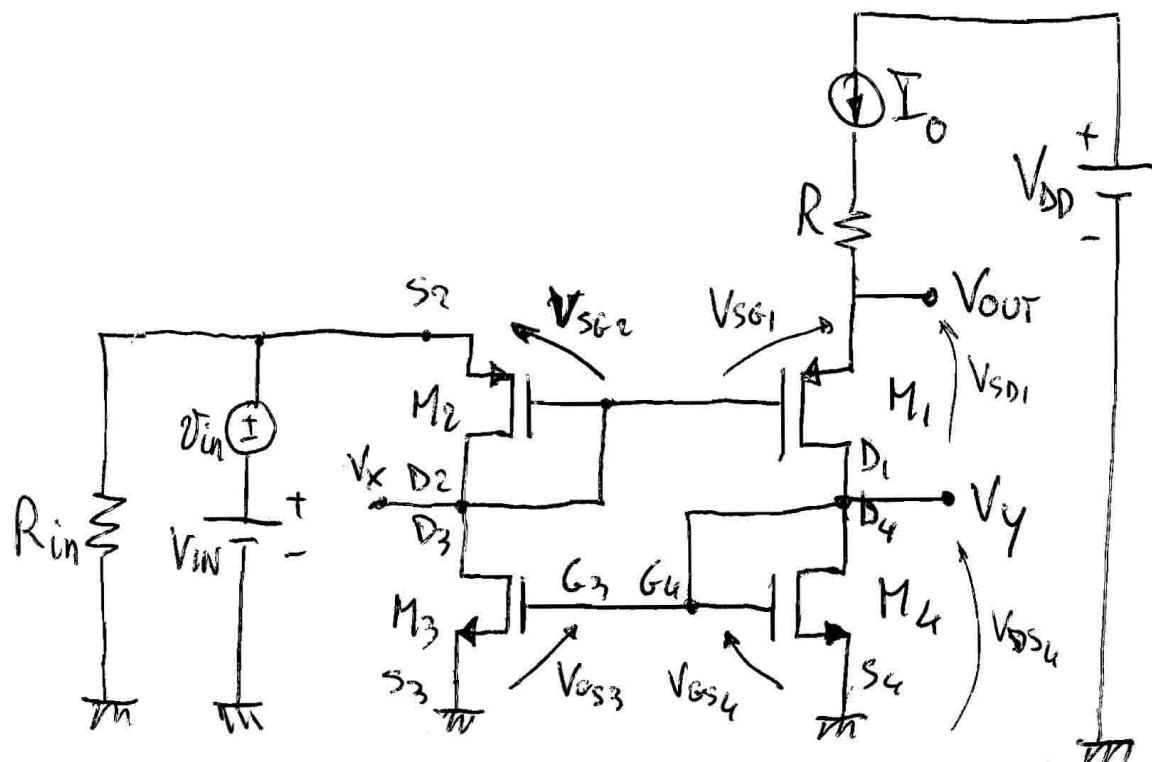
(espressione simbolica)  $v_{out}/v_{in} =$

$$v_{out}/v_{in} = [ ] . [ ] \text{ V/V}$$

# Es. 7c: Soluzione



## Es. 7c: Soluzione



M4 SAT

$$I_{D4} = I_{D1} = I_0$$

$$\underline{I_{D4} = 200 \mu A}$$

$$\underline{I_{D_1} = 200 \mu A}$$

$$I_{D4} = \frac{\beta_4}{2} (V_{GS4} - V_{TH4})^2 \Rightarrow V_{GS4} = \sqrt{\frac{2I_{D2}}{\beta_4}} + V_{TH4} = \sqrt{2+1} = 2.414 \text{ V}$$

## Es. 7c: Soluzione

$$V_y = V_{GS4} = \underline{2.414 \text{ V}}$$

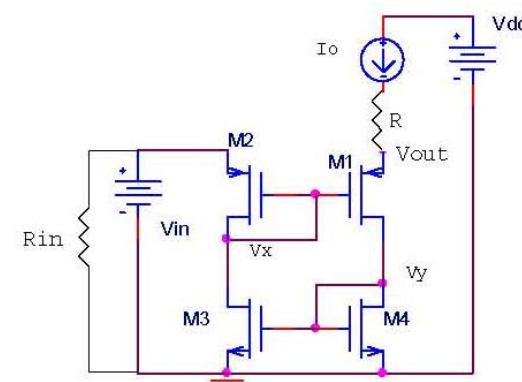
Hp M3 SAT  $V_{GS3} > V_{TH3}$   $V_{DS3} > V_{GS3} - V_{TH3}$

$$I_{D3} = \frac{\beta_3}{2} (V_{GS3} - V_{TH3})^2 ; \quad V_{GS3} = V_{GS4} = 2.414 \text{ V} > V_{TH3} = 1 \text{ V} \boxed{M_3 \text{ ON}}$$

$$\frac{I_{D3}}{I_{D4}} = \frac{\frac{\beta_3}{2} (V_{GS3} - V_{TH3})^2}{\frac{\beta_4}{2} (V_{GS4} - V_{TH4})^2} = \frac{\beta_3}{\beta_4} = 2 \quad I_{D3} = 2I_{D4} = \underline{400 \mu A}$$

M2 SAT  $V_{SG2} = V_{SD2}$

$$I_{D2} = I_{D3} = \underline{400 \mu A}$$



## Es. 7c: Soluzione

$$V_{SG2} = \sqrt{\frac{2 I_{D2}}{\beta_2}} - V_{TH2} = \sqrt{\frac{2 \cdot 400 \cdot 10^{-6}}{200 \cdot 10^{-6}}} + 1 = 2 + 1 = 3 V$$

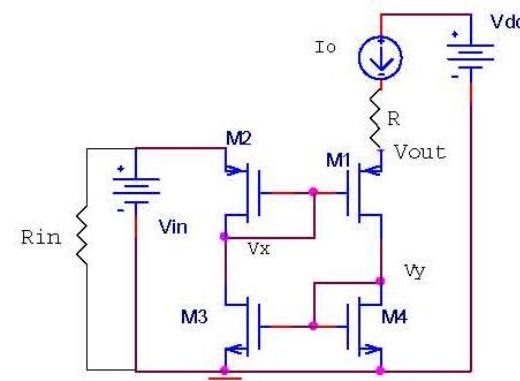
$$V_x = V_{IN} - V_{SG2} = 6 - 3 = \underline{3 V}$$

$$V_{DS3} = V_x = 3 \stackrel{?}{>} V_{GS3} - V_{TH3} = 2.414 - 1 = 1.414 \text{ oe}$$

M3 SAT

Hp. M1 SAT

$$I_{D1} = \frac{\beta_1}{2} (V_{GS1} - V_{TH1})^2 = 200 \mu A$$



## Es. 7c: Soluzione

$$V_{GS1} = -\sqrt{2 \frac{I_{D1}}{P_1}} + V_{TH1} = -\sqrt{2} - 1 = -2.414 \text{ V}$$

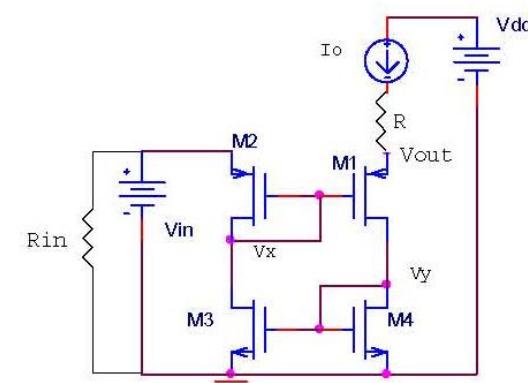
$$V_{SG1} = -V_{GS1} = 2.414 \text{ V}$$

$$V_{OUT} = V_{SG1} + V_x = 2.414 + 3 = \underline{5.414 \text{ V}}$$

$$V_{SD1} = V_{OUT} - V_y = 5.414 - 2.414 = 3 \text{ V} \quad V_{DS1} = -V_{SD1} = 3 \text{ V}$$

$$V_{DS1} = -3 \stackrel{?}{<} V_{GS1} - V_{TH1} = -2.414 + 1 = -1.414 \quad \text{OK}$$

M1 SAT



## Es. 7c: Soluzione

$$g_{m1} = \sqrt{2\beta_1 I_{D1}} = 282.8 \mu\text{s}$$

$$g_{o1} = 0 \mu\text{s}$$

$$g_{m2} = \sqrt{2\beta_2 I_{D2}} = 400 \mu\text{s}$$

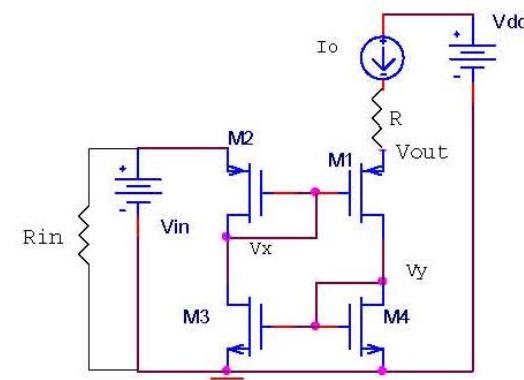
$$g_{o2} = 0 \mu\text{s}$$

$$g_{m3} = \sqrt{2\beta_3 I_{D3}} = 565.6 \mu\text{s}$$

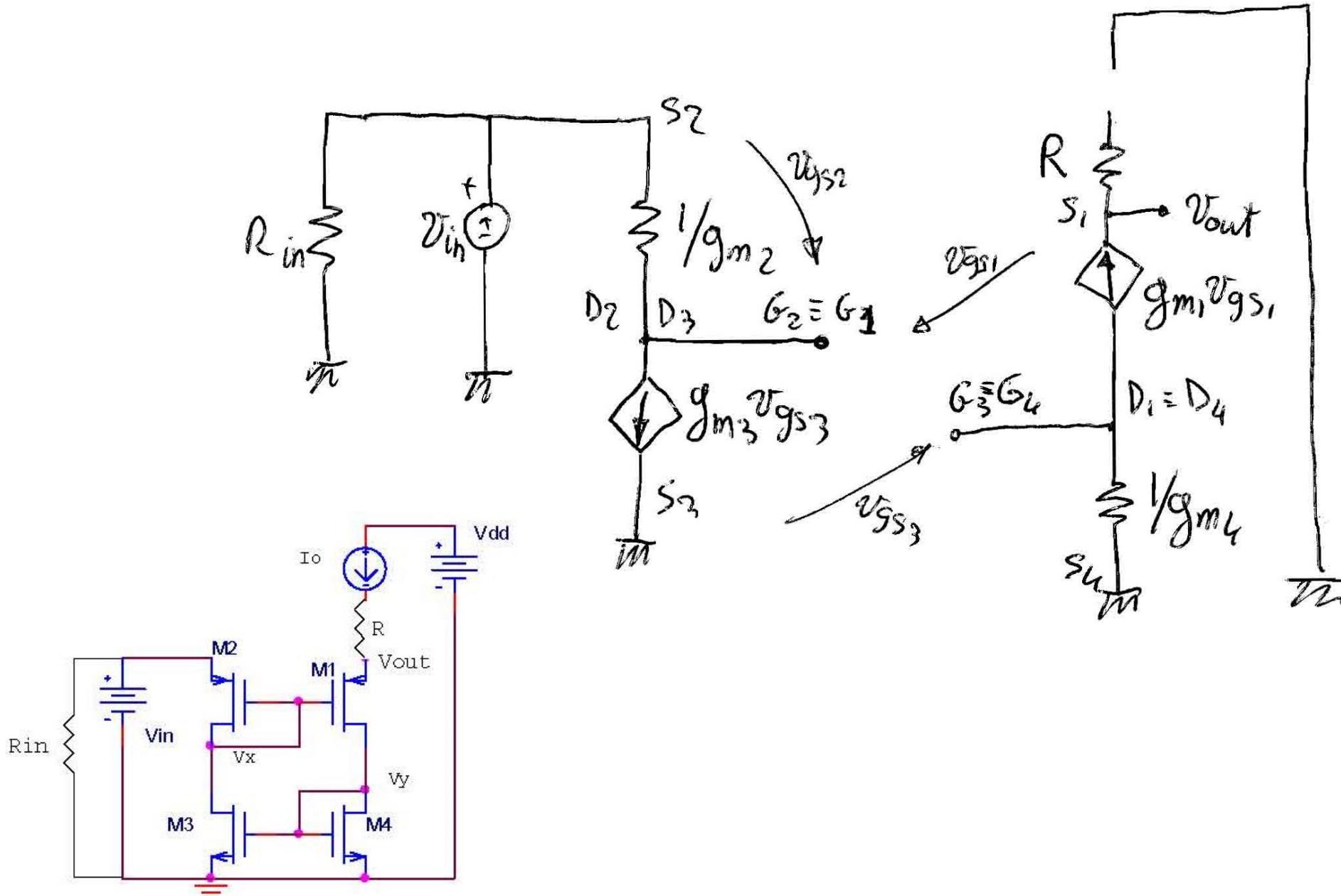
$$g_{o3} = 0 \mu\text{s}$$

$$g_{m4} = \sqrt{2\beta_4 I_{D4}} = 282.8 \mu\text{s}$$

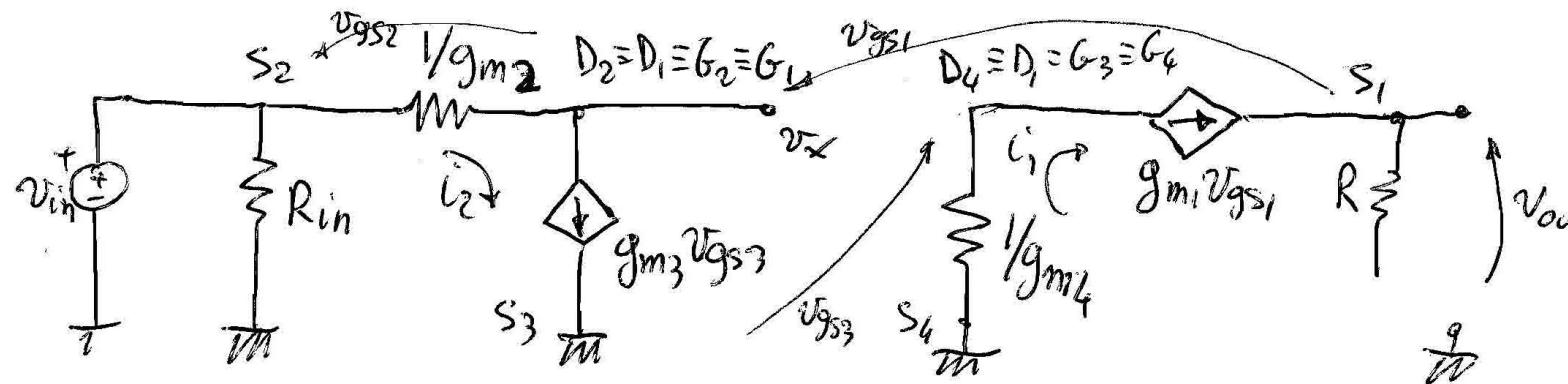
$$g_{o4} = 0 \mu\text{s}$$



# Es. 7c: Soluzione



# Es. 7c: Soluzione



$$g_{m1} V_{gs1} = 0 \Rightarrow V_{gs1} = 0$$

$$V_{gs3} = -i_1 \frac{1}{g_{m4}} = -\frac{g_{m1} V_{gs1}}{g_{m4}} = 0$$

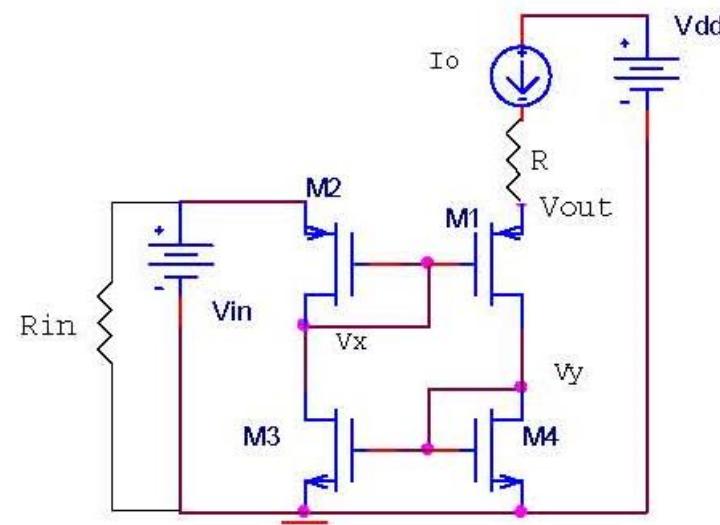
$$i_2 = g_{m3} V_{gs3} = 0 \quad V_x = V_{in}$$

$$V_{gs2} = C_2 \cdot \frac{1}{g_{m2}} = 0$$

$$V_{in} = V_{gs2} + V_{gs1} + V_{out}$$

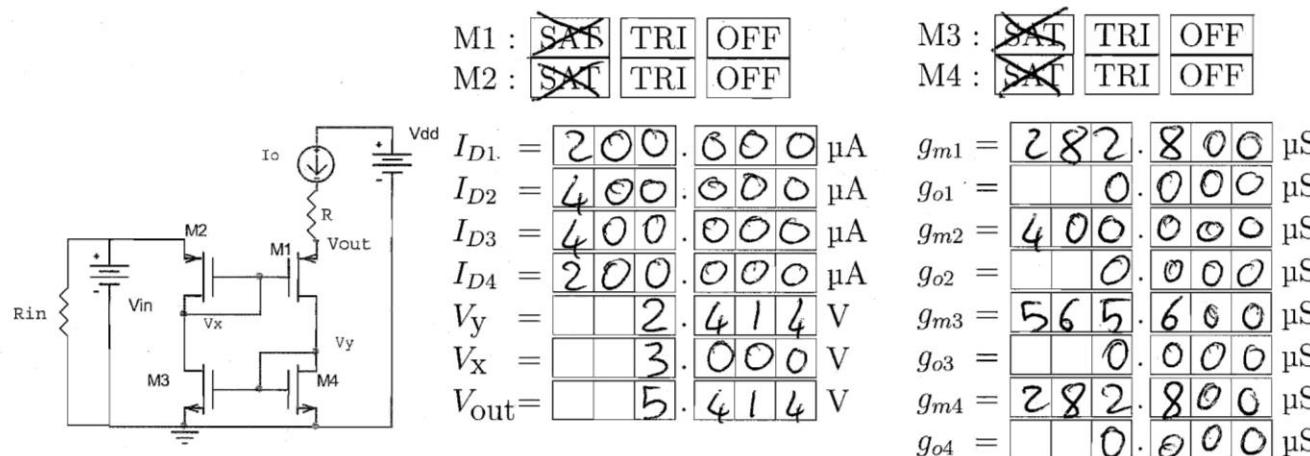
$$V_{out} = V_{in}$$

$$\frac{V_{out}}{V_{in}} = 1$$

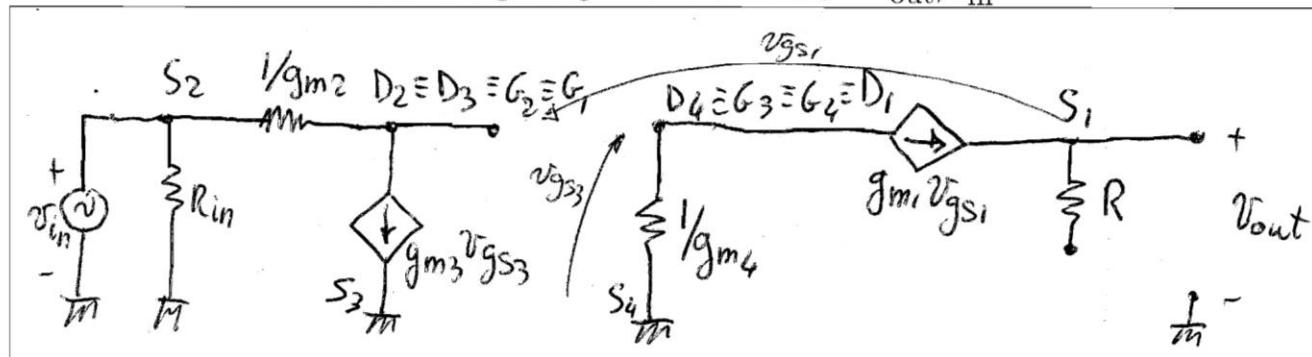


# Es. 7c: Soluzione

5. Dato il circuito in figura ( $V_{dd} = 8 \text{ V}$ ,  $V_{in} = 6 \text{ V}$ ,  $I_O = 200 \mu\text{A}$ ,  $V_{THn} = 1 \text{ V}$ ,  $V_{THp} = -1 \text{ V}$ ,  $R_{in} = 100 \text{ k}\Omega$ ,  $R = 1 \text{ k}\Omega$ ,  $\beta_1 = \beta_2 = \beta_4 = 200 \mu\text{A/V}^2$ ,  $\beta_3 = 400 \mu\text{A/V}^2$ ), determinare: i) la zona di funzionamento dei MOSFET; ii) le correnti  $I_{D1}, I_{D2}, I_{D3}, I_{D4}$  e le tensioni  $V_x, V_y, V_{out}$ ; iii) i parametri differenziali dei MOSFET.



6. Relativamente all'esercizio precedente, disegnare il circuito equivalente alle variazioni e calcolare sia in forma simbolica che numerica il guadagno di tensione  $A_v = v_{out}/v_{in}$

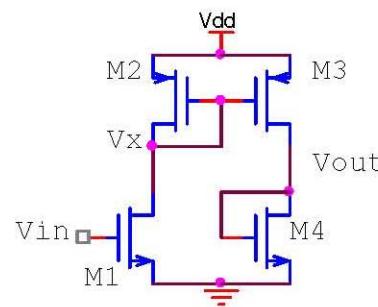


(espressione simbolica)  $v_{out}/v_{in} = 1$

$v_{out}/v_{in} = \boxed{\phantom{0}} \boxed{1.000} \text{ V/V}$

# Circuiti con MOSFET e BJT: Es. 8c

5. Dato il circuito in figura ( $V_{dd} = 5 \text{ V}$ ,  $V_{in} = 3 \text{ V}$ ,  $V_{THn} = 1 \text{ V}$ ,  $V_{THp} = -1 \text{ V}$ ,  $\beta_1 = \beta_2 = 20 \mu\text{A}/\text{V}^2$ ,  $\beta_3 = \beta_4 = 40 \mu\text{A}/\text{V}^2$ ), determinare: *i)* la zona di funzionamento dei MOSFET; *ii)* le correnti  $I_{D1}$ ,  $I_{D2}$ ,  $I_{D3}$ ,  $I_{D4}$  e le tensioni  $V_X$ ,  $V_{out}$ ; *iii)* i parametri differenziali dei MOSFET.



M1 : SAT TRI OFF  
M2 : SAT TRI OFF

M3 : SAT TRI OFF  
M4 : SAT TRI OFF

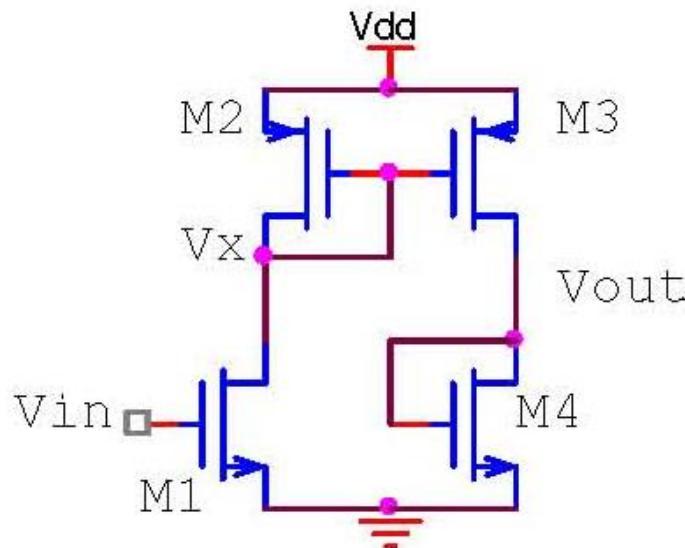
$$\begin{aligned}
 I_{D1} &= \boxed{\phantom{00}} \cdot \boxed{\phantom{00}} \mu\text{A} & g_{m1} &= \boxed{\phantom{00}} \cdot \boxed{\phantom{00}} \mu\text{s} \\
 I_{D2} &= \boxed{\phantom{00}} \cdot \boxed{\phantom{00}} \mu\text{A} & g_{o1} &= \boxed{\phantom{00}} \cdot \boxed{\phantom{00}} \mu\text{s} \\
 I_{D3} &= \boxed{\phantom{00}} \cdot \boxed{\phantom{00}} \mu\text{A} & g_{m2} &= \boxed{\phantom{00}} \cdot \boxed{\phantom{00}} \mu\text{s} \\
 I_{D4} &= \boxed{\phantom{00}} \cdot \boxed{\phantom{00}} \mu\text{A} & g_{o2} &= \boxed{\phantom{00}} \cdot \boxed{\phantom{00}} \mu\text{s} \\
 V_X &= \boxed{\phantom{00}} \cdot \boxed{\phantom{00}} \text{V} & g_{m3} &= \boxed{\phantom{00}} \cdot \boxed{\phantom{00}} \mu\text{s} \\
 V_{out} &= \boxed{\phantom{00}} \cdot \boxed{\phantom{00}} \text{V} & g_{o3} &= \boxed{\phantom{00}} \cdot \boxed{\phantom{00}} \mu\text{s} \\
 && g_{m4} &= \boxed{\phantom{00}} \cdot \boxed{\phantom{00}} \mu\text{s} \\
 && g_{o4} &= \boxed{\phantom{00}} \cdot \boxed{\phantom{00}} \mu\text{s}
 \end{aligned}$$

6. Relativamente all'esercizio precedente, disegnare il circuito equivalente alle variazioni e calcolare sia in forma simbolica che numerica il guadagno di tensione  $A_V = v_{out}/v_{in}$

(espressione simbolica)  $v_{out}/v_{in} =$

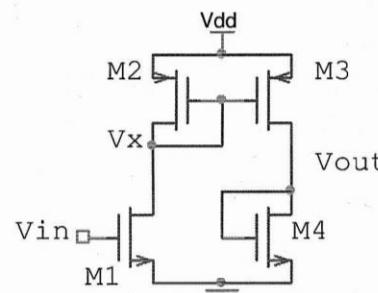
$$v_{out}/v_{in} = \boxed{\phantom{000}} \cdot \boxed{\phantom{000}} \text{V/V}$$

# Es. 8c: Soluzione



## Es. 8c: Soluzione

5. Dato il circuito in figura ( $V_{dd} = 5$  V,  $V_{in} = 3$  V,  $V_{THn} = 1$  V,  $V_{THp} = -1$  V,  $\beta_1 = \beta_2 = 20 \mu\text{A}/\text{V}^2$ ,  $\beta_3 = \beta_4 = 40 \mu\text{A}/\text{V}^2$ ), determinare: i) la zona di funzionamento dei MOSFET; ii) le correnti  $I_{D1}$ ,  $I_{D2}$ ,  $I_{D3}$ ,  $I_{D4}$  e le tensioni  $V_x$ ,  $V_{out}$ ; iii) i parametri differenziali dei MOSFET.



M1 : ~~SAT~~ TRI OFF  
 M2 : ~~SAT~~ TRI OFF

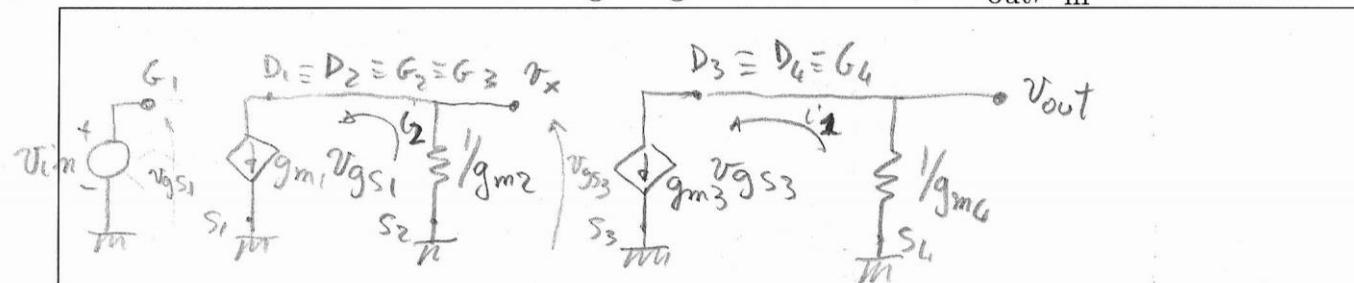
$I_{D1} =$	40	000
$I_{D2} =$	40	000
$I_{D3} =$	80	000
$I_{D4} =$	80	000
$V_X =$	2	000
$V_{out} =$	3	000

M3 : ~~SAT~~ TRI OFF  
 M4 : ~~SAT~~ TRI OFF

$$I_{D_i} = \frac{\beta_i}{2} (V_{GSi} - V_{THi})^2$$

$g_{m1} =$	40	000
$g_{o1} =$	0	000
$g_{m2} =$	40	000
$g_{o2} =$	0	000
$g_{m3} =$	80	000
$g_{o3} =$	0	000
$g_{m4} =$	80	000
$g_{o4} =$	0	000

6. Relativamente all'esercizio precedente, disegnare il circuito equivalente alle variazioni e calcolare sia in forma simbolica che numerica il guadagno di tensione  $A_V = v_{\text{out}}/v_{\text{in}}$



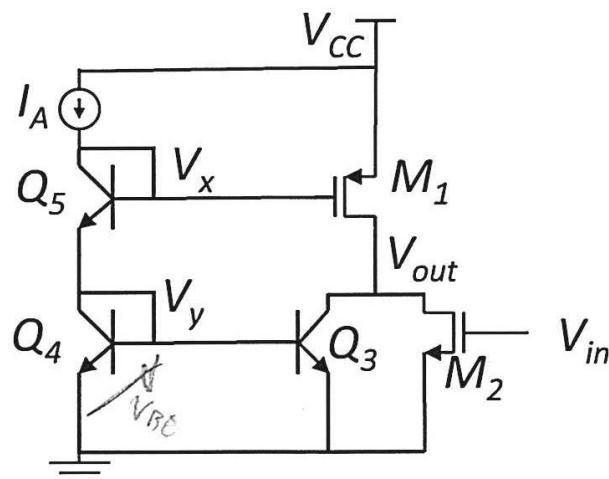
$$v_{out} = \frac{v_{gs_3}}{g_{m_4}}; \quad v_{gs_3} = v_{ce}; \quad v_x = \frac{v_{ce}}{g_{m_2}}; \quad i_2 = g_{m_1} v_{gs_1}; \quad v_{gs_1} = v_i$$

(espressione simbolica)  $v_{out}/v_{in} = \frac{(g_{m_1} g_{m_3})}{(g_{m_2} g_{m_4})}$

$v_{\text{out}}/v_{\text{in}} = \boxed{\phantom{0}} \boxed{\phantom{0}} \boxed{1} \cdot \boxed{0} \boxed{0} \boxed{0} \text{ V/V}$

# Circuiti con MOSFET e BJT: Es. 9c (14.01.2014)

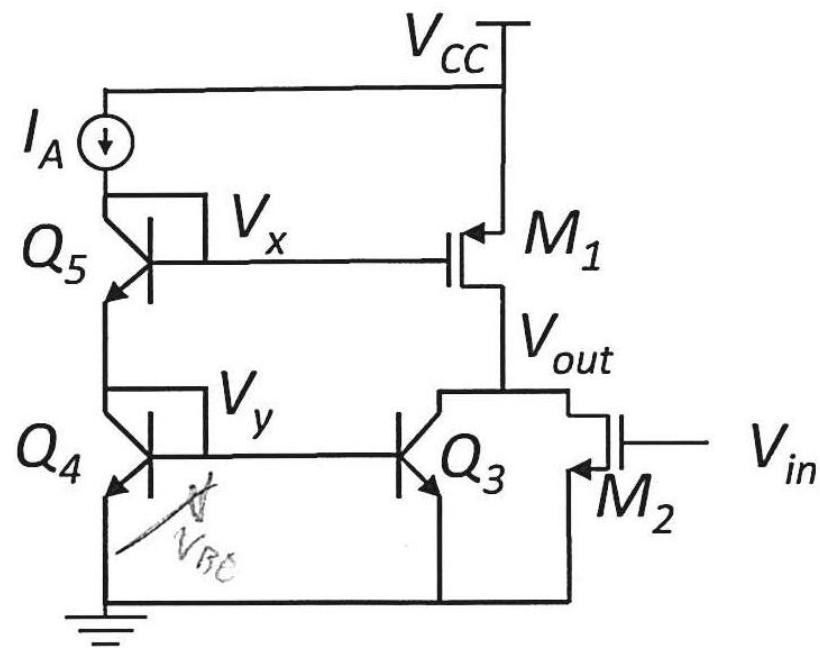
5. Dato il circuito in figura ( $V_{cc} = 5$  V,  $V_T = 25$  mV,  $V_\gamma = 0.6$  V,  $V_{THn} = 1$  V,  $V_{THp} = -1$  V,  $\beta_{M1} = \beta_{M2} = 800 \mu\text{A}/\text{V}^2$ ,  $\beta_{Q3} = \beta_{Q4} = \beta_{Q5} = 100$ ,  $I_A = 1.5$  mA,  $V_{in} = 2$  V), determinare: *i)* la zona di funzionamento di MOSFET e BJT; *ii)* le correnti  $I_{D1}$ ,  $I_{D2}$ ,  $I_{C3}$ ,  $I_{C4}$ ,  $I_{C5}$ , e le tensioni  $V_X$ ,  $V_Y$ ,  $V_{out}$ ; *iii)* i parametri differenziali di MOSFET e BJT.



Q3 :	OFF	SAT	<del>DTR</del>	INV
Q4 :	OFF	SAT	<del>DTR</del>	INV
Q5 :	OFF	SAT	<del>DTR</del>	INV
$I_{D1}$ =		1	8 7 1	mA
$I_{D2}$ =		0	4 0 0	mA
$I_{C3}$ =		1	4 7 1	mA
$I_{C4}$ =		1	4 7 1	mA
$I_{C5}$ =		1	4 8 5	mA
$V_x$ =		1	2 0 0	V
$V_y$ =		0	6 0 0	V
$V_{out}$ =		3	9 7 9	V

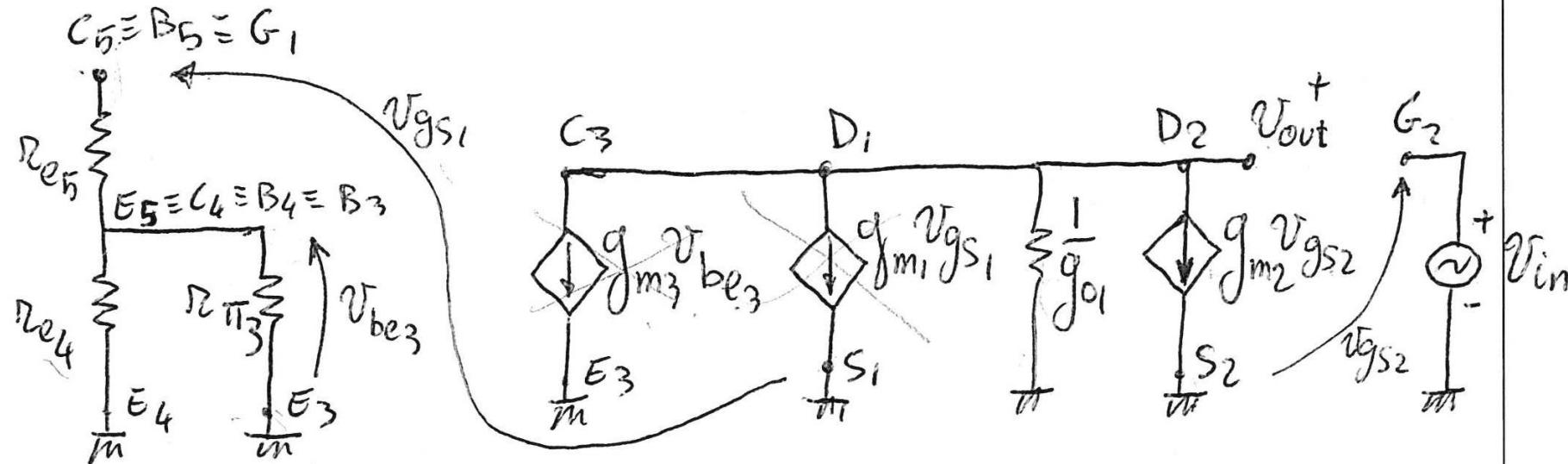
M1 :	SAT	<del>TRI</del>	OFF
M2 :	<del>SAT</del>	TRI	OFF
$g_{m1}$ =		0.	8 1 7
$g_{o1}$ =		1.	4 2 3
$g_{m2}$ =		0.	8 0 0
$g_{o2}$ =		0.	0 0 0
$g_{m3}$ =	5 8	.	8 2 4
$r_{\pi 3}$ =	1.	7 0 0	$k\Omega$
$g_{m4}$ =	5 8	.	8 2 4
$r_{\pi 4}$ =	1.	7 0 0	$k\Omega$
$g_{m5}$ =	5 9	.	4 0 6
$r_{\pi 5}$ =	1.	6 8 3	$k\Omega$

# Es. 9c (14.01.2014): Soluzione



# Es. 9c (14.01.2014): Soluzione

Relativamente all'esercizio precedente, disegnare il circuito equivalente alle variazioni e calcolare sia in forma simbolica che numerica il guadagno di tensione  $A_V = v_{\text{out}}/v_{\text{in}}$

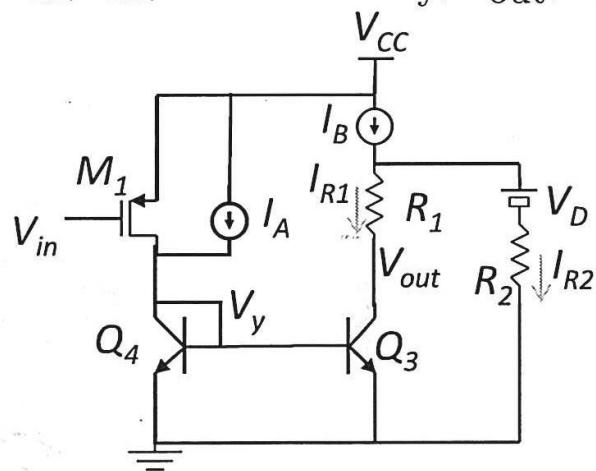


$$v_{\text{out}}/v_{\text{in}} = -g_{m2}/g_{m1}$$

$$v_{\text{out}}/v_{\text{in}} = - \boxed{\phantom{0}} \boxed{\phantom{0}} \boxed{0} \boxed{5} \boxed{6} \boxed{2} \text{ V/V}$$

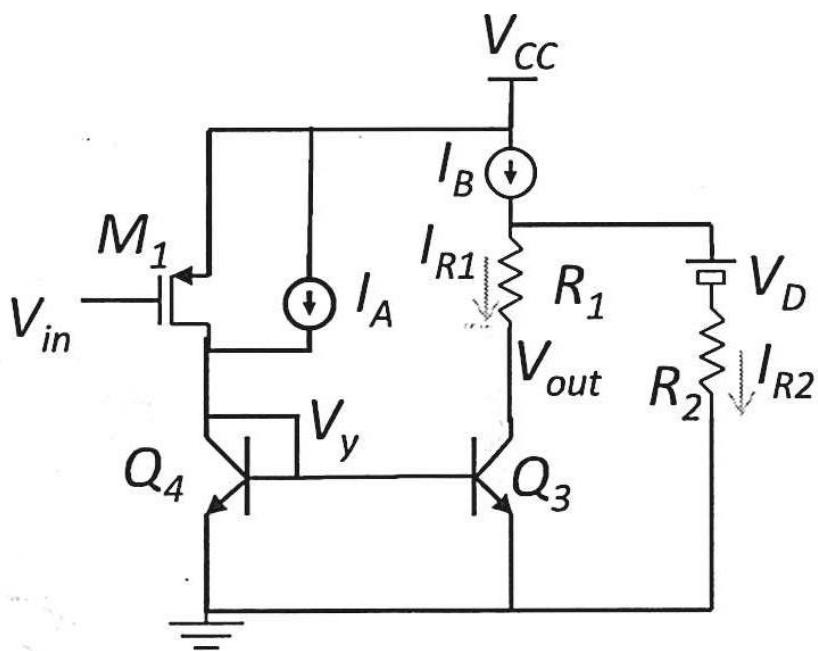
# Circuiti con MOSFET e BJT: Es. 10c (04.02.2014)

5. Dato il circuito in figura ( $V_{cc} = 5 \text{ V}$ ,  $V_T = 25 \text{ mV}$ ,  $V_\gamma = 0.6 \text{ V}$ ,  $V_{THp} = -1 \text{ V}$ ,  $R_1 = 100 \Omega$ ,  $R_2 = 1 \text{ k}\Omega$ ,  $\beta_{M1} = 400 \mu\text{A/V}^2$ ,  $\beta_{Q3} = \beta_{Q4} = 30$ ,  $V_{in} = 2 \text{ V}$ ,  $V_D = 4 \text{ V}$ ,  $I_A = 500 \mu\text{A}$ ,  $I_B = 2 \text{ mA}$ ), sapendo che il MOSFET lavora in saturazione e i BJT in normale diretta, determinare: *i)* le correnti  $I_{D1}$ ,  $I_{C3}$ ,  $I_{C4}$ ,  $I_{R1}$ ,  $I_{R2}$ , e le tensioni  $V_y$ ,  $V_{out}$ ; *ii)* i parametri differenziali di MOSFET e BJT.



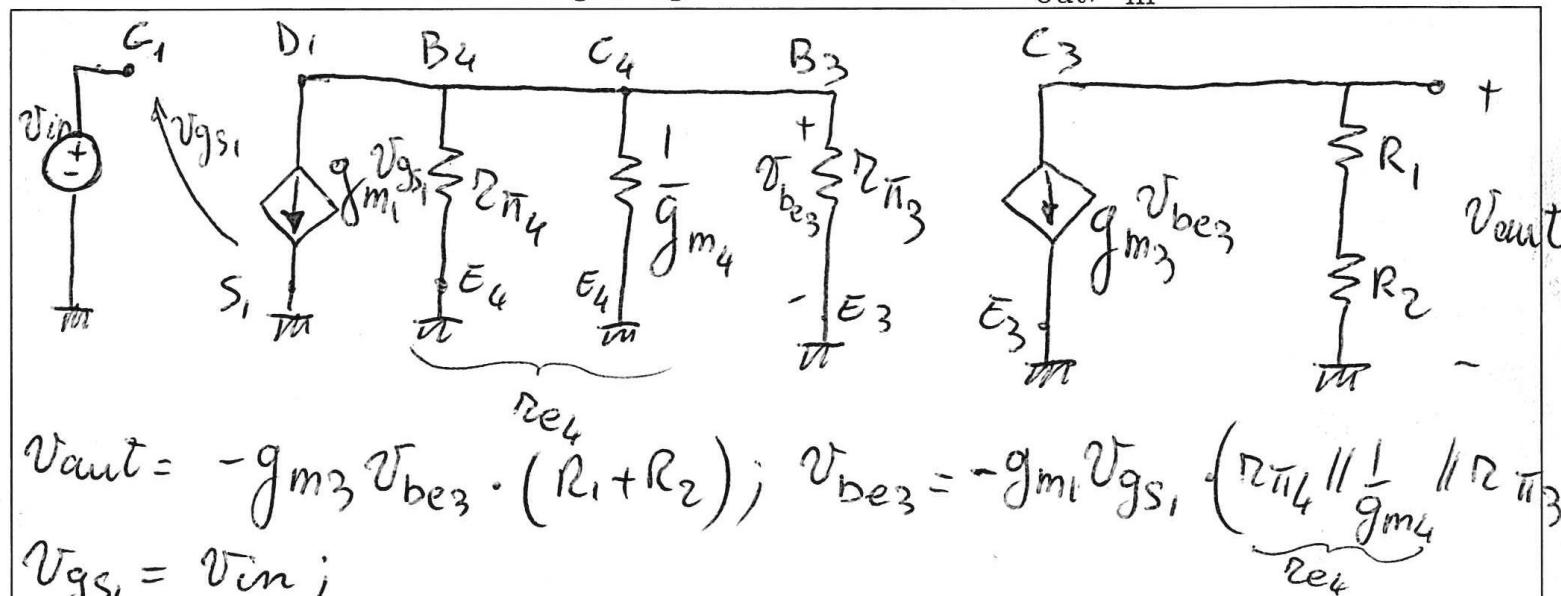
$$\begin{aligned}
 I_{D1} &= \boxed{\phantom{0}} \boxed{\phantom{0}} \boxed{0} \cdot \boxed{8} \boxed{0} \boxed{0} \text{ mA} \\
 I_{C3} &= \boxed{\phantom{0}} \boxed{\phantom{0}} \boxed{1} \cdot \boxed{2} \boxed{1} \boxed{9} \text{ mA } g_{m1} = \boxed{\phantom{0}} \boxed{\phantom{0}} \boxed{0} \cdot \boxed{8} \boxed{0} \boxed{0} \text{ mS} \\
 I_{C4} &= \boxed{\phantom{0}} \boxed{\phantom{0}} \boxed{1} \cdot \boxed{2} \boxed{1} \boxed{9} \text{ mA } g_{o1} = \boxed{\phantom{0}} \boxed{\phantom{0}} \boxed{0} \cdot \boxed{0} \boxed{0} \boxed{0} \text{ mS} \\
 I_{R1} &= \boxed{\phantom{0}} \boxed{\phantom{0}} \boxed{1} \cdot \boxed{2} \boxed{1} \boxed{9} \text{ mA } g_{m3} = \boxed{4} \boxed{8} \cdot \boxed{7} \boxed{6} \boxed{0} \text{ mS} \\
 I_{R2} &= \boxed{\phantom{0}} \boxed{\phantom{0}} \boxed{0} \cdot \boxed{7} \boxed{8} \boxed{1} \text{ mA } r_{\pi 3} = \boxed{\phantom{0}} \boxed{\phantom{0}} \boxed{0} \cdot \boxed{6} \boxed{1} \boxed{5} \text{ k}\Omega \\
 V_y &= \boxed{\phantom{0}} \boxed{\phantom{0}} \boxed{0} \cdot \boxed{6} \boxed{0} \boxed{0} \text{ V } g_{m4} = \boxed{4} \boxed{8} \cdot \boxed{7} \boxed{6} \boxed{0} \text{ mS} \\
 V_{out} &= \boxed{\phantom{0}} \boxed{\phantom{0}} \boxed{4} \cdot \boxed{6} \boxed{5} \boxed{9} \text{ V } r_{\pi 4} = \boxed{\phantom{0}} \boxed{\phantom{0}} \boxed{0} \cdot \boxed{6} \boxed{1} \boxed{5} \text{ k}\Omega
 \end{aligned}$$

# Es. 10c (04.02.2014): Soluzione



# Es. 10c (04.02.2014): Soluzione

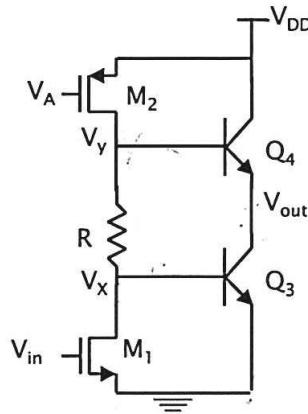
Relativamente all'esercizio precedente, disegnare il circuito equivalente alle variazioni e calcolare sia in forma simbolica che numerica il guadagno di tensione  $A_V = v_{\text{out}}/v_{\text{in}}$



$$\begin{aligned} v_{\text{out}}/v_{\text{in}} &= g_{m_1} \left( R_{\pi_3} \parallel R_{\pi_4} \parallel \frac{1}{g_{m_4}} \right) g_{m_3} (R_1 + R_2) \\ &= g_{m_1} (R_{\pi_3} \parallel R_{\text{eq}_4}) g_{m_3} (R_1 + R_2) \end{aligned}$$

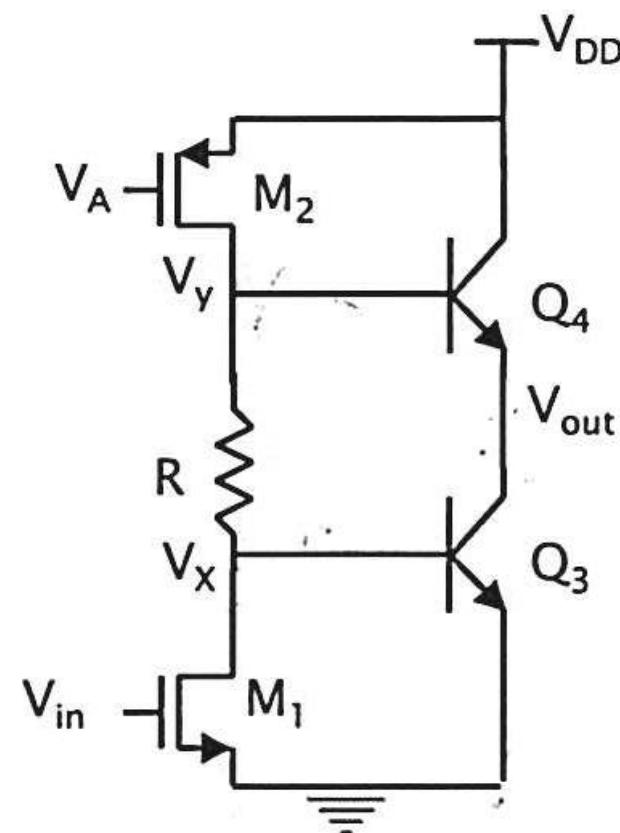
# Circuiti con MOSFET e BJT: Es. 11c (07.07.2015)

5. Dato il circuito in figura ( $V_{DD} = 5 \text{ V}$ ,  $V_A = 3.5 \text{ V}$ ,  $V_{IN} = 1 \text{ V}$ ,  $V_{THn} = 0.5 \text{ V}$ ,  $V_{THp} = -0.5 \text{ V}$ ,  $V_T = 25 \text{ mV}$ ,  $V_\gamma = 0.6 \text{ V}$ ,  $\beta_{M1} = 200 \mu\text{A}/\text{V}^2$ ,  $\beta_{M2} = 100 \mu\text{A}/\text{V}^2$ ,  $\beta_{Q3} = 100$ ,  $\beta_{Q4} = 50$ ,  $R = 100 \text{ k}\Omega$ , ipotizzando e verificando che M1 e M2 siano saturi e che Q3 e Q4 siano in normale diretta), determinare: i) le correnti  $I_{D1}, I_{D2}, I_{C3}, I_{C4}, I_R$  e le tensioni  $V_x, V_y, V_{out}$ ; ii) i parametri differenziali dei MOSFET e dei BJT.



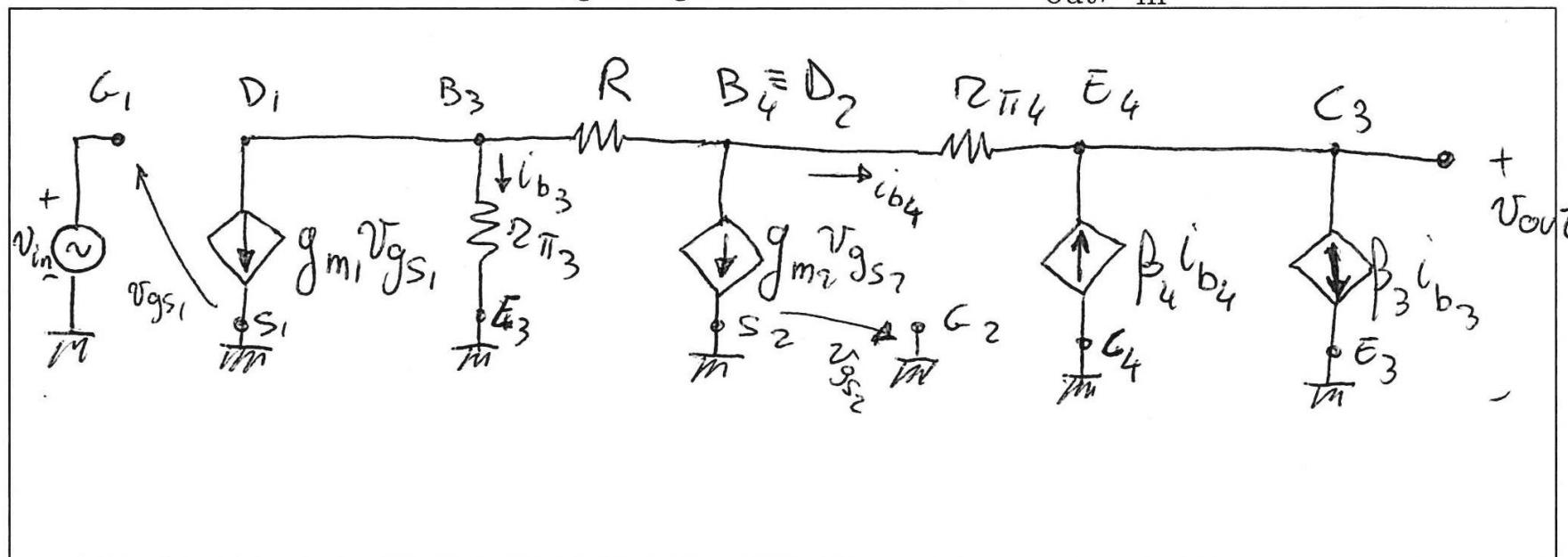
$I_{D1} =$	2	5	.	0	0	0	μA	$g_{m1} =$	1	0	0	.	0	0	0	μS
$I_{D2} =$	5	0	.	0	0	0	μA	$g_{o1} =$			0	.	0	0	0	μS
$I_{C3} =$	8	4	4	.	3		μA	$g_{m2} =$	1	0	0	.	0	0	0	μS
$I_{C4} =$	8	2	7	.	8		μA	$g_{o2} =$			0	.	0	0	0	μS
$I_R =$	3	3	.	4	4	3	μA	$g_{m3} =$	3	3	.	7	7	2	mS	
$V_x =$			0	.	6	0	0	$V r_{\pi 3} =$		2	.	9	6	1	kΩ	
$V_y =$			3	.	9	4	4	$V g_{m4} =$	3	3	.	1	1	2	mS	
$V_{out} =$			3	.	3	4	4	$V r_{\pi 4} =$		1	.	5	1	0	kΩ	

# Es. 11c (07.07.2015): Soluzione



# Es. 11c (07.07.2015): Soluzione

Relativamente all'esercizio precedente, disegnare il circuito equivalente alle variazioni e calcolare sia in forma simbolica che numerica il guadagno di tensione  $A_V = v_{\text{out}}/v_{\text{in}}$

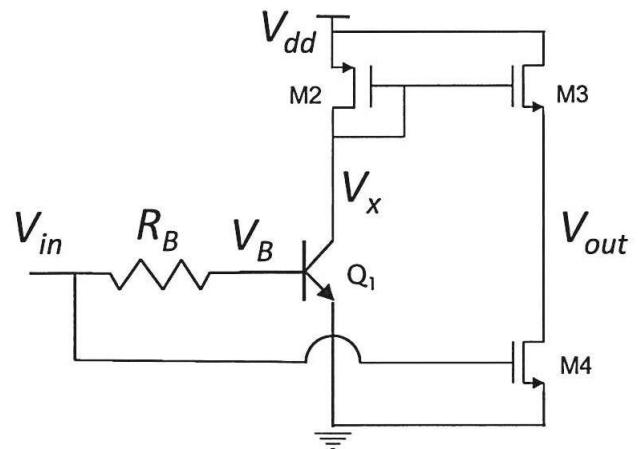


$$v_{\text{out}}/v_{\text{in}} = \left( R + R_{\pi 4} - R_{\pi 3} \frac{1 + \beta_4}{\beta_3} \right) \cdot \frac{g_{m1}}{1 + \frac{1 + \beta_4}{\beta_3}}$$

$$v_{\text{out}}/v_{\text{in}} = + \boxed{\phantom{0}} \boxed{\phantom{0}} \boxed{3} \cdot \boxed{i} \boxed{6} \boxed{3} \text{ V/V}$$

# Circuiti con MOSFET e BJT: Es. 12c (25.02.2016)

5. Dato il circuito in figura ( $V_{DD} = 5 \text{ V}$ ,  $R_B = 100 \text{ k}\Omega$ ,  $V_T = 25 \text{ mV}$ ,  $V_\gamma = 0.6 \text{ V}$ ,  $V_{THn} = 1 \text{ V}$ ,  $V_{THp} = -1 \text{ V}$ ,  $\beta_{Q1} = 20$ ,  $\beta_{M2} = 400 \mu\text{A}/\text{V}^2$ ,  $\beta_{M3} = 200 \mu\text{A}/\text{V}^2$ ,  $\beta_{M4} = 100 \mu\text{A}/\text{V}^2$ ,  $V_{IN} = 2 \text{ V}$ ) e supponendo il BJT in normale diretta, determinare: *i*) la zona di funzionamento dei MOSFET, *ii*) le correnti  $I_B$ ,  $I_C$ ,  $I_{D2}$ ,  $I_{D3}$ ,  $I_{D4}$ , e le tensioni  $V_x$ ,  $V_{out}$ ; *ii*) i parametri differenziali dei MOSFET.



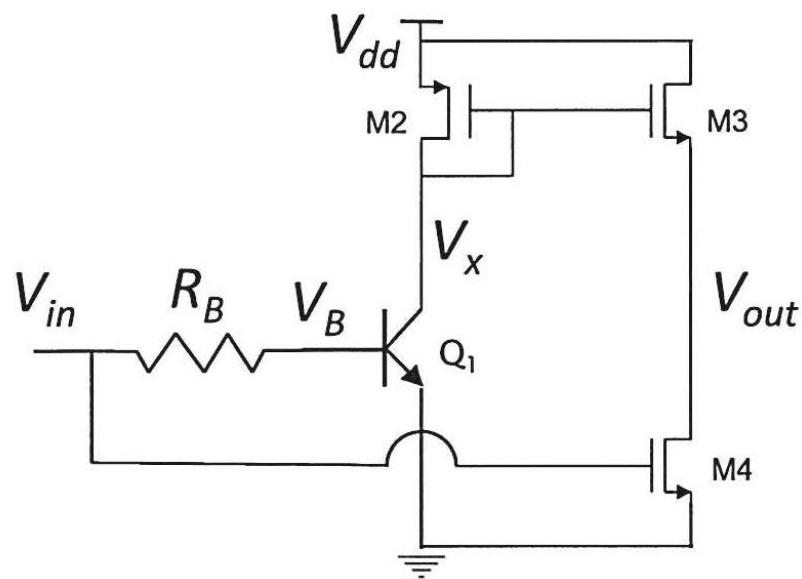
M2 : ~~SAT~~ TRI OFF  
M3 : ~~SAT~~ TRI OFF

$$\begin{aligned} I_B &= \boxed{\phantom{0}}. \boxed{0}. \boxed{0} \boxed{1} \boxed{4} \text{ mA} \\ I_C &= \boxed{\phantom{0}}. \boxed{0}. \boxed{2} \boxed{8} \boxed{0} \text{ mA} \\ I_{D2} &= \boxed{\phantom{0}}. \boxed{0}. \boxed{2} \boxed{8} \boxed{0} \text{ mA} \\ I_{D3} &= \boxed{\phantom{0}}. \boxed{0}. \boxed{0} \boxed{5} \boxed{0} \text{ mA} \\ I_{D4} &= \boxed{\phantom{0}}. \boxed{0}. \boxed{0} \boxed{5} \boxed{0} \text{ mA} \\ V_x &= \boxed{2}. \boxed{8} \boxed{1} \boxed{7} \text{ V} \\ V_{out} &= \boxed{\phantom{0}}. \boxed{1}. \boxed{1} \boxed{1} \boxed{0} \text{ V} \end{aligned}$$

M4 : ~~SAT~~ TRI OFF

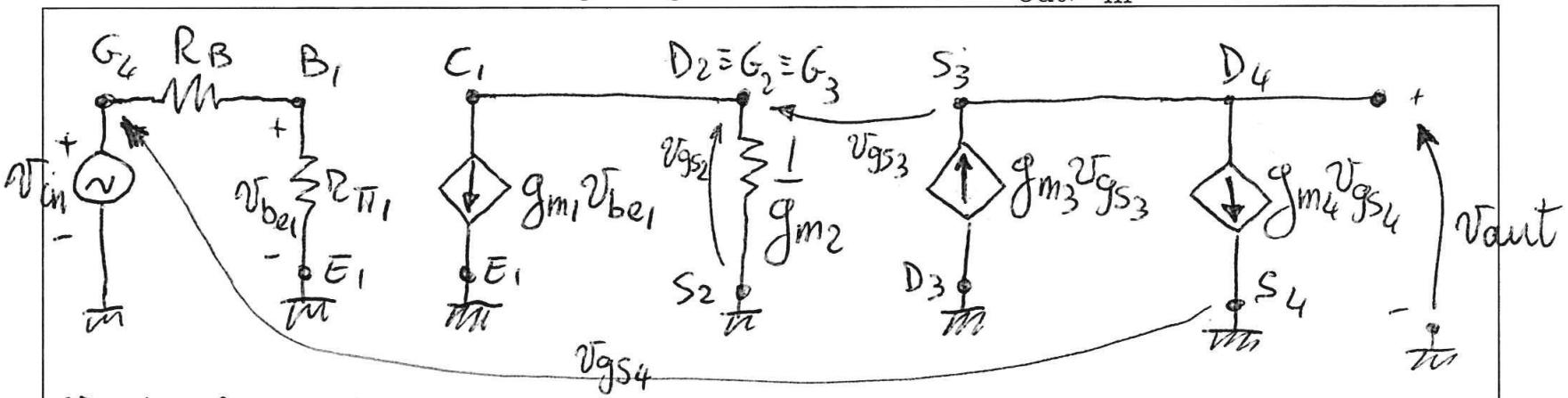
$$\begin{aligned} g_{m1} &= \boxed{1} \boxed{1}. \boxed{2} \boxed{\phantom{0}} \text{ mS} \\ r_{\pi 1} &= \boxed{\phantom{0}}. \boxed{1}. \boxed{7} \boxed{8} \boxed{6} \text{ k}\Omega \\ g_{m2} &= \boxed{4} \boxed{7} \boxed{3}. \boxed{2} \boxed{8} \boxed{6} \text{ } \mu\text{S} \\ g_{o2} &= \boxed{\phantom{0}}. \boxed{0} \boxed{\phantom{0}} \boxed{\phantom{0}} \text{ } \mu\text{S} \\ g_{m3} &= \boxed{1} \boxed{4} \boxed{1}. \boxed{4} \boxed{2} \boxed{1} \text{ } \mu\text{S} \\ g_{o3} &= \boxed{\phantom{0}}. \boxed{0} \boxed{\phantom{0}} \boxed{\phantom{0}} \text{ } \mu\text{S} \\ g_{m4} &= \boxed{1} \boxed{0} \boxed{0}. \boxed{0} \boxed{\phantom{0}} \text{ } \mu\text{S} \\ g_{o4} &= \boxed{\phantom{0}}. \boxed{0} \boxed{\phantom{0}} \boxed{\phantom{0}} \text{ } \mu\text{S} \end{aligned}$$

# Circuiti con MOSFET e BJT: Es. 12c (25.02.2016)



# Circuiti con MOSFET e BJT: Es. 12c (25.02.2016)

6. Relativamente all'esercizio precedente, disegnare il circuito equivalente alle variazioni e calcolare sia in forma simbolica che numerica il guadagno di tensione  $A_V = v_{\text{out}}/v_{\text{in}}$



$$v_{\text{out}} = v_{gs2} - v_{gs3}; \quad g_m_3 v_{gs3} = g_m_4 v_{gs4}; \quad v_{gs4} = v_{in}; \quad v_{gs2} = -g_{m1} v_{be1} \cdot \frac{1}{g_{m2}}$$

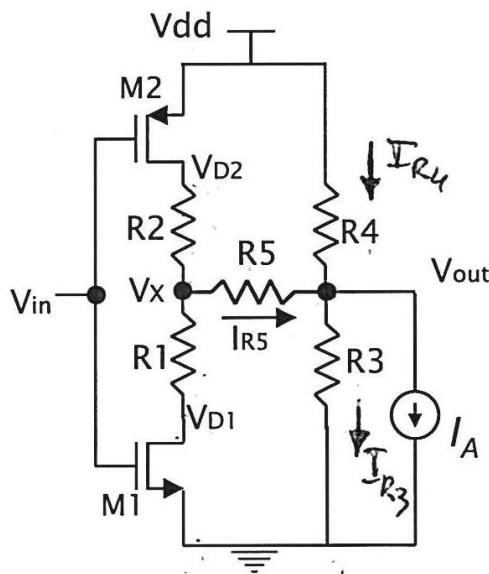
$$v_{be1} = [R_{\pi 1}/(R_{\pi 1} + R_B)] \cdot v_{in}$$

$$v_{\text{out}}/v_{\text{in}} = -\frac{g_{m1}}{g_{m2}} \cdot \frac{R_{\pi 1}}{R_{\pi 1} + R_B} - \frac{g_{m4}}{g_{m3}}$$

$$v_{\text{out}}/v_{\text{in}} = \boxed{-} \boxed{\phantom{0}} \boxed{1} \cdot \boxed{1} \boxed{2} \boxed{2} \text{ V/V}$$

# Circuiti con MOSFET e BJT: Es. 13c (09.02.2016)

5. Dato il circuito in figura ( $V_{DD} = 5 \text{ V}$ ,  $I_A = 100 \mu\text{A}$ ,  $R_1 = R_2 = 500 \Omega$ ,  $R_3 = R_4 = 2 \text{ k}\Omega$ ,  $R_5 = 1 \text{ k}\Omega$ ,  $V_{THn} = 1 \text{ V}$ ,  $V_{THp} = -1 \text{ V}$ ,  $\beta_{M1} = 100 \mu\text{A/V}^2$ ,  $\beta_{M2} = 200 \mu\text{A/V}^2$ ,  $V_{IN} = 2.2 \text{ V}$ ), determinare: i) la zona di funzionamento di MOSFET, ii) le correnti  $I_{D1}$ ,  $I_{D2}$ ,  $I_{R3}$ ,  $I_{R4}$ ,  $I_{R5}$ , e le tensioni  $V_x$ ,  $V_{D1}$ ,  $V_{D2}$ ,  $V_{out}$ ; iii) i parametri differenziali dei MOSFET.

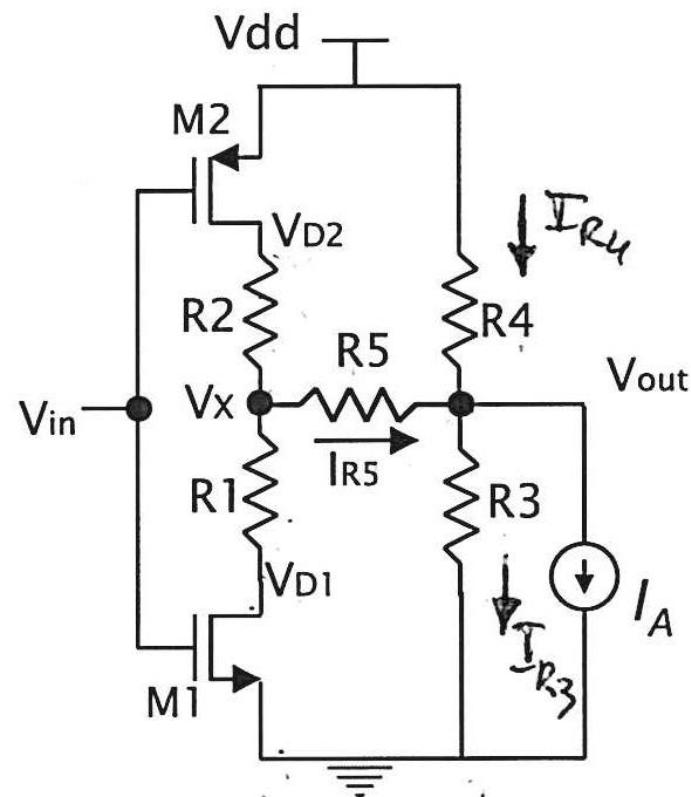


$$\begin{aligned}
 I_{D1} &= \boxed{\phantom{0}}.072 \text{ mA} \\
 I_{D2} &= \boxed{\phantom{0}}.324 \text{ mA} \\
 I_{R3} &= \boxed{1}.326 \text{ mA} \\
 I_{R4} &= \boxed{1}.174 \text{ mA} \\
 I_{R5} &= \boxed{0}.252 \text{ mA} \\
 V_x &= \boxed{2}.904 \text{ V} \\
 V_{D1} &= \boxed{2}.868 \text{ V} \\
 V_{D2} &= \boxed{3}.066 \text{ V} \\
 V_{out} &= \boxed{2}.652 \text{ V}
 \end{aligned}$$

$$\begin{aligned}
 M1 : & \quad \boxed{\text{SAT}} \quad \boxed{\text{TRI}} \quad \boxed{\text{OFF}} \\
 M2 : & \quad \boxed{\text{SAT}} \quad \boxed{\text{TRI}} \quad \boxed{\text{OFF}}
 \end{aligned}$$

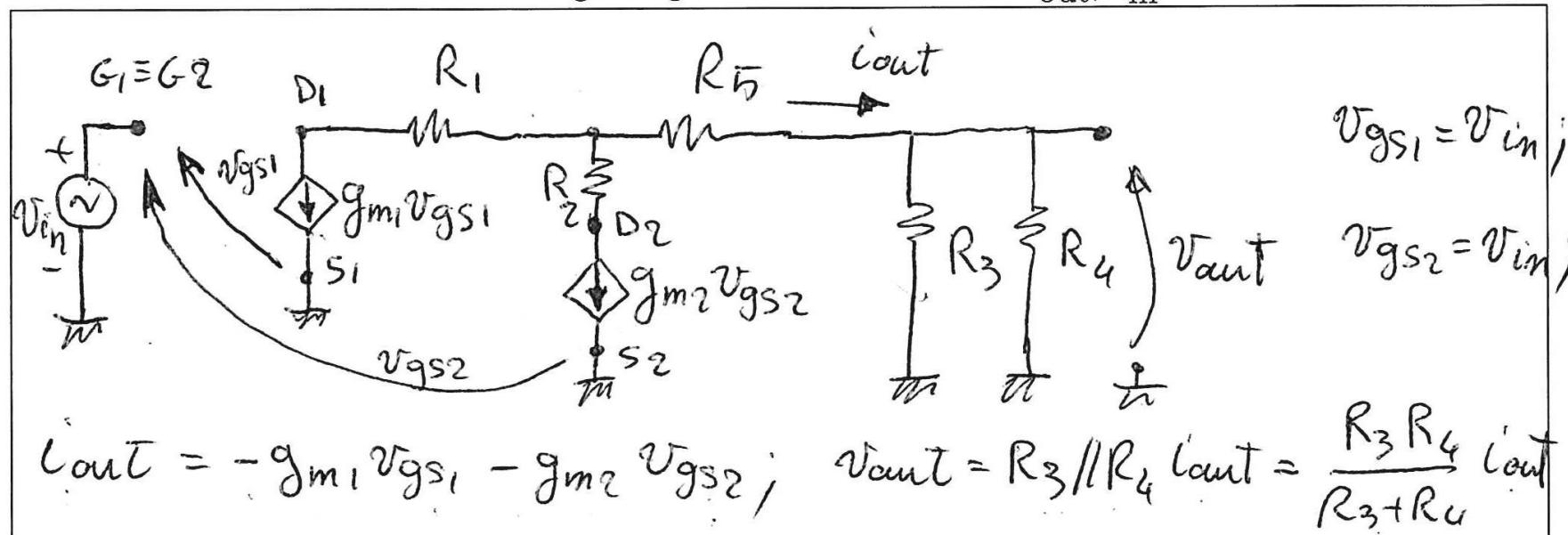
$$\begin{aligned}
 g_{m1} &= \boxed{1}.20.000 \mu\text{S} \\
 g_{o1} &= \boxed{0}.00.000 \mu\text{S} \\
 g_{m2} &= \boxed{3}.60.000 \mu\text{S} \\
 g_{o2} &= \boxed{0}.00.000 \mu\text{S}
 \end{aligned}$$

# Circuiti con MOSFET e BJT: Es. 13c (09.02.2016)



# Circuiti con MOSFET e BJT: Es. 13c (09.02.2016)

6. Relativamente all'esercizio precedente, disegnare il circuito equivalente alle variazioni e calcolare sia in forma simbolica che numerica il guadagno di tensione  $A_V = v_{\text{out}}/v_{\text{in}}$

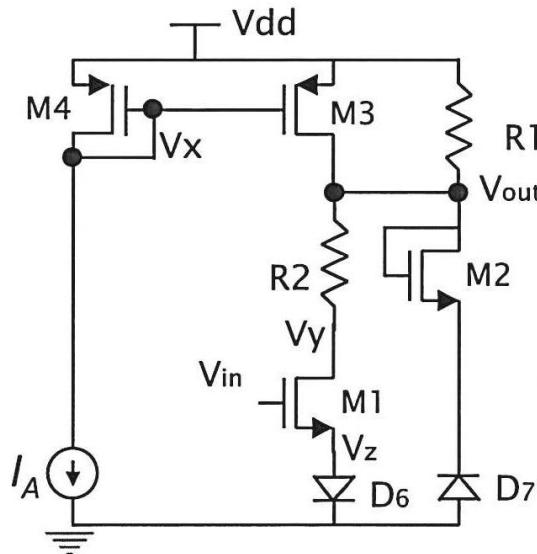


$$v_{\text{out}}/v_{\text{in}} = -(g_{m1} + g_{m2}) \frac{R_3 R_4}{R_3 + R_4}$$

$$v_{\text{out}}/v_{\text{in}} = \boxed{-} \boxed{\phantom{0}} \boxed{0} \boxed{.} \boxed{4} \boxed{8} \boxed{0} \text{ V/V}$$

# Circuiti con MOSFET e BJT: Es. 14c (12.01.2016)

5. Dato il circuito in figura ( $V_{DD} = 5 \text{ V}$ ,  $I_A = 100 \mu\text{A}$ ,  $V_\gamma = 0.6 \text{ V}$ ,  $V_{THn} = 1 \text{ V}$ ,  $V_{THp} = -1 \text{ V}$ ,  $\beta_{M1} = \beta_{M2} = 400 \mu\text{A}/\text{V}^2$ ,  $\beta_{M3} = \beta_{M4} = 800 \mu\text{A}/\text{V}^2$ ,  $V_{IN} = 3.3 \text{ V}$ ,  $R_1 = 20 \text{ k}\Omega$ ,  $R_2 = 1 \text{ k}\Omega$ ), determinare: *i) la zona di funzionamento di MOSFET e diodi, ii) le correnti  $I_{D1}, I_{D2}, I_{D3}, I_{D4}, I_{R1}$ , e le tensioni  $V_x, V_y, V_{out}$ ; iii) i parametri differenziali dei MOSFET.*



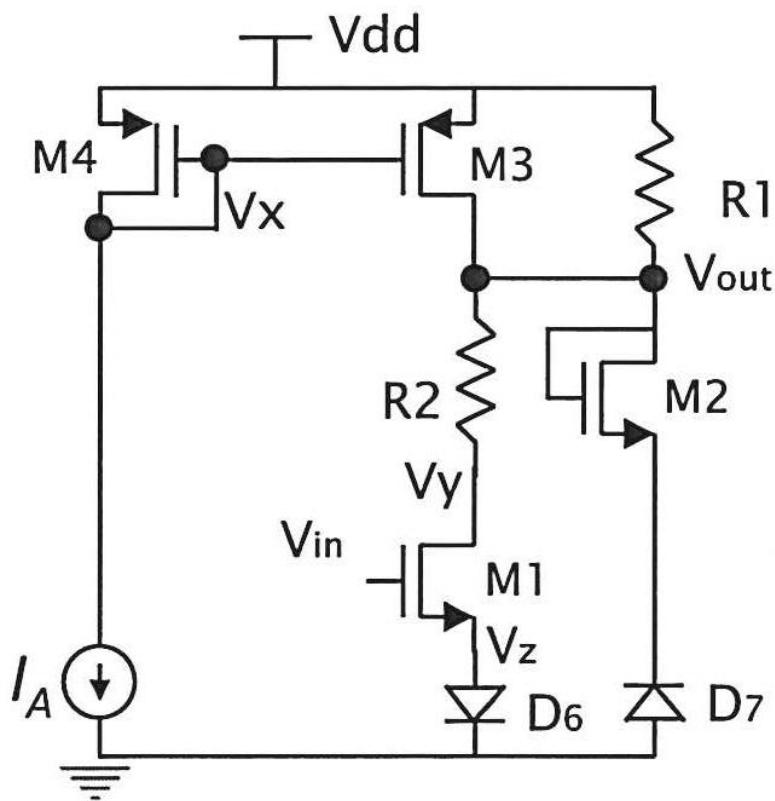
M1 :	SAT	<del>TRI</del>	OFF
M2 :	SAT	TRI	<del>OFF</del>
M3 :	<del>SAT</del>	TRI	OFF

M4 :	<del>SAT</del>	TRI	OFF
D6 :	<del>ON</del>	OFF	
D7 :	ON	<del>OFF</del>	

$$\begin{aligned}
 I_{D1} &= 281.8 \mu\text{A} \\
 I_{D2} &= 0.0 \mu\text{A} \\
 I_{D3} &= 100.0 \mu\text{A} \\
 I_{D4} &= 100.0 \mu\text{A} \\
 I_{R1} &= 181.8 \mu\text{A} \\
 V_x &= 3.5 \text{ V} \\
 V_y &= 1.083 \text{ V} \\
 V_{out} &= 1.365 \text{ V}
 \end{aligned}$$

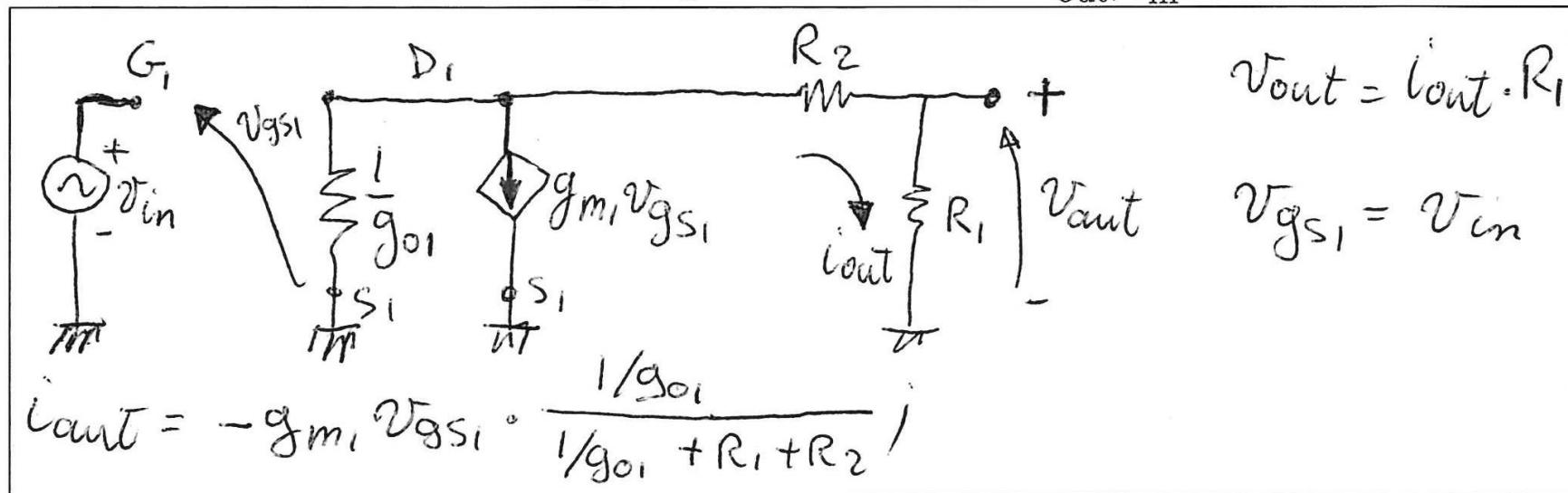
$$\begin{aligned}
 g_{m1} &= 193.2 \mu\text{s} \\
 g_{o1} &= 486.8 \mu\text{s} \\
 g_{m2} &= 0.0 \mu\text{s} \\
 g_{o2} &= 0.0 \mu\text{s} \\
 g_{m3} &= 400.0 \mu\text{s} \\
 g_{o3} &= 0.0 \mu\text{s} \\
 g_{m4} &= 400.0 \mu\text{s} \\
 g_{o4} &= 0.0 \mu\text{s}
 \end{aligned}$$

# Circuiti con MOSFET e BJT: Es. 14c (12.01.2016)



# Circuiti con MOSFET e BJT: Es. 14c (12.01.2016)

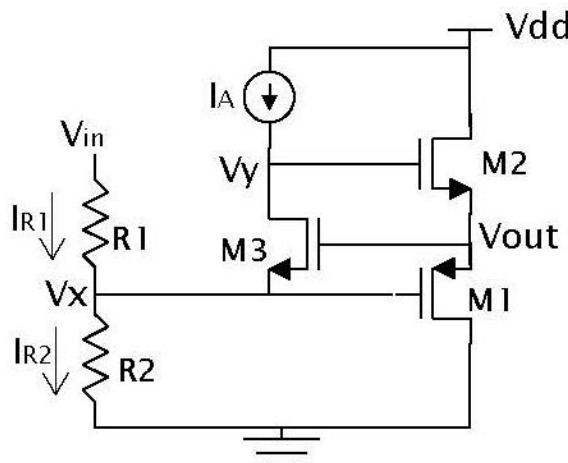
6. Relativamente all'esercizio precedente, disegnare il circuito equivalente alle variazioni e calcolare sia in forma simbolica che numerica il guadagno di tensione  $A_V = v_{\text{out}}/v_{\text{in}}$



$$v_{\text{out}}/v_{\text{in}} = - \frac{g_m \cdot R_1}{1 + g_{o1} (R_1 + R_2)} = - \frac{g_m}{\frac{1}{R_1} + g_{o1} \left(1 + \frac{R_2}{R_1}\right)} v_{\text{out}}/v_{\text{in}} = - \boxed{\phantom{000}} \cdot \boxed{4} \boxed{\phantom{0}} \text{ V/V}$$

# Circuiti con MOSFET e BJT: Es. 15c (09.01.2018)

5. Dato il circuito in figura ( $V_{dd} = 6 \text{ V}$ ,  $V_{in} = 1 \text{ V}$ ,  $I_A = 50 \mu\text{A}$ ,  $R_1 = 10 \text{ k}\Omega$ ,  $R_2 = 40 \text{ k}\Omega$ ,  $V_{THn} = 1 \text{ V}$ ,  $V_{THp} = -1 \text{ V}$ ,  $\beta_{M1} = \beta_{M2} = 100 \mu\text{A/V}^2$ ,  $\beta_{M3} = 200 \mu\text{A/V}^2$ ), determinare: *i) la zona di funzionamento dei MOSFET; ii) le correnti  $I_{R1}$ ,  $I_{R2}$ ,  $I_{D1}$ ,  $I_{D2}$ ,  $I_{D3}$* , e le tensioni  $V_x$ ,  $V_y$ ,  $V_{out}$ ; iii) i parametri differenziali dei MOSFET.



M1 : [SAT] [TRI] [OFF]

M2 : [SAT] [TRI] [OFF]

M3 : [SAT] [TRI] [OFF]

$$\begin{aligned} I_{R1} &= \boxed{\phantom{000}} \cdot \boxed{\phantom{000}} \mu\text{A} \\ I_{R2} &= \boxed{\phantom{000}} \cdot \boxed{\phantom{000}} \mu\text{A} \\ I_{D1} &= \boxed{\phantom{000}} \cdot \boxed{\phantom{000}} \mu\text{A} \\ I_{D2} &= \boxed{\phantom{000}} \cdot \boxed{\phantom{000}} \mu\text{A} \\ I_{D3} &= \boxed{\phantom{000}} \cdot \boxed{\phantom{000}} \mu\text{A} \\ V_x &= \boxed{\phantom{000}} \cdot \boxed{\phantom{000}} \text{V} \\ V_y &= \boxed{\phantom{000}} \cdot \boxed{\phantom{000}} \text{V} \\ V_{out} &= \boxed{\phantom{000}} \cdot \boxed{\phantom{000}} \text{V} \end{aligned}$$

$$\begin{aligned} g_{m1} &= \boxed{\phantom{000}} \cdot \boxed{\phantom{000}} \mu\text{s} \\ g_{o1} &= \boxed{\phantom{000}} \cdot \boxed{\phantom{000}} \mu\text{s} \\ g_{m2} &= \boxed{\phantom{000}} \cdot \boxed{\phantom{000}} \mu\text{s} \\ g_{o2} &= \boxed{\phantom{000}} \cdot \boxed{\phantom{000}} \mu\text{s} \\ g_{m3} &= \boxed{\phantom{000}} \cdot \boxed{\phantom{000}} \mu\text{s} \\ g_{o3} &= \boxed{\phantom{000}} \cdot \boxed{\phantom{000}} \mu\text{s} \end{aligned}$$

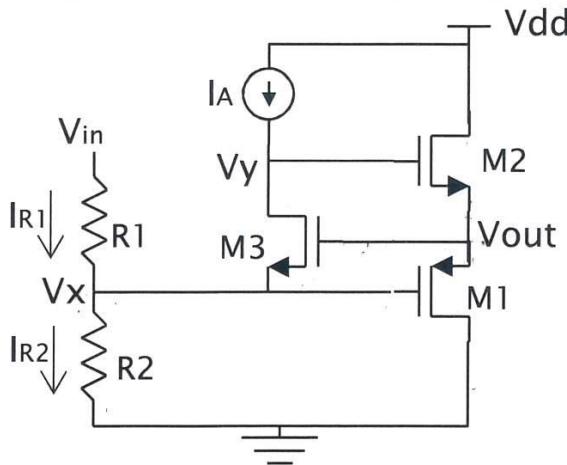
6. Relativamente all'esercizio precedente, disegnare il circuito equivalente alle variazioni e calcolare sia in forma simbolica che numerica il guadagno di tensione  $A_V = v_{\text{out}}/v_{\text{in}}$

$$v_{\text{out}}/v_{\text{in}} =$$

$$v_{\text{out}}/v_{\text{in}} = \boxed{\phantom{0}} \boxed{\phantom{0}} \boxed{\phantom{0}} \boxed{\phantom{0}} . \boxed{\phantom{0}} \boxed{\phantom{0}} \boxed{\phantom{0}} \text{ V/V}$$

# Es. 15c (09.01.2018): Soluzione

5. Dato il circuito in figura ( $V_{dd} = 6 \text{ V}$ ,  $V_{in} = 1 \text{ V}$ ,  $I_A = 50 \mu\text{A}$ ,  $R_1 = 10 \text{ k}\Omega$ ,  $R_2 = 40 \text{ k}\Omega$ ,  $V_{THn} = 1 \text{ V}$ ,  $V_{THp} = -1 \text{ V}$ ,  $\beta_{M1} = \beta_{M2} = 100 \mu\text{A}/\text{V}^2$ ,  $\beta_{M3} = 200 \mu\text{A}/\text{V}^2$ ), determinare: *i)* la zona di funzionamento dei MOSFET; *ii)* le correnti  $I_{R1}$ ,  $I_{R2}$ ,  $I_{D1}$ ,  $I_{D2}$ ,  $I_{D3}$ , e le tensioni  $V_x$ ,  $V_y$ ,  $V_{out}$ ; *iii)* i parametri differenziali dei MOSFET.



M1 : ~~SAT~~ TRI OFF

$$\begin{aligned} I_{R1} &= 20.000 \mu\text{A} \\ I_{R2} &= 30.000 \mu\text{A} \\ I_{D1} &= 25.000 \mu\text{A} \\ I_{D2} &= 25.000 \mu\text{A} \\ I_{D3} &= 50.000 \mu\text{A} \\ V_x &= 1.200 \text{ V} \\ V_y &= 4.614 \text{ V} \\ V_{out} &= 2.907 \text{ V} \end{aligned}$$

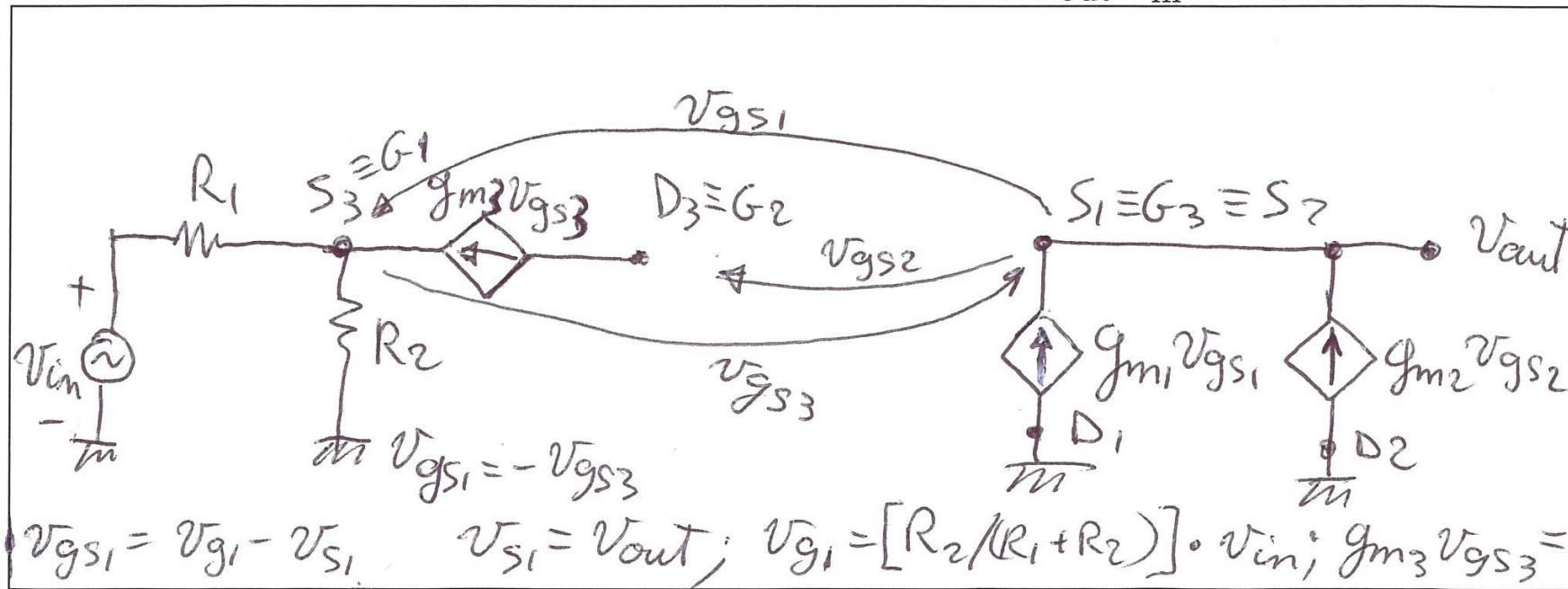
M2 : ~~SAT~~ TRI OFF

M3 : ~~SAT~~ TRI OFF

$$\begin{aligned} g_{m1} &= 70.711 \mu\text{s} \\ g_{o1} &= 0.000 \mu\text{s} \\ g_{m2} &= 70.711 \mu\text{s} \\ g_{o2} &= 0.000 \mu\text{s} \\ g_{m3} &= 141.421 \mu\text{s} \\ g_{o3} &= 0.000 \mu\text{s} \end{aligned}$$

# Es. 15c (09.01.2018): Soluzione

6. Relativamente all'esercizio precedente, disegnare il circuito equivalente alle variazioni e calcolare sia in forma simbolica che numerica il guadagno di tensione  $A_V = v_{\text{out}}/v_{\text{in}}$

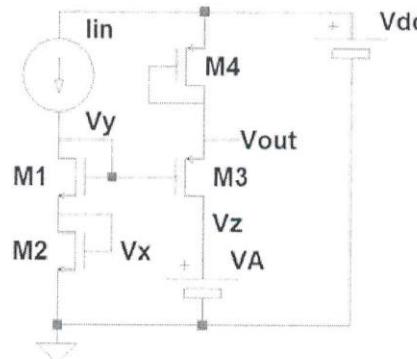


$$v_{\text{out}}/v_{\text{in}} = \frac{R_2}{R_1+R_2}$$

$$v_{\text{out}}/v_{\text{in}} = + \boxed{\phantom{0}}. \boxed{0} \boxed{0} \boxed{0} \text{ V/V}$$

Circuiti con MOSFET e BJT: Es. 16c (08.01.2019)

5. Dato il circuito in figura ( $V_{dd} = 10 \text{ V}$ ,  $V_A = 1 \text{ V}$ ,  $I_{IN} = 100 \mu\text{A}$ ,  $V_{THn} = 1 \text{ V}$ ,  $V_{THp} = -1 \text{ V}$ ,  $\beta_{M1} = \beta_{M2} = \beta_{M3} = \beta_{M4} = 200 \mu\text{A/V}^2$ ), determinare: *i)* la zona di funzionamento e i parametri differenziali dei MOSFET; *ii)* le correnti e le tensioni indicate.

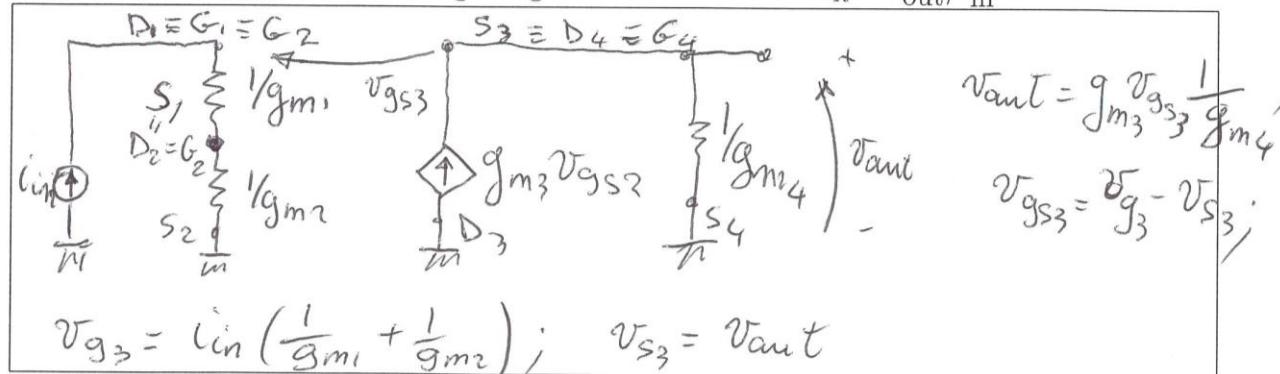


M1 : ~~SAT~~ TRI OFF  
 M2 : ~~SAT~~ TRI OFF

M3 : ~~SAT~~ TRI OFF  
M4 : ~~SAT~~ TRI OFF

$I_{D1} =$	1	0	0	.	0	0	0	μA	$g_{m1} =$	2	0	0	.	0	0	0	μA
$I_{D2} =$	1	0	0	.	0	0	0	μA	$g_{o1} =$		0	.	0	0	0	0	μA
$I_{D3} =$	4	0	0	.	0	0	0	μA	$g_{m2} =$	2	0	0	.	0	0	0	μA
$I_{D4} =$	4	0	0	.	0	0	0	μA	$g_{o2} =$		0	.	0	0	0	0	μA
$V_x =$		2		.	0	0	0	V	$g_{m3} =$	4	0	0	.	0	0	0	V
$V_y =$		4		.	0	6	0	V	$g_{o3} =$		0	.	0	0	0	0	V
$V_z =$		1		.	8	0	0	V	$g_{m4} =$	4	0	0	.	0	0	0	V
$V_{out} =$		7		.	0	0	0	V	$g_{o4} =$		0	.	0	0	0	0	V

6. Relativamente all'esercizio precedente, disegnare il circuito equivalente alle variazioni e calcolare sia in forma simbolica che numerica il guadagno di transresistenza  $A_R = v_{\text{out}}/i_{\text{in}}$



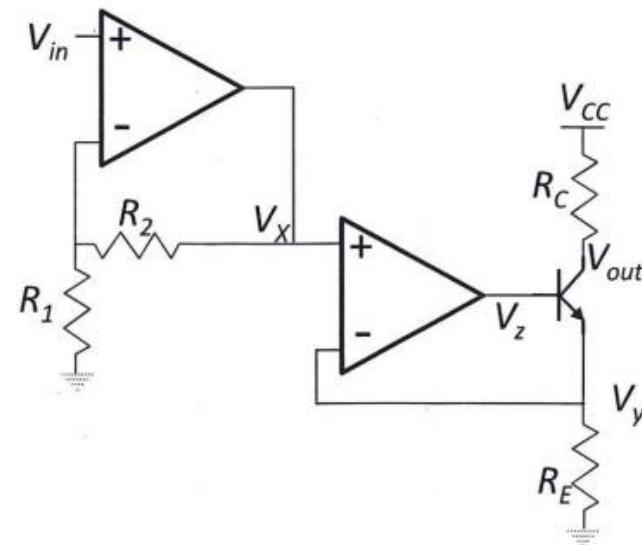
$$v_{\text{out}}/i_{\text{in}} = \frac{g_{m_3}}{g_{m_3} + g_{m_4}} \left( \frac{1}{g_{m_1}} + \frac{1}{g_{m_2}} \right)$$

$$v_{\text{out}}/i_{\text{in}} = + \underline{\hspace{2mm}} \underline{\hspace{2mm}} \underline{\hspace{2mm}} 5.\underline{\hspace{2mm}} \underline{\hspace{2mm}} \underline{\hspace{2mm}} \text{ k}\Omega$$

# Circuiti con OP-AMP: Es. 1d

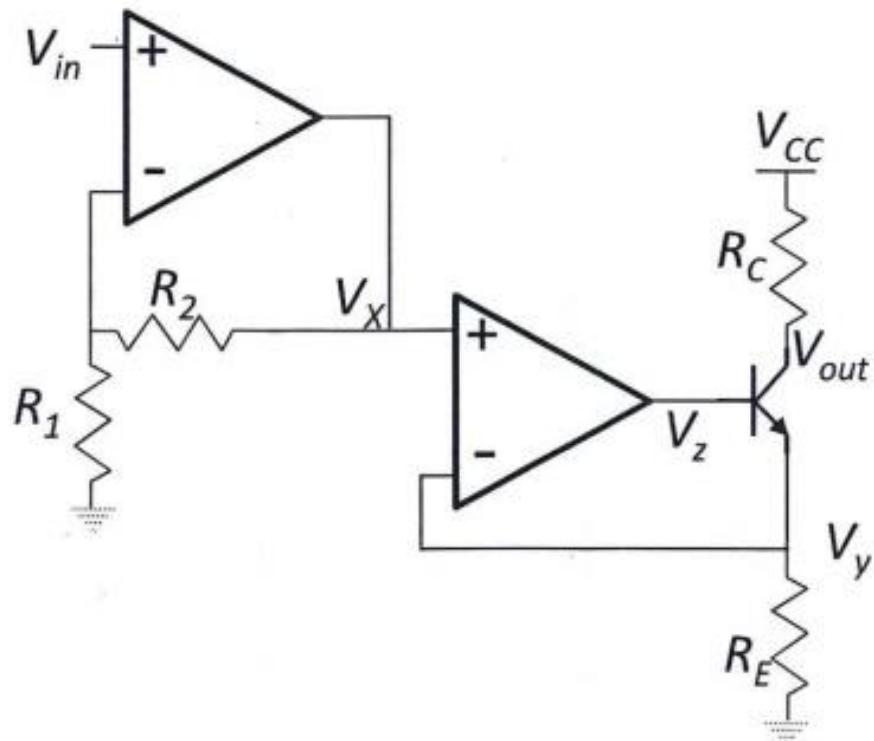
Dato il circuito ( $V_{in} = 0.5$  V,  $V_{CC} = 5$  V,  $R_1 = R_2 = 1 \text{ k}\Omega$ ,  $R_E = 1 \text{ k}\Omega$ ,  $R_C = 2 \text{ k}\Omega$ ,  $\beta = 50$ ,  $V_{BE} = 0.6$  V), determinare: i) l'espressione simbolica che lega  $V_{out}$  a  $V_{in}$ ; ii) i valori numerici indicati.

$$V_{out} = V_{CC} - R_C \cdot \frac{\beta}{1+\beta} \frac{1}{R_E} \left( 1 + \frac{R_2}{R_1} \right) V_{IN} = V_{CC} - V_{IN} \frac{R_C (R_1 + R_2) \beta}{R_E R_1 (\beta + 1)}$$



$V_x$	=	□	□	□	1	.	0	0	0	V
$V_y$	=	□	□	□	1	.	0	0	0	V
$V_z$	=	□	□	□	1	.	6	0	0	V
$V_{out}$	=	□	□	□	3	.	0	3	9	V

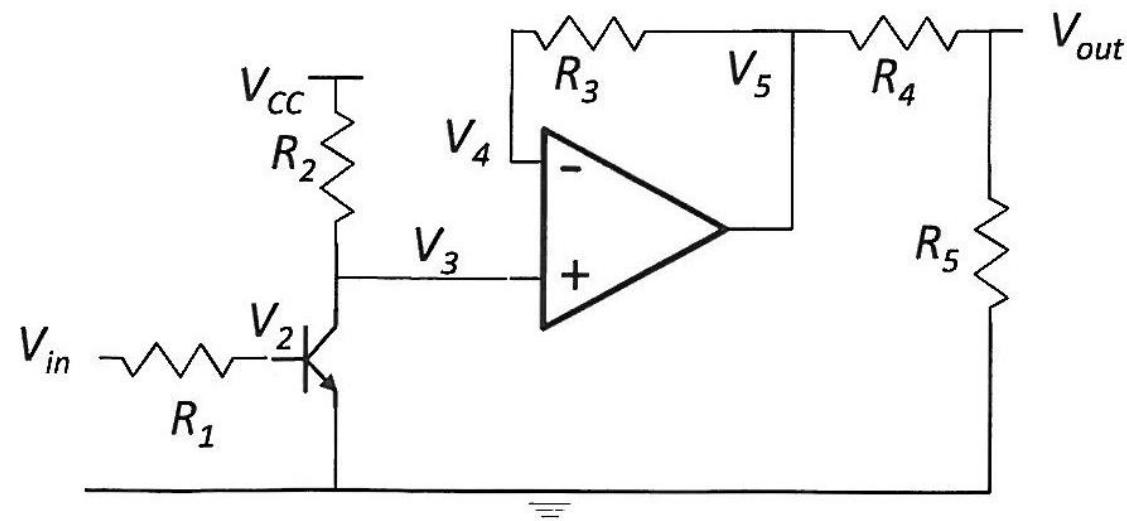
# Circuiti con OP-AMP: Es. 1d



# Circuiti con OP-AMP: Es. 2d

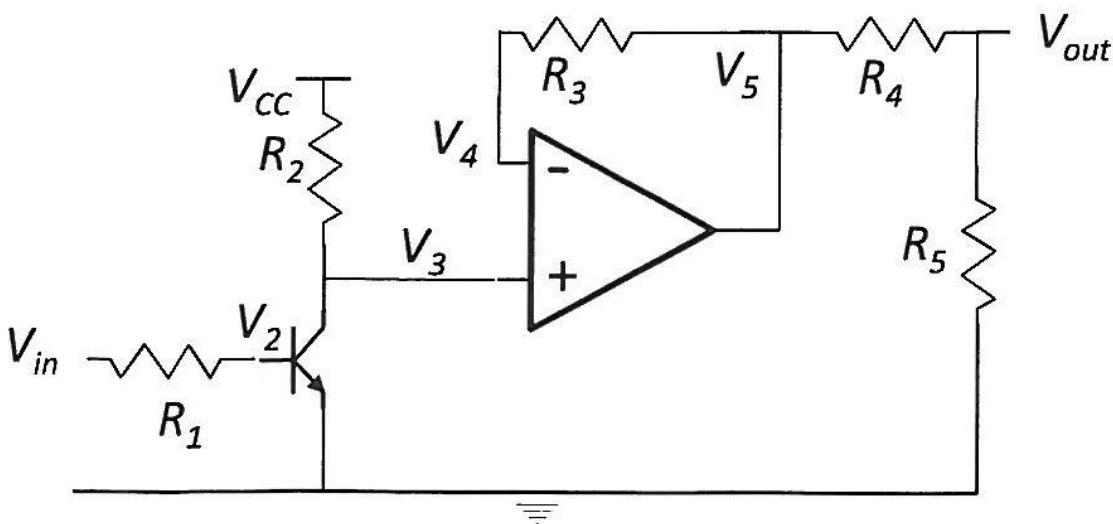
Dato il circuito ( $V_{in} = 1 \text{ V}$ ,  $V_{CC} = 3 \text{ V}$ ,  $R_1 = 50 \text{ k}\Omega$ ,  $R_2 = 1 \text{ k}\Omega$ ,  $R_3 = R_4 = R_5 = 10 \text{ k}\Omega$ , ), determinare: i) l'espressione simbolica che lega  $V_{out}$  a  $V_{in}$ ; ii) i valori numerici indicati.  $V_{BE}=0.6 \text{ V}$

$$V_{out} = \frac{R_5}{R_4 + R_5} \left[ V_{CC} - R_2 \beta \frac{(V_{in} - V_{BE})}{R_1} \right] \quad \beta = 100$$



$V_2$	=	+	0.	6	0	0	V
$V_3$	=	+	2.	2	0	0	V
$V_4$	=	+	2.	2	0	0	V
$V_5$	=	+	2.	2	0	0	V
$V_{out}$	=	+	1.	1	0	0	V

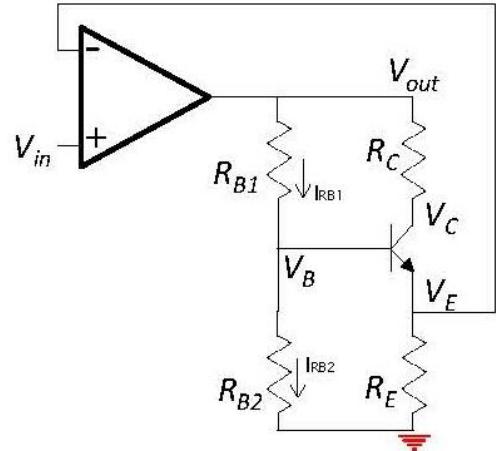
# Circuiti con OP-AMP: Es. 2d



# Circuiti con OP-AMP: Es. 3d (09.01.2018)

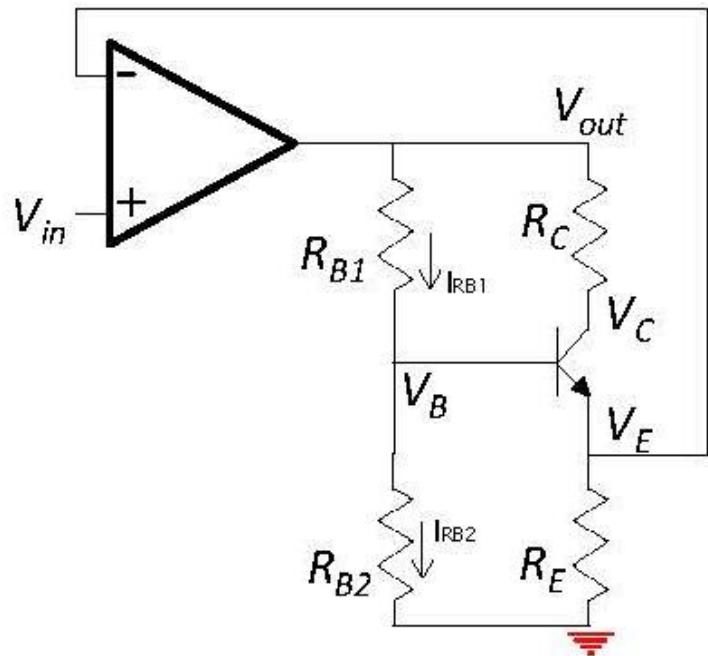
4. Dato il circuito in figura ( $V_{in} = 1 \text{ V}$ ,  $R_{B1} = R_{B2} = 20 \text{ k}\Omega$ ,  $R_E = 1 \text{ k}\Omega$ ,  $R_C = 1 \text{ k}\Omega$ ,  $\beta = 100$ ,  $V_\gamma = 0.6 \text{ V}$ ), determinare: *i)* l'espressione simbolica che lega  $V_{out}$  a  $V_{in}$ ; *ii)* i valori numerici indicati.

$$V_{\text{out}} =$$



$I_E$	<input type="text"/>	<input type="text"/>	<input type="text"/>	.	<input type="text"/>	<input type="text"/>	<input type="text"/>	mA
$I_C$	<input type="text"/>	<input type="text"/>	<input type="text"/>	.	<input type="text"/>	<input type="text"/>	<input type="text"/>	mA
$I_B$	<input type="text"/>	<input type="text"/>	<input type="text"/>	.	<input type="text"/>	<input type="text"/>	<input type="text"/>	$\mu$ A
$I_{RB1}$	<input type="text"/>	<input type="text"/>	<input type="text"/>	.	<input type="text"/>	<input type="text"/>	<input type="text"/>	$\mu$ A
$I_{RB2}$	<input type="text"/>	<input type="text"/>	<input type="text"/>	.	<input type="text"/>	<input type="text"/>	<input type="text"/>	$\mu$ A
$V_E$	<input type="text"/>	<input type="text"/>	<input type="text"/>	.	<input type="text"/>	<input type="text"/>	<input type="text"/>	V
$V_B$	<input type="text"/>	<input type="text"/>	<input type="text"/>	.	<input type="text"/>	<input type="text"/>	<input type="text"/>	V
$V_C$	<input type="text"/>	<input type="text"/>	<input type="text"/>	.	<input type="text"/>	<input type="text"/>	<input type="text"/>	V
$V_{out}$	<input type="text"/>	<input type="text"/>	<input type="text"/>	.	<input type="text"/>	<input type="text"/>	<input type="text"/>	V

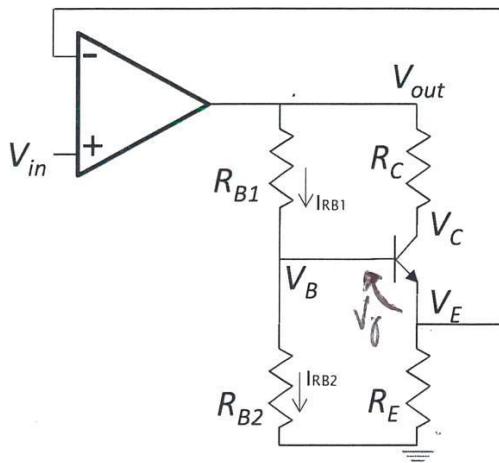
# Circuiti con OP-AMP: Es. 3d (09.01.2018)



# Es. 3d (09.01.2018): Soluzione

4. Dato il circuito in figura ( $V_{in} = 1 \text{ V}$ ,  $R_{B1} = R_{B2} = 20 \text{ k}\Omega$ ,  $R_E = 1 \text{ k}\Omega$ ,  $R_C = 1 \text{ k}\Omega$ ,  $\beta = 100$ ,  $V_\gamma = 0.6 \text{ V}$ ), determinare: *i)* l'espressione simbolica che lega  $V_{out}$  a  $V_{in}$ ; *ii)* i valori numerici indicati.

$$V_{\text{out}} = V_{\text{in}} \left( 1 + \frac{R_{B1}}{(\beta+1)R_E} + \frac{R_{B1}}{R_{B2}} \right) + V_f \left( 1 + \frac{R_{B1}}{R_{B2}} \right)$$



$I_E$	=	+			.0   0   0	mA
$I_C$	=	+		0	.9   9   0	mA
$I_B$	=	+		9	.9   0   1	µA
$I_{RB1}$	=	+	8	9	.9   0   1	µA
$I_{RB2}$	=	+	8	0	.0   0   0	µA
$V_E$	=	+		1	.0   0   0	V
$V_B$	=	+		1	.6   0   0	V
$V_C$	=	+		2	.4   0   8	V
$V_{out}$	=	+		3	.3   9   8	V